



Measurements of the spin wave stiffness in helimagnets by small-angle polarized neutron scattering

Sergey Grigoriev

Petersburg Nuclear Physics Institute,
RNC “Kurchatov institute”,
Gatchina, St-Petersburg 188300, Russia



Outline

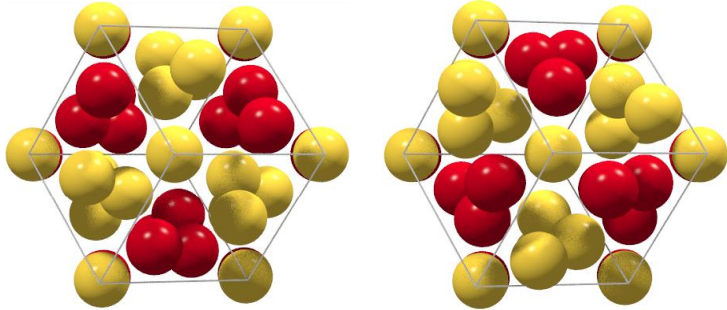
Motivation

Small-angle polarized neutron scattering as a method to study spin waves in helimagnets

Example of MnSi

Example of FeGe

Conclusion



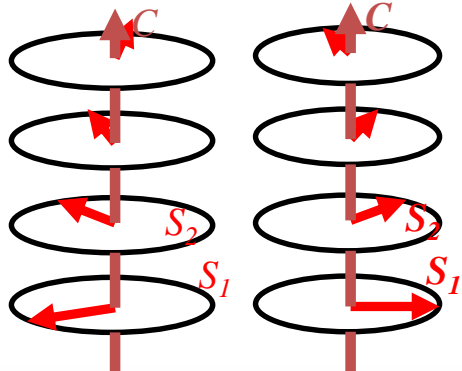
Driving forces in magnetic system of B20 compounds

[1] O. Nakanishi, A. Yanase, A. Hasegawa, M. Kataoka, Solid State Commun. 35 (1980) 995.

[2] P.Bak, M.H.Jensen, J.Phys. C13 (1980) L881.

Left-handed helix

Right-handed helix



Free energy density

1) isotropic ferromagnetic exchange

$$W(q) = (B/2) (q^2 + \kappa_0^2) \delta_{\alpha\beta} \mathbf{S}_q^\alpha \mathbf{S}_{-q}^\beta +$$

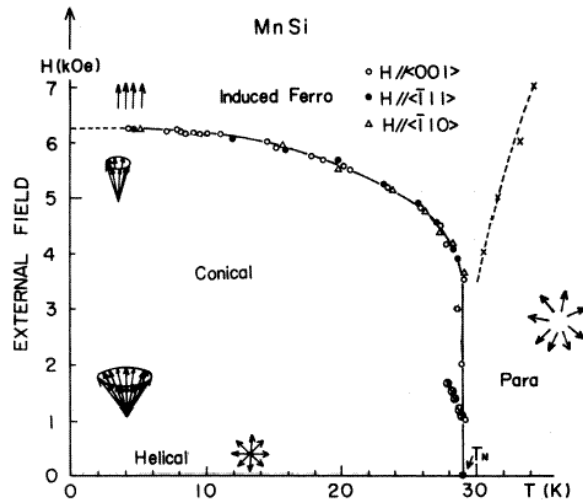
2) isotropic antisymmetric spin exchange Dzyaloshinskii-Moria (DM) due to lack of a symmetry center:

$$+ i D \varepsilon_{\alpha\beta\gamma} q_\gamma \mathbf{S}_q^\alpha \mathbf{S}_{-q}^\beta +$$

3) weak anisotropic exchange (AE) interaction fixes direction of spiral along $\langle 1,1,1 \rangle$:

$$+ (F/2)(q_x^2 |\mathbf{S}_q^x|^2 + q_y^2 |\mathbf{S}_q^y|^2 + q_z^2 |\mathbf{S}_q^z|^2)$$

(H-T) phase diagrams



$$W(\mathbf{q}) = E_{EX} + E_{DM} + E_{AE} =$$

$$= (A/2) (\mathbf{q}^2 + \kappa_0^2) \mathbf{S}_q^2 +$$

$$+ D (\mathbf{q} [\mathbf{S}_q \times \mathbf{S}_{-\mathbf{q}}]) + E_{AE}$$

- 1) $k = S D / A$ the helix wave vector
- 2) $A k^2 = g \mu_B H_{C2}$ the critical field of transition to the fully polarized state

for MnSi

$$1) A = g \mu_B H_{C2} / k = 50 \text{ meV } \text{\AA}^2$$

$$2) S D a = A k a = 8 \text{ meV } \text{\AA}^2$$

[1] Y. Ishikawa, G. Shirane, J.A. Tarvin, M. Kohgi,
Phys.Rev.B **16** (1977) 4956.



