

Особенности поиска структурных параметров наночастиц по данным малоуглового рассеяния

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Features of searching of structural parameters of nanoparticles from small-angle scattering data

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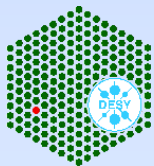
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Polydisperse systems of nanoparticles

Complex case: different formfactors “k”, different sizes, interparticle interference.



k=1



$$I(s) = \text{const} \sum_{k=1}^K \varphi_k I_k(s, R_{0k}, \Delta R_k) S_k(s, R_k^{sh}, \eta_k, \tau_k)$$



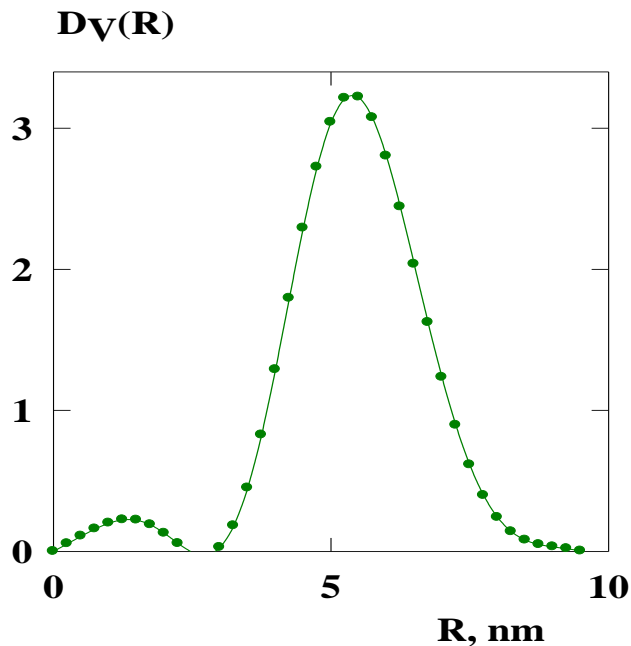
k=2

k=3



Size distribution can be found by a regularization method
(no analytical shape of distribution is assumed).
The cost: the only shape for all particles is to be assumed.
Program GNOM: non-parametric approach

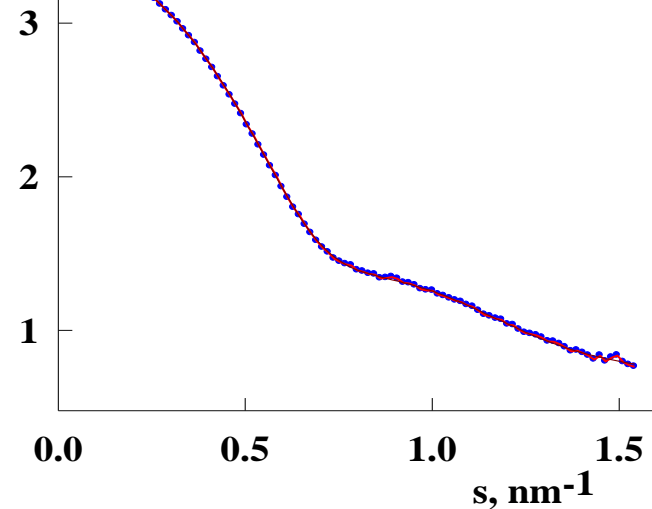
$$I(s) = \int_0^{\infty} D_V(R) \cdot m^1(R) \cdot i(sR) \cdot dR$$



$$i(sR) = \{[\sin(sR) - sR \cos(sR)] / (sR)^3\}^2$$

$\lg I$

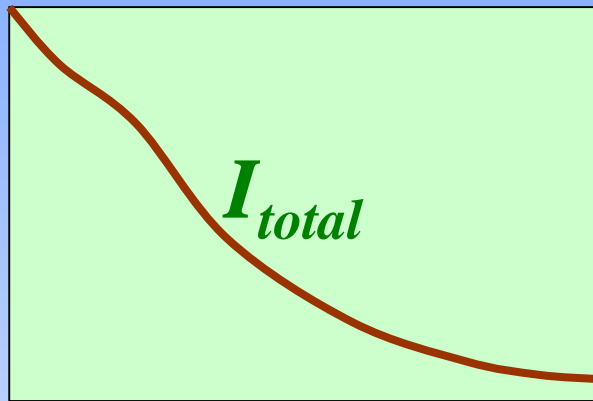
$$m(R) = (4\pi/3)R^3 \Delta\rho$$



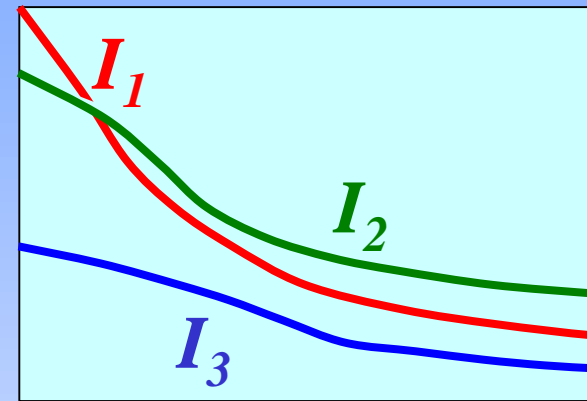
GNOM: a Program Package for Small-Angle Scattering
Data Processing / A.V. Semenyuk, D.I. Svergun // J.
Appl. Cryst. – 1991. – V. 24. – P. 537 – 540.

$$\min \left\{ \left\| I_{\text{exp}}(s) - I_{\text{calc}}(s) \right\|^2 + \alpha \left\| \frac{dD_V(r)}{dr} \right\|^2 \right\}$$

Program MIXTURE (ATSAS) – search for a model as a sum of partial analytical distributions of known shape with *a priori* unknown parameters and weights. The particle shapes are the same if a frame of one component.

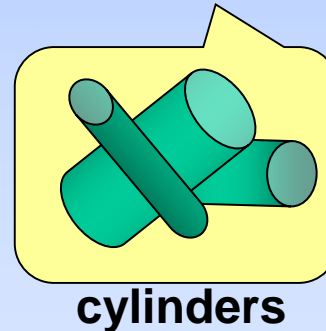
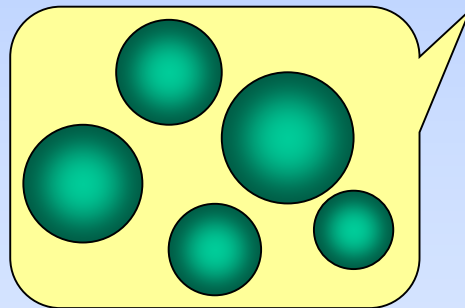


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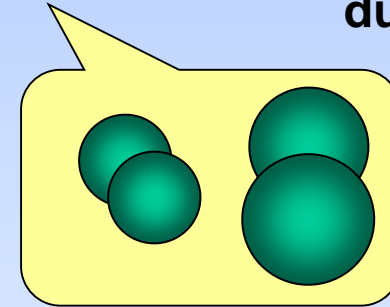


$$I_{total} = c_1 I_1 + c_2 I_2 + c_3 I_3$$

spherical
particles



cylinders



dumb-bells

$c_i = ?$ *distribution parameters = ?*

Program MIXTURE (ATSAS package)

Total scattering is a sum of “K” partial scattering intensities from K components each having its own distribution profile:

$$I(s) = \sum_k v_k I_k(s)$$

v_k – relative volume fraction of k -th component,

$I_k(s)$ - SAS intensity from k -th component, s – scattering vector: $|s| = \frac{4\pi}{\lambda} \sin \theta$

2θ - scattering angle

For each component, SAS intensity is determined as:

$$I_k(s) = \int D_k(R) \cdot i_k(sR) \cdot S_k(sR) \cdot v_k(R) \cdot dR$$

где R - effective size of the particle,

$i_{ok}(sR)$ – normalized (to a unity volume) formfactor used for k -th component,

$D_k(R)$ - normalized size distribution of k -th component

$S_k(sR)$ - structure factor for k -th component used for dense samples

$v_k(R)$ - effective particle volumes.

We may use, for example, the Schulz distribution formula to describe polydispersity:

$$D(R) = \frac{1}{R_0} (z+1)^{z+1} \frac{1}{\Gamma(z+1)} \left(\frac{R}{R_0}\right)^z \exp\left[-\frac{(z+1)R}{R_0}\right]$$

R_0 – mean size of the particle

ΔR – distribution width

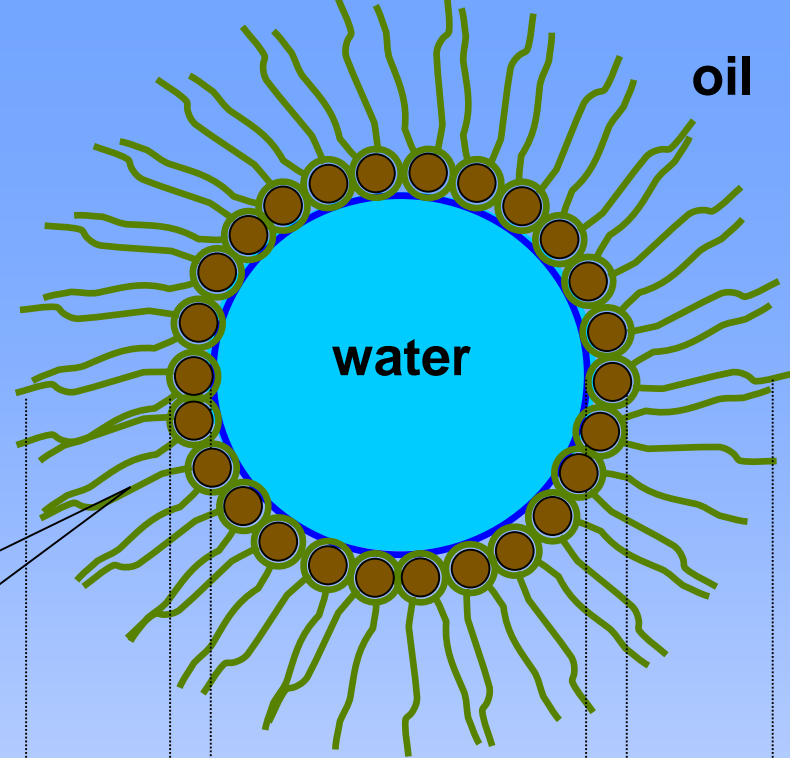
$\Gamma(z)$ – Gamma function

$$z = \left(\frac{R_0}{\Delta R}\right)^2 - 1$$

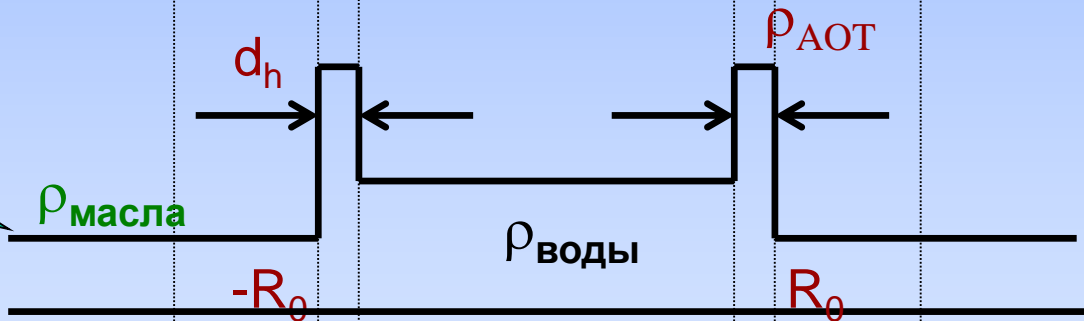
A small angle x-ray scattering study of the droplet-cylinder transition in oil-rich sodium bis(2-ethylhexyl) sulfosuccinate microemulsions / D. I. Svergun, P. V. Konarev, V. V. Volkov, M. H. J. Koch, W. F. C. Sager, J. Smeets, E. M. Blokhuis // J. Chem. Phys. – 2000. – V. 113. – P. 1651 – 1665.

An example of formfactor used to describe structure of inverse water micelles in oil, stabilized by the AOT surfactant

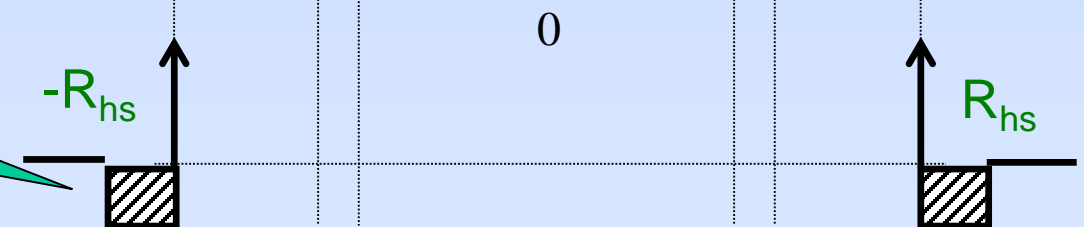
AOT molecules



Electron density profile as a radial distribution for spherical particles

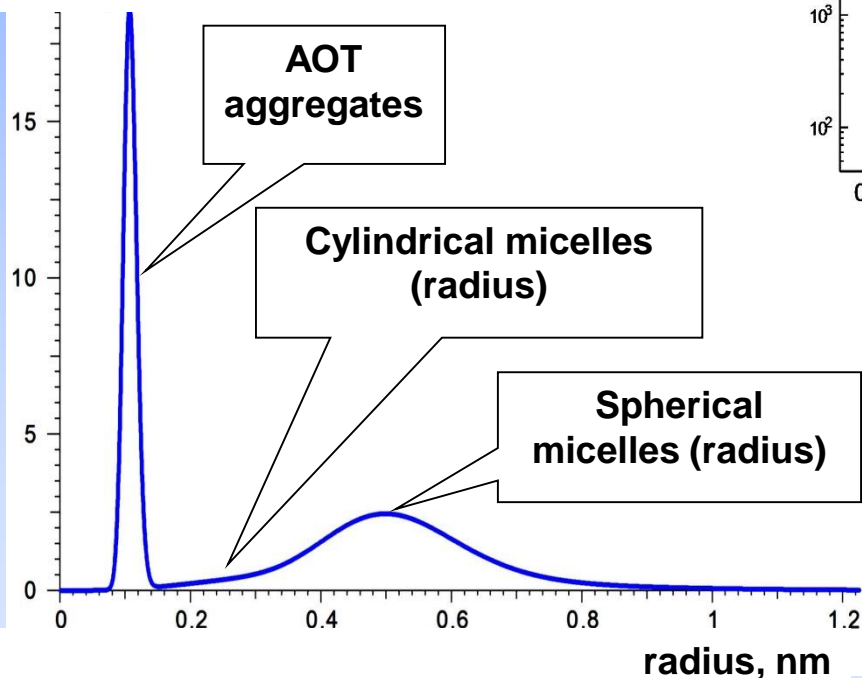


Interparticle interaction potential



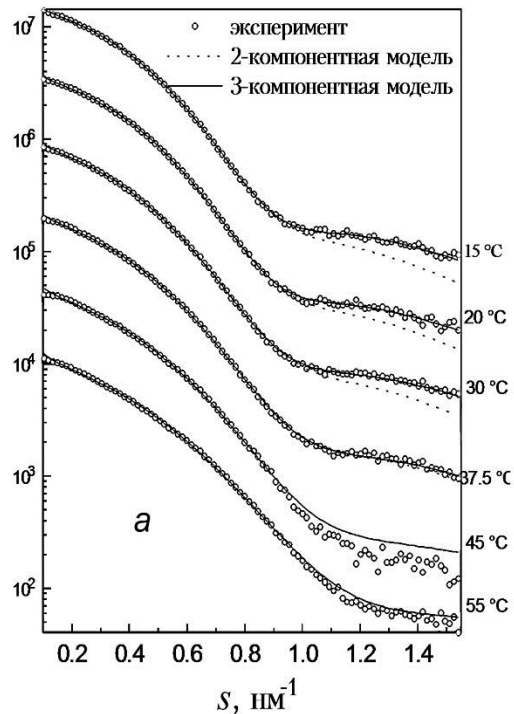
Three-component model of polydisperse solution of inverse water micelles

Volume fraction

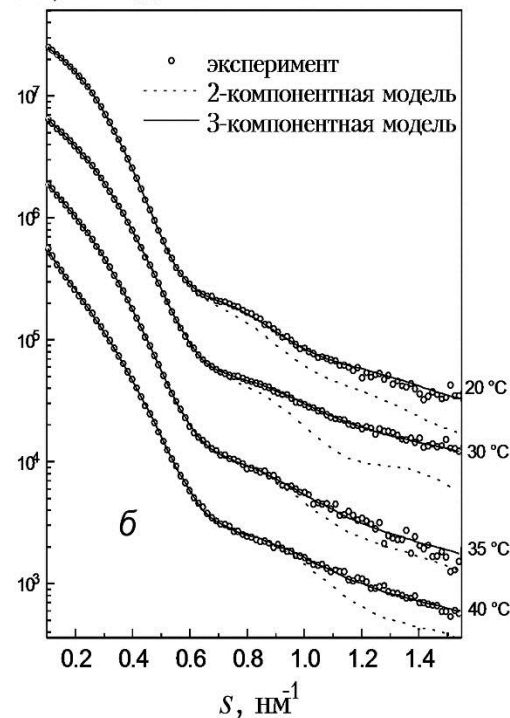


Typical shape of the combined volume distribution

$I(s)$, отн.ед.



$I(s)$, отн.ед.



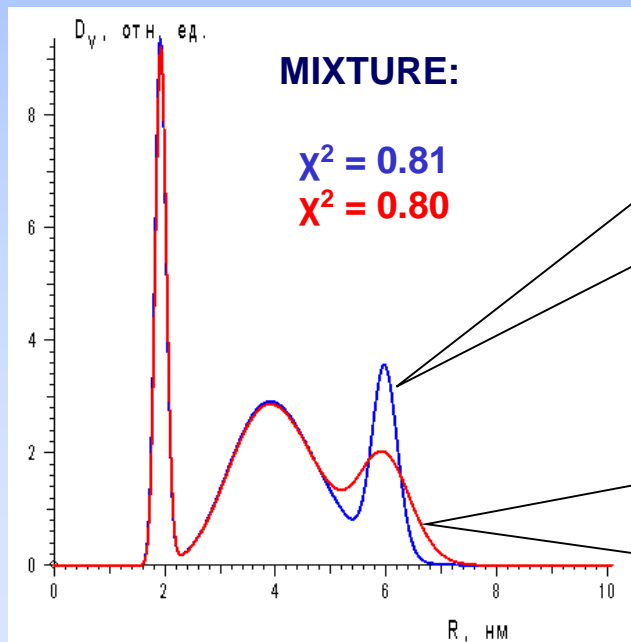
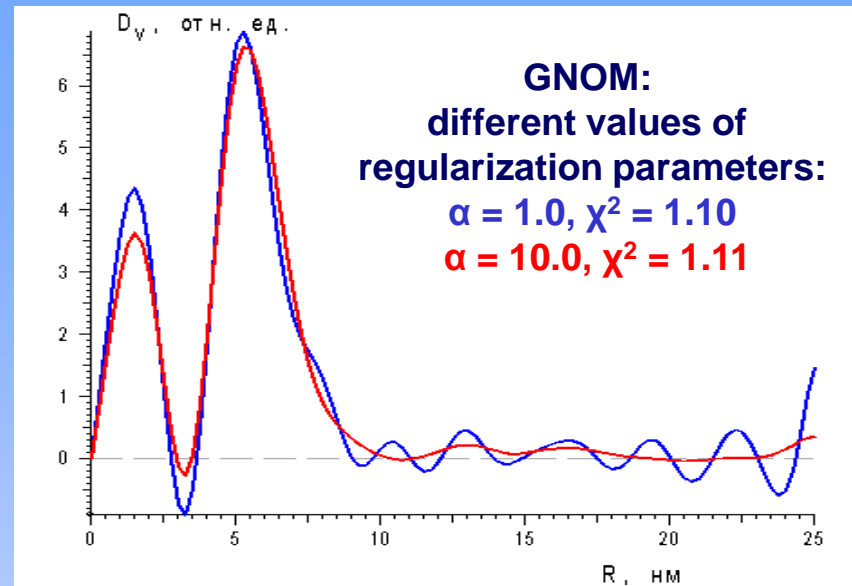
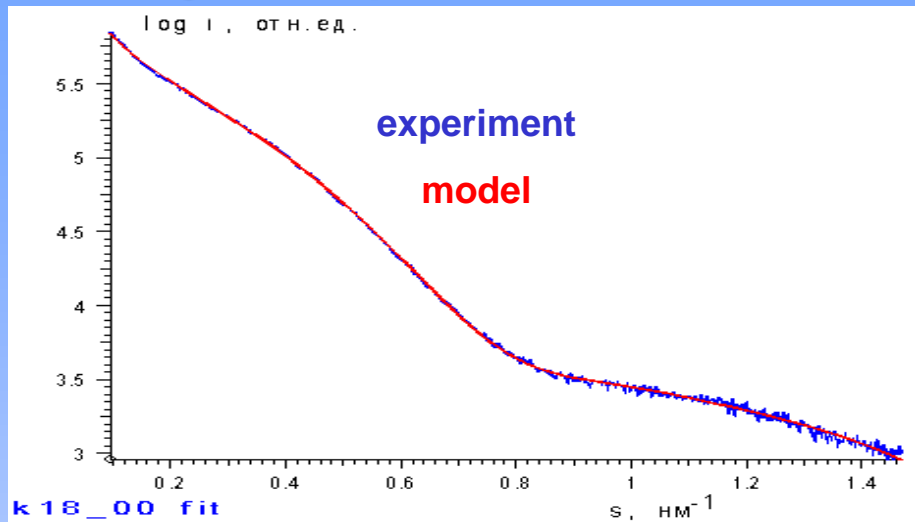
Typical fits to the experimental data.

Point: experiment;

dashed lines: 3-component model without AOT aggregates;

solid lines (coincide with experimental scattering): complete 4-component model

To overcome the problem of poor stability of solutions one may compare solution obtained at different conditions



Minimization of chi-square

$$\chi^2 = \frac{1}{M-1} \cdot \sum_{j=1}^M \left[\frac{I_{\text{эксп}} - I_{\text{теор}}}{\sigma_j} \right]^2$$

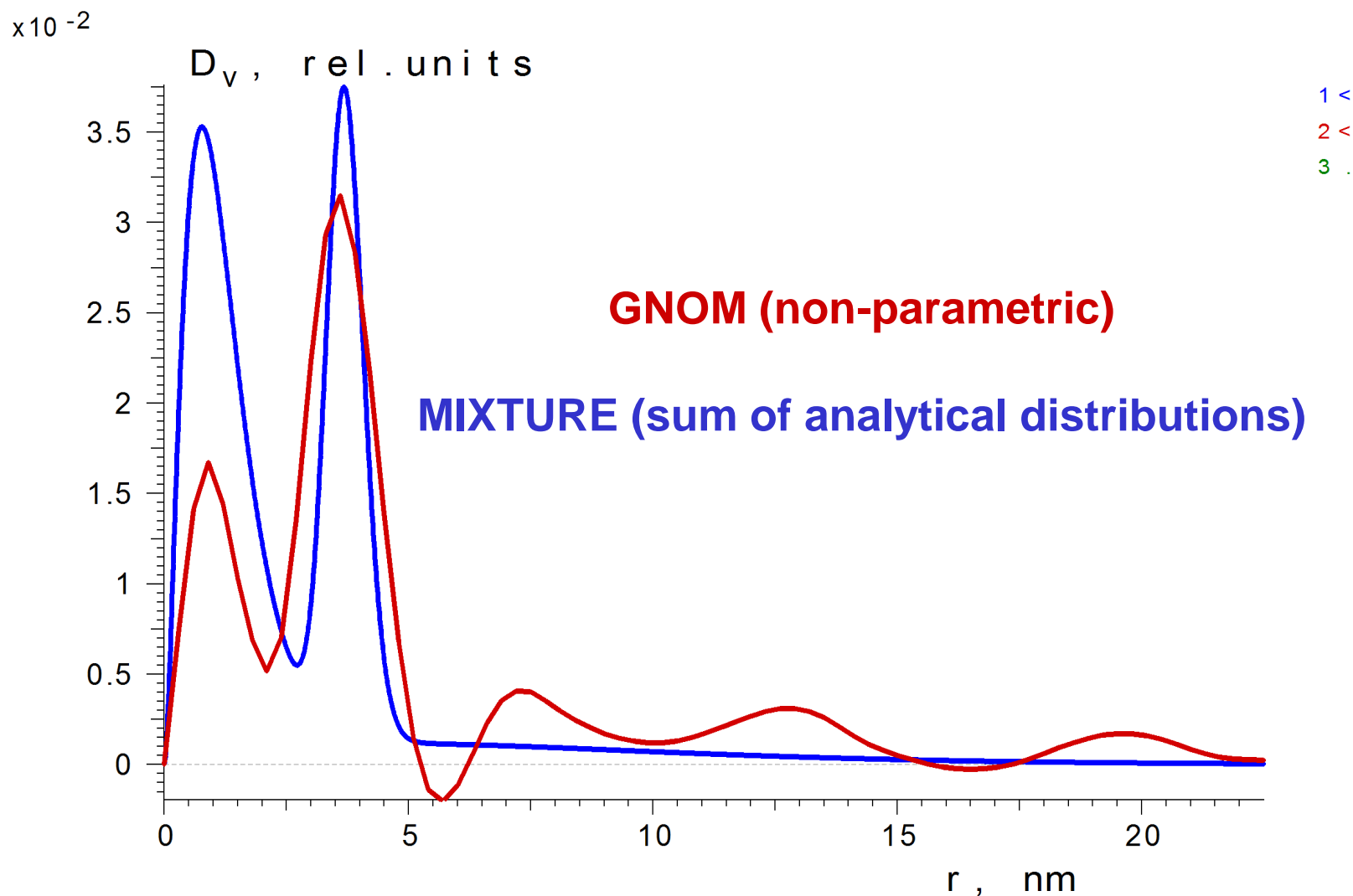
Minimization of R-factor

$$R^2 = \frac{1}{\|I_{\text{эксп}}\|^2} \cdot \sum_{j=1}^M \left[\frac{I_{\text{эксп}} - I_{\text{теор}}}{\sqrt[2/3]{I_{\text{эксп}}}} \right]^2$$

One may estimate the errors in solutions by -

- varying the regularization parameter,
- calculation of distribution using different angular ranges of weights applied to SAS data.

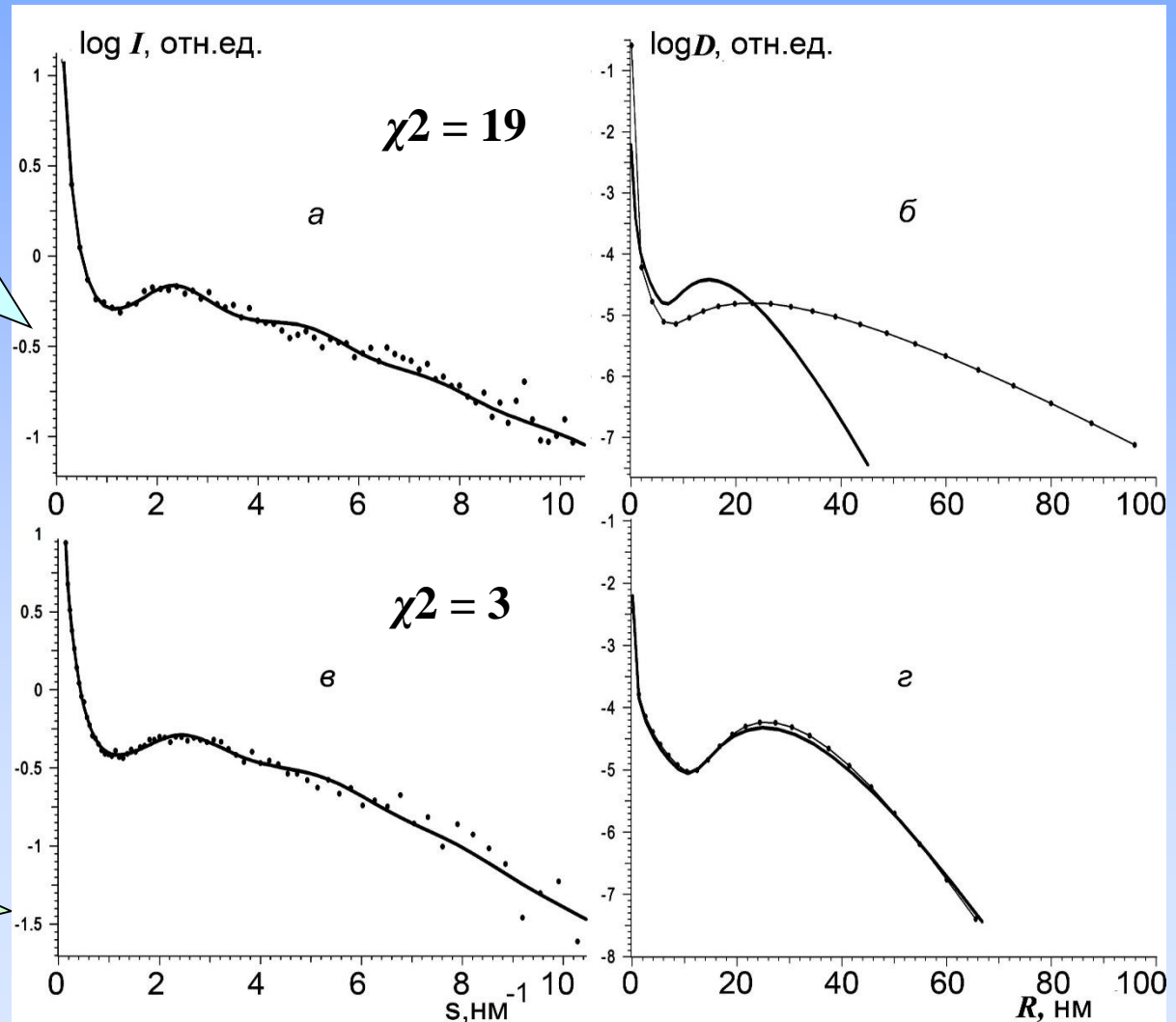
GNOM vs MIXTURE



Enhancing the solution stability by using non-equidistant progressive sampling grid. The starting and trailing sizes of intervals may be set as $\Pi/4R_{g_{start}}$ and $\Pi/R_{g_{end}}$

In spite of large amount of data points (160) the solution is unstable. Left: the best fit. Right: two solutions obtained from different starting approximations.

Progressive grid: 80 points. The solution is stable.



