

SPIN-WAVE INTERACTION IN B20 MAGNETS

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PNPI

MODEL

$$H = -1/2 \sum J_{\mathbf{q}}(\mathbf{S}_{\mathbf{q}} \cdot \mathbf{S}_{-\mathbf{q}}) + \sum \mathbf{D}_{\mathbf{q}} \cdot [\mathbf{S}_{\mathbf{q}} \times \mathbf{S}_{-\mathbf{q}}] + \sqrt{N}(\mathbf{H} \cdot \mathbf{S}_0),$$

$$\mathbf{D}_{\mathbf{q}} = iD\mathbf{q}.$$

$$\mathbf{H} = 0 : [\mathbf{S}_0, H] = 0$$

Gapless spin-waves

Kaplan Helix: Six free parameters.

Classical energy minimum.

B-J RESULTS

- FM exchange+DMI->planar helix.
Classical results:

Helix wave vector $\mathbf{k} = (SD/A)\hat{c}$.

A and D are the spin-wave stiffness
and DM constant.

$\hat{c} \perp$ to the spin rotation plane.

D
e
r
r
r
r

Cone angle $\sin \alpha = -H/H_c$.

$\mathbf{H} \parallel \hat{c}$, $H_c = Ak^2$

SPIN-WAVE S

- Helical state

$$\epsilon_{\mathbf{q}}^2 = A^2 [q^4 + q^2 k^2 \cos^2 \alpha]$$

- Ferromagnetic state

$$\epsilon_{\mathbf{q}} = A(\mathbf{q} - \mathbf{k})^2 + H - H_c$$

UMKLAPPS

- DMI: Spin-wave with momenta \mathbf{q} and $\mathbf{q} \pm \mathbf{k}$ are mixed

$$H_2^U = \sum_{\mathbf{q}} (d_{\mathbf{q}} a_{\mathbf{q}+\mathbf{k}}^+ a_{\mathbf{q}} + d_{\mathbf{q}}^* a_{\mathbf{q}-\mathbf{k}}^+ a_{\mathbf{q}});$$

$$d_{\mathbf{q}} = -Ak(q_a - iq_b) \cos \alpha$$

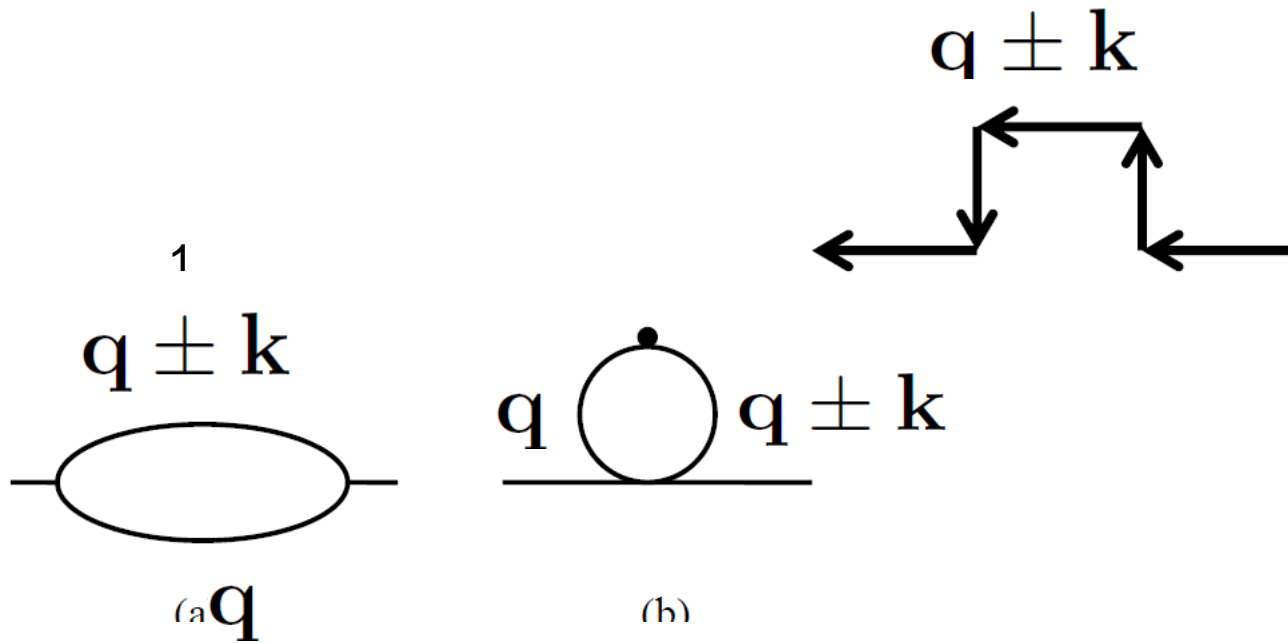
$$\hat{a}, \hat{b} \perp \hat{c} \sim \mathbf{k} : |d|^2 \sim \mathbf{q}_{\perp}^2.$$