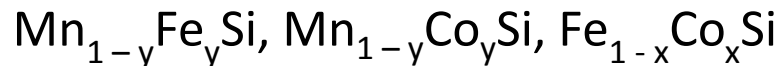
Triple-axis neutron spectroscopy for MnSi

- [1] Y. Ishikawa, G. Shirane, J. A. Tarvin, and M. Kohgi,
Phys. Rev. B 16, 4956 (1977)
[2] J. A. Tarvin, G. Shirane, Y. Endoh, and Y. Ishikawa,
Phys. Rev. B 18, 4815 (1978)
[3] F. Semadeni, P. Boni, Y. Endoh, B. Roessli, G. Shirane,
Physica B 267-268, 248-251 (1999)

The dispersion of SW in fully polarized state
like in ferromagnets

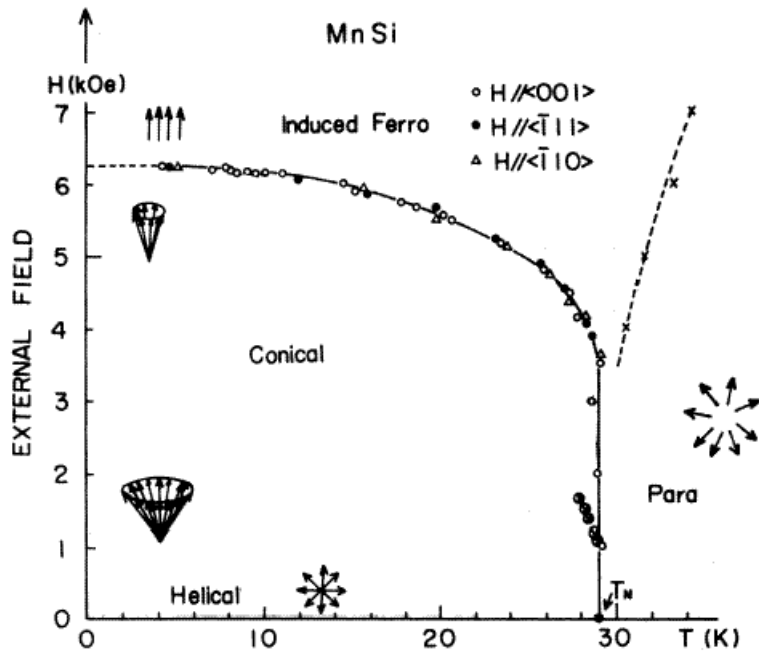
$$\varepsilon_q = Dq^2 + g\mu H \text{ with}$$
$$D = 52 \pm 2 \text{ meV \AA}^2 \text{ at } T = 5 \text{ K}$$

Question reads: what about other compounds ?



Answer reads: not with this method, which
requires (i) large single crystals and
(ii) long time for measurements.

Spin-waves in helimagnets with DM interaction



Mitsuo Kataoka, J.Phys.Soc.Jap. 56 (1987) 3635

- Dynamics in the - “field-induced ferromagnetic” – fully polarized state $H > H_{C2}$

Ferromagnet
 $\varepsilon_q = Dq^2 + g\mu H$

Helimagnet ($H > H_{C2}$)
 $\varepsilon_q = D(\mathbf{q} - \mathbf{k})^2 + g\mu (H - H_{C2})$

[1] Y. Ishikawa, G. Shirane, J.A. Tarvin, M. Kohgi,
 Phys.Rev.B **16** (1977) 4956.

Kinematics of the neutron scattering on spin waves in helimagnets

Energy conservation law (1) $\hbar\omega = E' - E = \left(\frac{\hbar^2}{2m}\right)(k'^2 - k^2) = \varepsilon_q$

$$\varepsilon_q = D(\mathbf{q} - \mathbf{k}_s)^2 + g\mu(H - H_{C2})$$

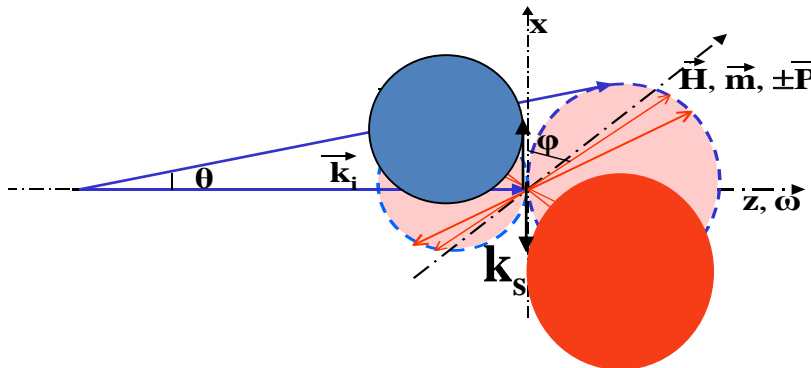
Impulse conservation law (2) $q^2 = k'^2 + k^2 - 2k'k \cos \theta$

One receives the following solution:

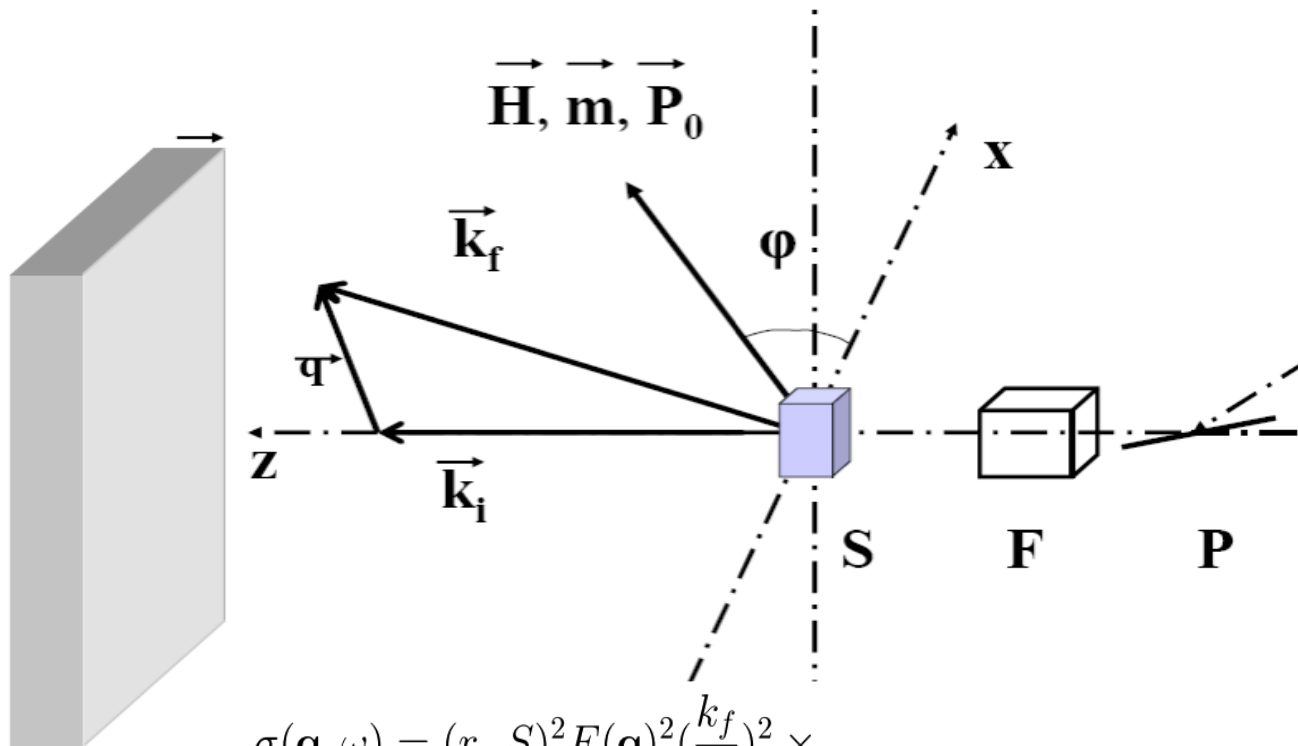
$$\frac{\omega_{1,2}}{2E} = \theta_0 + \frac{k_s}{k_i} \sin \phi \mp \sqrt{C - \left(\theta^2 - \theta \cdot 2 \frac{k_s}{k_i} \cos \phi\right)}$$

$$C = \theta_0^2 - \theta_0 \cdot \frac{H}{E} + \theta_0 \cdot 2 \frac{k_s}{k_i} \sin \phi + \left(\frac{k_s}{k_i}\right)^2 \sin^2 \phi$$

$$\theta_0 = \alpha^{-1} = \hbar^2 / 2Dm$$



Experimental setup

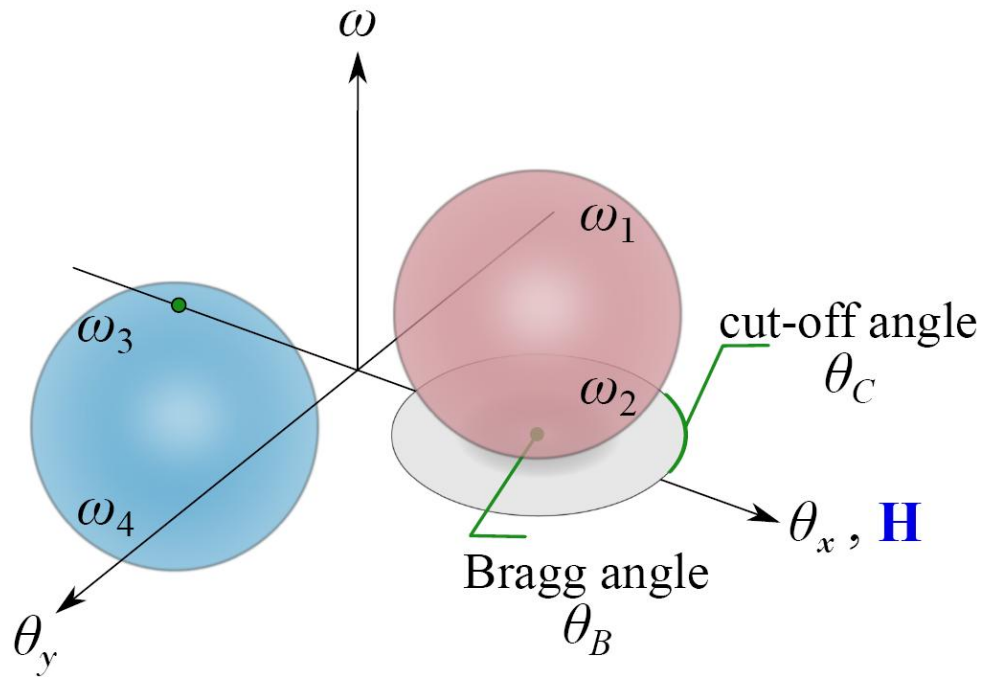


$$\sigma(\mathbf{q}, \omega) = (r_m S)^2 F(\mathbf{q})^2 \left(\frac{k_f}{k_i}\right)^2 \times$$

$$\times \{ [1 + (\mathbf{em})^2 + 2(\mathbf{em})(\mathbf{eP}_0)] n_q \delta(\omega - \epsilon_q) +$$