Information content in the scattering data

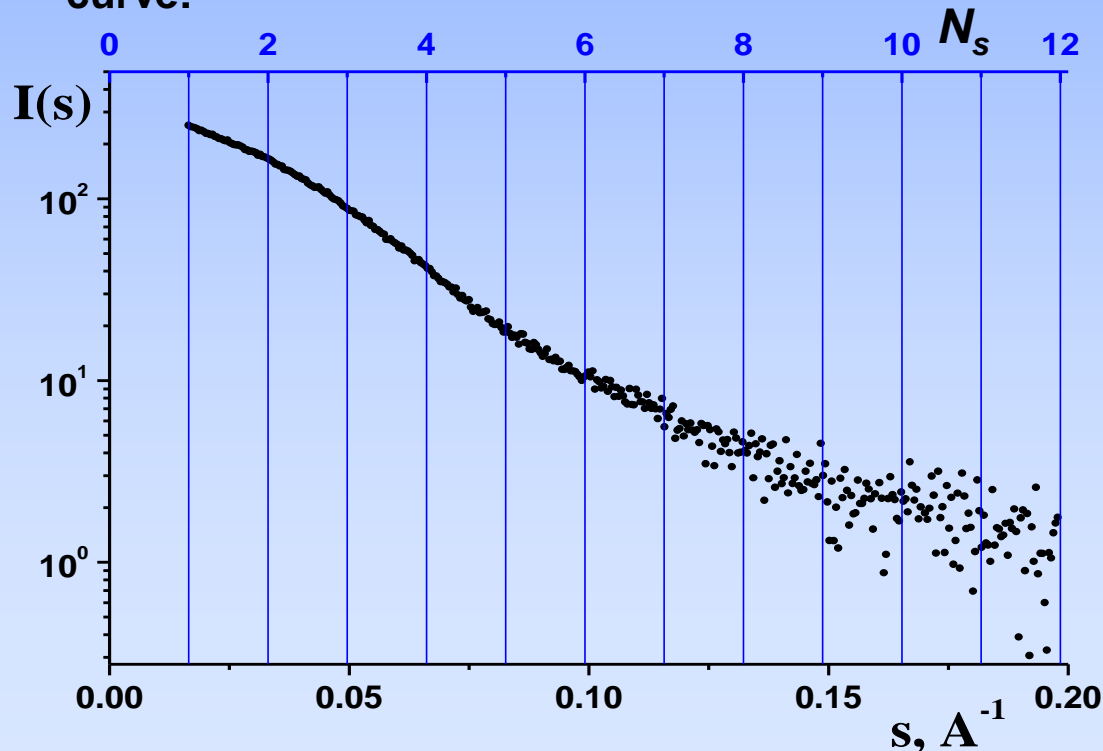
Conclusion from the Kotelnikov-Shannon theorem (theorem on sampling frequency):

number of independent parameters describing a SAS curve is approximately

$$N_s = s_{max} D_{max} / \pi,$$

where D_{max} is the maximum diameter of the particle. In practice, N_s is small, usually $10 \div 20$.

N_s specifies the maximum allowable sampling interval in the scattering curve:



Particle structure must be represented by low resolution model with small number (?) of independent parameters.

**Monodisperse systems (e.g.,
solutions of proteins,
identical polymer and inorganic
macromolecules,
metal and magnetite
particles,...)**

Scattering from a system of identical particles (dilute solution of protein molecules) – an overview

$$I_i(s) = \langle A^2(s) \rangle_{\Omega} = 4\pi \int_{r=0}^{\infty} r^2 \langle \rho(\mathbf{r}) \otimes \rho(\mathbf{r}) \rangle_{\omega} \frac{\sin(sr)}{sr} dr$$

Scattering intensity
from i -th particle
(molecule)

Correlation function (averaged self-convolution of the electron density)

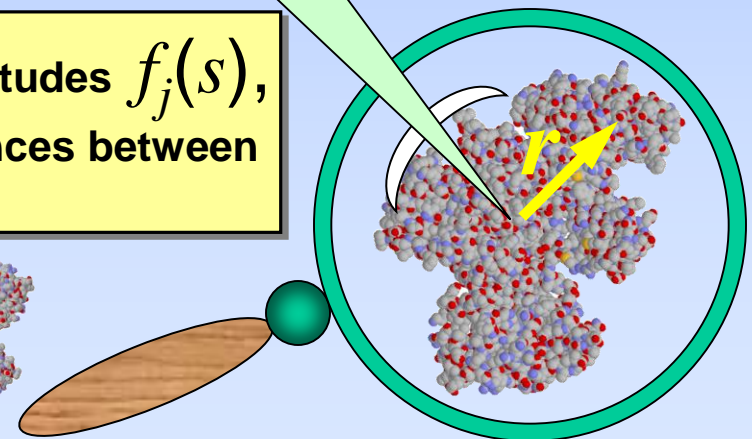
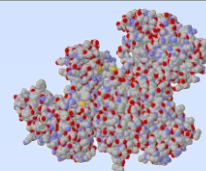
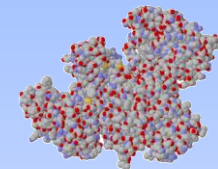
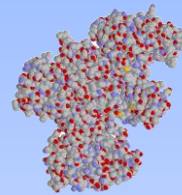
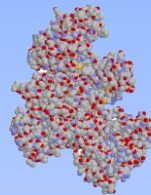
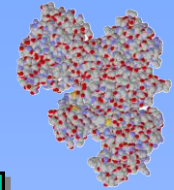
$$I_i(s) = \sum_j^N \sum_k^N f_j(s) f_k(s) \frac{\sin sr_{jk}}{sr_{jk}}$$

$$I_{total}(s) = \sum_{k=1}^M I_i(s)$$

N atom scattering amplitudes $f_j(s)$,
 $r_{jk} = r_j - r_j$ are the distances between
atoms

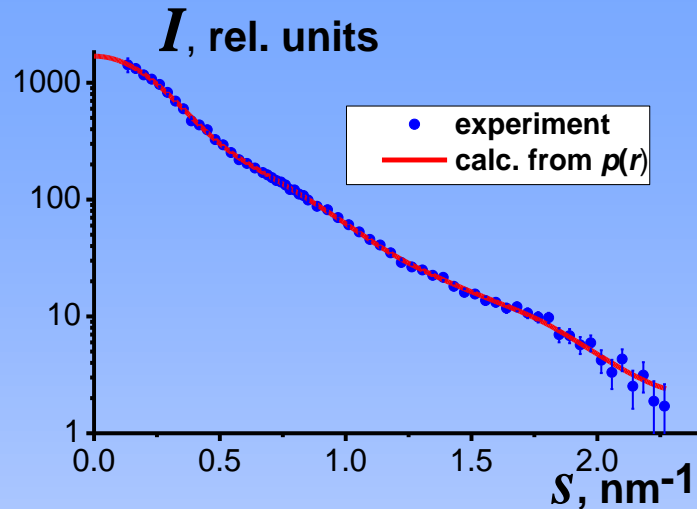
Scattering from the entire
sample: sum over all M
particles.

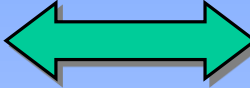
Structure
described by
electron
density
 $\rho(\mathbf{r})$

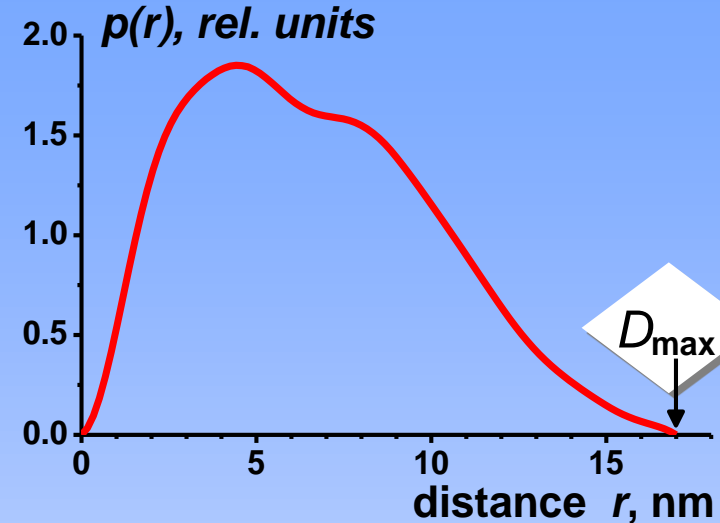


Unambiguous two-way street

calculation of $I(s)$ from known structures.



Fourier

transform
(unique)



$$I(s) = \langle I(s) \rangle_{\Omega} = 4\pi \int_{r=0}^{\infty} r^2 \gamma(r) \cdot \frac{\sin(sr)}{sr} dr$$

$$\gamma(r) = \langle P(\mathbf{r}) \rangle_{\omega} = \frac{1}{2\pi^2} \int_{s=0}^{\infty} s^2 I(s) \cdot \frac{\sin(sr)}{sr} ds$$

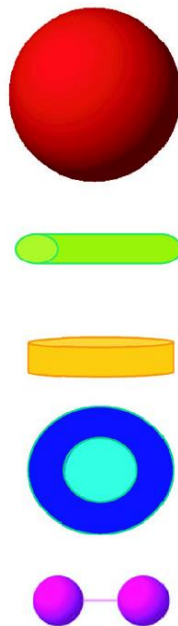
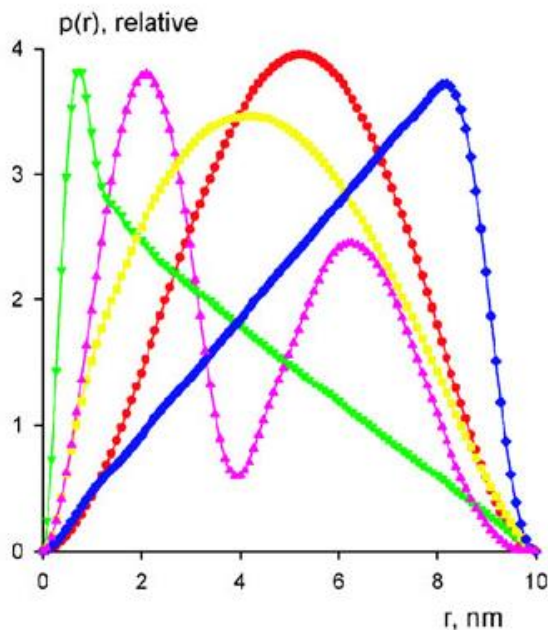
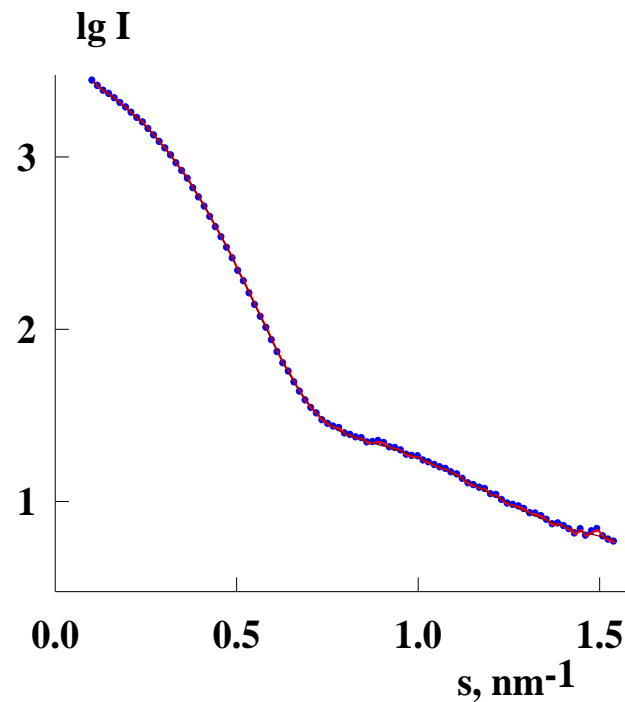
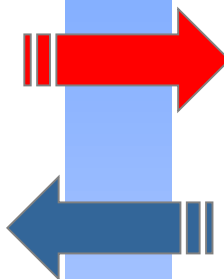
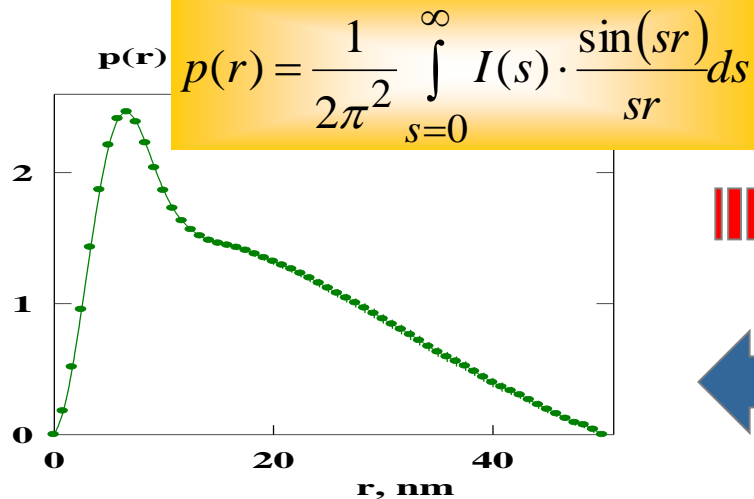
$I(s)$ defined in the reciprocal space is related by a Fourier transformation (i.e. in a unique way) only with the one-dimensional distance distribution function $p(r)$ in real space:

$$p(r) = r^2 \cdot \gamma(r)$$

$$\gamma(r) \Big|_{r=|r_1-r_2|=const} = \langle \rho(\mathbf{r}_1) \cdot \rho(\mathbf{r}_2) \rangle_{\omega} = \langle P(\mathbf{r}) \rangle_{\omega} = \frac{1}{4\pi} \int_{\omega=0}^{4\pi} P(\mathbf{r}) \cdot d\omega,$$

where $P(\mathbf{r}) = \int d\mathbf{r}_1 \cdot \rho(\mathbf{r}_1) \cdot \rho(\mathbf{r}_1 - \mathbf{r})$

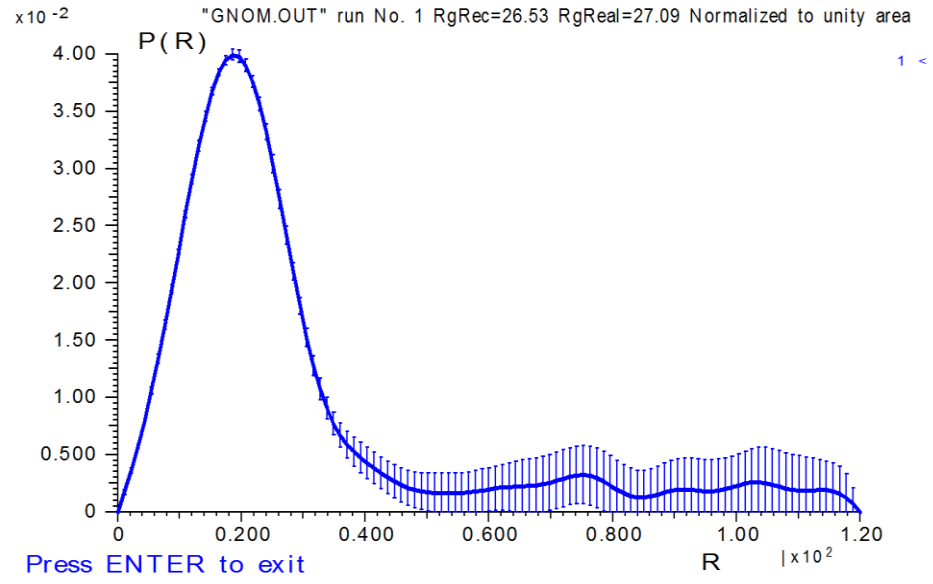
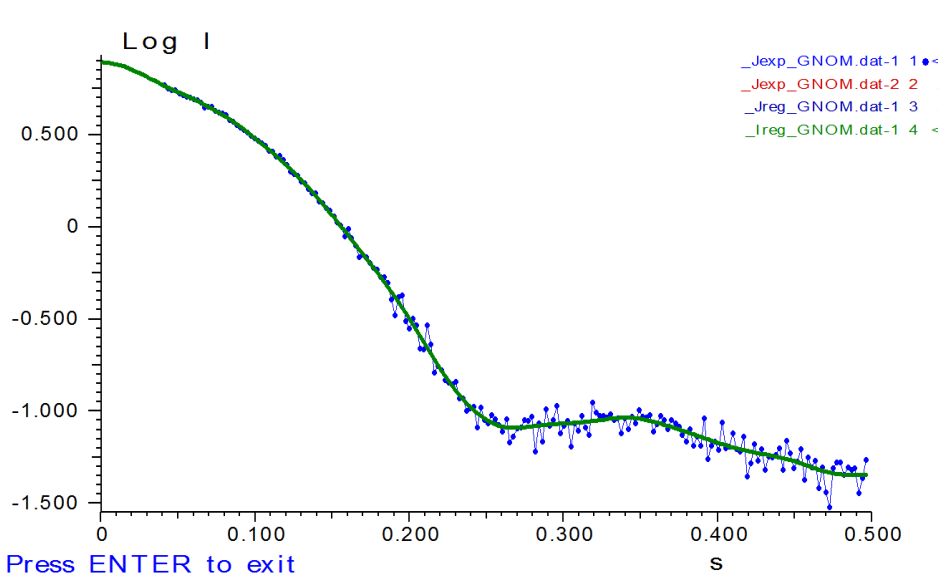
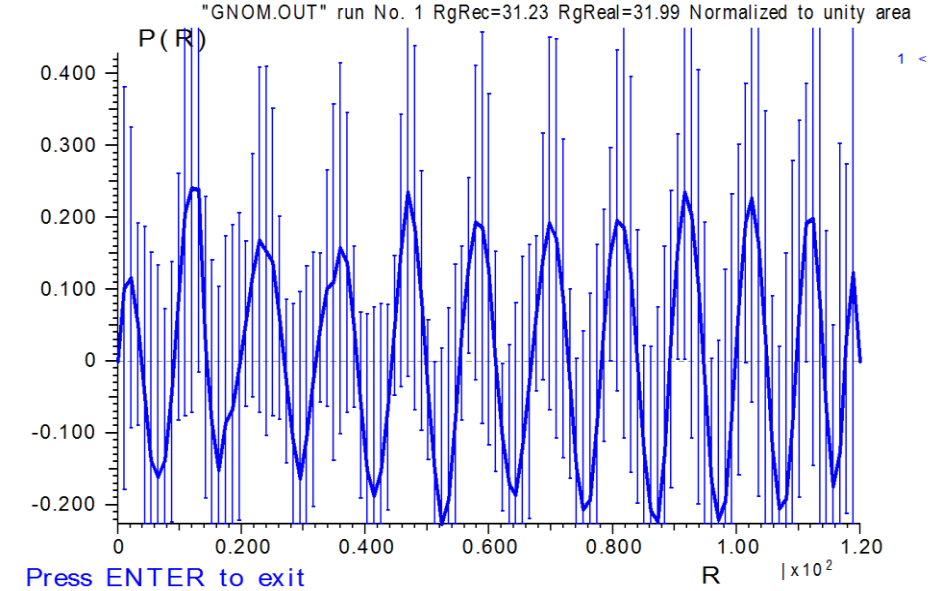
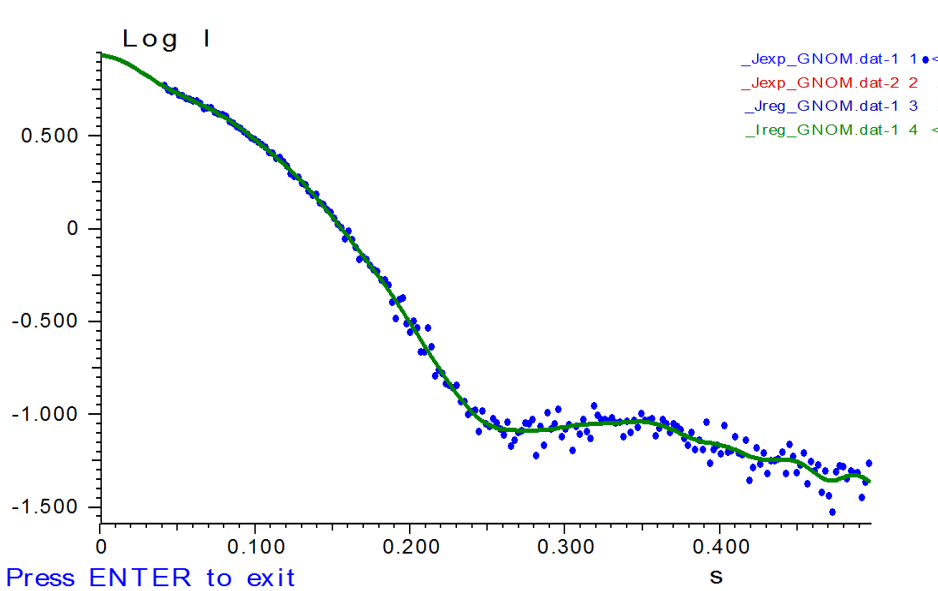
Indirect Fourier transform of SAS data gives us the pair distribution function (statistics of pair distances)



$$\min \left\{ \left\| I_{\text{exp}}(s) - I_{\text{calc}}(s) \right\|^2 + \alpha \left\| \frac{dp(r)}{dr} \right\|^2 \right\}$$

GNOM: a Program Package for Small-Angle Scattering
Data Processing / A.V. Semenyuk, D.I. Svergun // J.
Appl. Cryst. – 1991. – V. 24. – P. 537 – 540.

Indirect Fourier transform of SAS data gives us the pair distribution function (statistics of distances)



Structure invariants which may be calculated from scattering data (from dilute systems of identical particles)

$$I(s) = \langle I(s) \rangle_{\Omega} = 4\pi \int_{r=0}^{\infty} p(r) \cdot \frac{\sin(sr)}{sr} dr$$

$I(s) = I(0) \cdot \exp(-R_g^2 \cdot s^2 / 3)$ (Guinier approximation, $s R_g < 1.3$), **gyration radius (1)**

where $I(0) \sim N \cdot (V \cdot \rho)^2 \sim N \cdot M^2$;

volume (1) & density

$$R_g^2 = \frac{\int \rho(r) \cdot r^2 dr}{\int \rho(r) dr} = \frac{\int r^4 \cdot \gamma(r) dr}{2 \int r^2 \gamma(r) dr}$$

gyration radius (2)

$$V = 4 \cdot \pi \int r^2 \cdot \gamma(r) dr = 4 \cdot \pi \int p(r) dr;$$

volume(2)

$$S = \lim \{4 V [(1 - \gamma_0(r))/r]\}$$

surface area

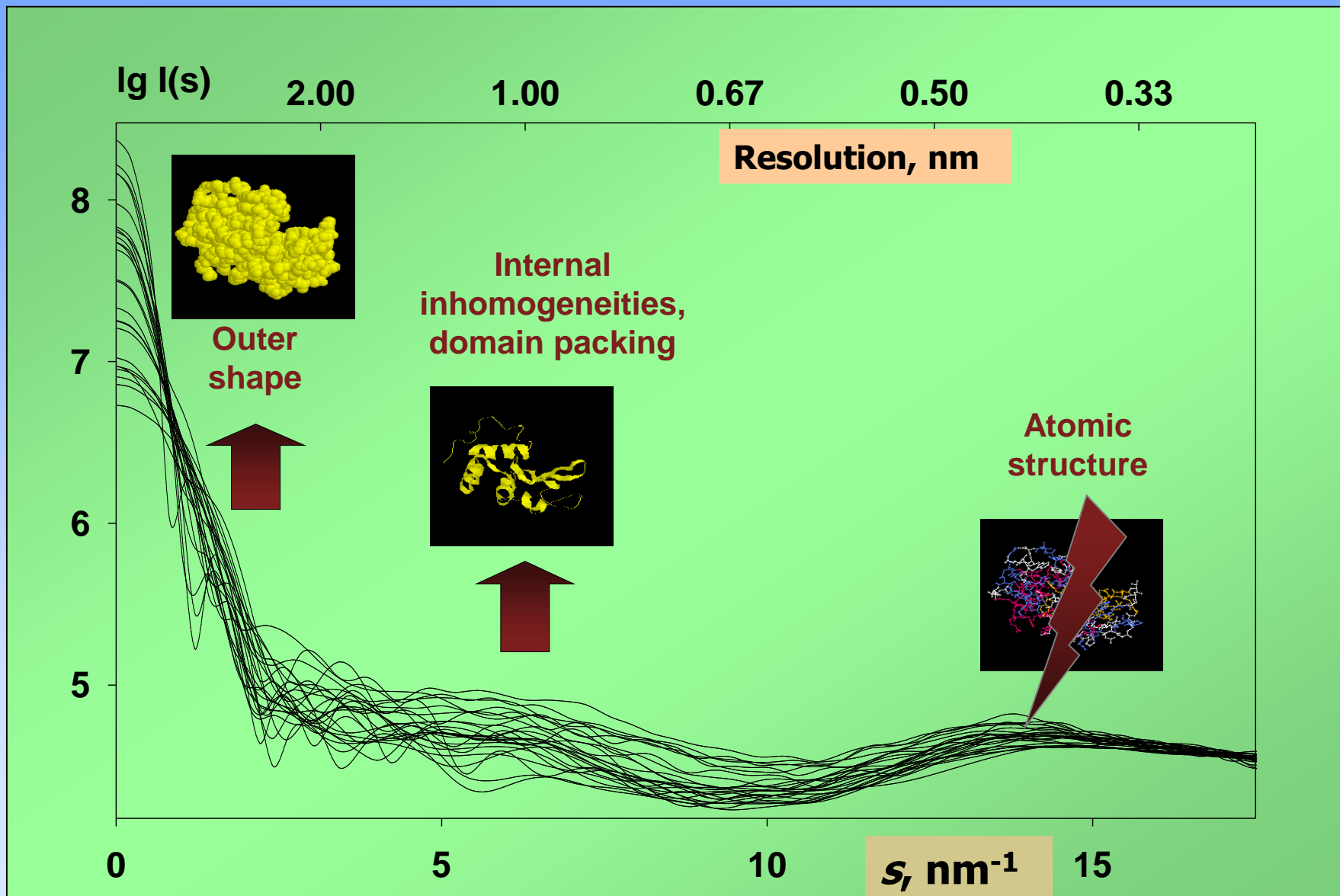
$$l_m = 2 \int \gamma_0(r) dr;$$

mean size

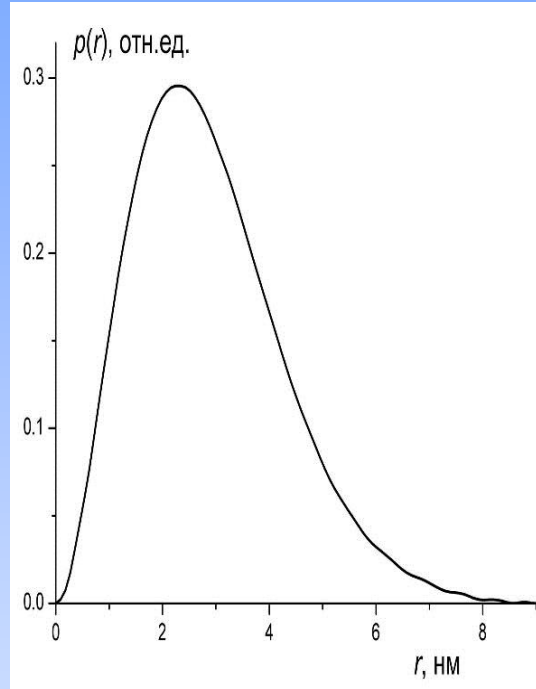
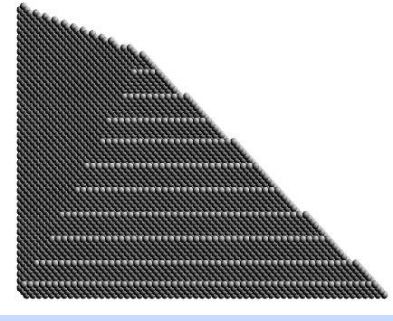
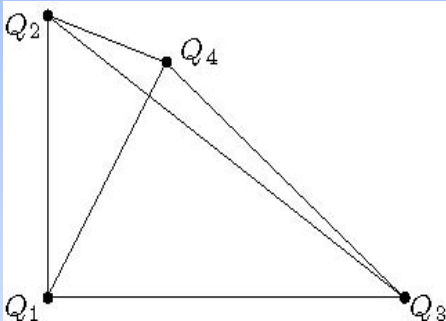
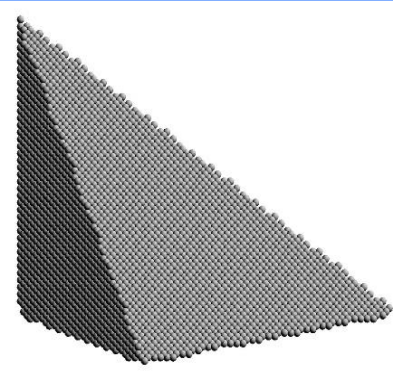
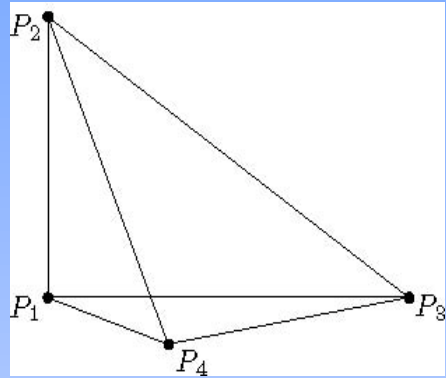
$$D_{\max}$$

maximum size (from p(r))

SAS: information contents



Ambiguity of shape determination: an example



**These two
structures
are different!**

**Pair
distribution
functions
coincide!**

$$p(r) = \frac{r^2}{2\pi^2} \int_0^{\infty} s^2 I(s) \frac{\sin(sr)}{sr} ds$$

The pair distribution function is calculated from $I(s)$ in a unique way.

Then - all the structure invariants:

- Radius of gyration R_g ,
 - particle volume V ,
 - maximum diameter $D_{\text{макс}}$ -
- are defined by $I(s)$ uniquely.