$$q < k, H = 0 \quad \epsilon_{\mathbf{q}} \sim q \rightarrow q_{\parallel}$$

$T > 0$ -infra-red divergence.

DIAGRAMS

- Diagrams for the spin-wave U interactions



Vertexes: d and d^* .

BELAYEV TECHNIQUE

$$G = \frac{E + \bar{\Sigma} + \omega}{Z}; \quad F = -\frac{B + \Pi}{Z};$$

$$Z = \omega^2 - \epsilon^2 - \omega(\Sigma - \bar{\Sigma}) -$$

$$\omega(\Sigma + \bar{\Sigma}) + 2B\Pi - (\Sigma\bar{\Sigma} - \Pi^2).$$

$$\bar{\Sigma} = \Sigma(-\omega) \quad \epsilon^2 = E^2 - B^2$$

$$E = Aq^2 + B; \quad B = (Ak^2/2) \cos^2 \alpha$$

U2 APPROXIMATION

$$\Sigma_{\mathbf{q}} = |d|^2 \sum_j \frac{E_j + \omega}{\omega^2 - \epsilon_j^2}; \quad \Pi_{\mathbf{q}} = |d|^2 \sum_j \frac{B}{\omega^2 - \epsilon_j^1};$$

$$|d|^2 = (Akp_{\perp})^2; \quad j = \mathbf{q} \pm \mathbf{k}.$$

$$E = Aq^2 + B; \quad B = (Ak^2/2) \cos^2 \alpha$$

RESULTS

- Spin-wave energy ($H=0$).

$$\epsilon_{\mathbf{q}}^2 = A^2 \{ k^2 [q_{\parallel}^2 + (gq_{\perp}^2)/2S] + (q_{\parallel}q_{\perp})^2/2 + q_{\parallel}^4 + 3q_{\perp}^4/2 \}$$

$$q < k, \quad H = 0$$

$$\text{Factor } g = (ka)^2 (Q_M a) / 8\pi^2 \ll 1$$

Q_M is the spin-wave band width.

ENERGY 1

$$E = S^2[Ak^2/2S - D(\mathbf{k} \cdot \hat{c})]\cos^2\alpha + HS \sin\alpha + E_{SW};$$

$$E_{SW} = \sum [E_{\mathbf{p}} \langle a_{\mathbf{p}}^+ a_{\mathbf{p}} \rangle + B \langle a_{\mathbf{p}} a_{-\mathbf{p}} \rangle + d \langle a_{\mathbf{p}+\mathbf{k}}^+ a_{\mathbf{p}} \rangle + d^* \langle a_{\mathbf{p}}^+ a_{-\mathbf{p}} \rangle],$$

The last two terms connect

\mathbf{q} and $\mathbf{q} \pm \mathbf{k}$ modes.