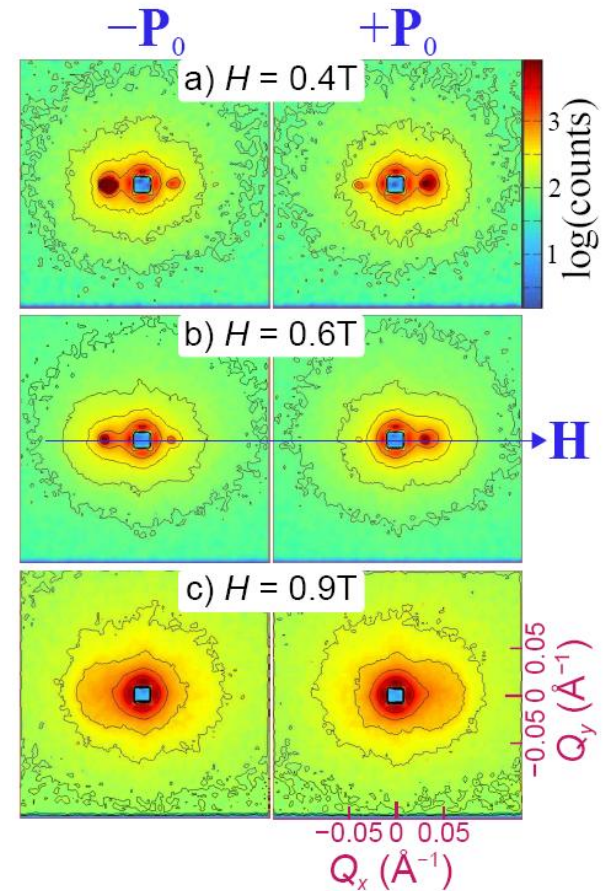
$$+ [1 + (\mathbf{em})^2 - 2(\mathbf{em})(\mathbf{eP}_0)] (n_q + 1) \delta(\omega + \epsilon_q) \},$$

Small Angle Polarized Neutron scattering on magnons in MnSi

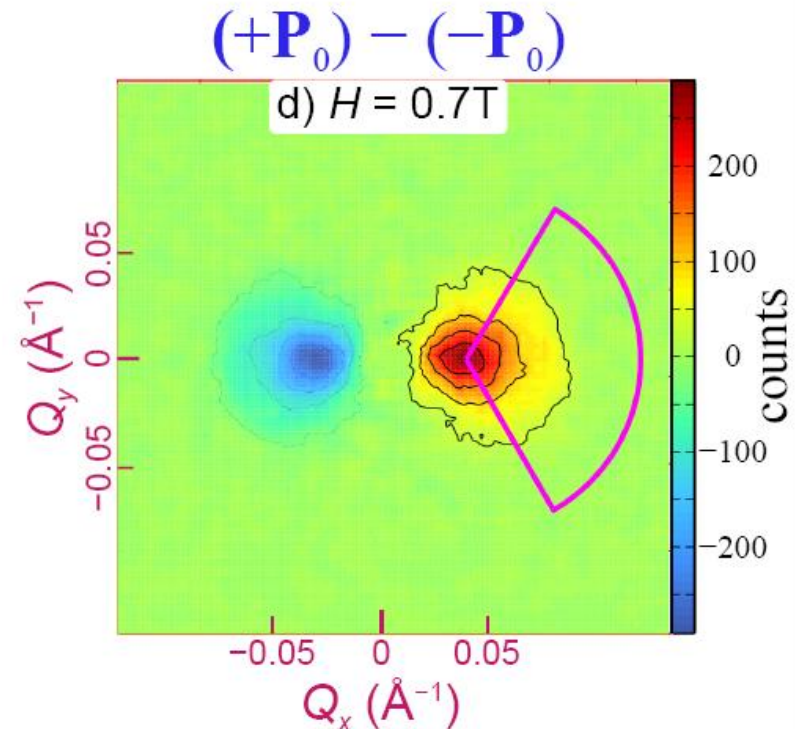
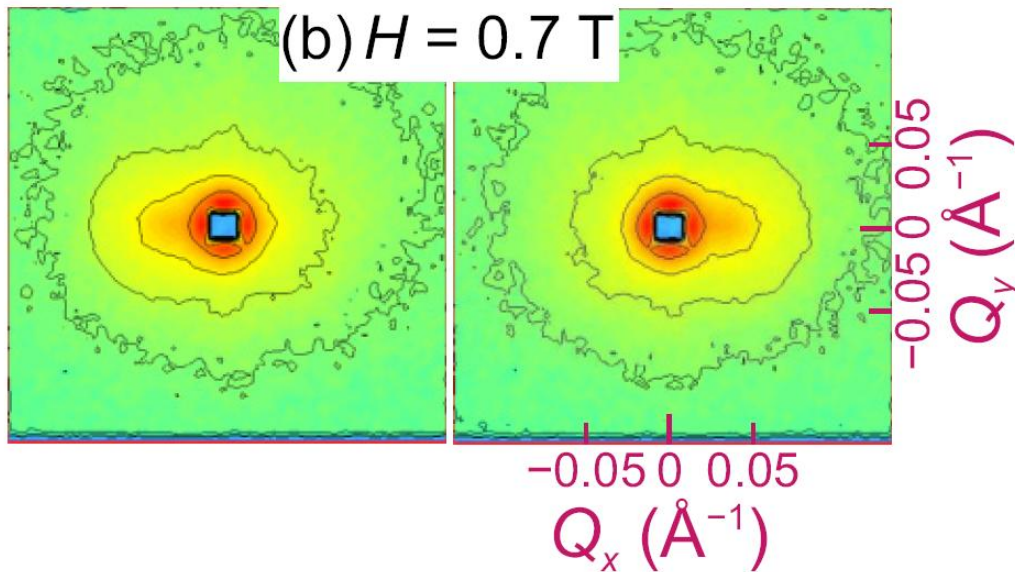