Shape parametrization by spherical harmonics: program SASHA

Homogeneous particle

$F(\omega)$ is an envelope function

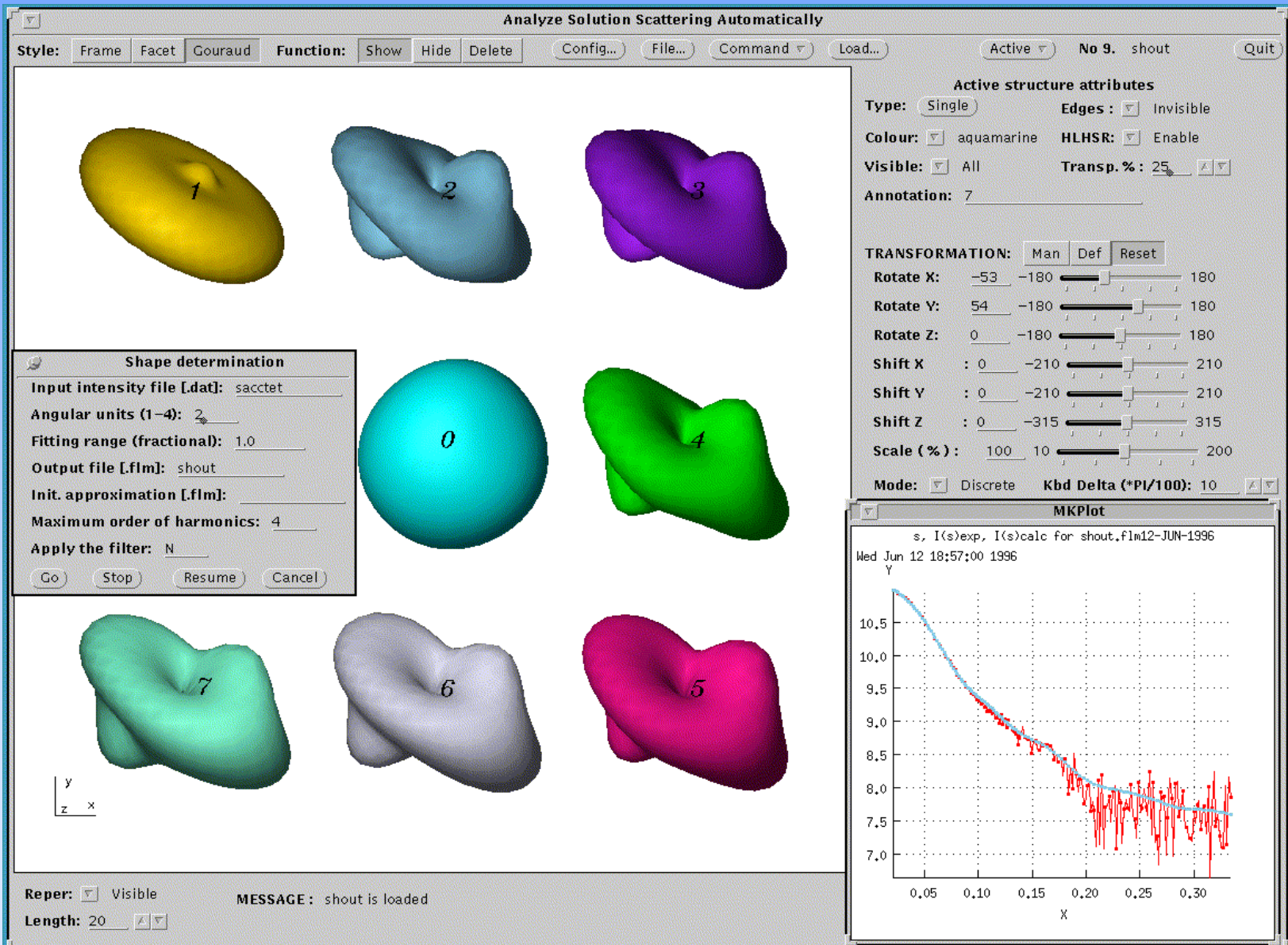
$$\begin{aligned}
 &= f_{00} A_{00}(s) + f_{11} A_{11}(s) + f_{20} A_{20}(s) + f_{22} A_{22}(s) + \dots
 \end{aligned}$$

Spatial resolution: $\delta = \frac{\pi R}{(L+1)}$, R – radius of an equivalent sphere.

Number of model parameters f_{lm} is $(L+1)^2$.

One can easily impose symmetry by selecting appropriate harmonics in the sum. This significantly reduces the number of parameters describing $F(\omega)$ for a given L .

Program SASHA



Checking for solution uniqueness: what will happen in the case of insufficient data contents?

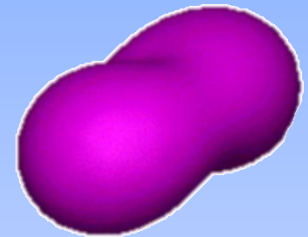
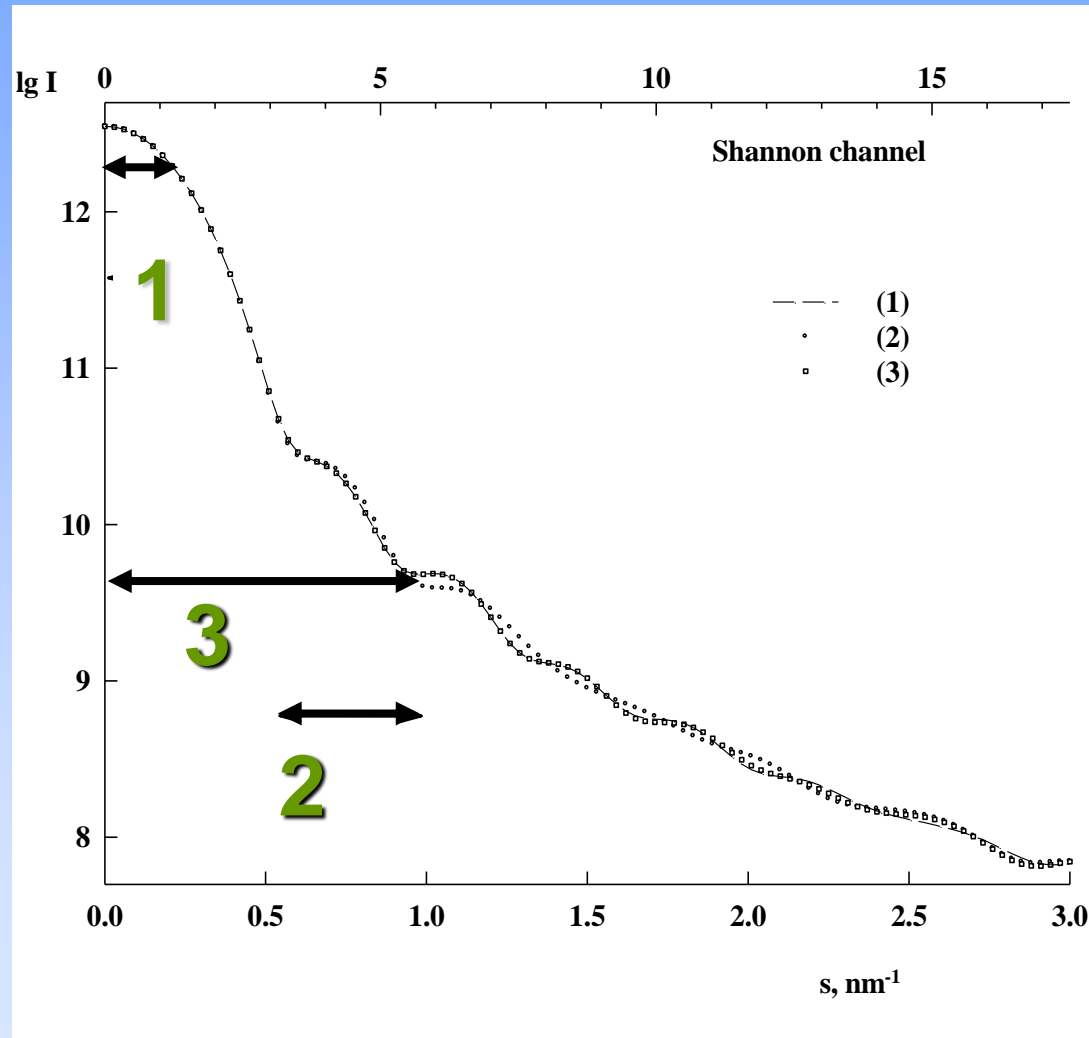
A numerical experiment:

Restoration of shapes from known model theoretical scattering.

**Region 1:
only 1
Shannon channel!**

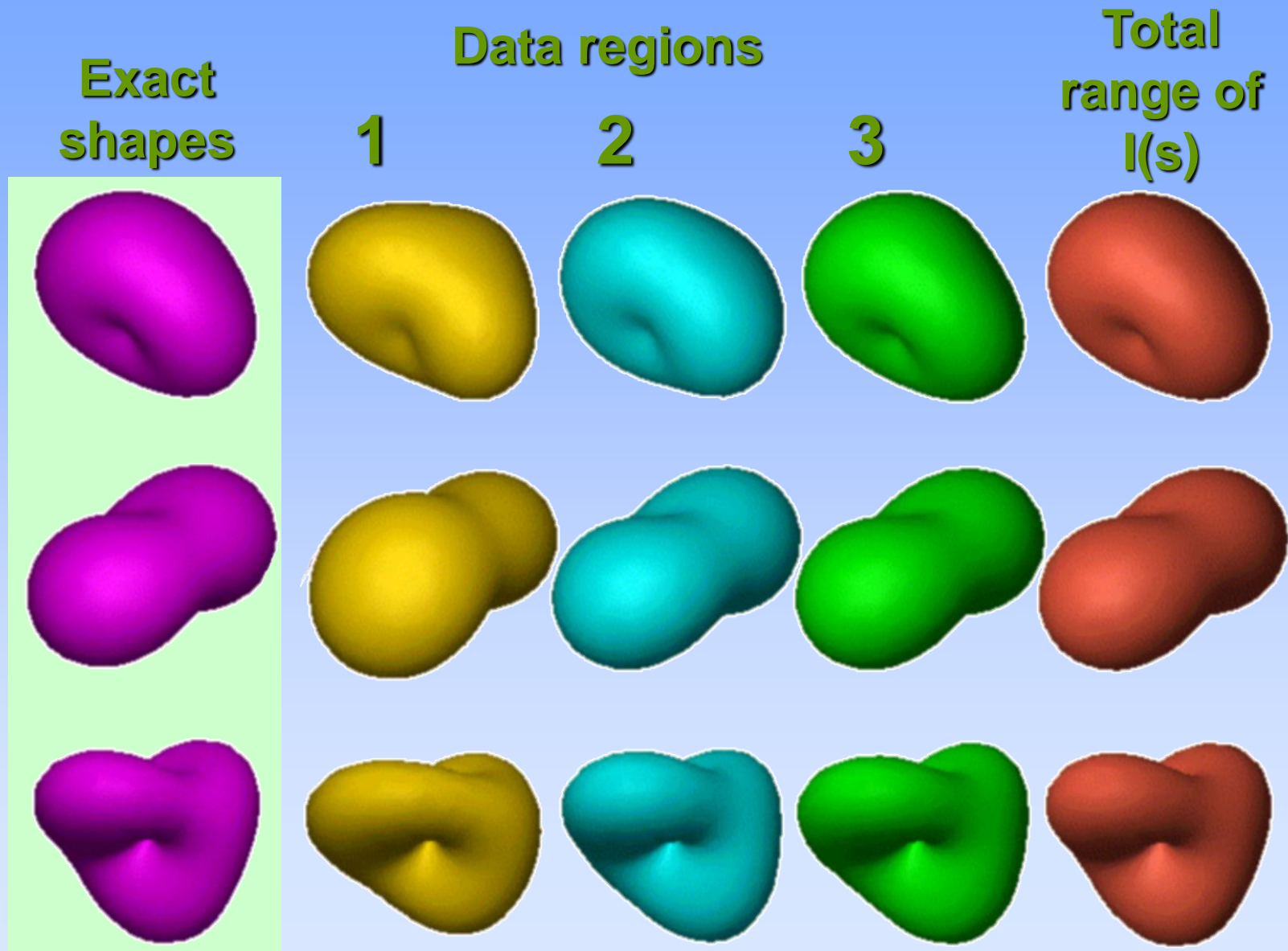
**Region 2:
internal short part**

**Region 3:
normal width.**



**Test bodies:
 $L_{\max}=3$,
 $16 - 6 = 10$
independent
parameters**

Restorations with $L_{\max}=3$ (10 independent parameters in the model, exact data)



The same conditions of restoration, but $I(s)$ with added 1 % rel. noise.

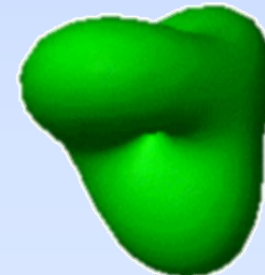
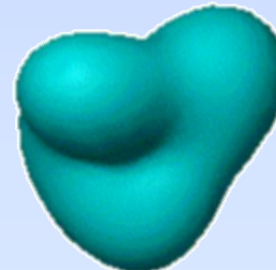
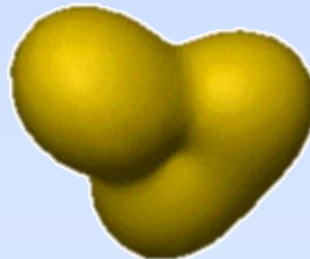
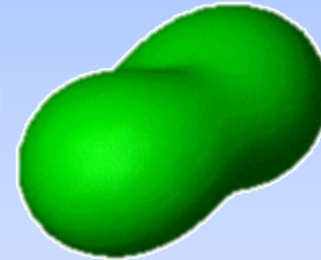
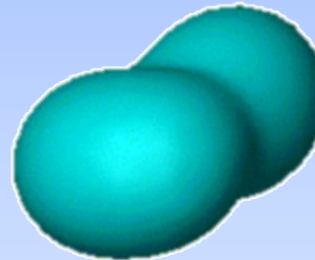
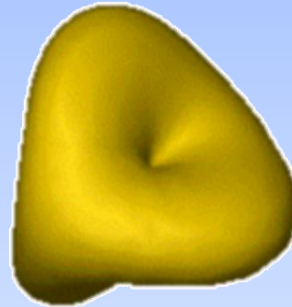
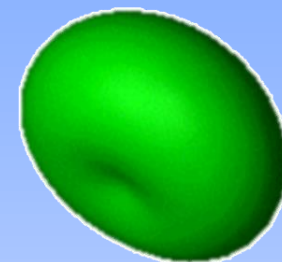
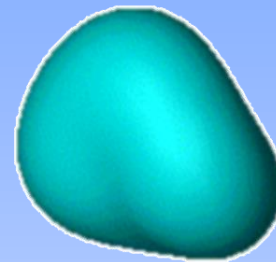
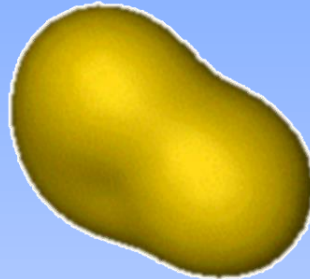
Exact
models

Regions of $I(s)$

1

2

3



Bead models: program DAMMIN

Using simulated annealing, finds a compact dummy atoms configuration x that fits the scattering data by minimizing

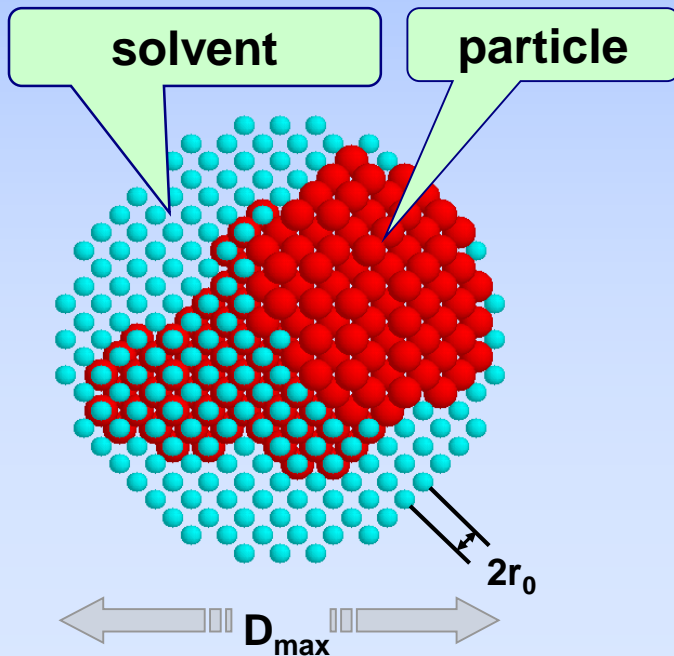
$$f(x) = \chi^2 [I_{\text{exp}}(s), I(s, x)] + \alpha P(x)$$

where χ is the discrepancy between the experimental and calculated curves, $P(x)$ are the penalties to ensure compactness and connectivity with weights $\alpha > 0$

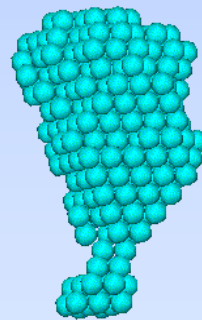
Scattering from a structure $I(s, x) = 2\pi^2 \sum_{l=0}^L \sum_{m=-l}^l |A_{lm}(s)|^2$

with the partial amplitudes $A_{lm}(s) = i^l \sqrt{2/\pi} \sum_j j_l(sr_j) Y_{lm}(\omega_j)$

and the sum running over atoms

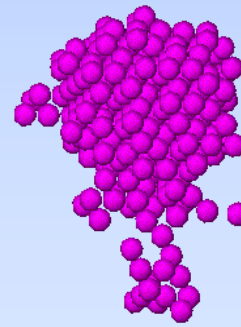


Must be:

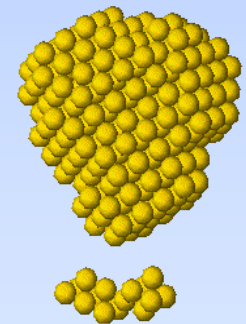


compact

Penalty terms for:



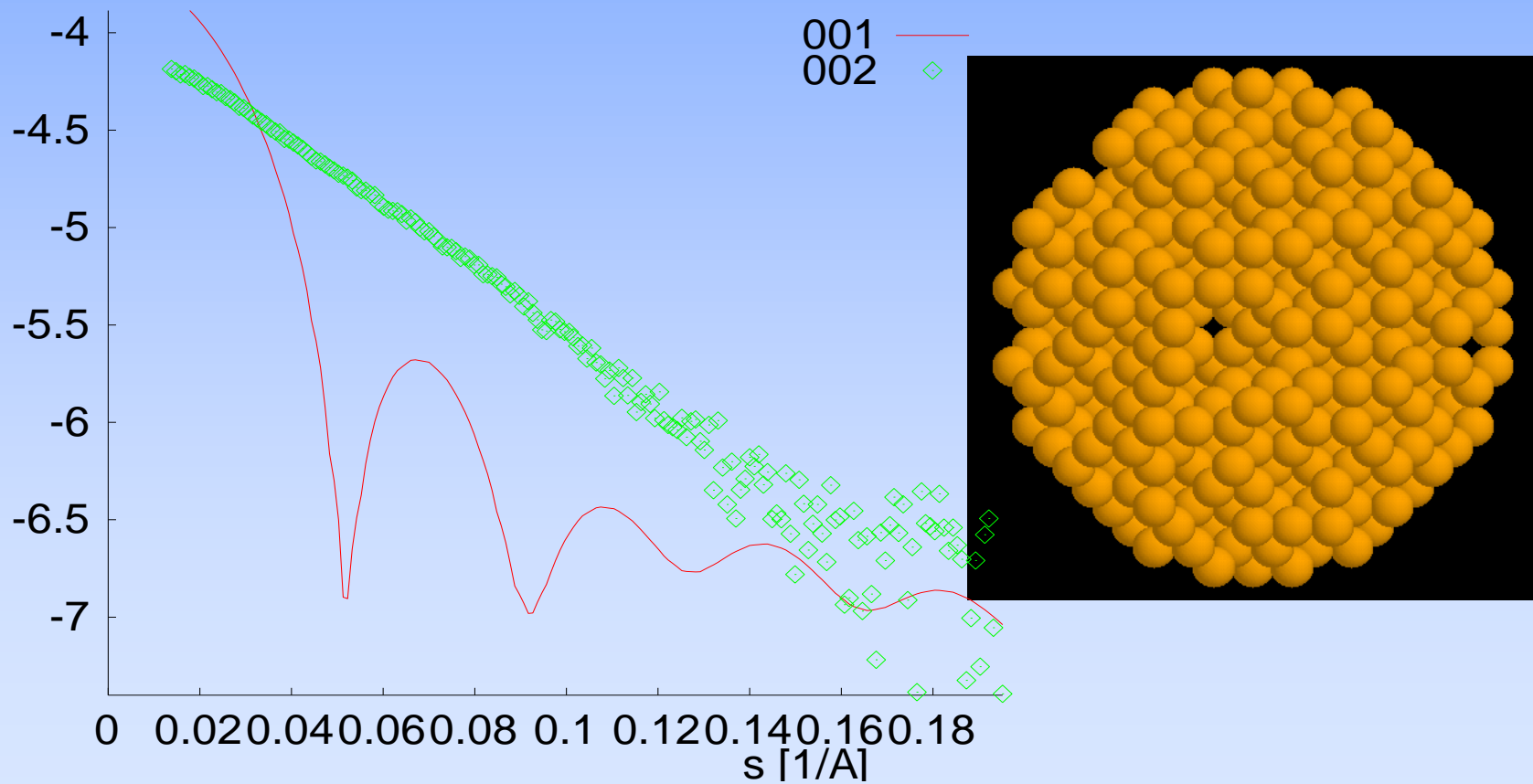
loose



disconnected

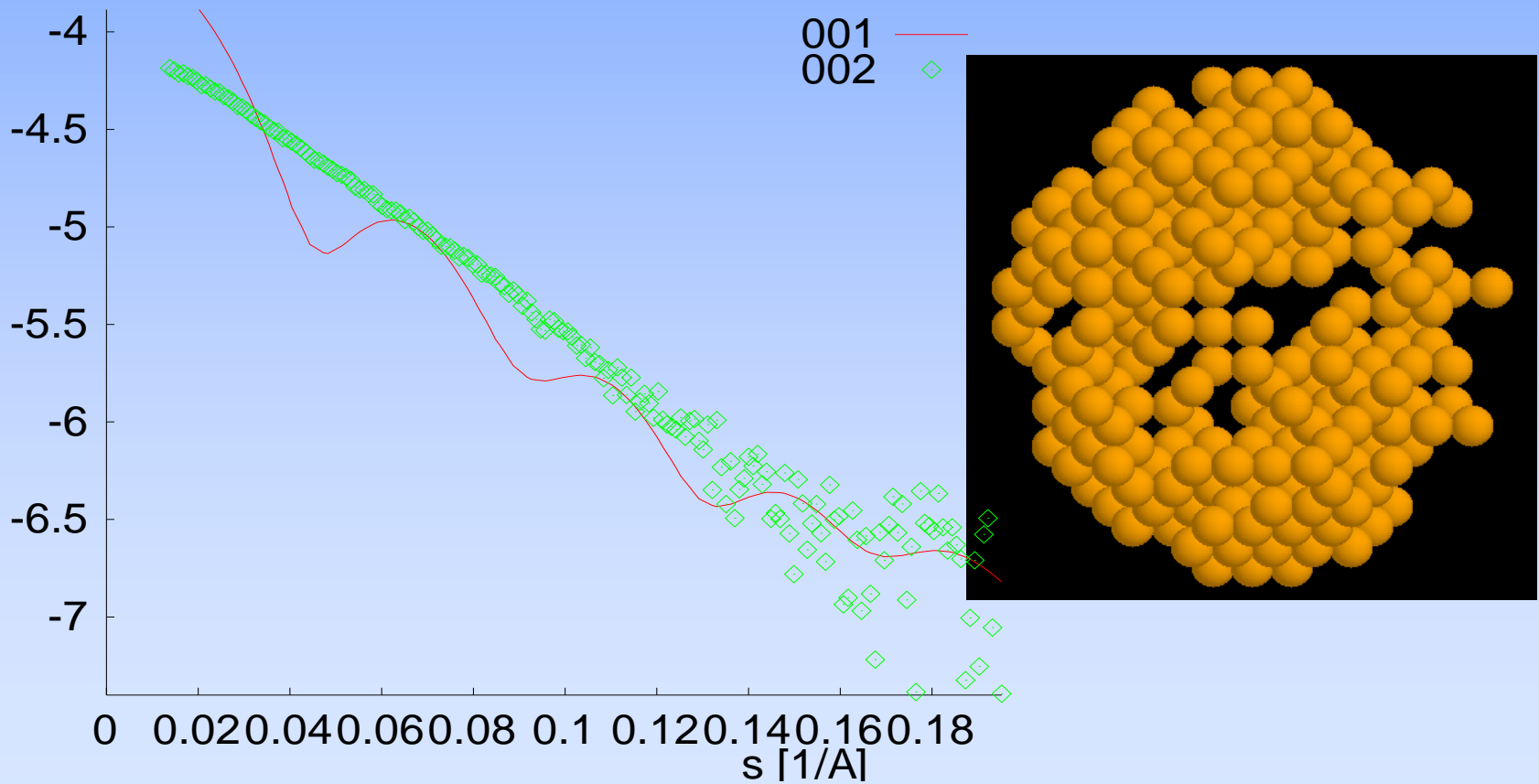
Case study: determination of structure of the myosin head S1

Step 0 Temperature = 0.100E-02 Chi= 36.38



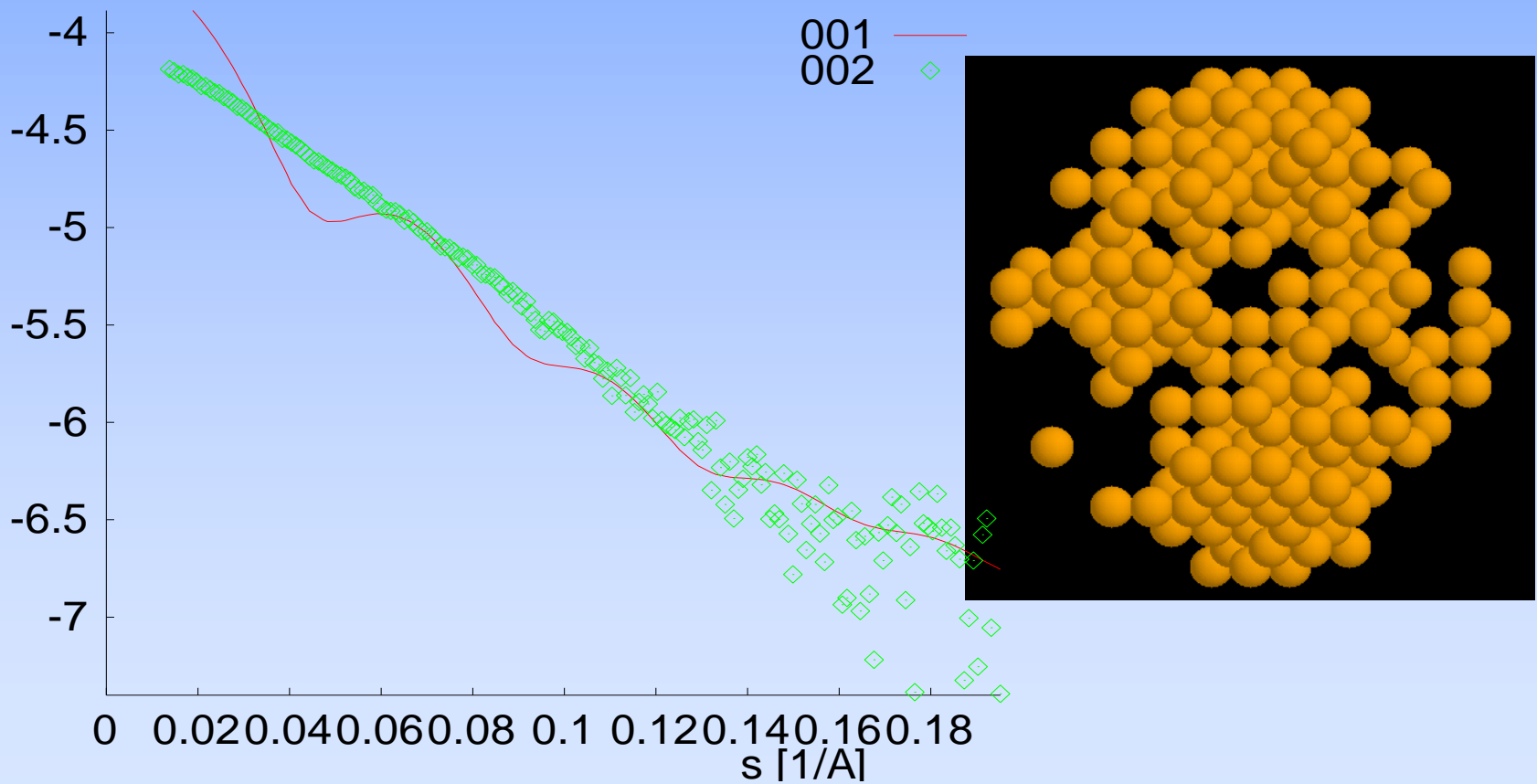
Case study: determination of structure of the myosin head S1

Step 1 Temperature = 0.100E-02 Chi= 37.47



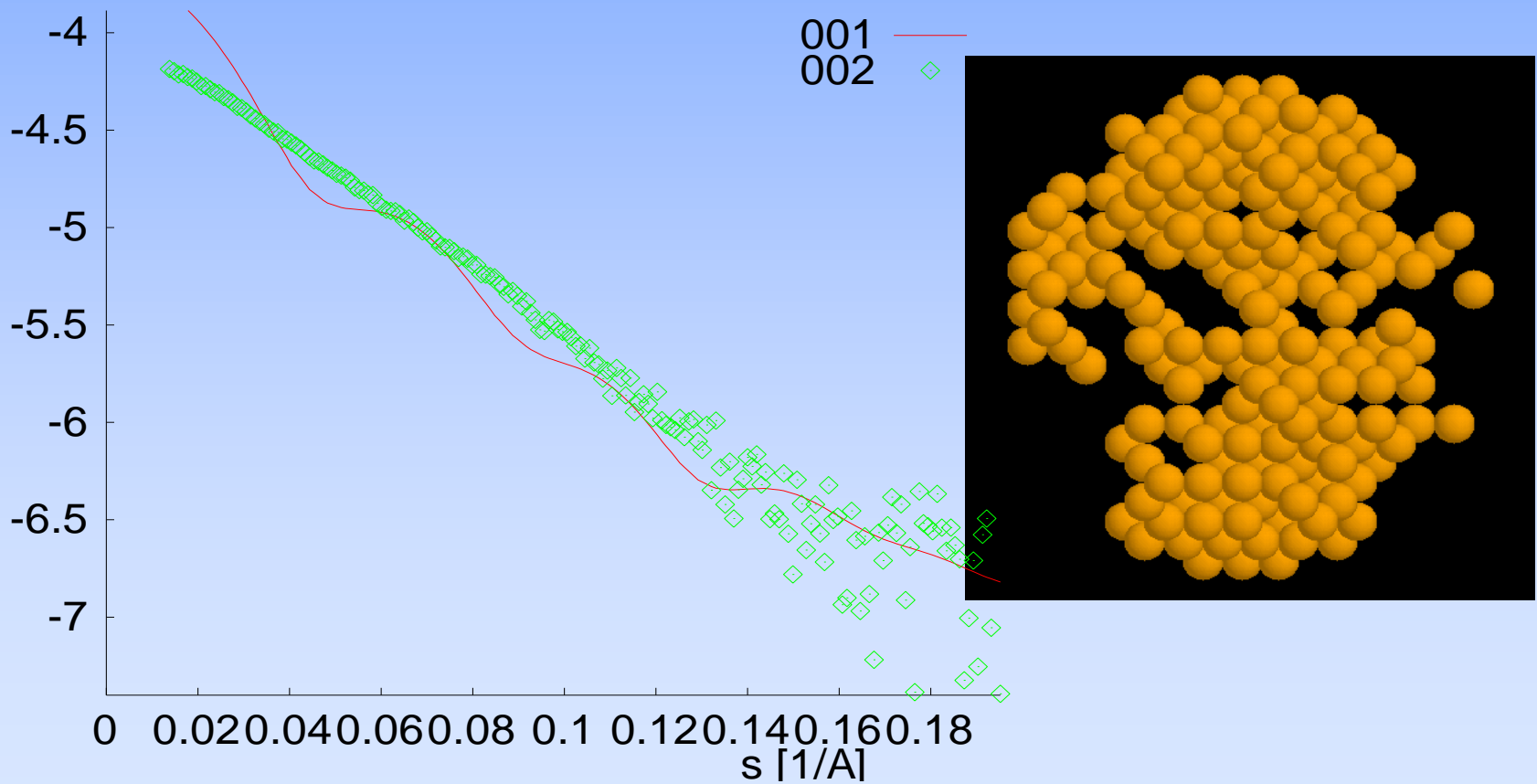
Case study: determination of structure of the myosin head S1