$$d \langle \dots \rangle + d^* \langle \dots \rangle = \Sigma \bar{G} - \Pi F$$

ENERGY 2

$$E_{SW} = -T \sum_{\omega, \mathbf{p}} \frac{\epsilon_0^2 + W - (E + 2\Sigma - \bar{\Sigma})i\omega}{(i\omega)^2 - \epsilon_0^2 - W};$$

$$W = E(\Sigma + \bar{\Sigma}) - 2B\Pi + (\Sigma\bar{\Sigma} - \Pi^2) +$$

$$i\omega(\Sigma - \bar{\Sigma}); \epsilon_0^2 = E^2 - B^2,$$

ENERGY 3

$$E = S^2[Ak^2/2S - D(\mathbf{k} \cdot \hat{c})]\cos^2\alpha + HS \sin\alpha +$$

$$E_{SW} = \sum \left\{ \epsilon_{\mathbf{p}} N_{\mathbf{p}} - 3 \sum_{j=\pm} \frac{|d_{\mathbf{p}}|^2 [\epsilon_{\mathbf{p}}(2N_{\mathbf{p}}+1) - \epsilon_j(2N_j+1)]}{2(\epsilon_{\mathbf{p}}^2 - \epsilon_j^2)} \right\};$$

$$\mathbf{p}_j = \mathbf{p} + j\mathbf{k}; \quad |d_{\mathbf{p}}|^2 = (Akp_{\perp})^2 \cos^2\alpha.$$

$\epsilon_{\mathbf{p}}$ is U renormalized.

RENORMALIZATION

$$k = k_{BJ}(1 + R); \quad H_c = H_{BJ}(1 + R);$$

$$R = \frac{3}{S} \sum \frac{p_{\perp}^2}{p^2} (2N_{\mathbf{p}} + 1) = \frac{(Q_{Ma})^3}{3\pi^2 S} + \frac{0.12}{S} \left(\frac{T}{T_0} \right)^{3/2},$$

$$T_0 = A/a^2$$

$$MnSi \quad Q_{Ma} \sim 1, T_0 = 30K \simeq T_c, S = 1.6$$

Experiment:

$k(T)$ increases, $H_c(T)$ decreases

FERROMAGNETIC STATE

- Ferromagnetic without zero-point fluctuations: At $T = 0$ $(k, H_c) = (k, H_c)_{BJ}$

$$\epsilon_{\mathbf{q}} = A(\mathbf{q} - \mathbf{k})^2 + H - H_c.$$

$$k_F = k_{BJ} [1 - 0.06(T/T_0)^{3/2}/S] \text{ decreases.}$$

$$H_F = H_{BJ} [1 - 0.15(T_0)^{3/2}/S] \text{ decreases.}$$

$$H_F < H_c^H \text{ the first order transition.}$$

SPECIFIC HEAT 1

1. $T < Ak^2$ At $H = 0$

$$\epsilon_{\mathbf{p}} = A\sqrt{(kp_{\parallel})^2 + p_{\parallel}^4 - p_{\perp}^2 p_{\parallel}^2/2 + 3p_{\perp}^4/2};$$

$$C_V = 0.12(T/Ak^2)^2(ka)^3 \simeq C_F\sqrt{\frac{T}{Ak^2}}.$$

$C_F = 0.11\sqrt{T/T_0}$ is FM CH.

$$C_V(H = 0) < C_V(H = Ak^2) = C_F.$$

Holds if $T > \Delta$ - the spin-wave gap-
the result of anisotropy.

MnSi : $Ak^2 \simeq 0.6T \simeq 1.2K$ $\Delta < 0.1T$???. $T_0 = 30K$.

SPECIFIC HEAT 2

$$T > AK^2; H = 0.$$

$$E_{SW} = \sum A \left[p^2 - \frac{3(kp_{\perp}^2)}{p^2} \right] N_{\mathbf{p}}$$

$$C_V = C_F (1 - 1.6Ak^2/T).$$

In general

$$C_V(H = 0) = C_F \Phi[Ak^2/$$

What is at $T \sim Ak^2$?

OTHER U SYSTEMS

- Lonolayers;
- Fe on W , Mn on W (Cycloid)
- Multiferroixes.
- Frustrated helices
- : dipolar ineraction,
- Diferent directions of the helix and anisotropt xeces.

THANK YOU