$$\Delta\sigma(\mathbf{q}, \omega) = \sigma(\mathbf{q}, \omega, +P_0) - \sigma(\mathbf{q}, \omega, -P_0) =$$

$$= 4(r_m S)^2 F(\mathbf{q})^2 \left(\frac{k_f}{k_i}\right)^2 (\mathbf{e}\mathbf{m})^2 n_q [\delta(\omega - \epsilon_q) - \delta(\omega + \epsilon_q)].$$



Small Angle Polarized Neutron scattering on magnons in MnSi



$$\Delta\sigma(\mathbf{q}, \omega) = \sigma(\mathbf{q}, \omega, +P_0) - \sigma(\mathbf{q}, \omega, -P_0) =$$

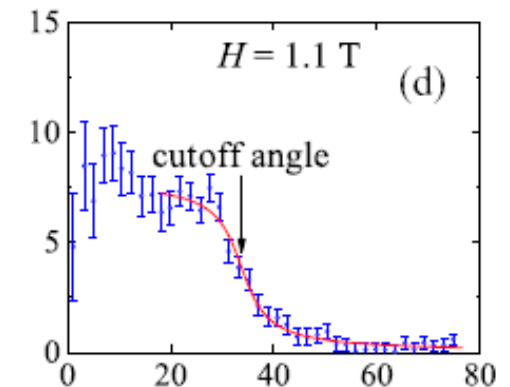
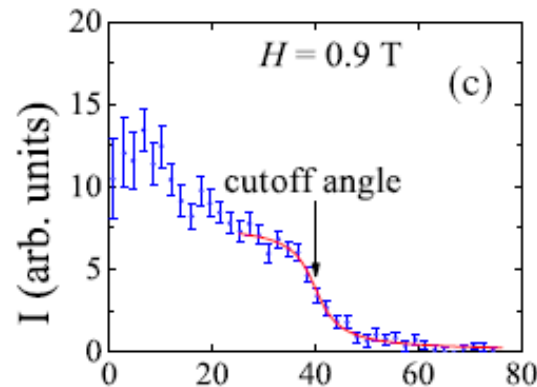
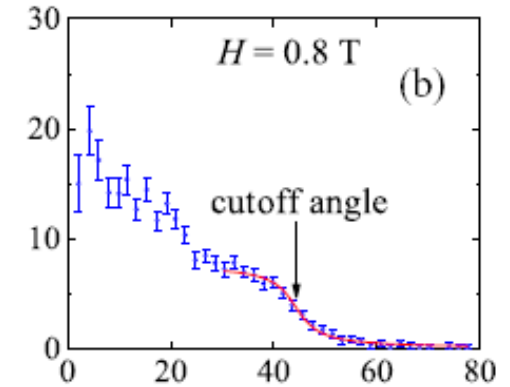
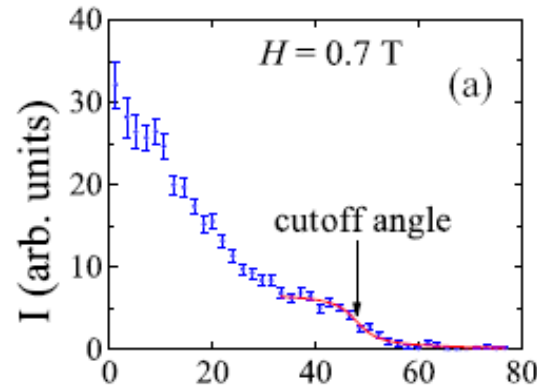
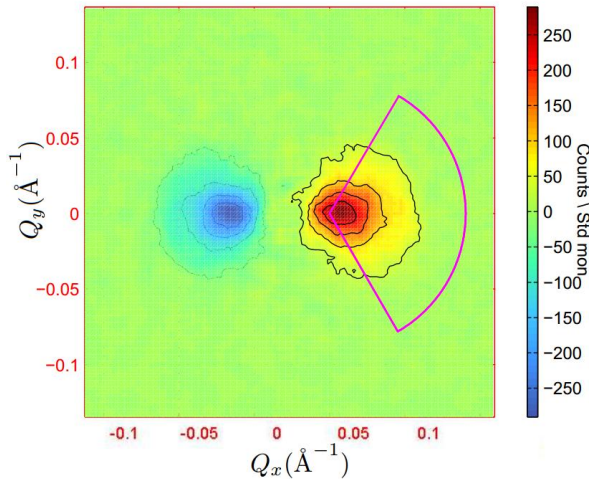
$$= 4(r_m S)^2 F(\mathbf{q})^2 \left(\frac{k_f}{k_i}\right)^2 (\mathbf{e}\mathbf{m})^2 n_q [\delta(\omega - \epsilon_q) - \delta(\omega + \epsilon_q)].$$