Step 2 Temperature = 0.900E-03 Chi= 31.57



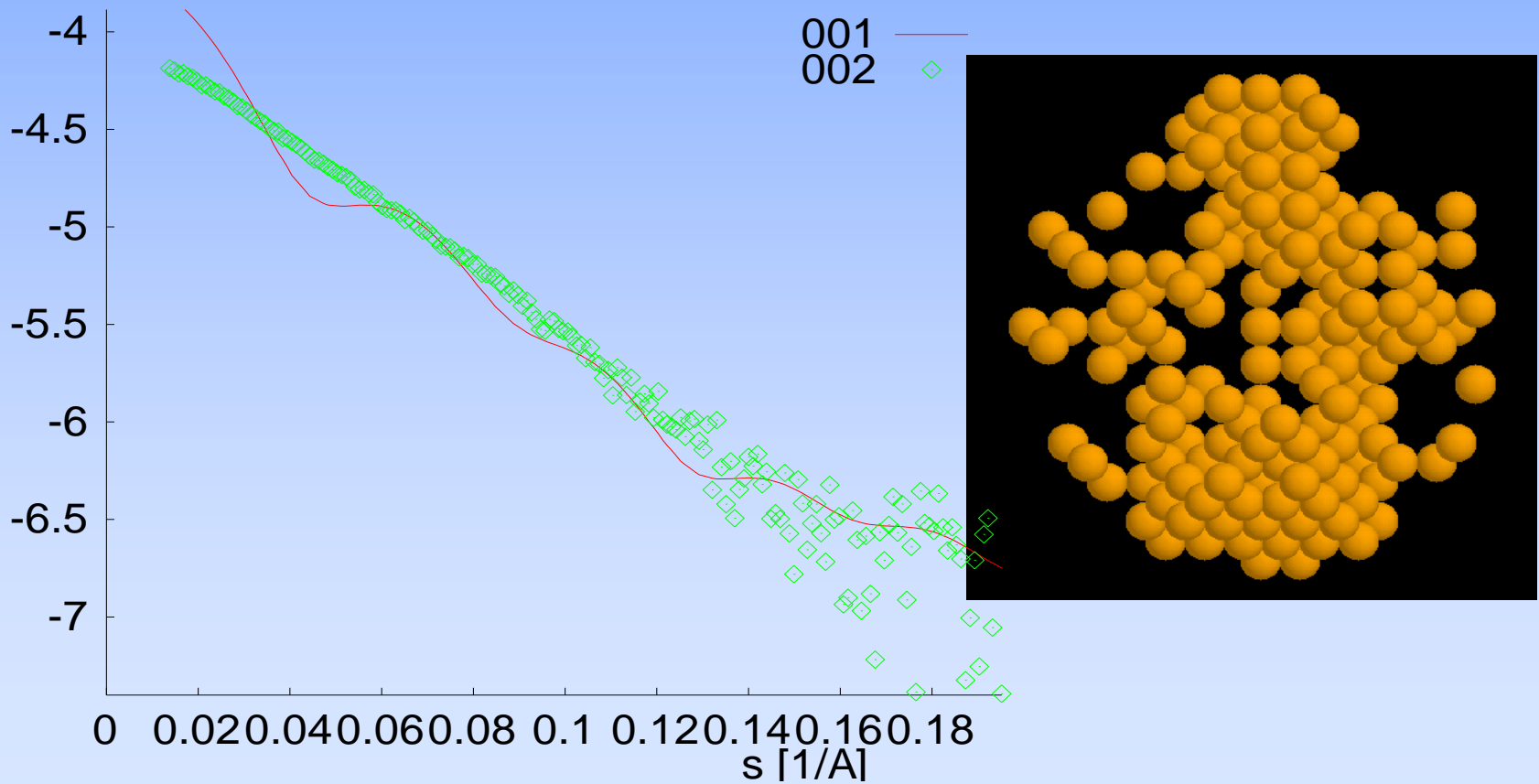
Case study: determination of structure of the myosin head S1

Step 3 Temperature = 0.810E-03 Chi= 28.21



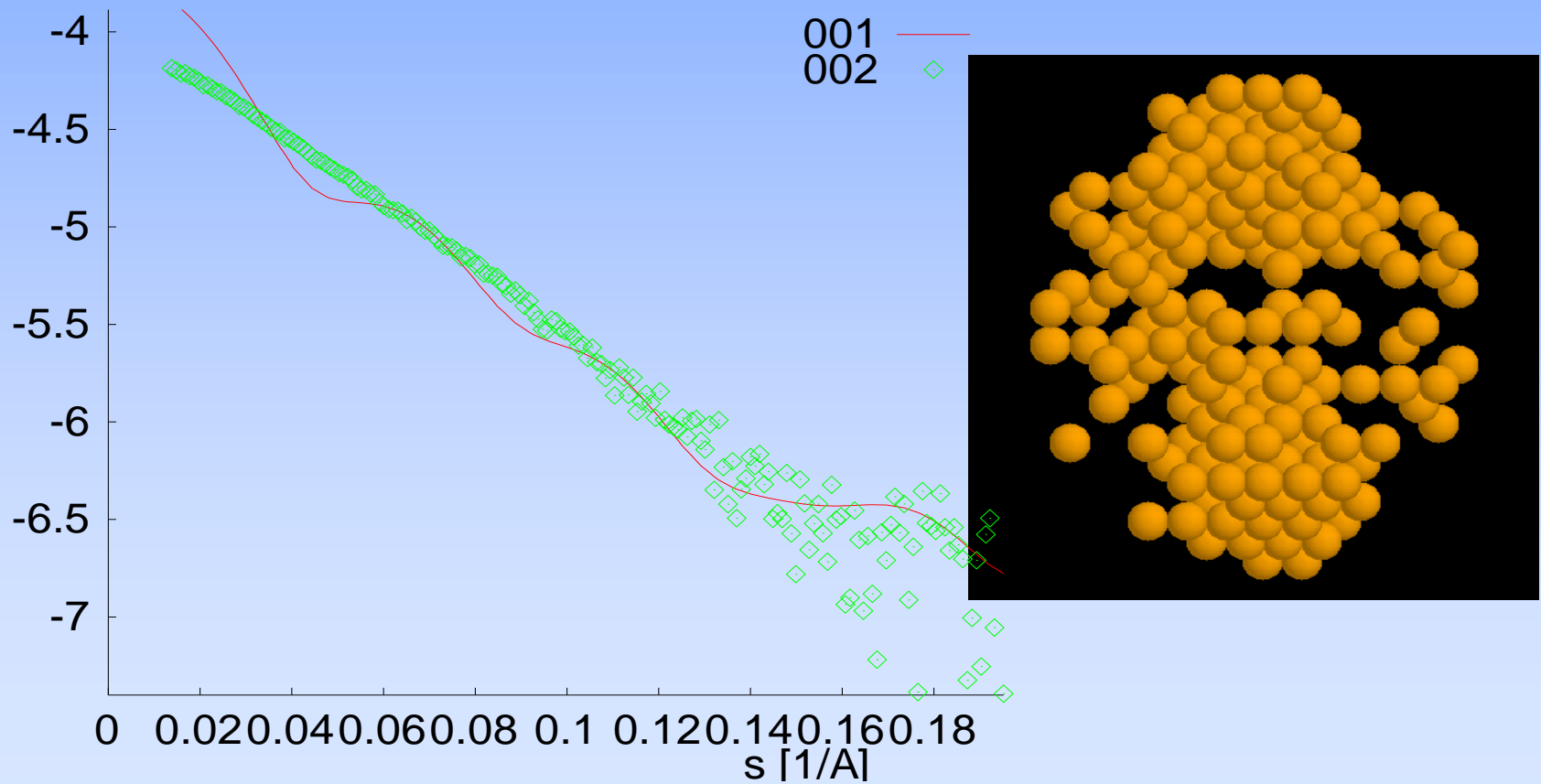
Case study: determination of structure of the myosin head S1

Step 4 Temperature = 0.729E-03 Chi= 26.08



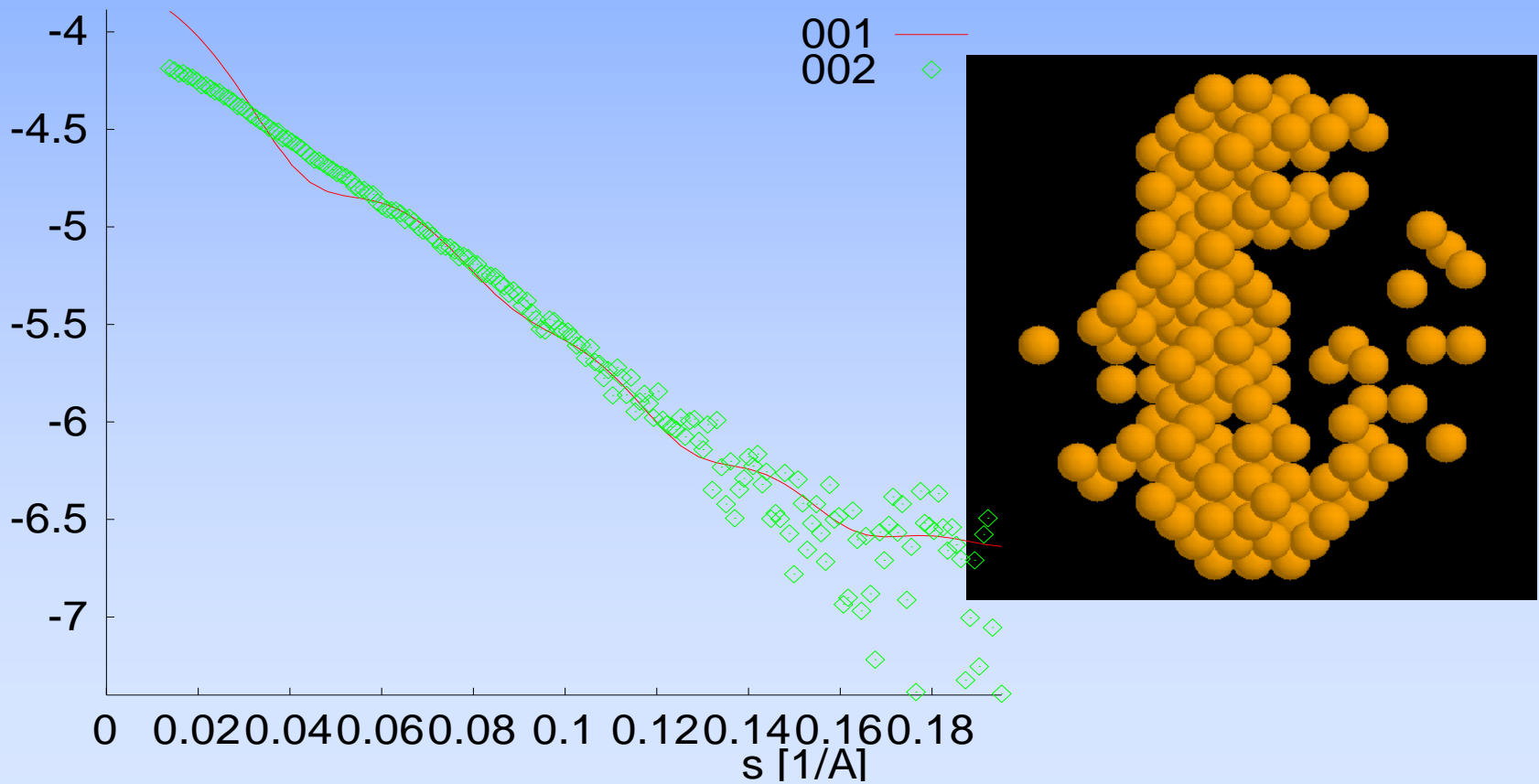
Case study: determination of structure of the myosin head S1

Step 5 Temperature = 0.656E-03 Chi= 23.54



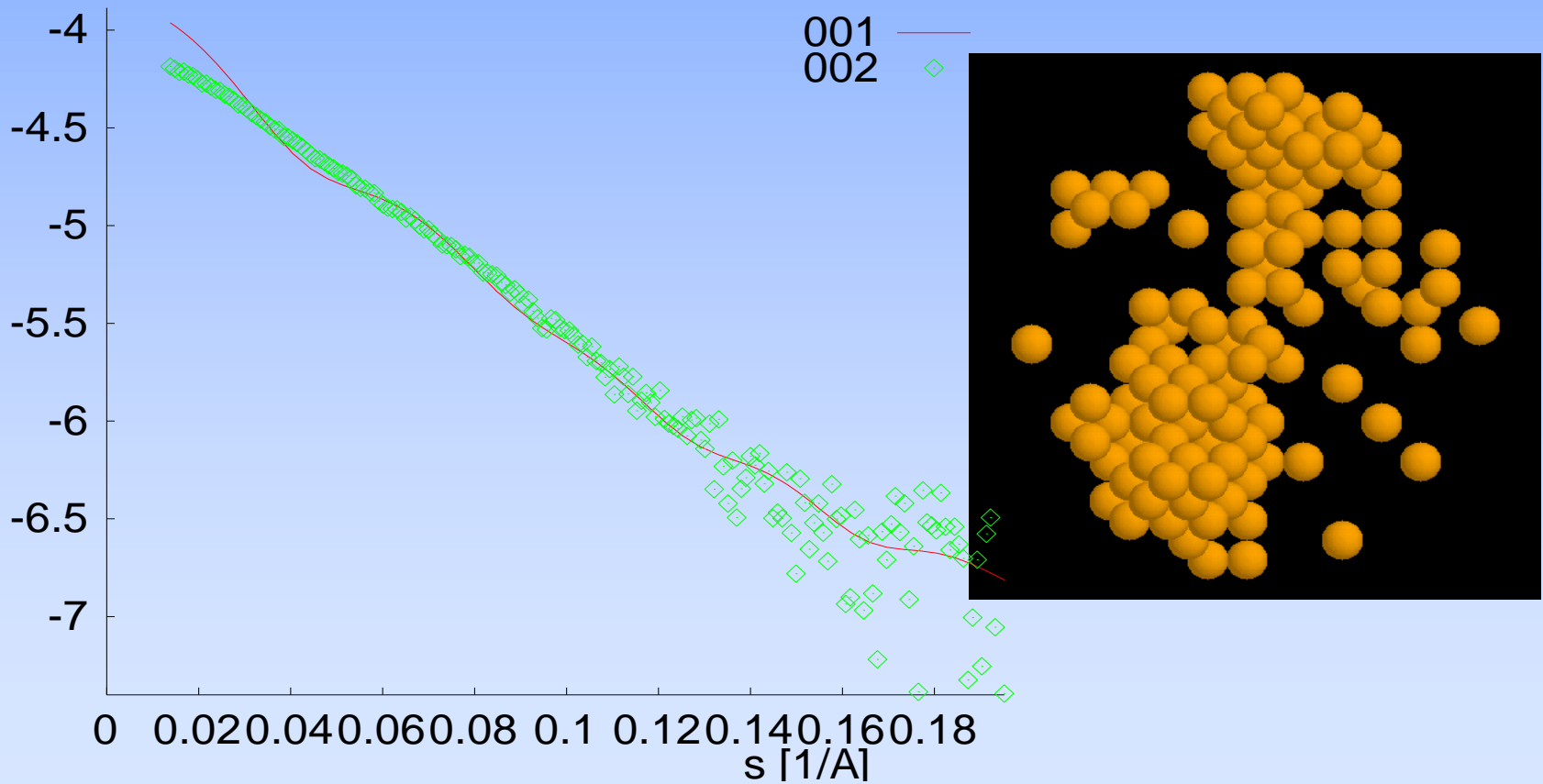
Case study: determination of structure of the myosin head S1

Step 8 Temperature = 0.478E-03 Chi= 18.51



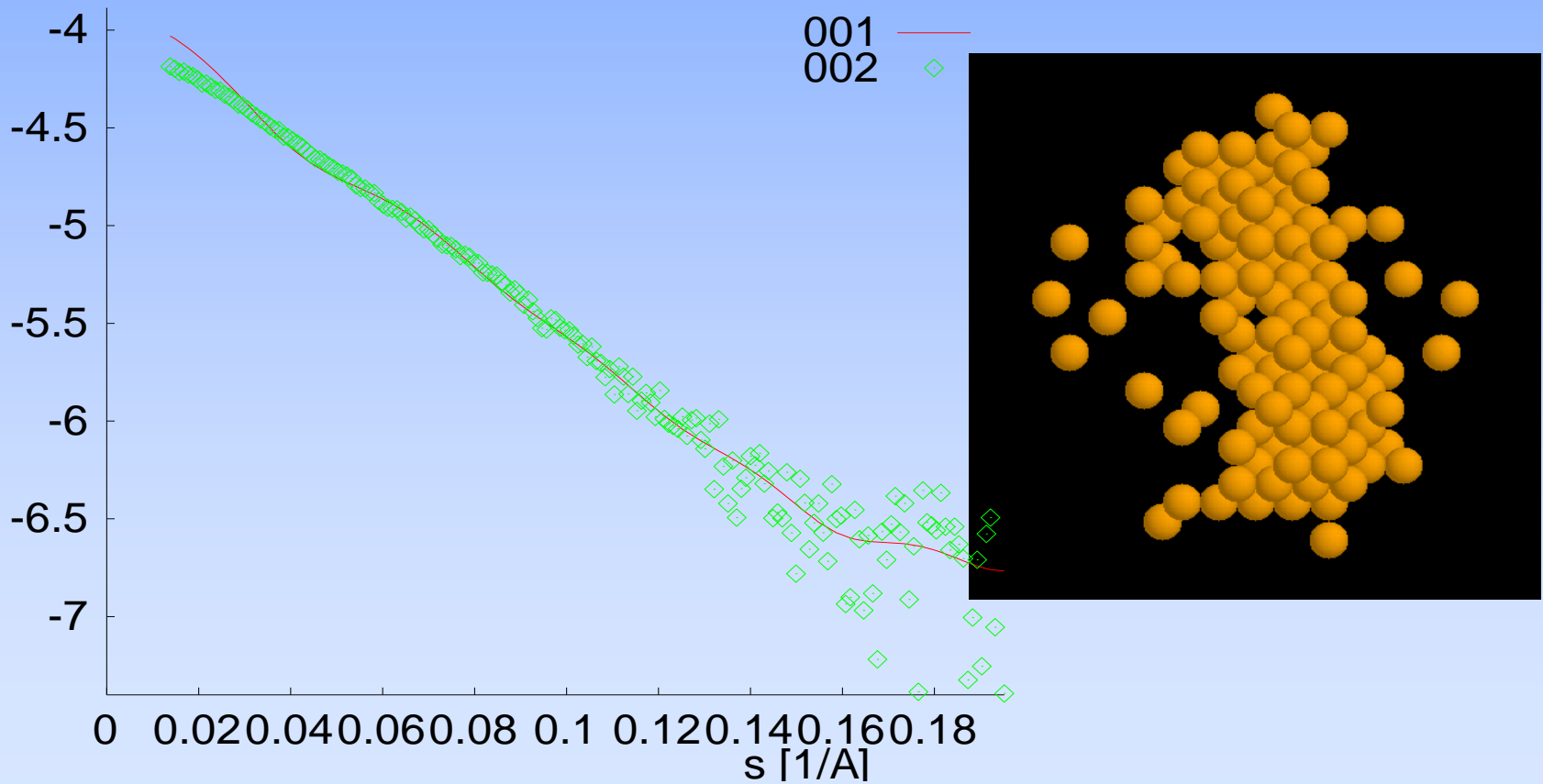
Case study: determination of structure of the myosin head S1

Step 11 Temperature = 0.349E-03 Chi= 13.11



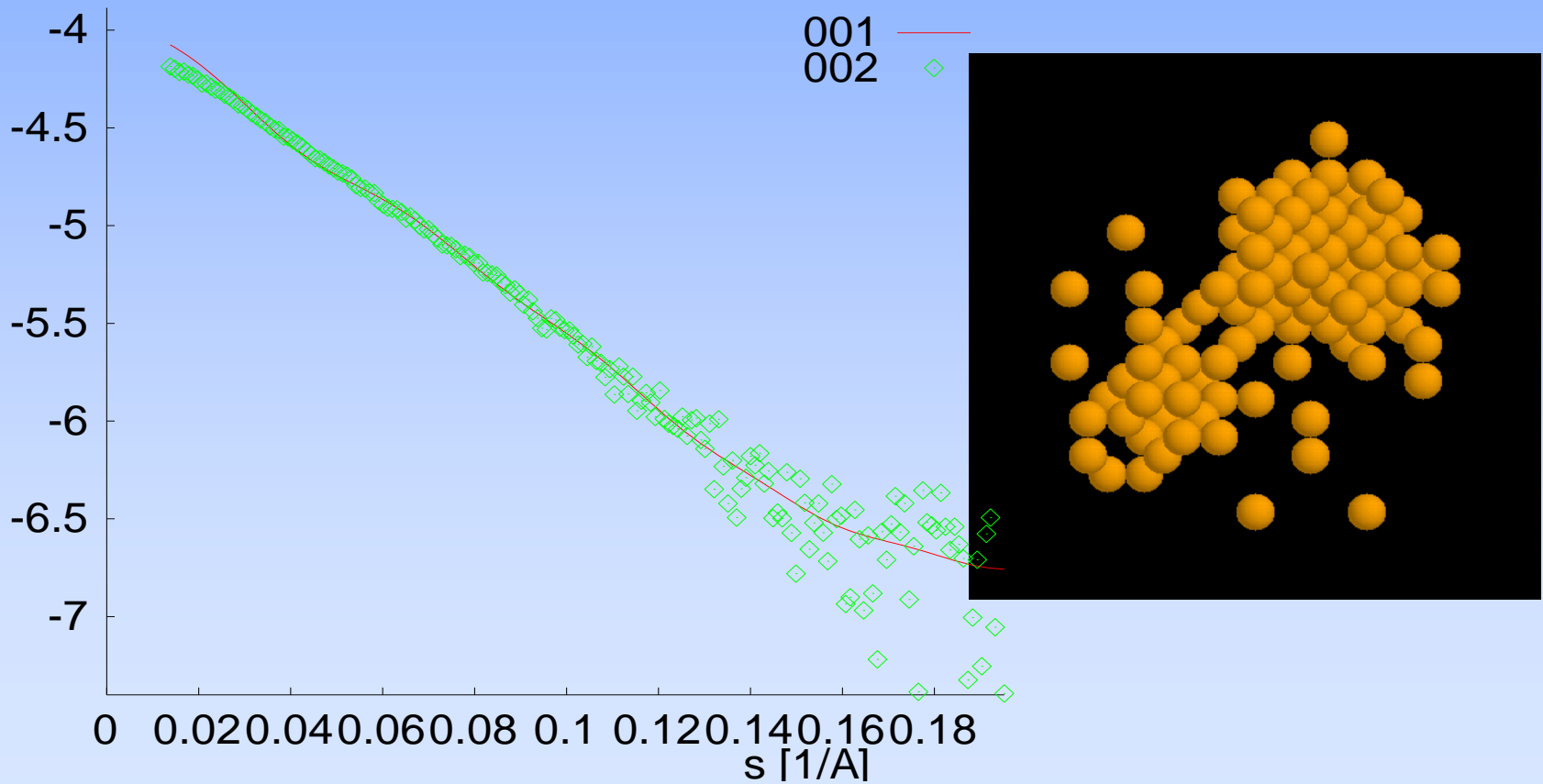
Case study: determination of structure of the myosin head S1

Step 15 Temperature = 0.229E-03 Chi= 8.37



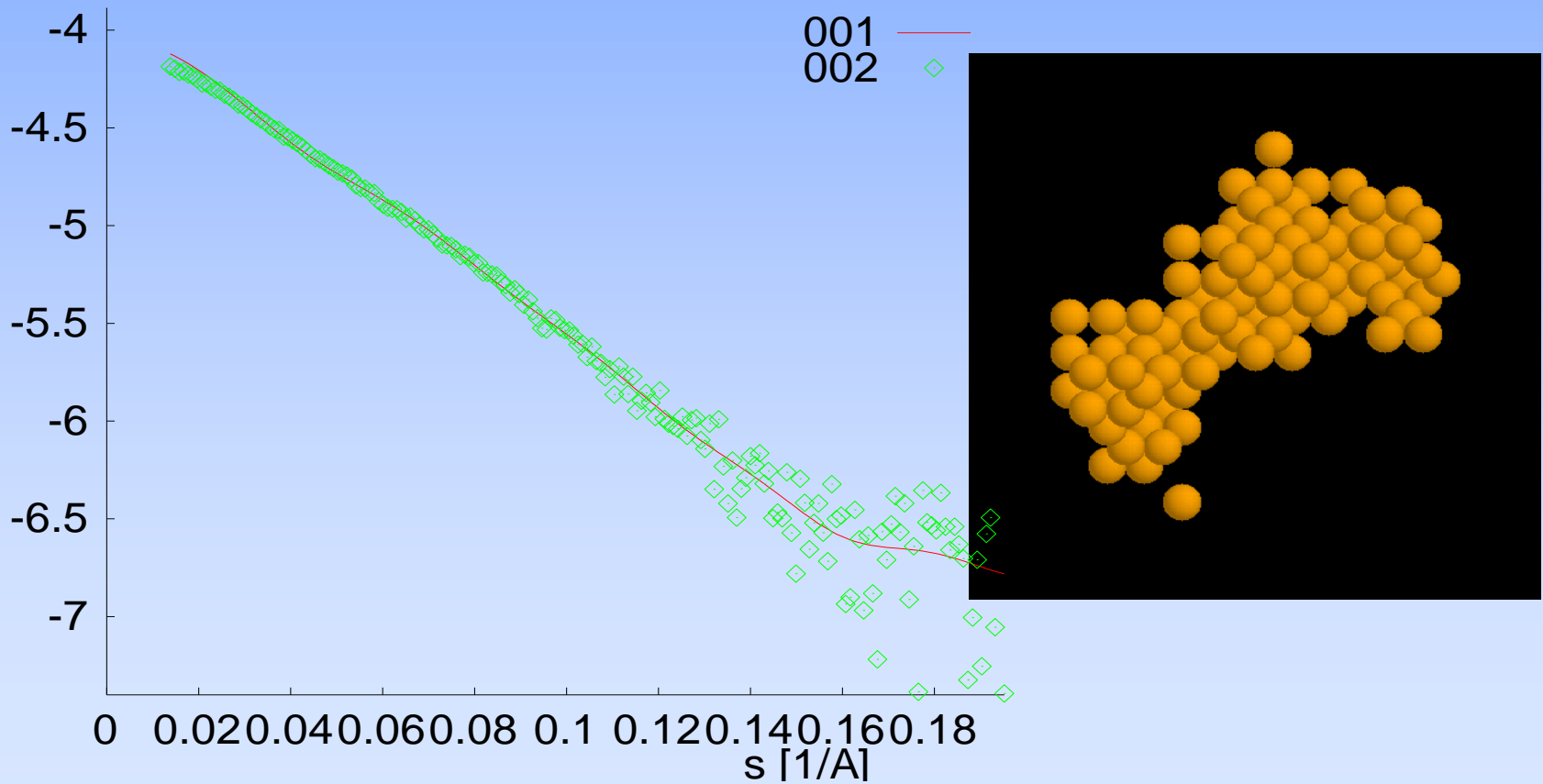
Case study: determination of structure of the myosin head S1

Step 20 Temperature = 0.135E-03 Chi= 5.63



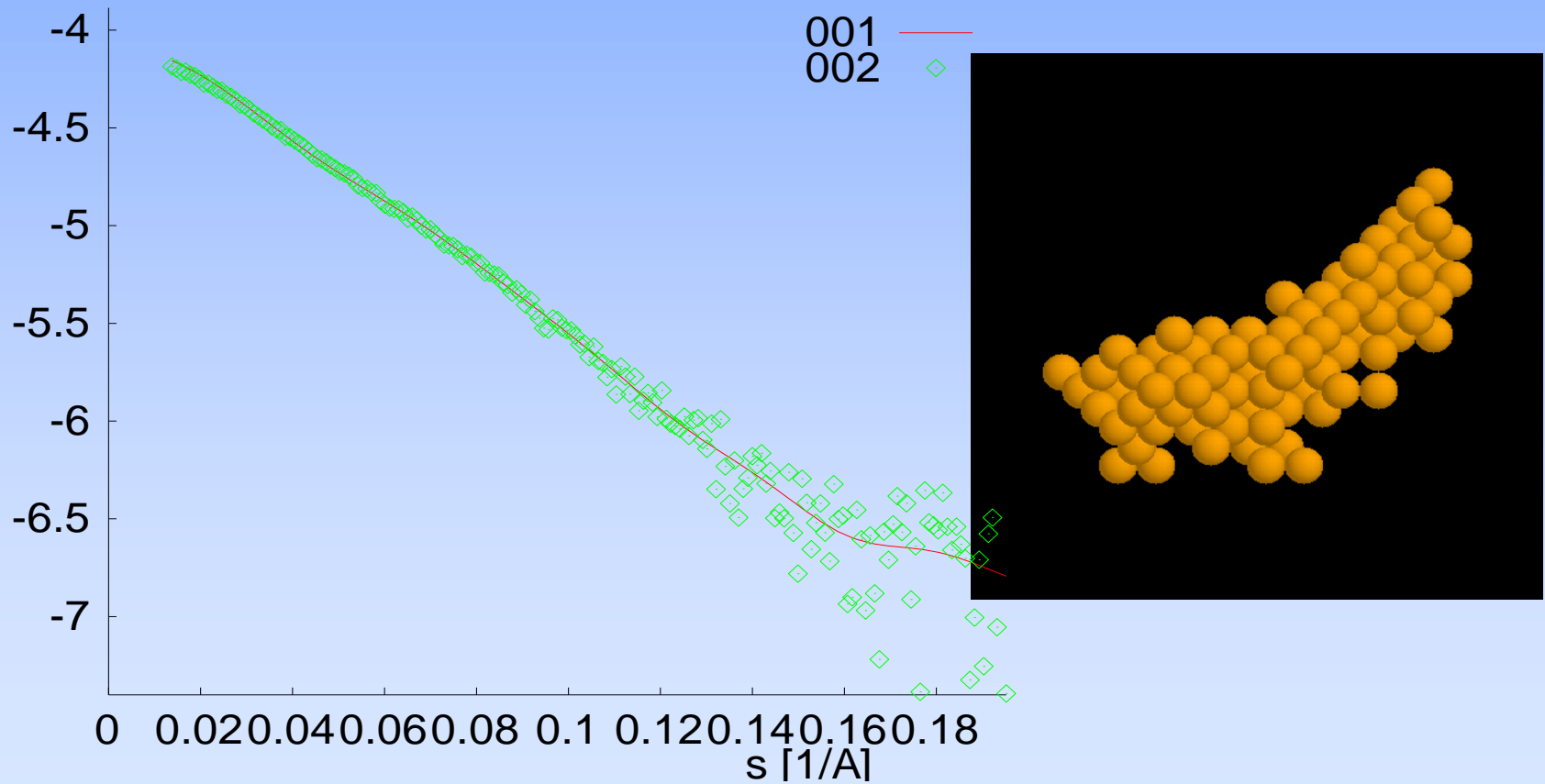
Case study: determination of structure of the myosin head S1

Step 25 Temperature = 0.798E-04 Chi= 3.33



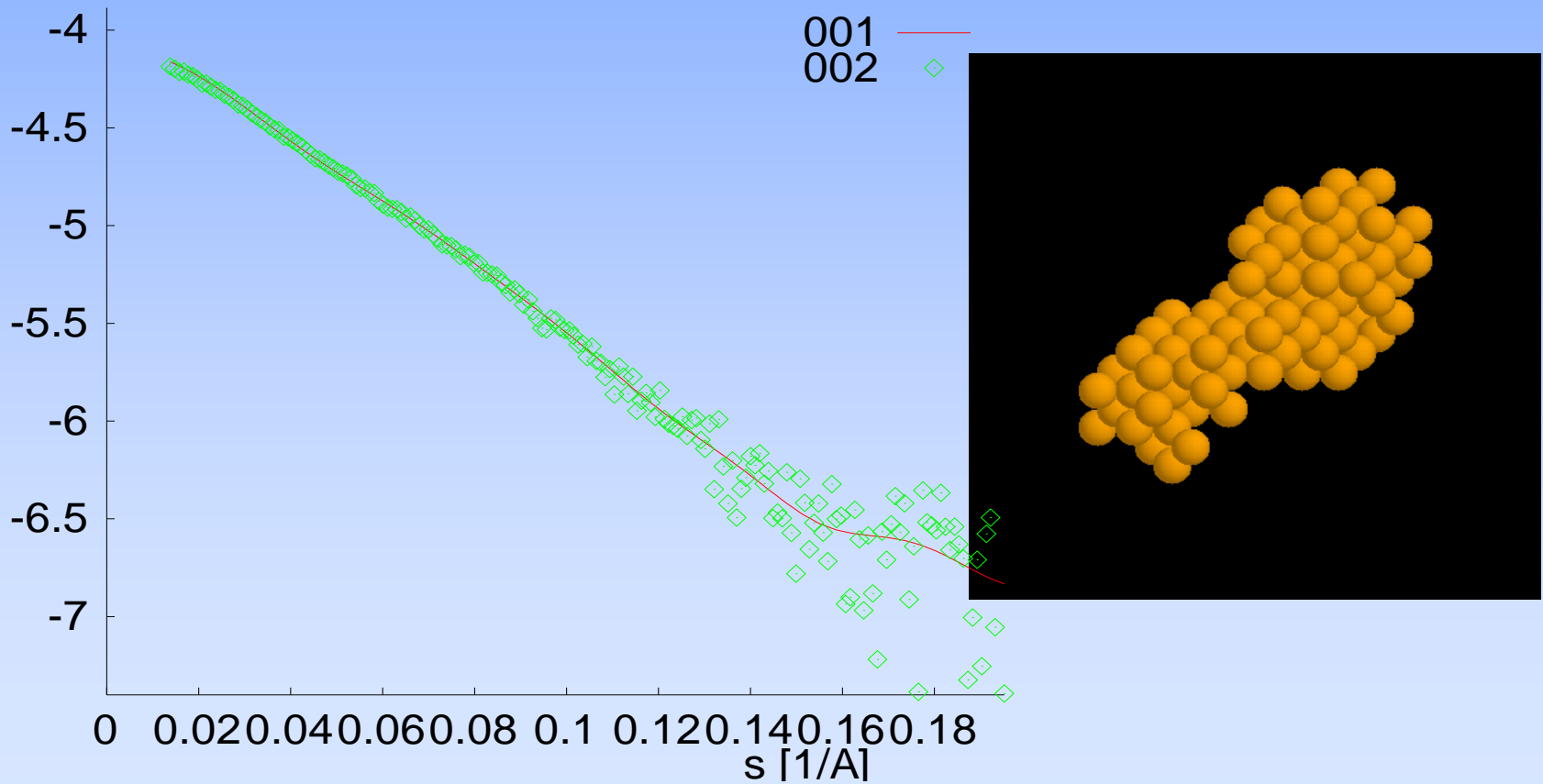
Case study: determination of structure of the myosin head S1

Step 30 Temperature = 0.471E-04 Chi= 1.82



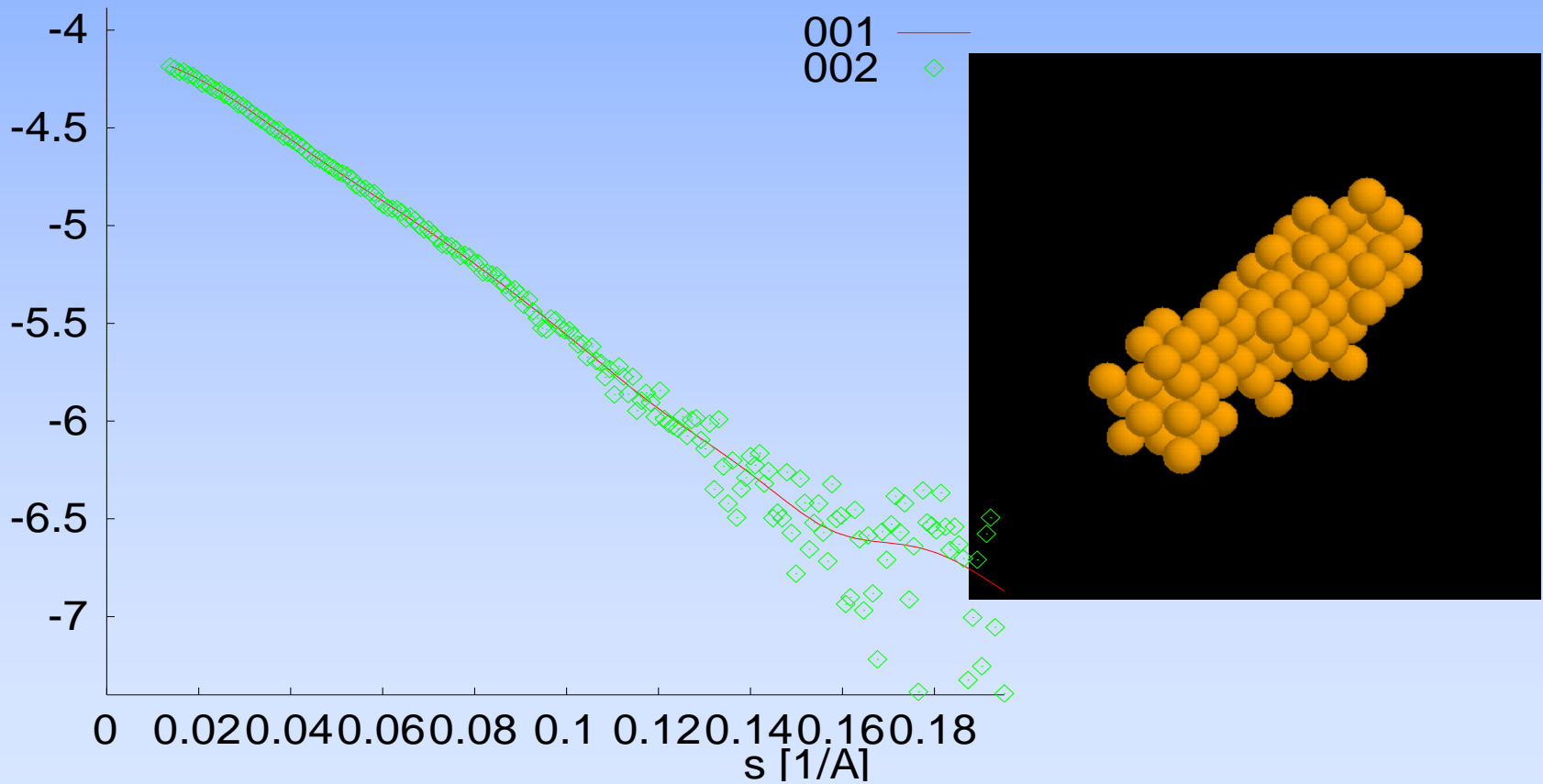
Case study: determination of structure of the myosin head S1

Step 35 Temperature = 0.278E-04 Chi= 1.56



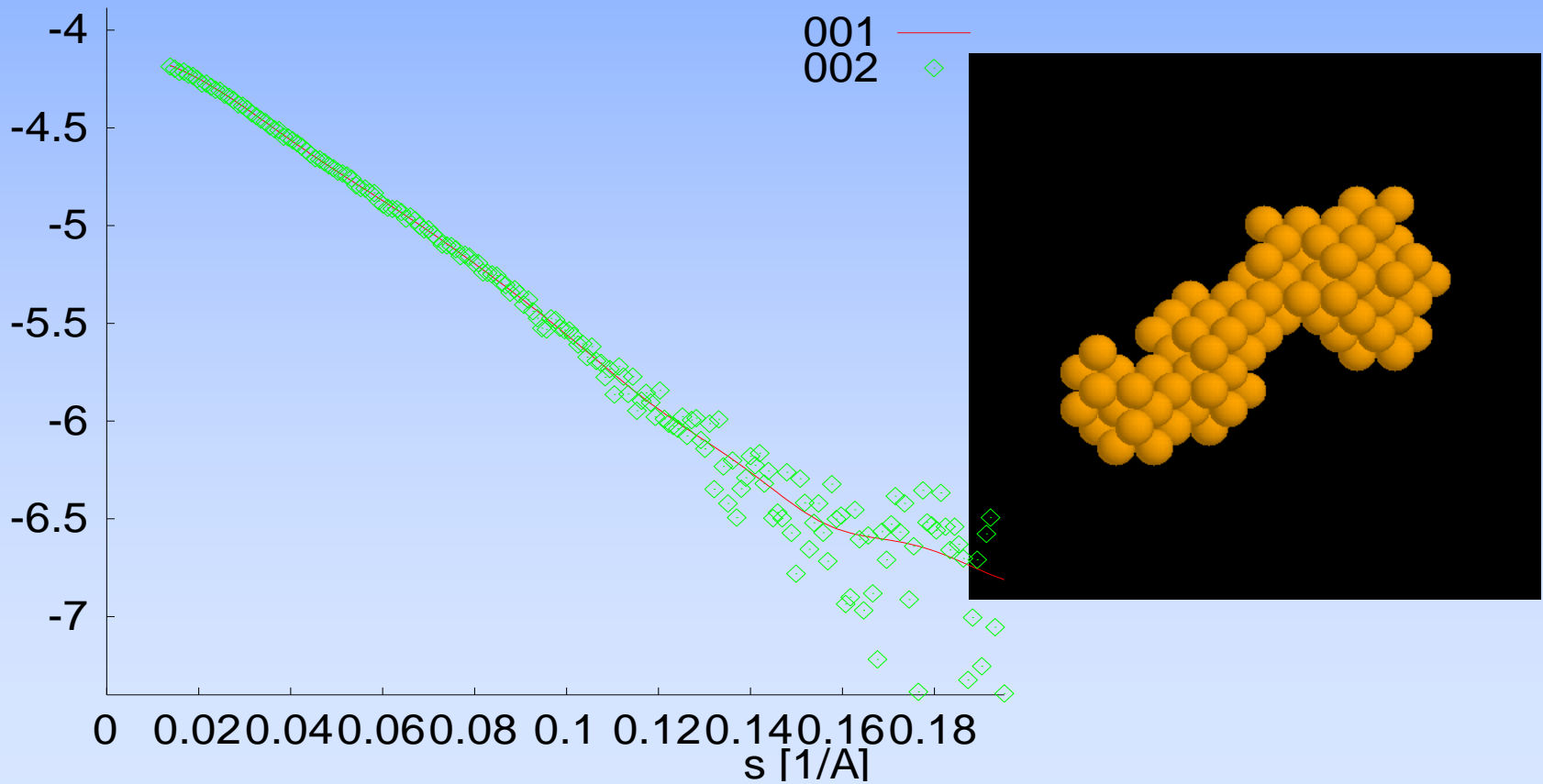
Case study: determination of structure of the myosin head S1

Step 40 Temperature = 0.164E-04 Chi= 1.08



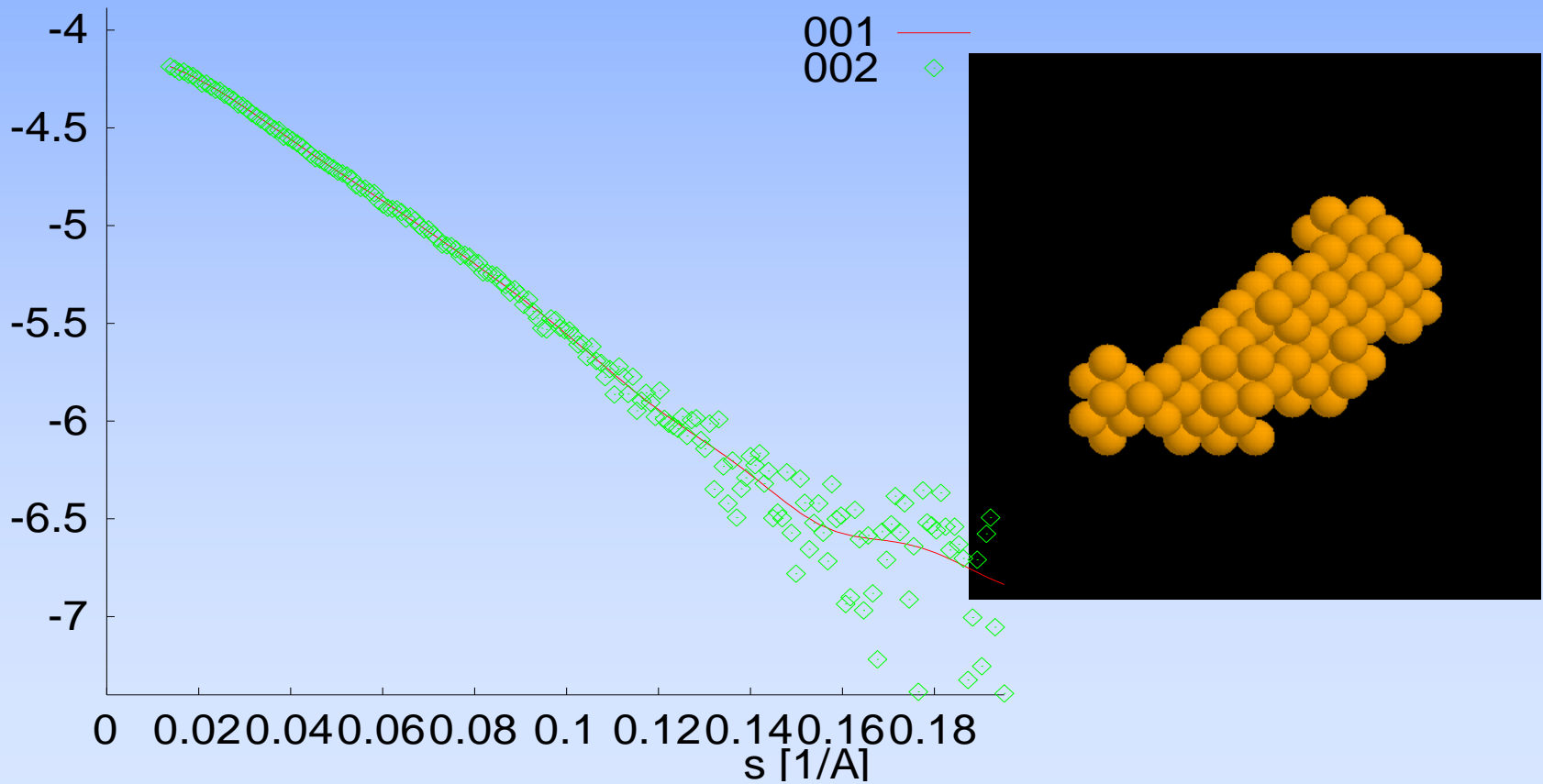
Case study: determination of structure of the myosin head S1

Step 45 Temperature = 0.970E-05 Chi= 1.10



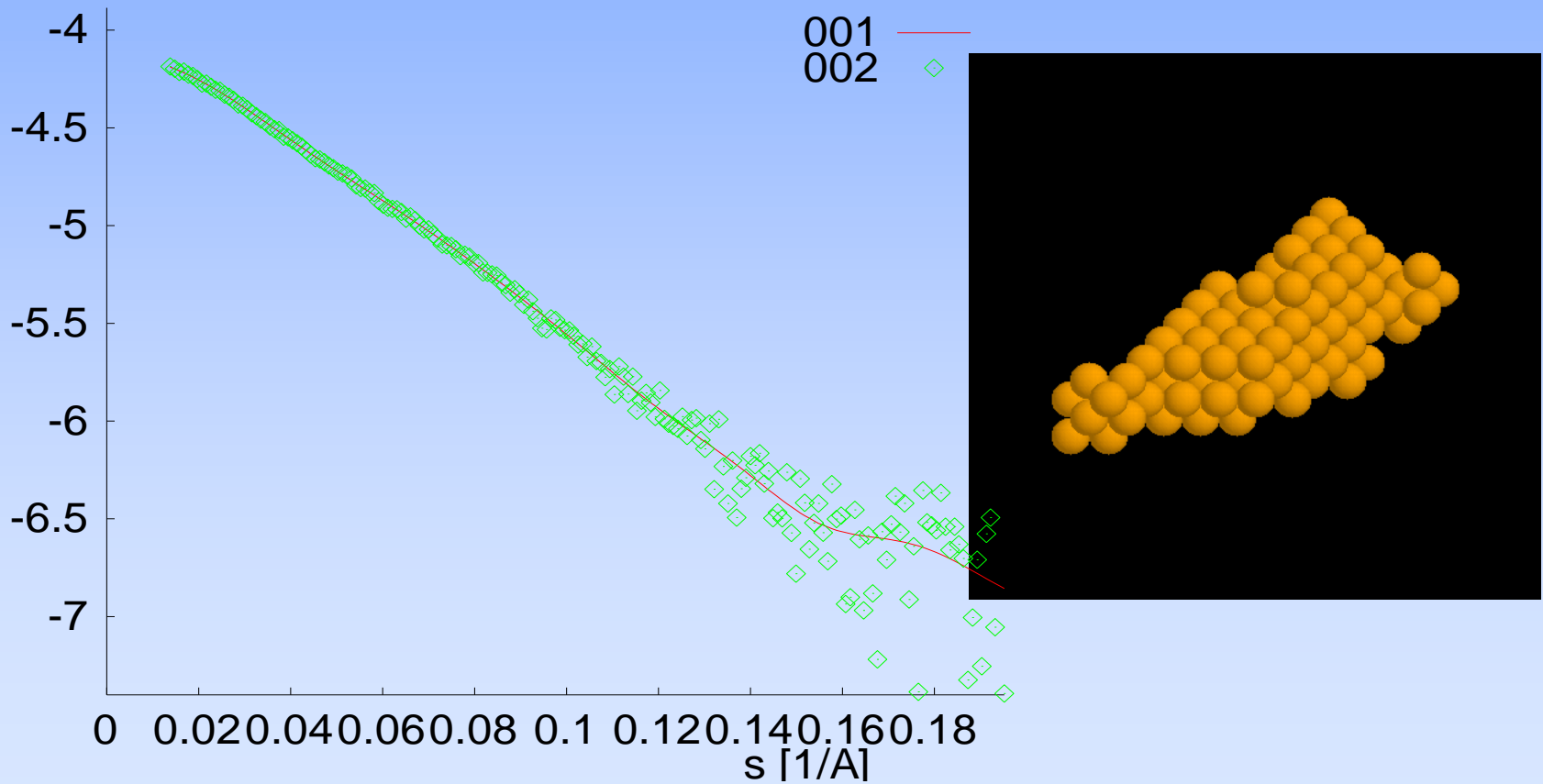
Case study: determination of structure of the myosin head S1

Step 50 Temperature = 0.573E-05 Chi= 1.05



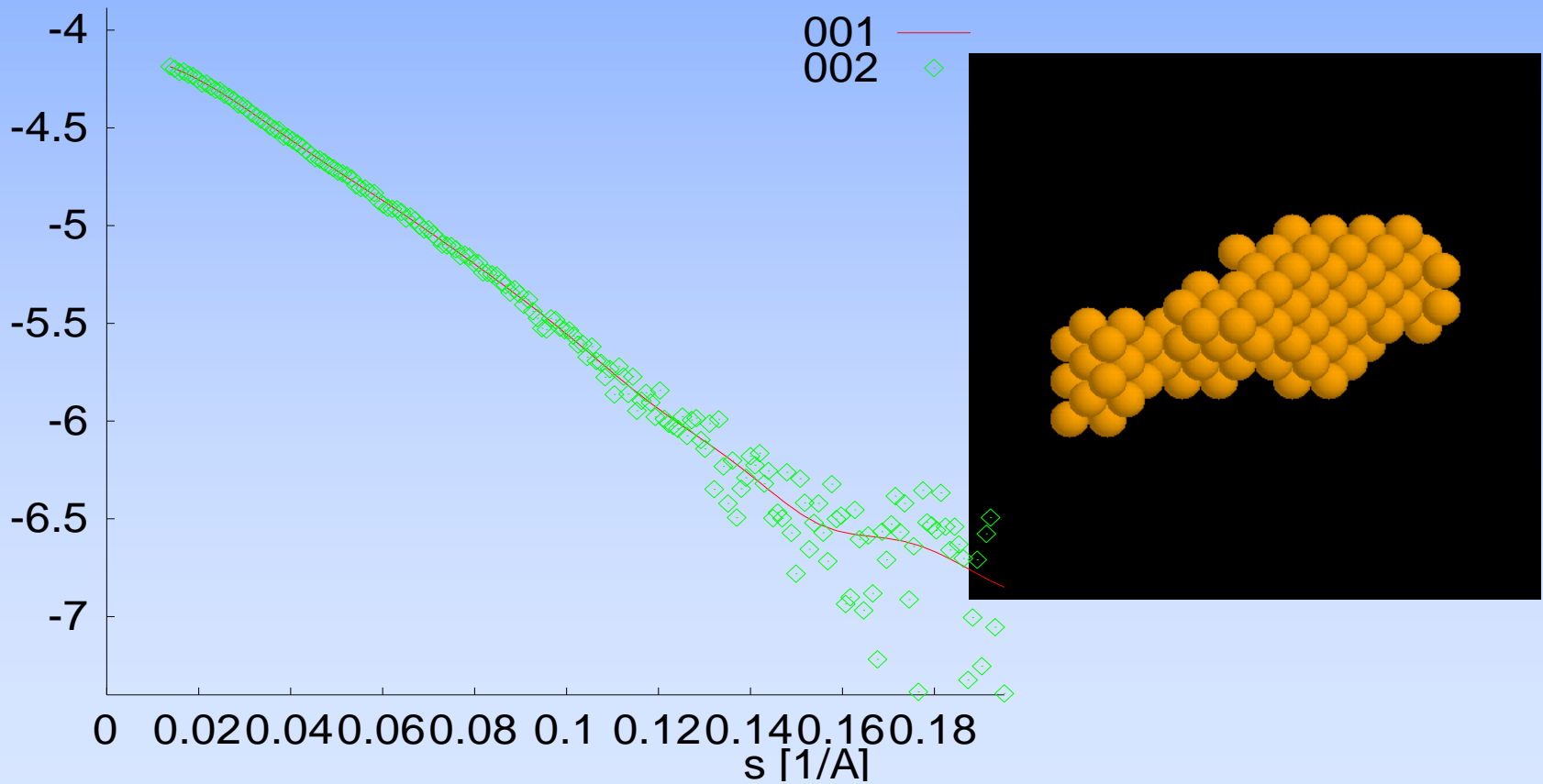
Case study: determination of structure of the myosin head S1

Step 55 Temperature = 0.338E-05 Chi= 1.04



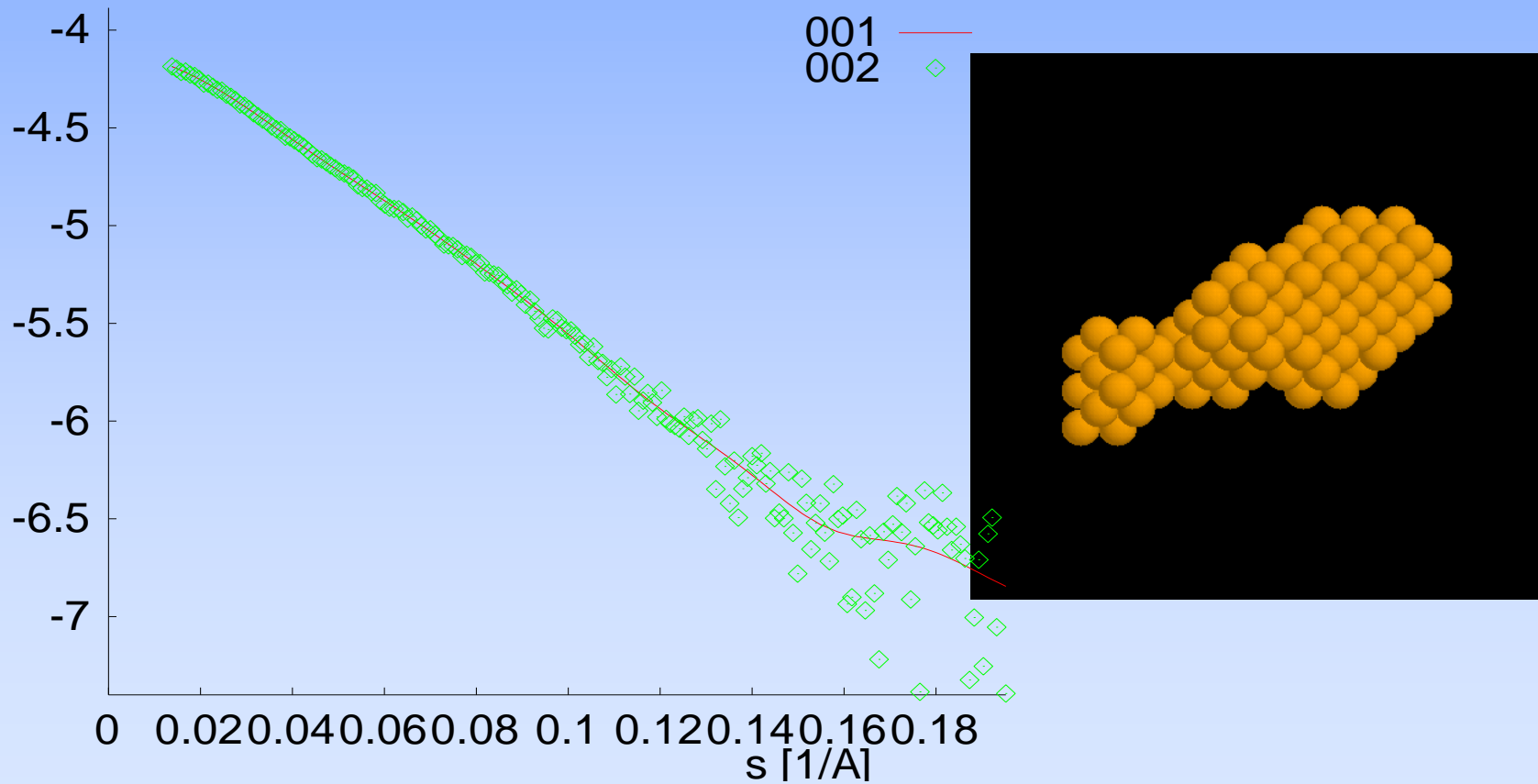
Case study: determination of structure of the myosin head S1

Step 60 Temperature = 0.200E-05 Chi= 1.04



Case study: determination of structure of the myosin head S1

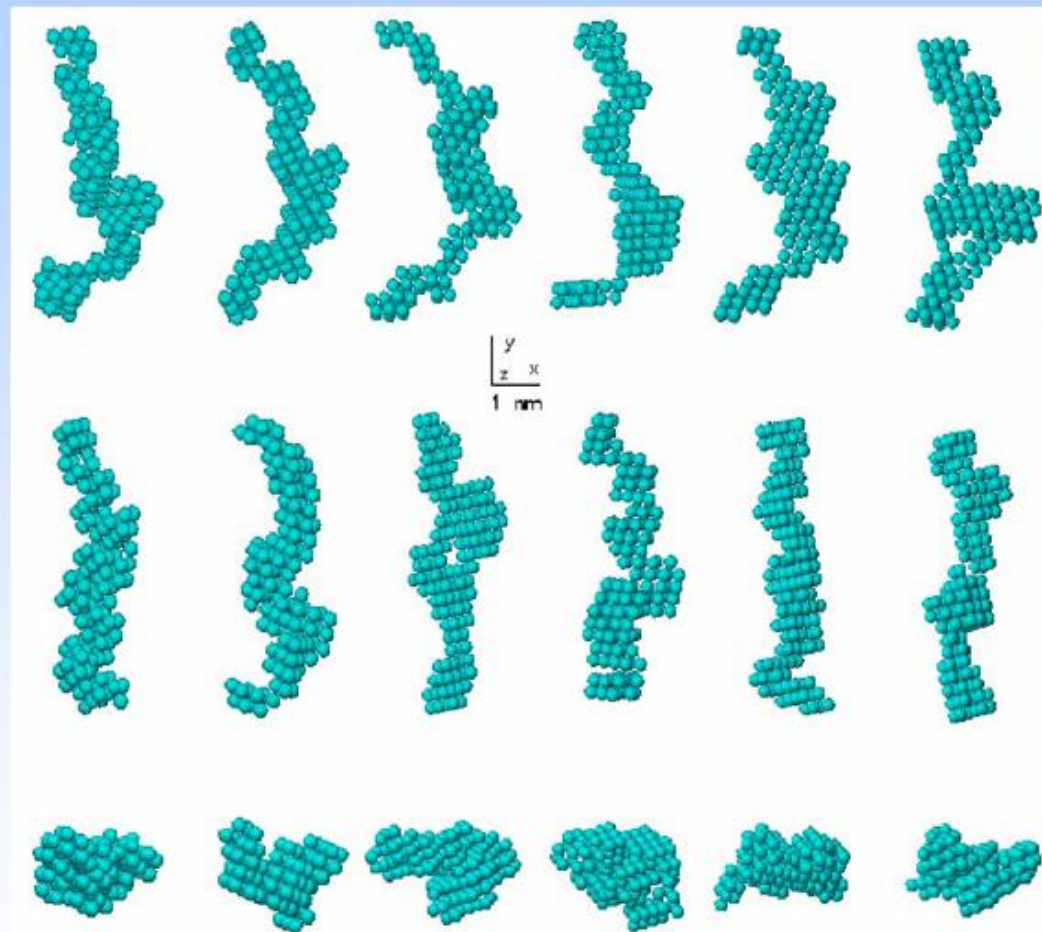
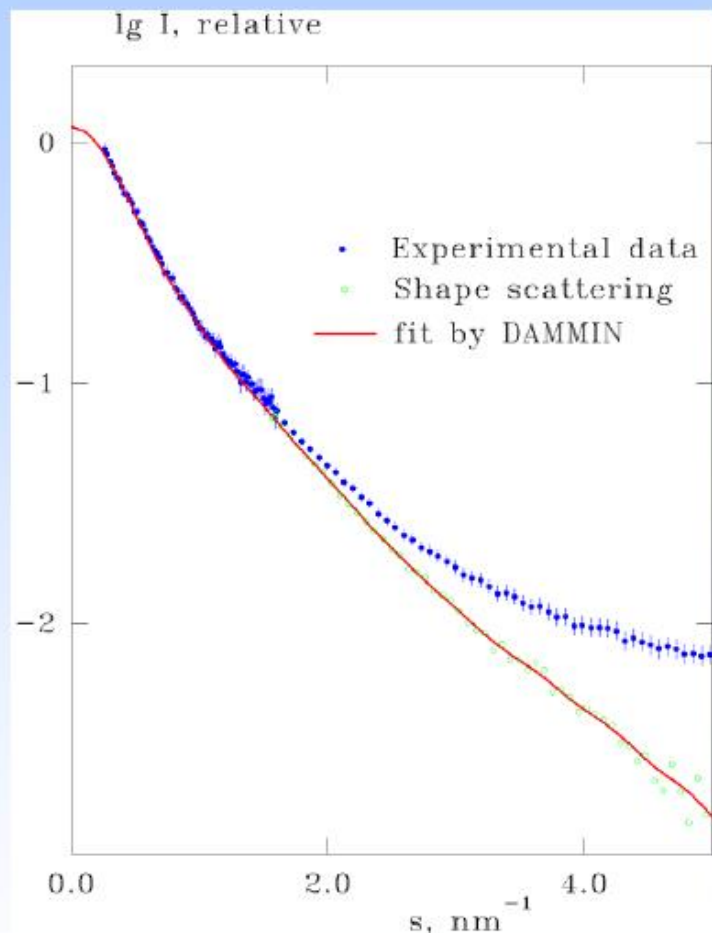
Step 64 Temperature = 0.131E-05 Chi= 1.04



Structure restoration using DAMMIN with stability estimate

1. Find a set of solutions starting from random initial models.
2. Find a reference model (which is on average least different from all the others) and align all the other models with the reference one
3. Average all the models using SUPCOMB to obtain the solution spread region and compute the spatial occupancy density.
4. Reduce the spread region by rejecting knots with lowest occupancy to find the most populated volume (all these steps are automatically done in the package DAMAVER).
5. This volume may be considered a most probable structure model, but the scattering from this volume would generally not fit the experimental data. One may refine this model by running DAMMIN with the search volume defined by the entire spread region.