Field-evolution of anti-symmetric part of neutron scattering in MnSi

MnSi, $T = 15$ K

$H = 0.7$ T





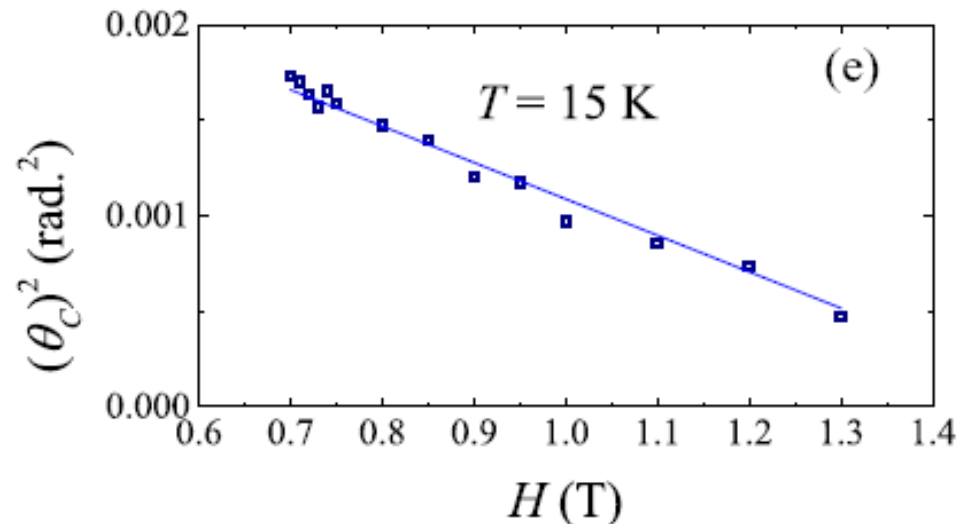
Field dependence of cut-off angle

MnSi

$$\theta_C^2(H) = \theta_0^2 - \frac{g\mu H \theta_0}{E}$$

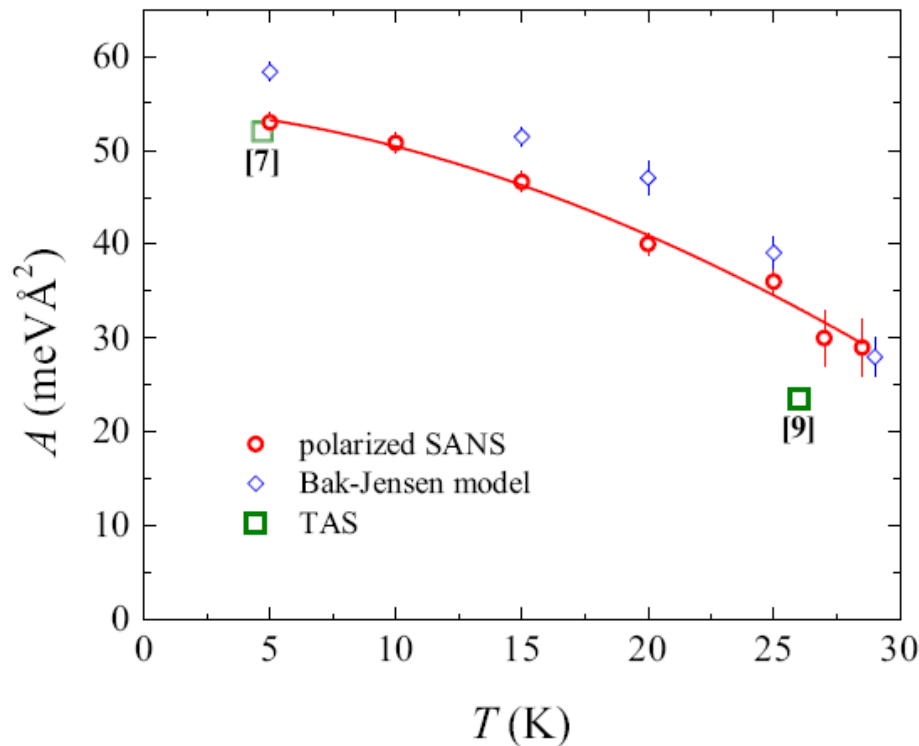
$$\theta_0 = \alpha^{-1} = \hbar^2 / 2Dm$$