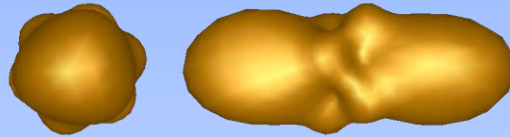
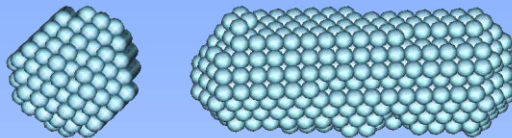
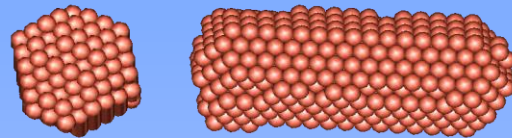
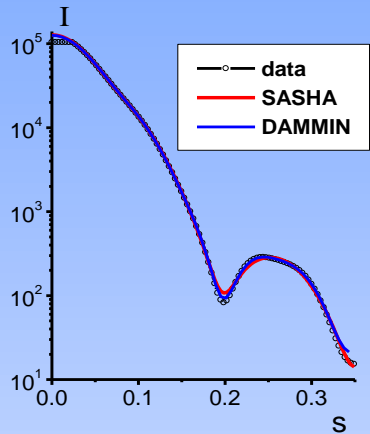
Shape determination of 5S RNA: a variety of DAMMIN models yielding identical fits



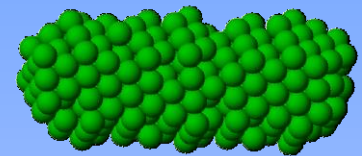
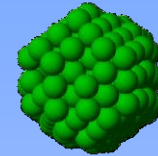
Funari, S., Rapp, G., Perbandt, M., Dierks, K., Vallazza, M., Betzel, Ch., Erdmann, V. A. & Svergun, D. I. (2000) *J. Biol. Chem.* **275**, 31283-31288.

Stable solutions

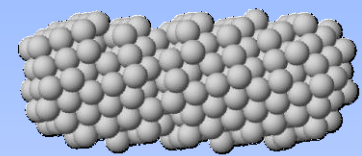
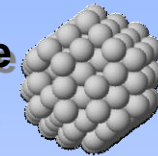
cylinder 2:5



Spread
region

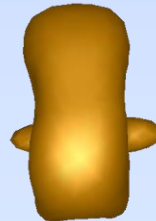
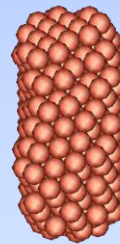
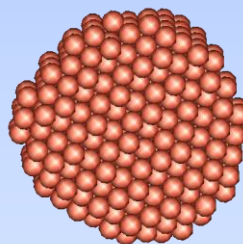
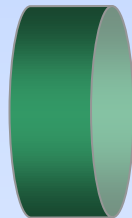
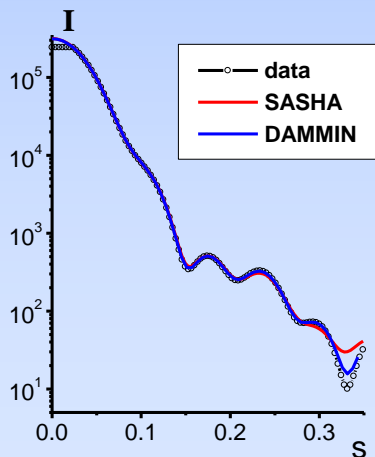


Most
probable
volume

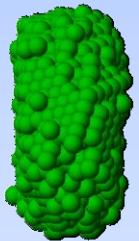
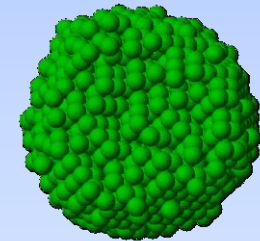


Average NSD ≈ 0.5

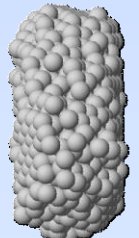
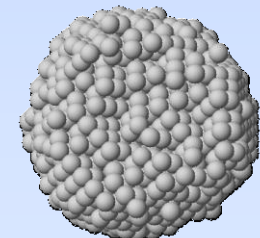
cylinder 5:2



Spread
region

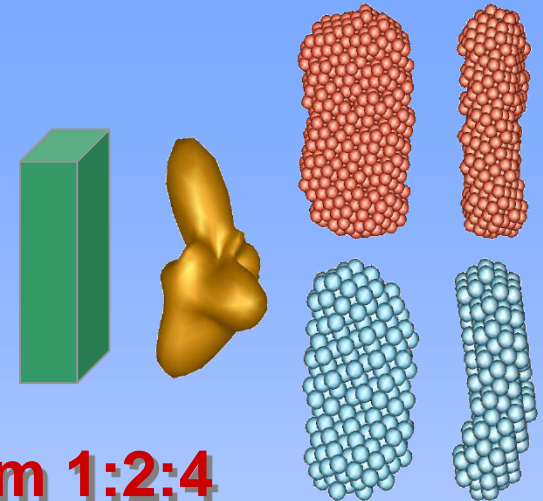
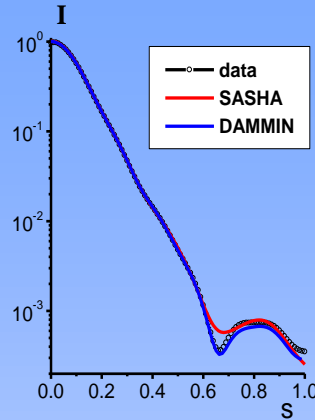
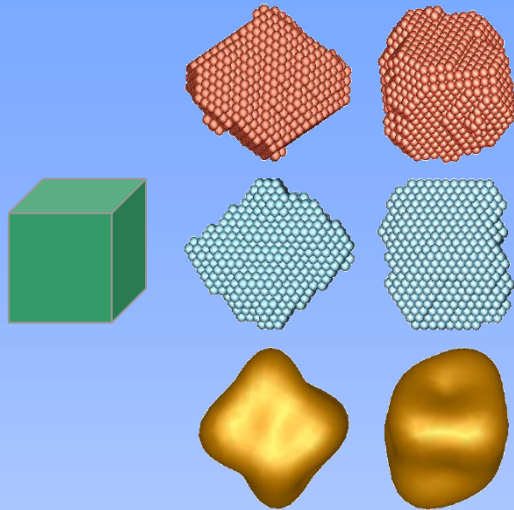
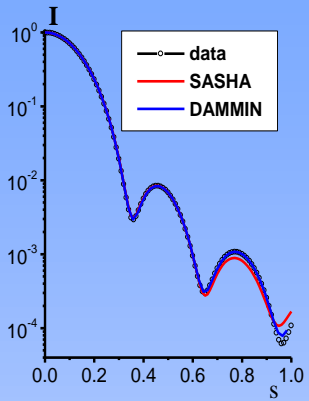


Most
probable
volume



Stable solutions

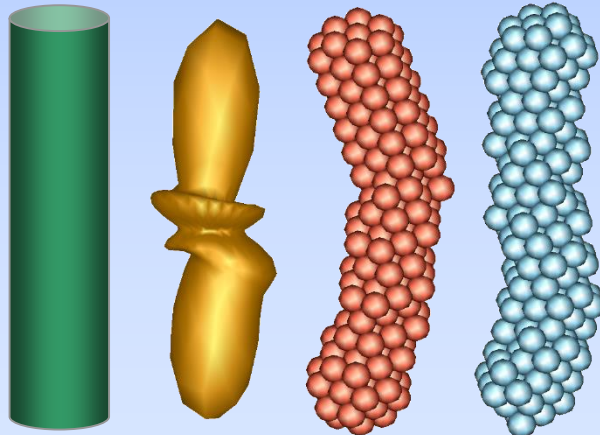
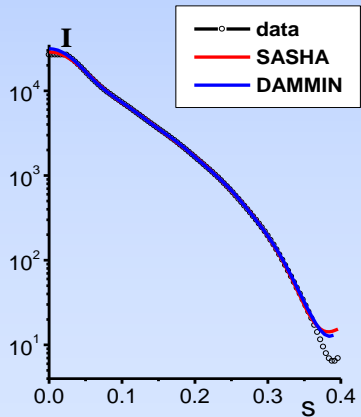
cube



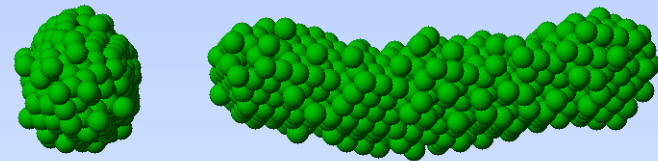
Prism 1:2:4

cylinder 2:5

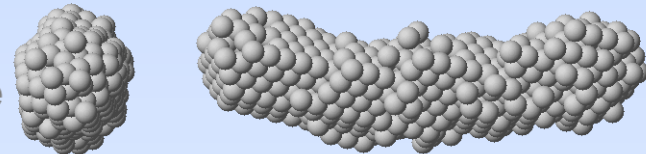
Average NSD ≈ 0.5



Spread region

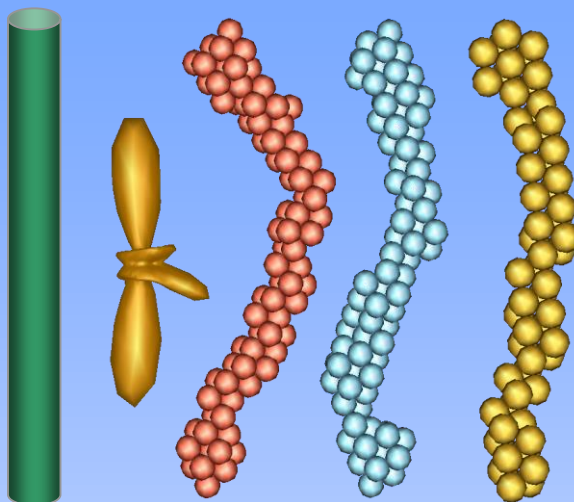
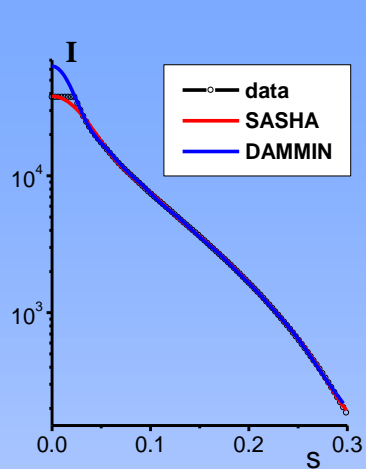


Most probable volume

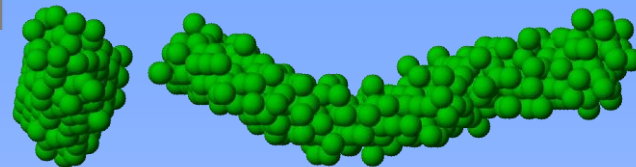


Fair stability

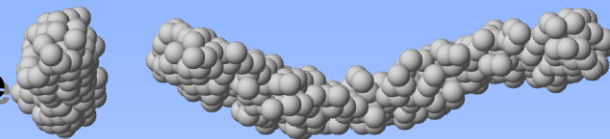
cylinder 1:10



Spread
region

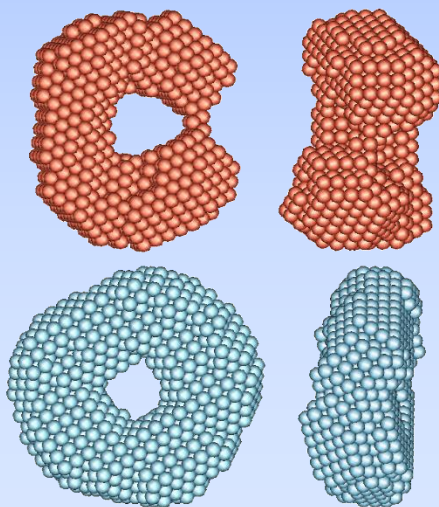
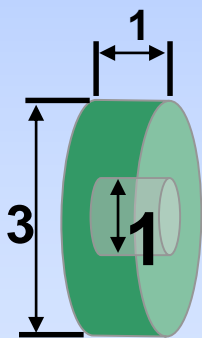
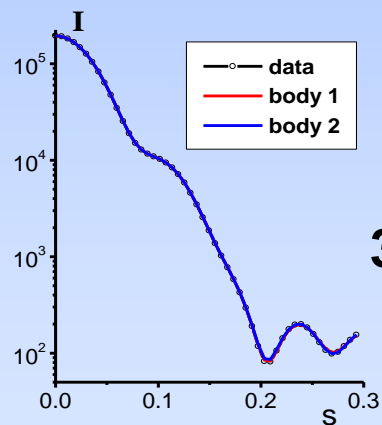


Most
probable
volume

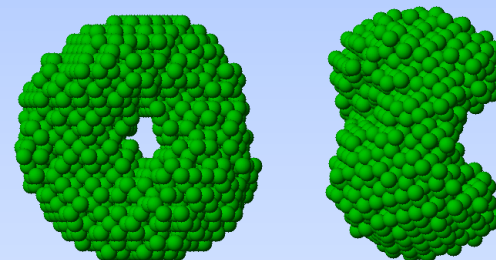


Average NSD ≈ 0.9

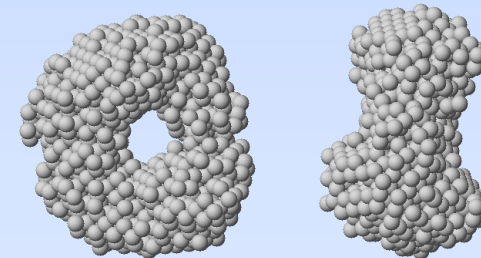
Ring 1:3:1



Spread
region

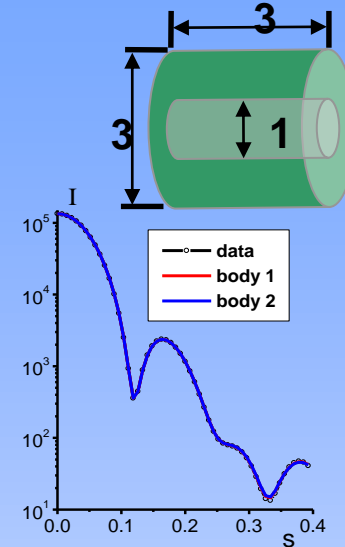
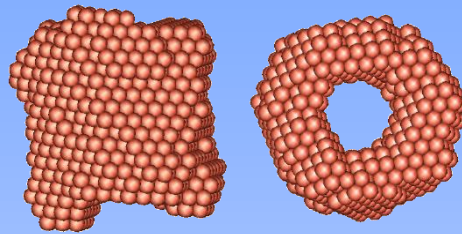
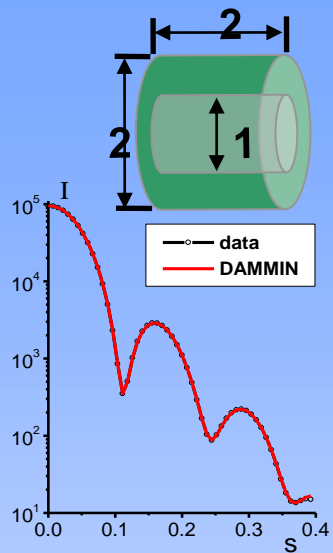


Most
probable
volume

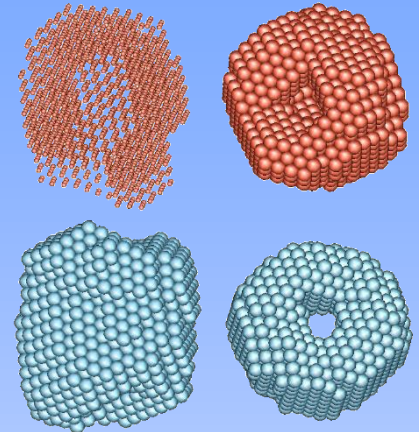


Fair stability

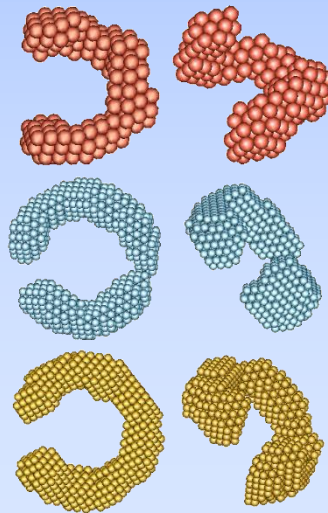
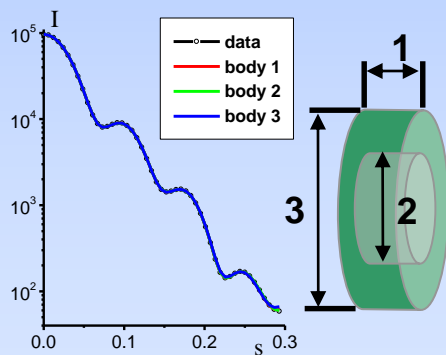
tube 1:2:2



Tube 1:3:3

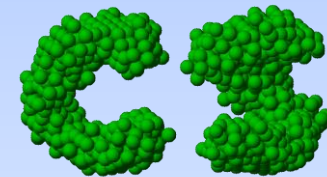


ring 1:3:2

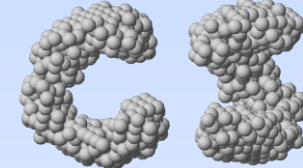


Average NSD ≈ 1.0

Spread
region

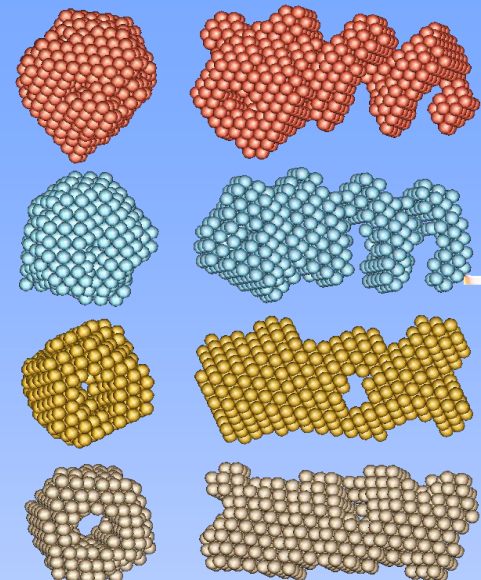
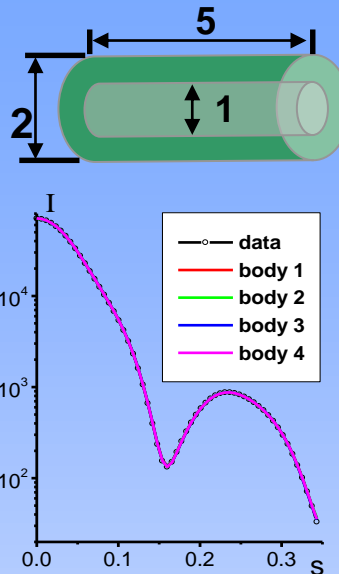
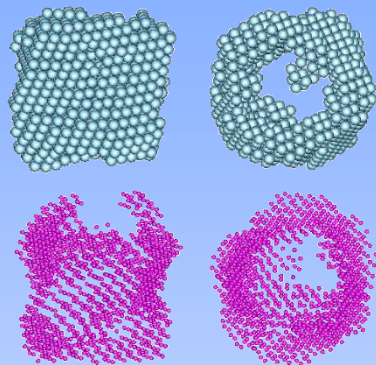
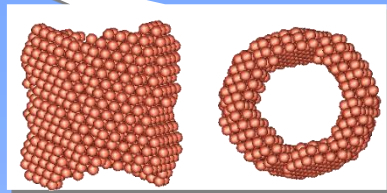
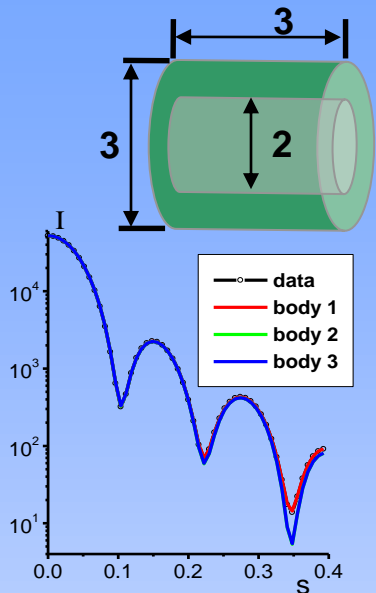


Most
probable
volume



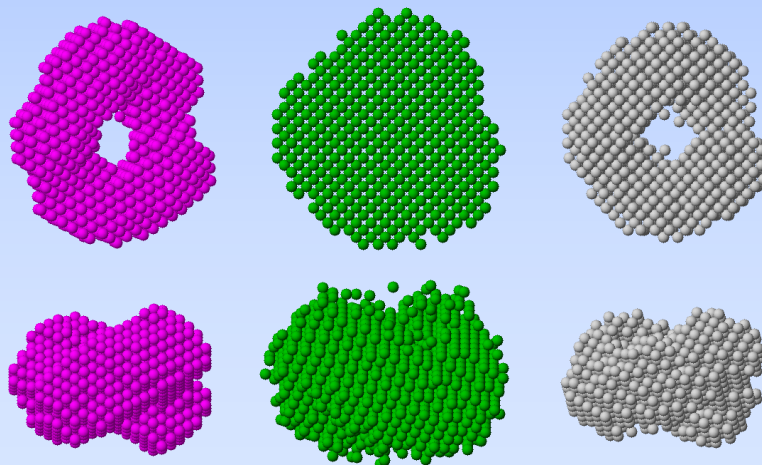
Fair stability

Very long search may provide more accurate model



Average NSD ≈ 1.0

This structure can not be restored without use of additional information

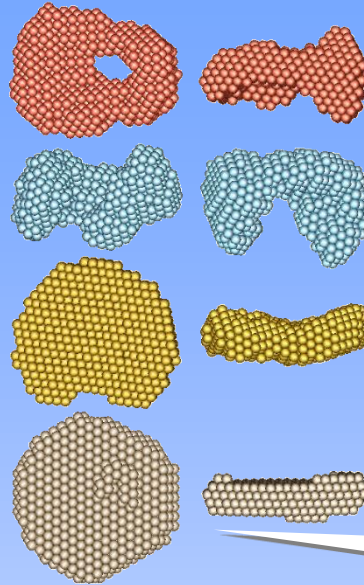
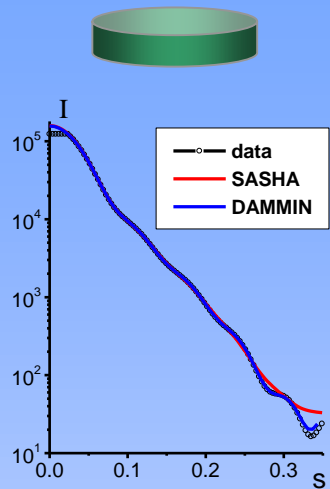


Spread region

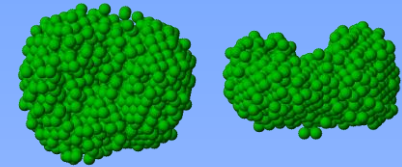
Most probable volume

Poor stability

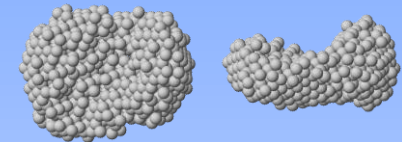
Disk 5:1



Spread
region

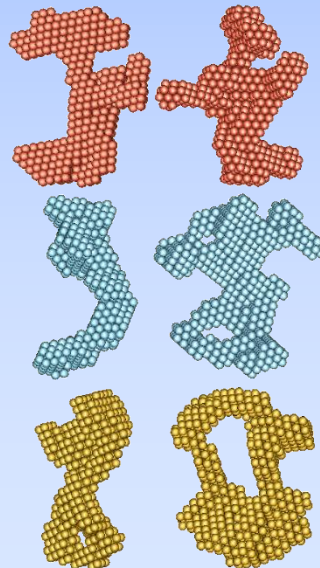
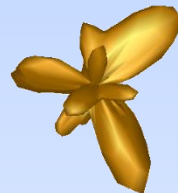
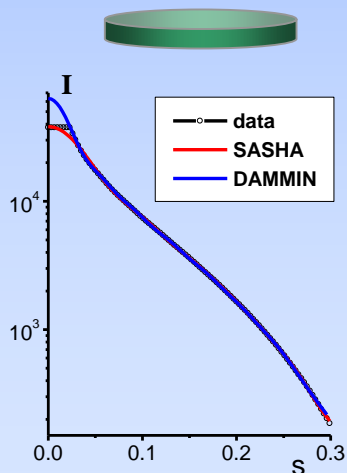


Most
probable
volume

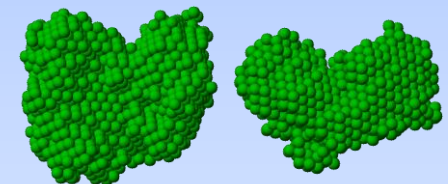


Very long search may
provide more
accurate model

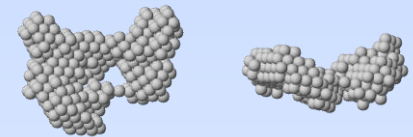
Disk 10:1



Spread
region



Most
probable
volume

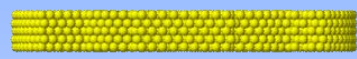
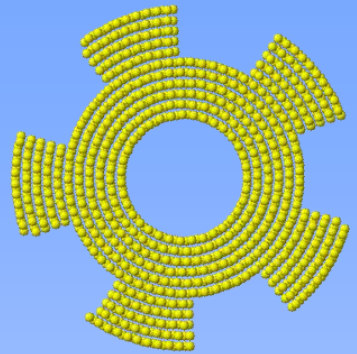


Average NSD >1.0

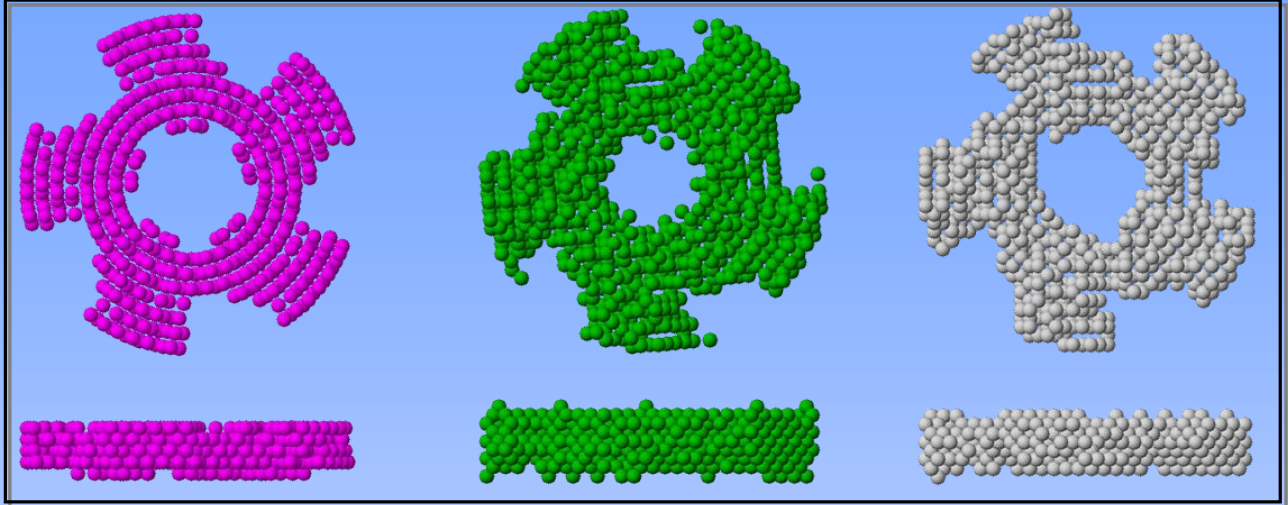
This structure can not be
restored without use of
additional information

Use of symmetry

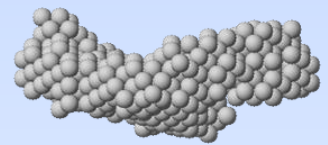
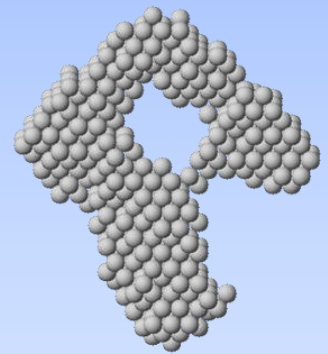
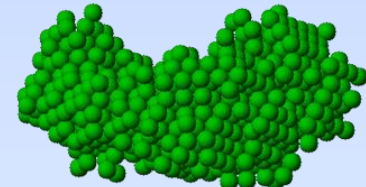
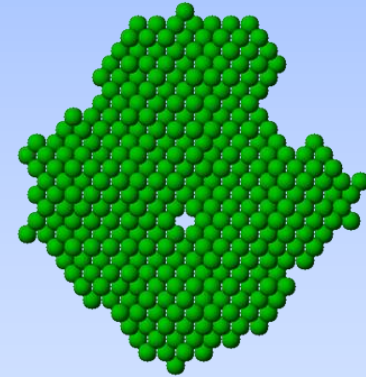
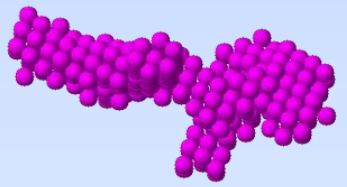
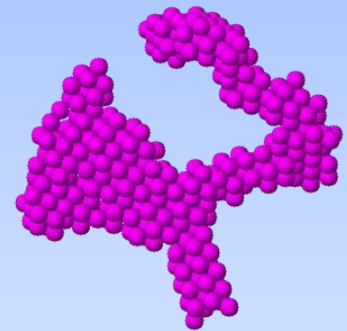
Typical solution with P5 symmetry



Original body



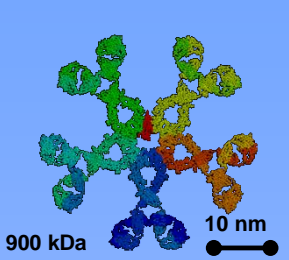
Typical solution with no symmetry



Spread region

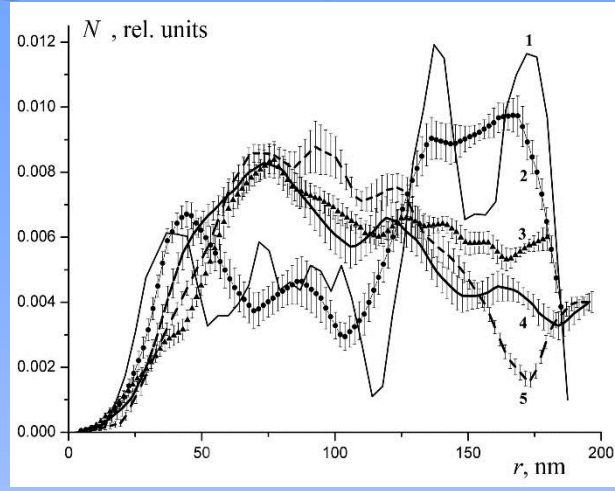
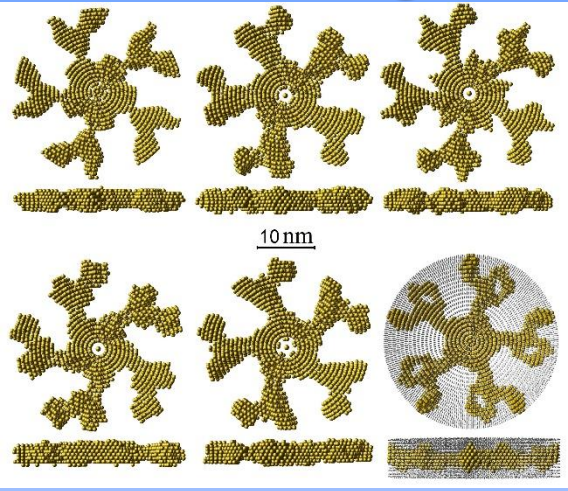
Most probable volume

DAMMIN restoration of IgM & IgM-RF shape in solution



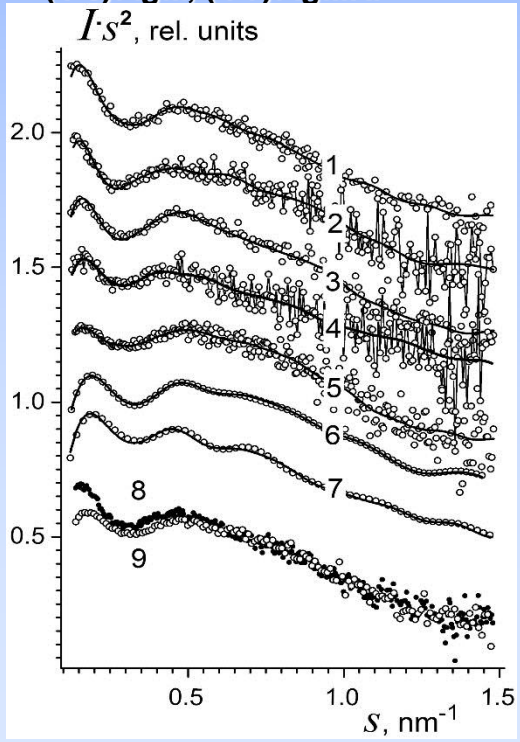
Tentative atomic model (S.Perkins, 1991)

Restored modes

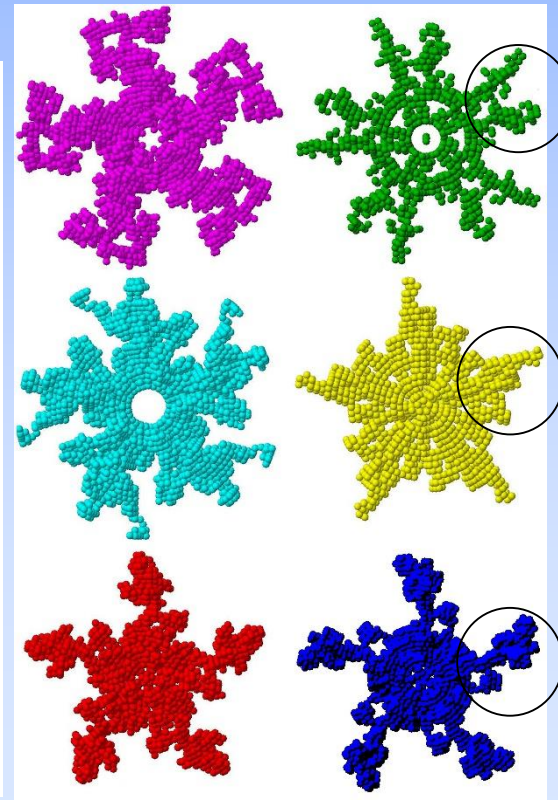
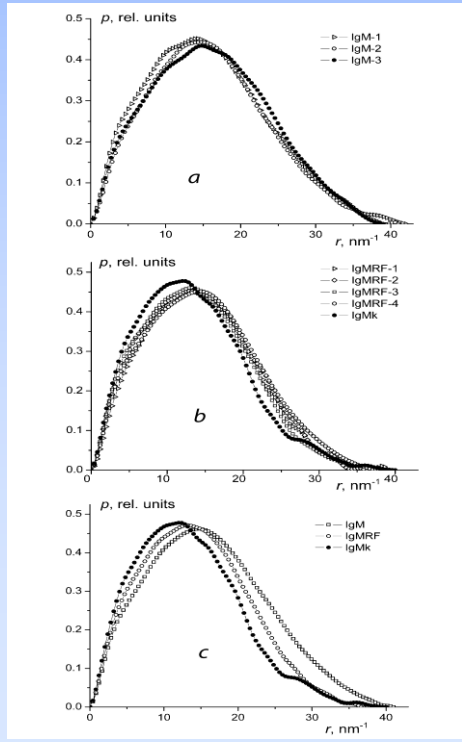


Radial electron density distributions show for IgMRF (4,5) less values at the peripheral region

Experimental SAXS data (1-3): IgM, (4-7): IgMRF



Pair distribution profiles



IgM

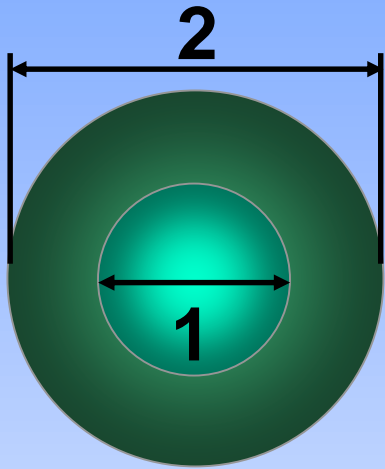
IgMRF

IgMRFq

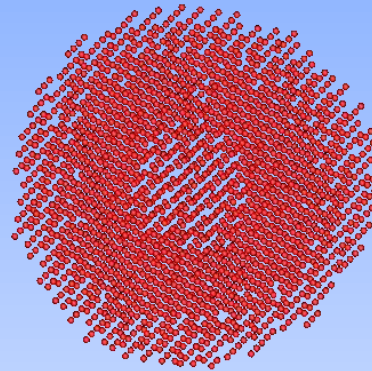
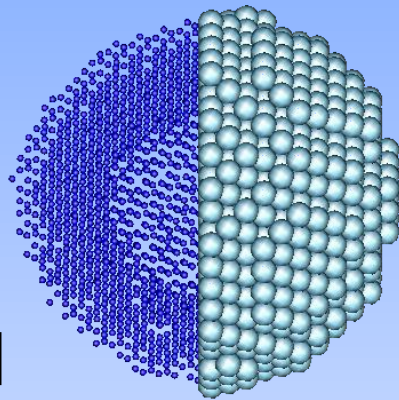
Слева и справа: пара типичных решений

Hollow spheres

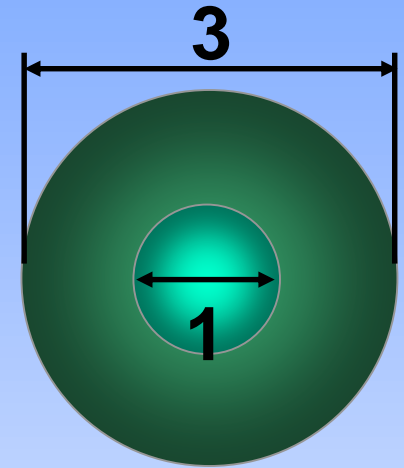
Coaxial cavities are restored with more stability than the shifted ones...



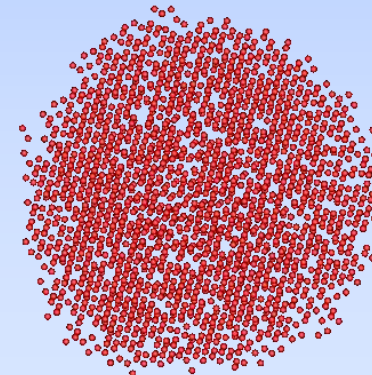
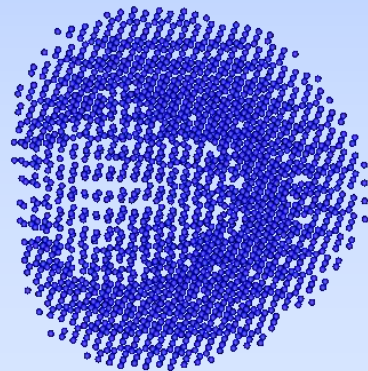
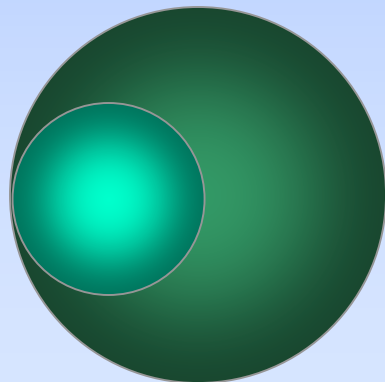
1



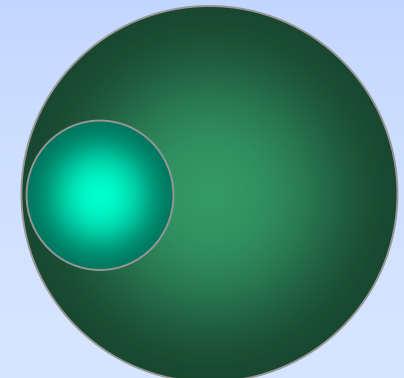
3



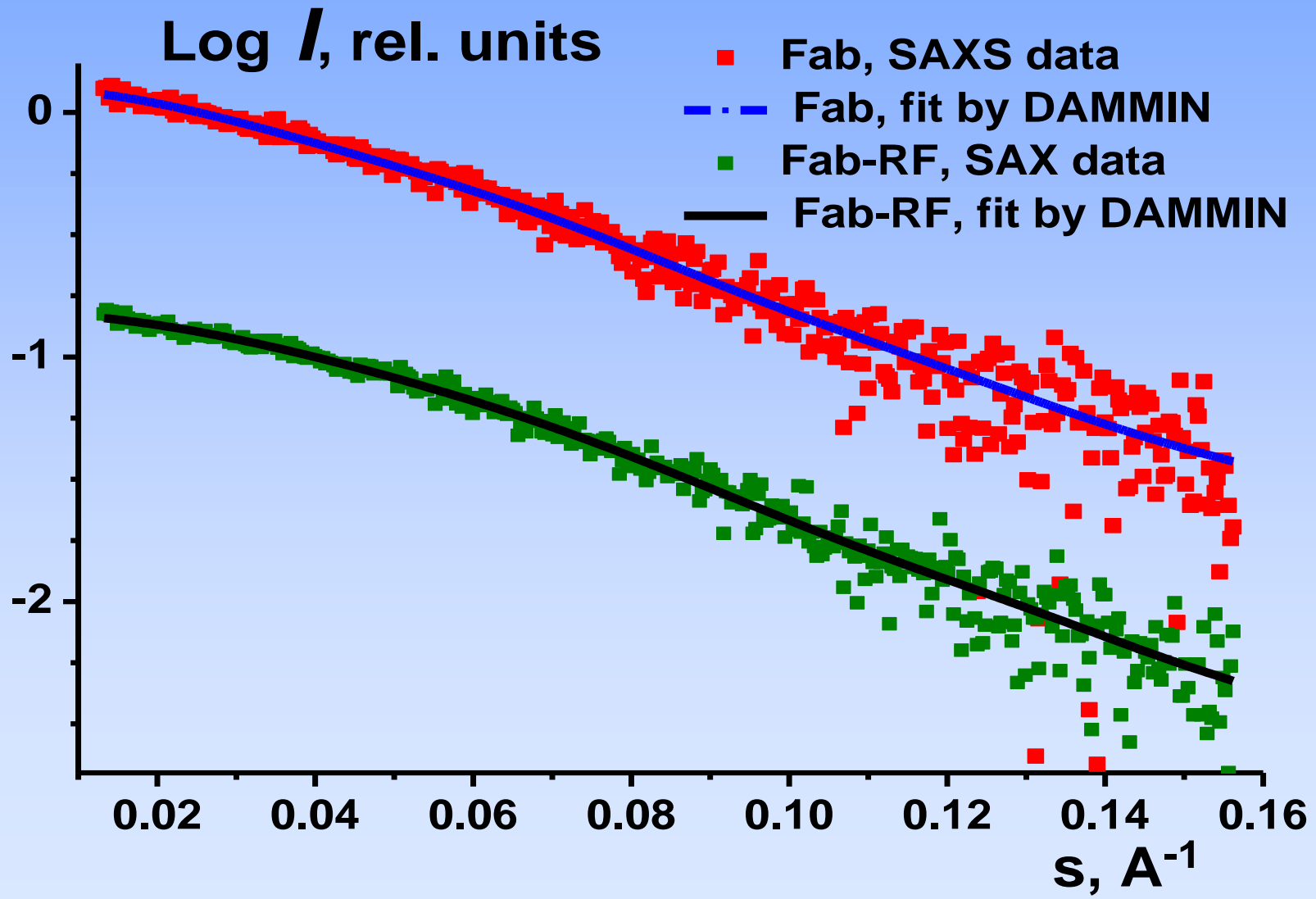
2



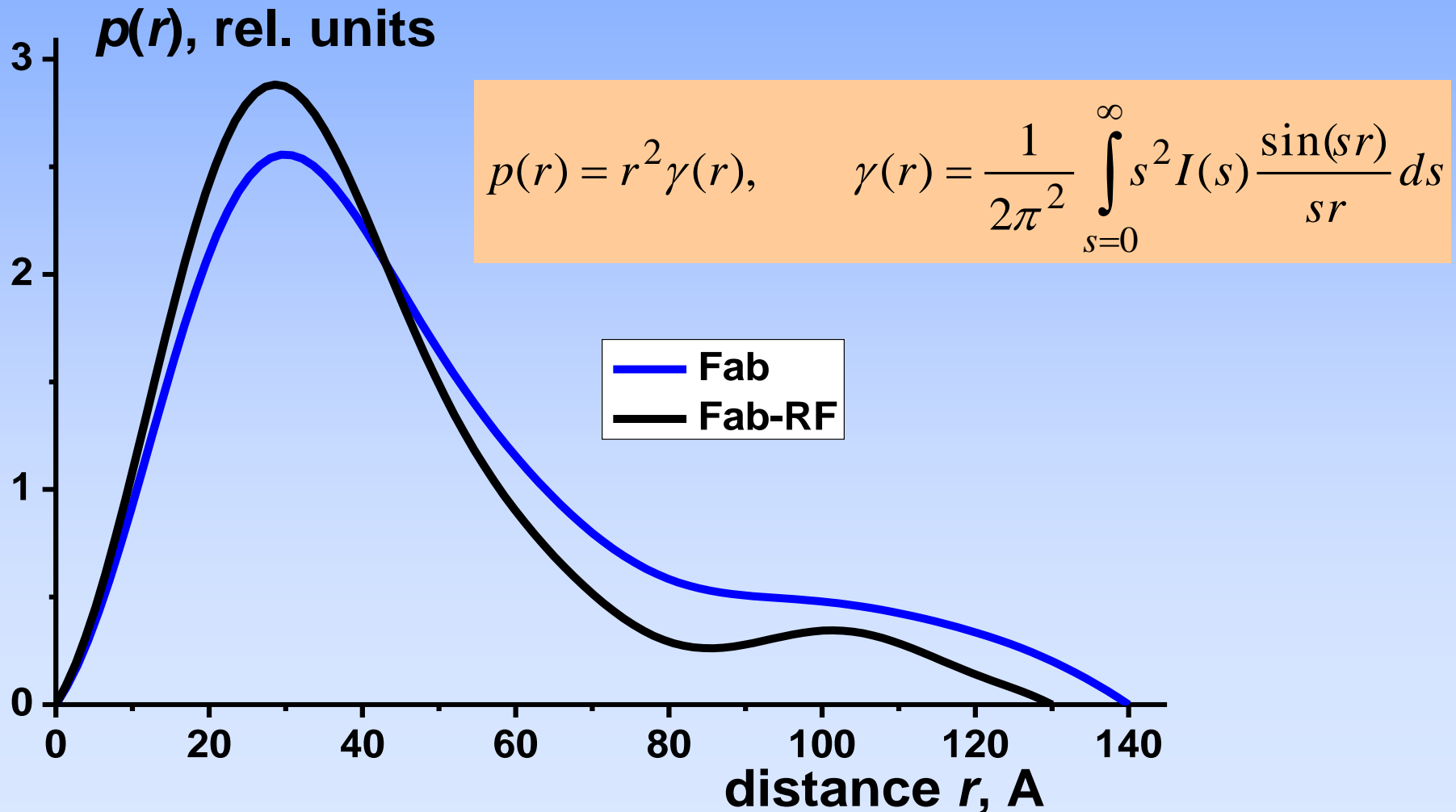
4



SAXS from solutions of Fab и Fab-RF fragments (dots) and scattering from obtained models (next slide)

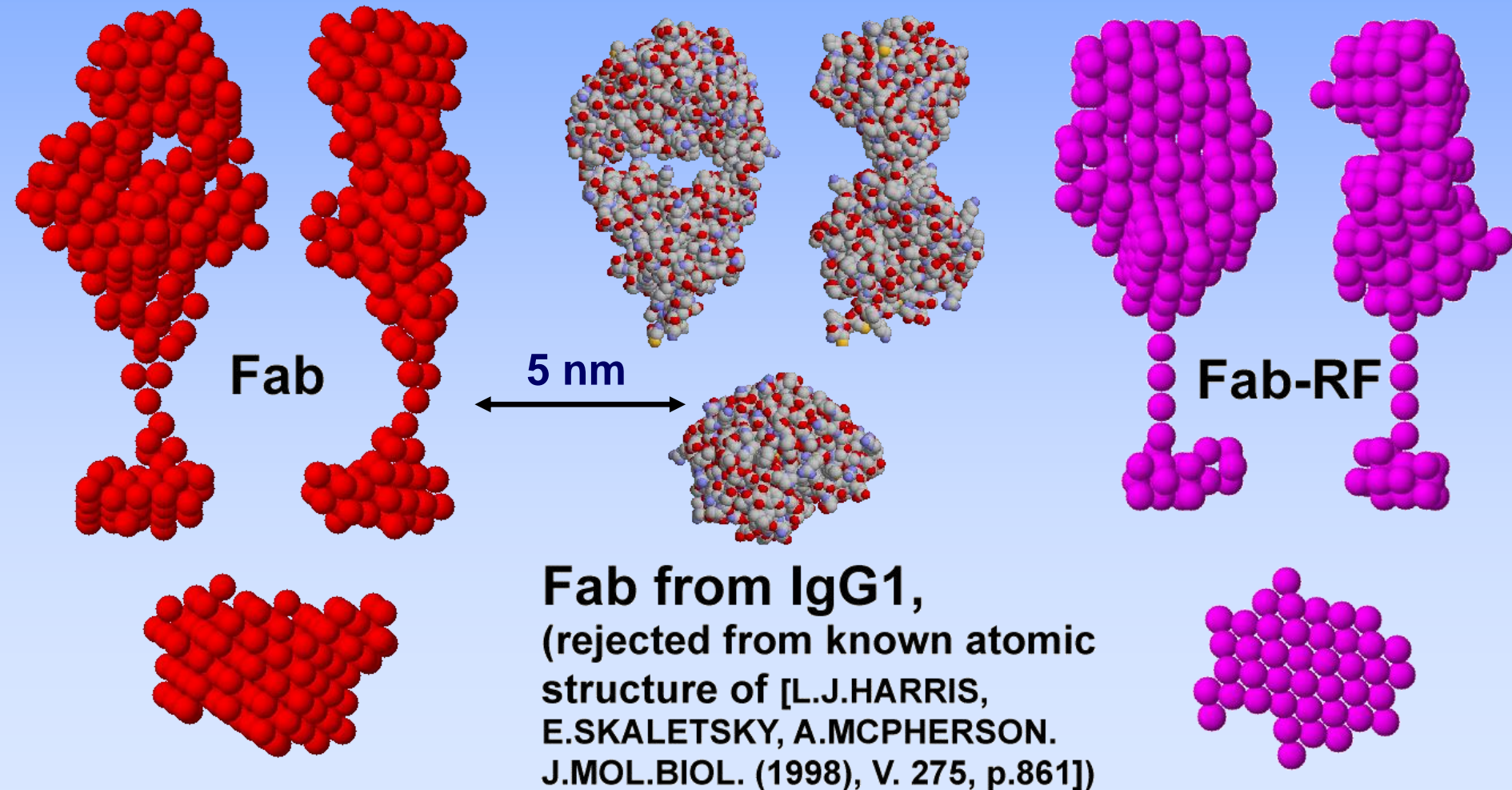


Pair distribution functions for Fab и Fab-RF fragments

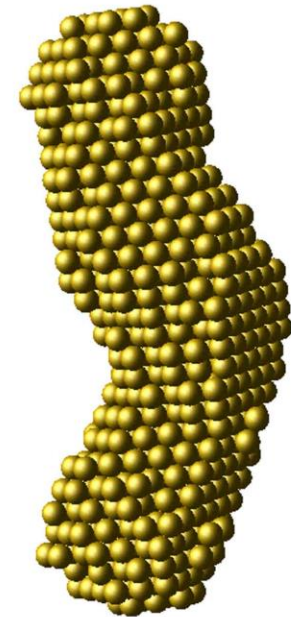
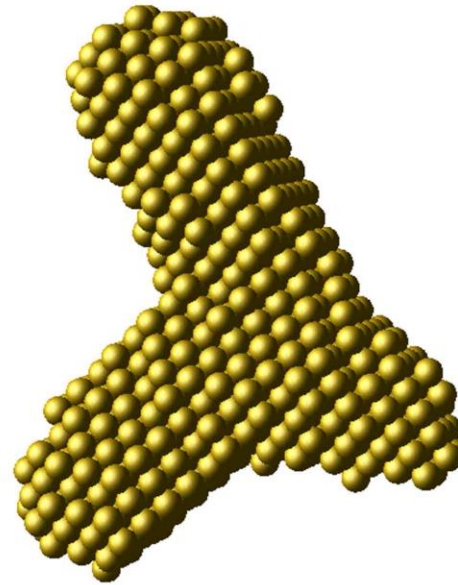
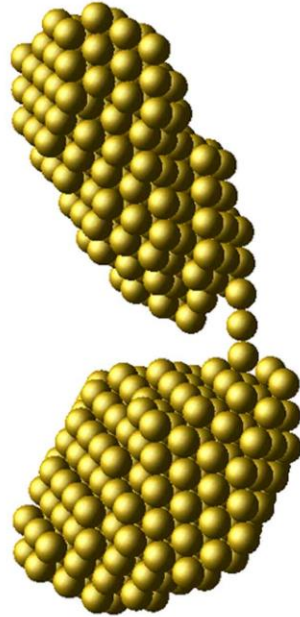
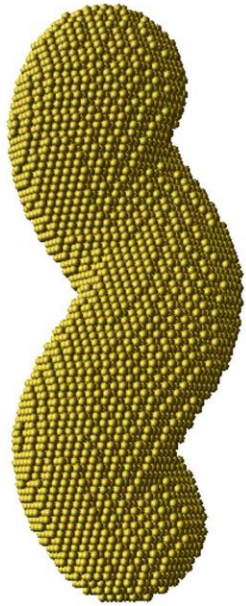


Comparison of DAMMIN models of Fab & Fab-RF fragments with known crystal structure of Fab from IgG.

[DAMMIN: Svergun, D.I. (1999) *Biophys. J.* 76, 2879-2886]



Improvement of the search strategy: a sequence of restarts with higher "temperature" and different penalty proportions (the rightmost body)



**Original
body**

**conventional
solution**

**weight
 $I(s)*s^2$**

**weight
 $I(s)*s$**

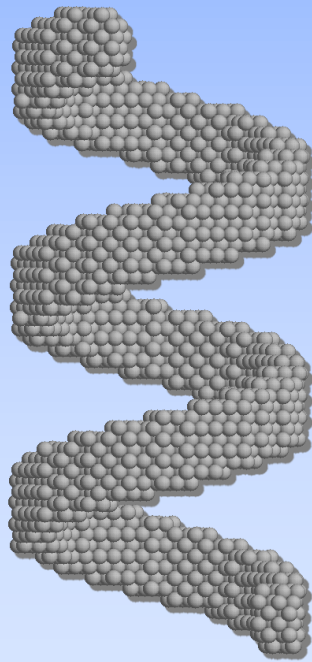
The weight functions used: $I(s)*s^2$ or $I(s)*s$

Now consider *ab initio* restoration of complex structures.