$$D = 48 \text{ meV } \text{\AA}^2$$
$$T = 15 \text{ K } (H > H_{C2})$$





Temperature dependence of spin wave stiffness in MnSi

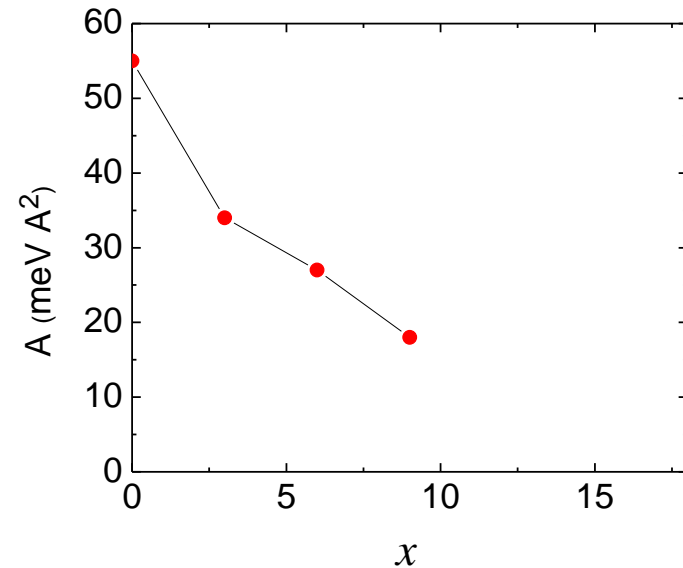
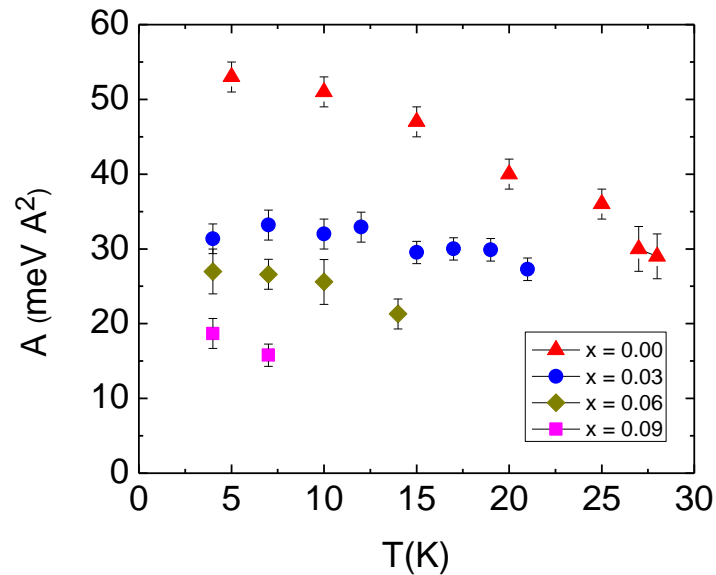


$$A = g \mu_B H_{C2} / k$$

S. V. Grigoriev, A. S. Sukhanov, E. V. Altyntbaev, S.-A. Siegfried, A. Heinemann, P. Kizhe, and S. V. Maleyev, Phys. Rev. B 92, 220415(R) (2015)



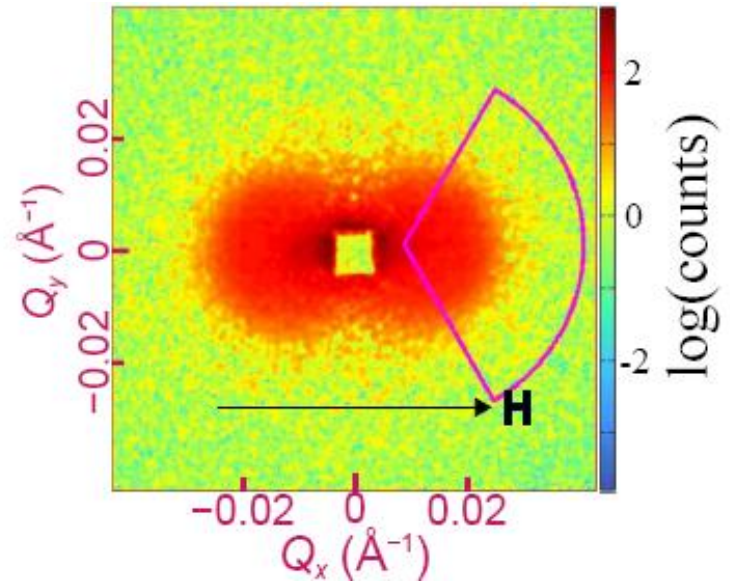
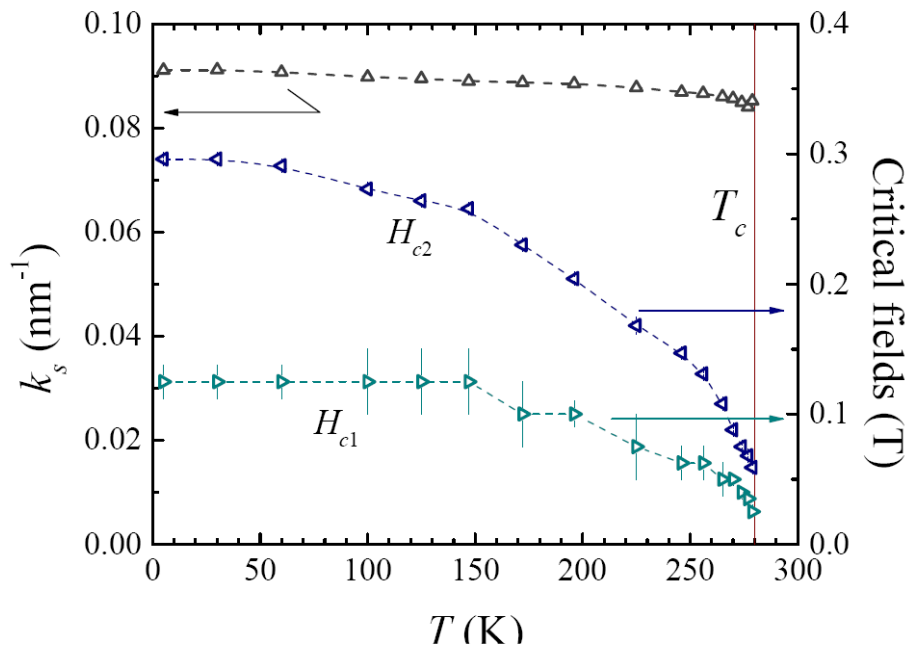
Spin wave stiffness in $\text{Mn}_{1-x}\text{Fe}_x\text{Si}$



E. V. Altyntbaev, S.-A. Siegfried, D. Menzel, G. Chaboussant, and S. V. Grigoriev, unpublished data.

Temperature dependence of spin wave stiffness in FeGe

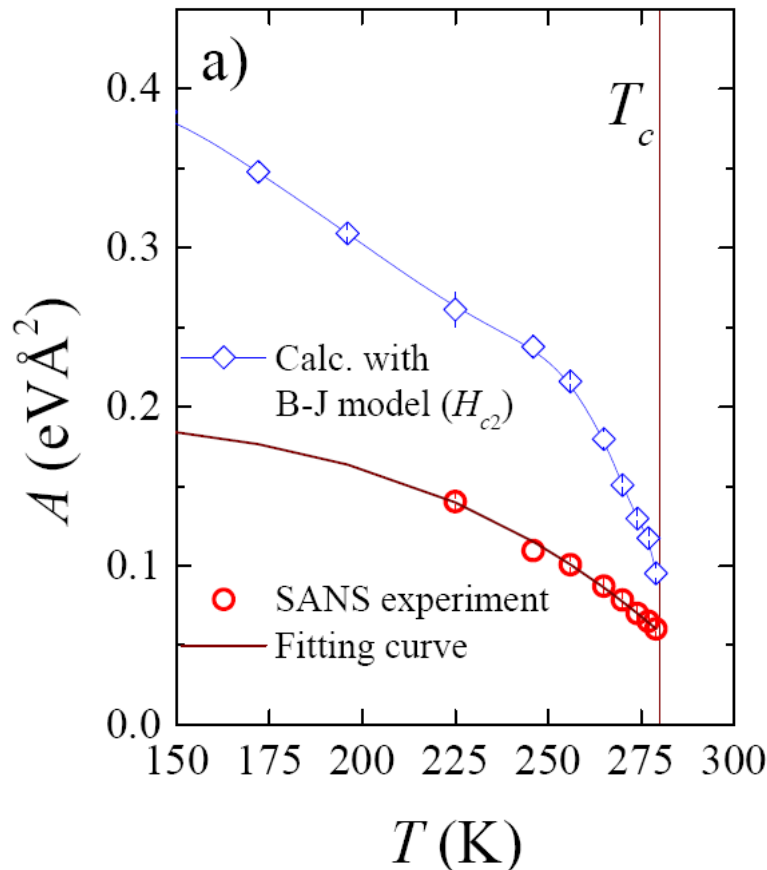
$$A = g \mu_B H_{c2} / k$$



S.-A. Siegfried, A. S. Sukhanov, E. V. Altyntbaev, D. Honnecker, A. Heinemann, and S. V. Grigoriev, unpublished data.



Temperature dependence of spin wave stiffness in FeGe



$$g \mu_B H_{c2} = A k^2$$

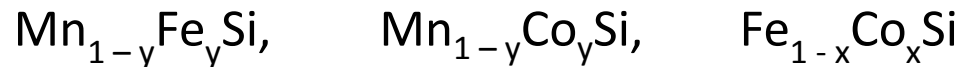
$$H_{c2} = A k_s^2 + 10/3 K S_\xi^3$$

S. V. Grigoriev, A. S. Sukhanov, and S. V. Maleyev, Phys. Rev. B **91** (2015) 224429



Perspectives of the SANS method to study spin wave stiffness of helimagnets

Question reads: what about other compounds ?



Answer reads: can be measured by SANS method.

Method can work with

- (i) the powder samples and
- (ii) with acceptable statistics in reasonable time to make the wide range temperature scans.



Summary

We have experimentally proven the validity of the spin-wave dispersion relation for helimagnets with the DM interaction in the full-polarized state

$$\varepsilon_{\mathbf{q}} = D(\mathbf{q} - \mathbf{k}_s)^2 + g\mu (H - H_{C2})$$

Small-angle polarized neutron scattering is shown to be a method to study spin waves in helimagnets.



Acknowledgements

A.S. Sukhanov, E.V. Altynbayev, S.V. Maleyev,

Petersburg Nuclear Physics Institute, NRC KI
Gatchina, St-Petersburg 188300, Russia

S.-A. Siegfried, A. Heinemann

Helmholz Zentrum Geesthacht,
21502 Geesthacht, Germany

Dirk Honnecker

Institut Laue-Langevin, 38042 Grenoble Cedex 9, France

The work is supported by the

Russian Foundation of Basic Research (Grant No 14-22-01073)

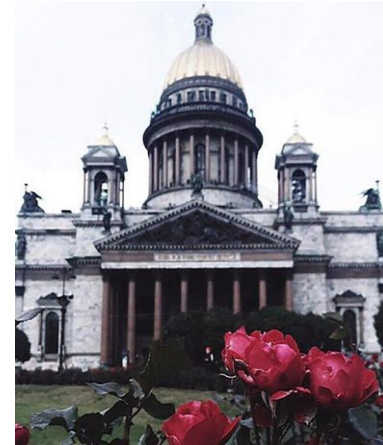


Many thanks for your attention!

ECNS -2019

European Conference on Neutron Scattering
July 1 - 5, 2019 | St. Petersburg, Russia

**European Conference
on Neutron Scattering**
July 1-5, 2019
St. Petersburg, Russia



B.P. Konstantinov
Petersburg Nuclear Physics Institute
(PNPI)