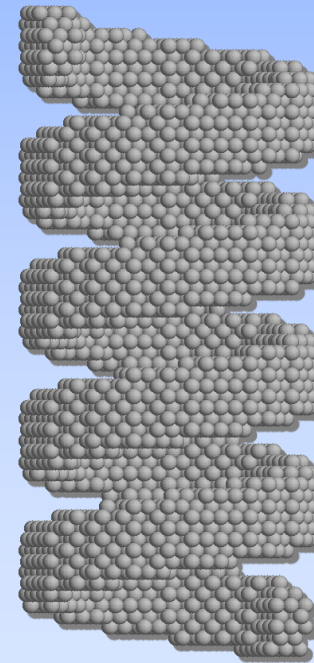
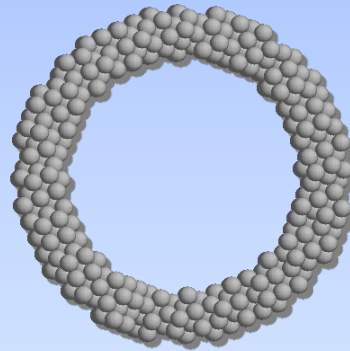
The problem of optimal angular range

We will try to restore helix particles from simulated SAS data calculated on different angular ranges from two helicoidal bodies of the same length and diameter:

Here, the inner structure seems to be more pronounced than for the 4.5-turns model on the right



2.5-turns



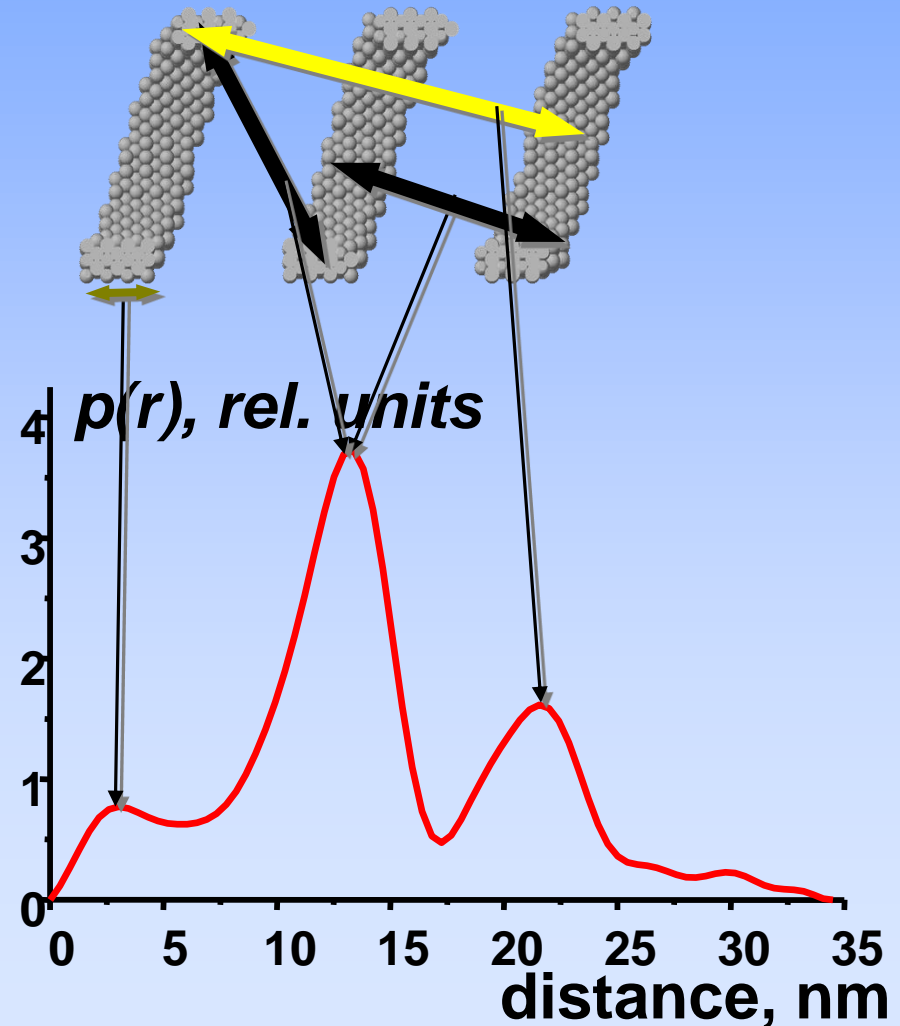
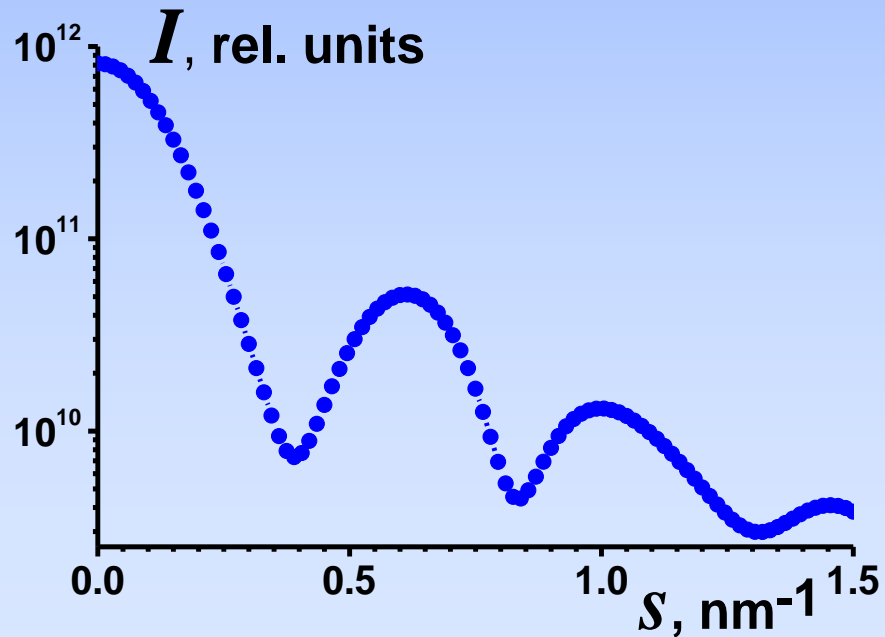
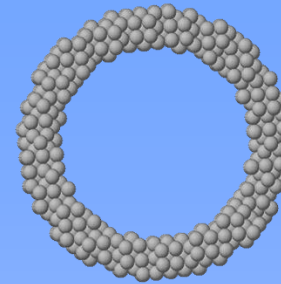
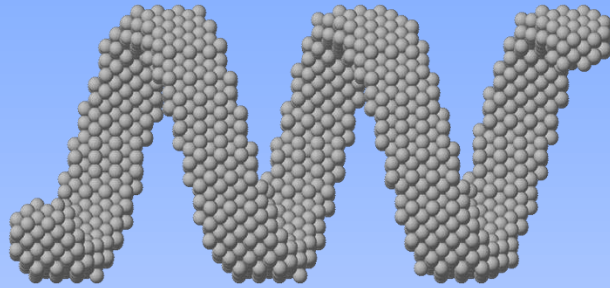
4.5-turns

This model is expected to be too complex to be restored...

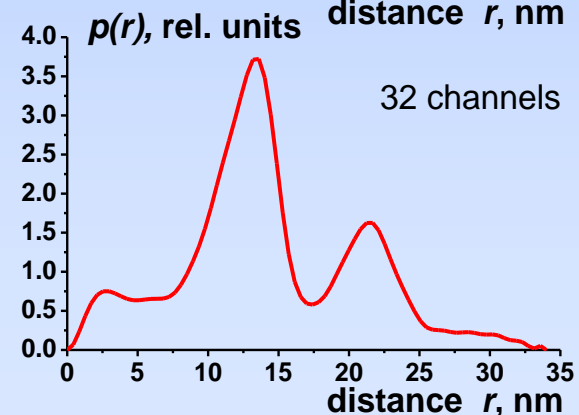
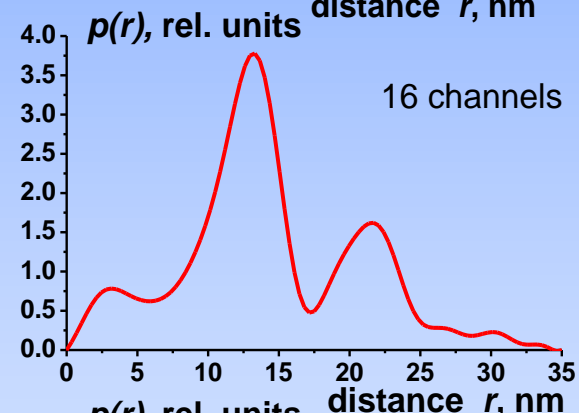
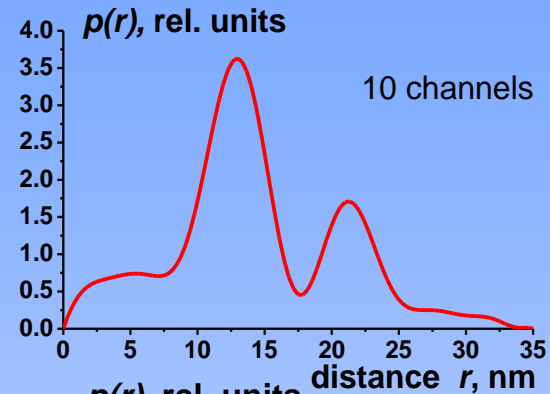
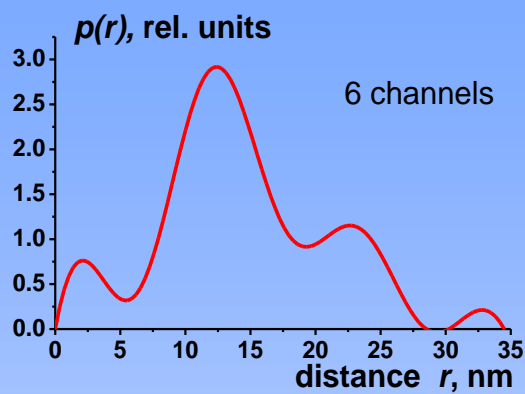
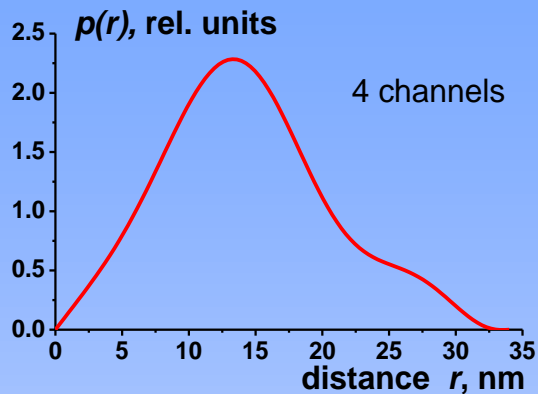
OK, we will try and see what happen

Complex particle: 2.5-turns helix

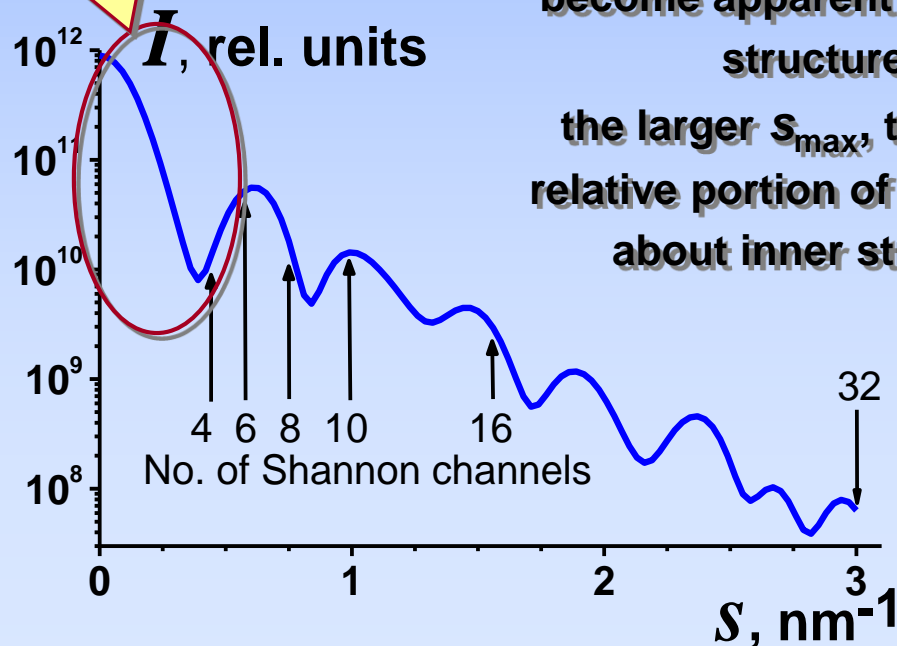
How to see the frequently occurring distances



Dependence of $p(r)$ calculated from SAS patterns from S_{\max}



Scattering from particle shape



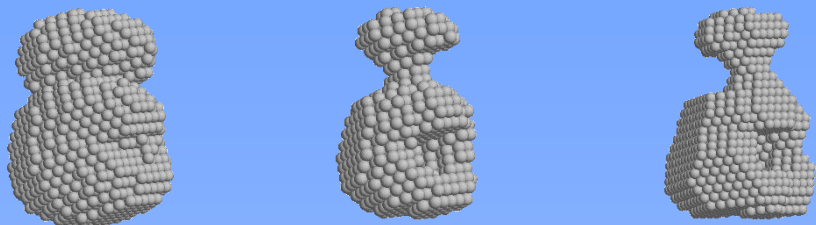
The difference in $p(r)$ should become apparent in restored structures:

the larger S_{\max} , the greater relative portion of information about inner structure.

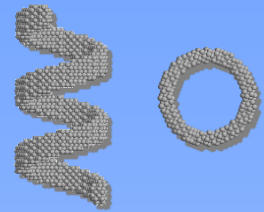
Dependence of structure details from S_{max}

No. of Shann. chann.:

4

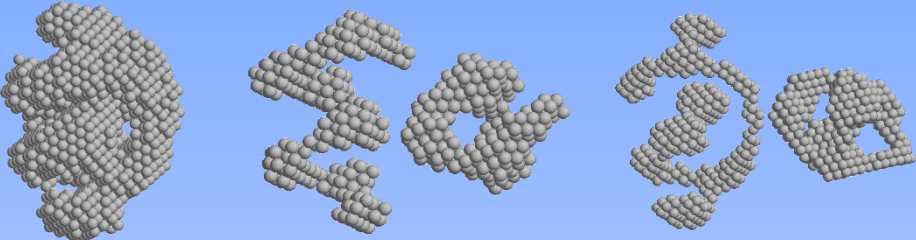


Unsuccessful information about inner structure



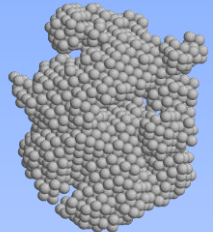
exact structure

6

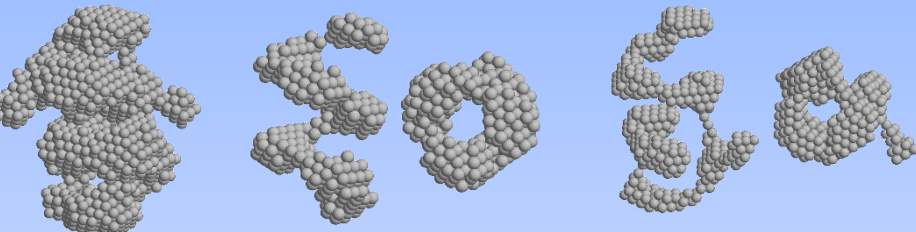


Stable solution, optimum balance between information portions about shape and inner structure

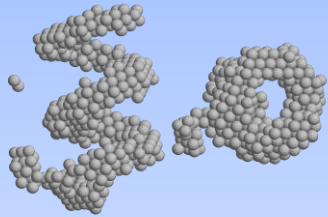
32 channels



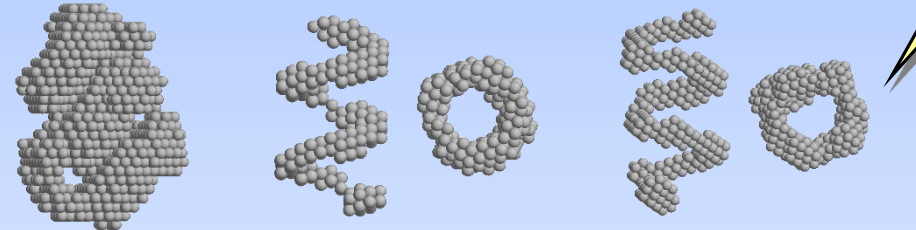
8



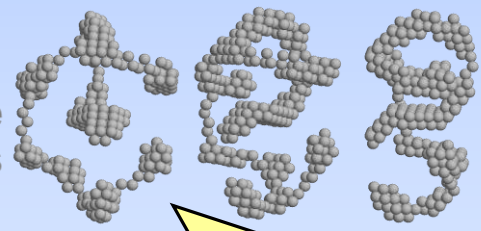
Most probable volume



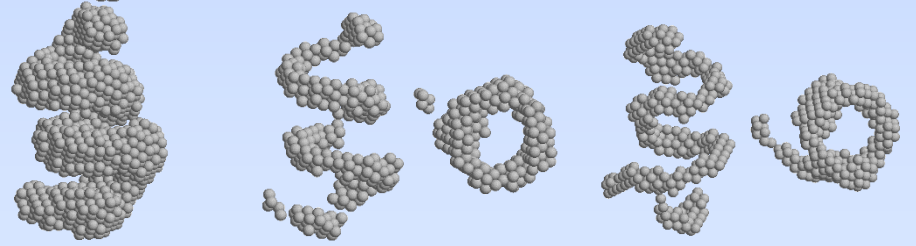
10



One of the solutions



16



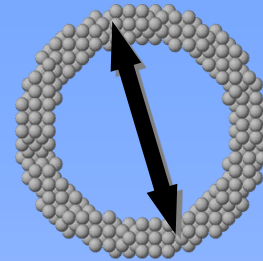
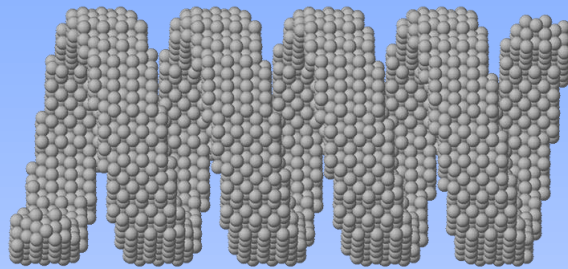
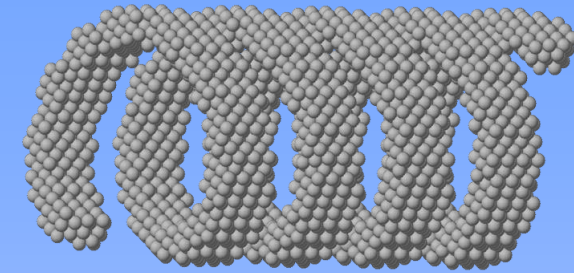
32 channels: too small relative information content about shape (small portion of the beginning part of $I(s)$)

Spread region

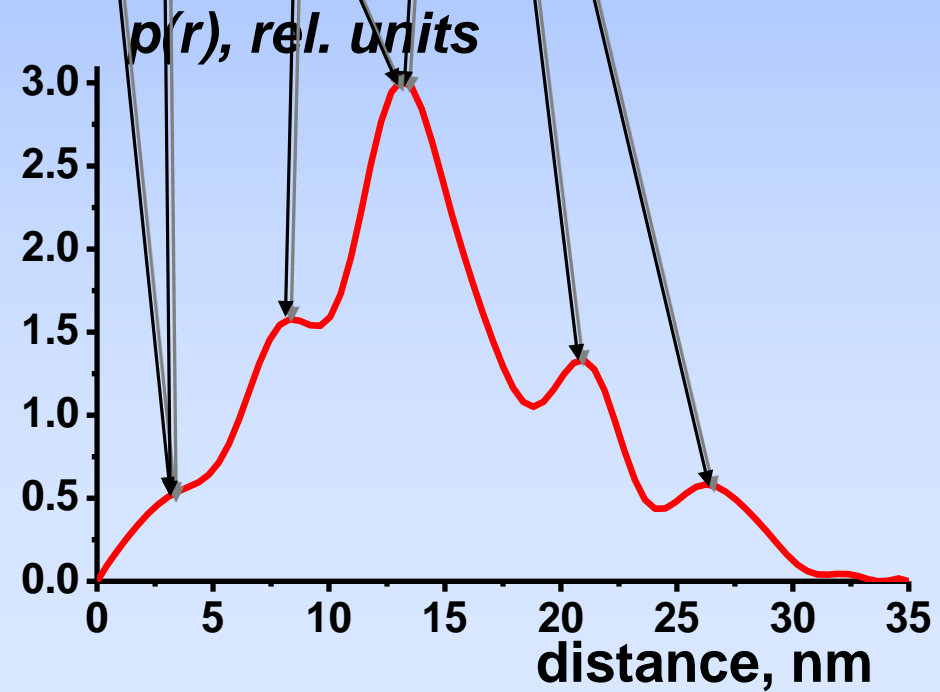
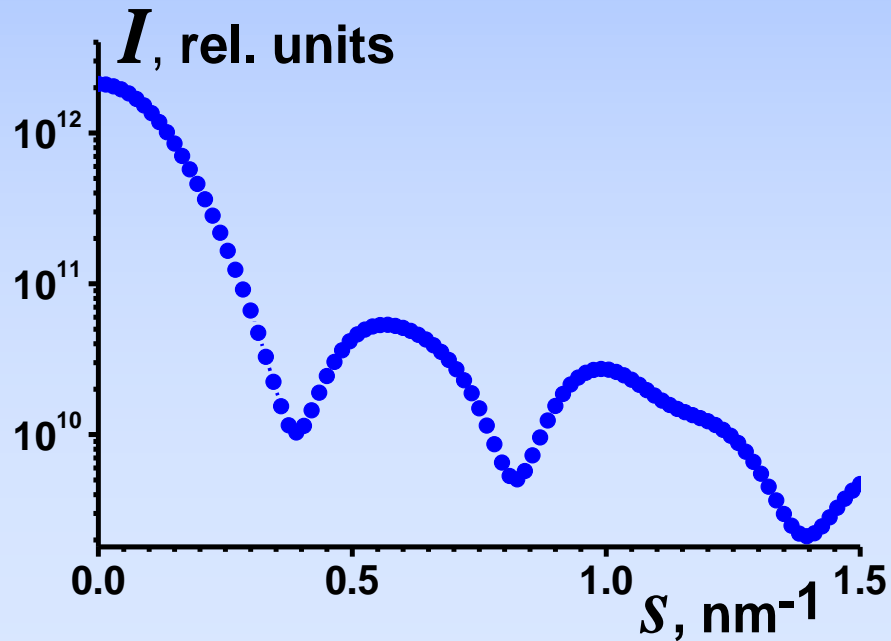
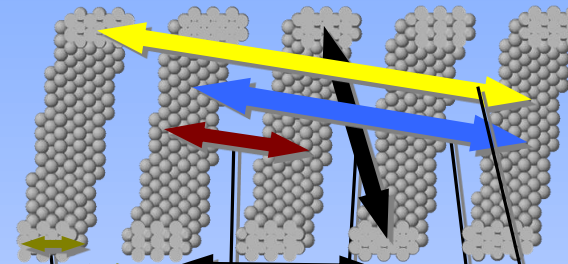
Most probable volume

One of the solutions

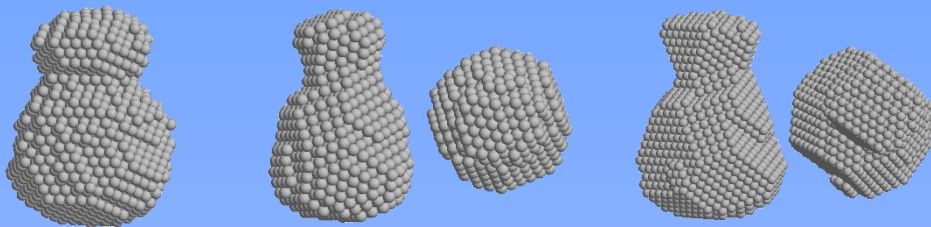
Complex particle: 4.5-turns helix



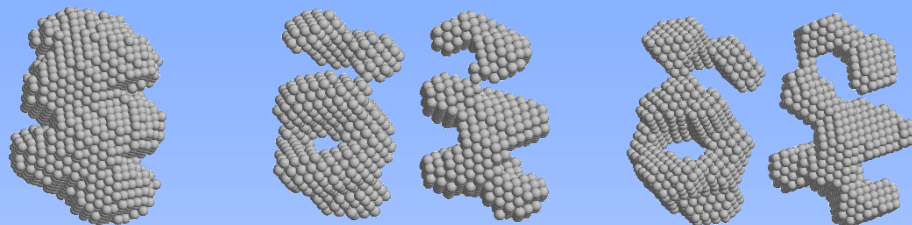
See the frequently occurring distances



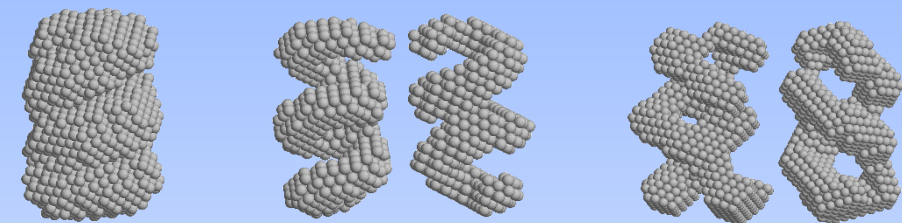
4



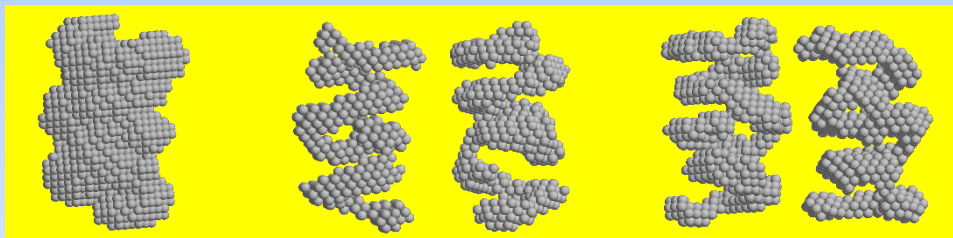
6



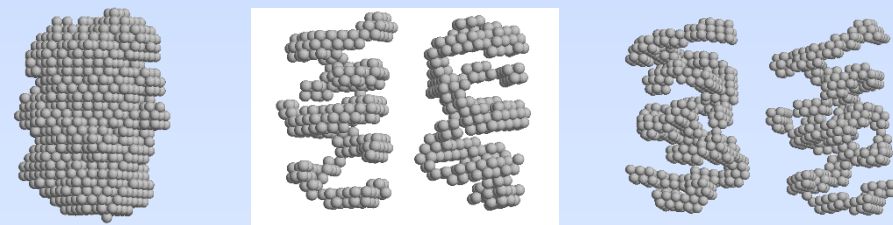
8



10



16

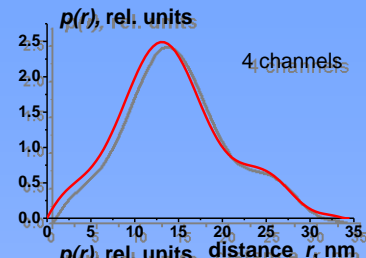


No. of
Shann.
chann.

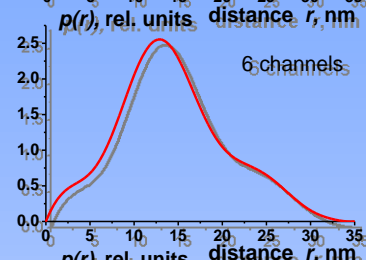
Spread
region

Most probable
volume

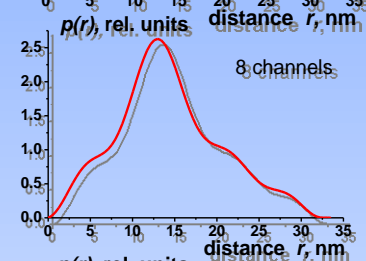
One of the
solutions



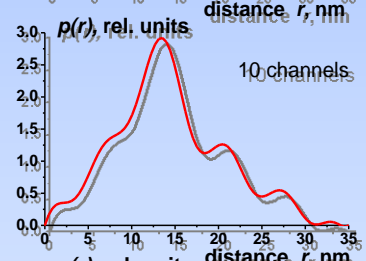
Unsufficient
information about
inner details



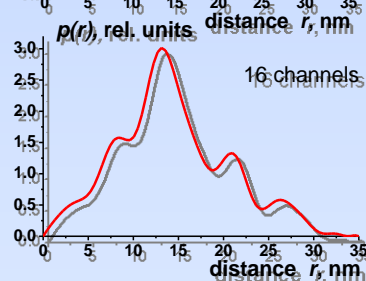
Still unsufficient
information about
inner details



Tries to restore
helix but with
wrong number of
turns



The structure
seems to be too
difficult for
retoration, but its
feature is clear.

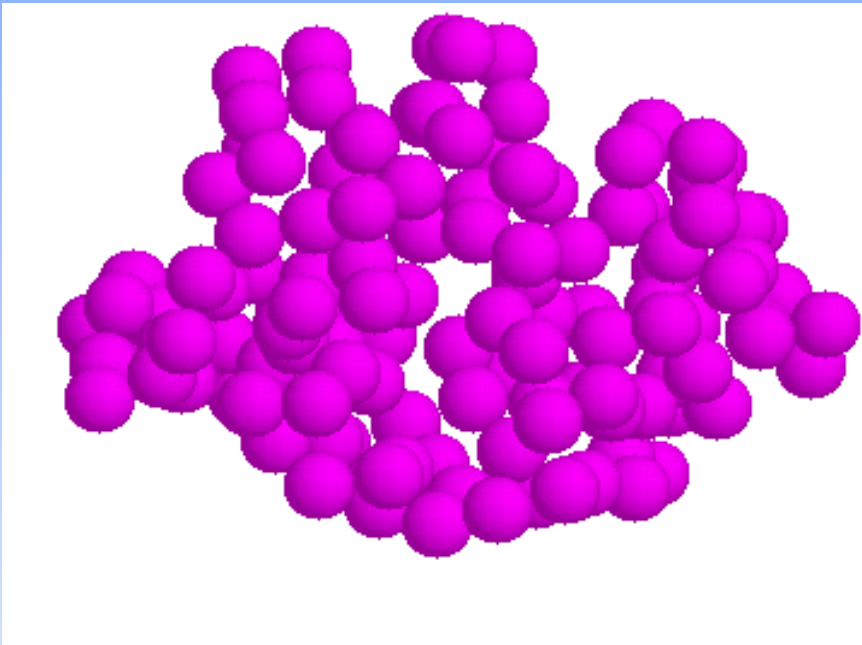


Increasing data
interval has no
effect

Distance distribution

Ab initio программа GASBOR

При разрешении 0.5 нм белок строится в виде ансамбля K модельных псевдо-аминокислотных остатков, "закреплённых" в местах расположения $C\alpha$ атомов с координатами $\{r_{ij}\}$.



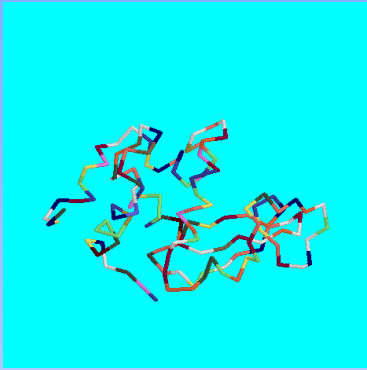
Рассеяние от модели
рассчитывается по
формуле Дебая

$$I_{DR}(s) = \sum_{i=1}^K \sum_{j=1}^K g_i(s) g_j(s) \frac{\sin sr_{ij}}{sr_{ij}}$$

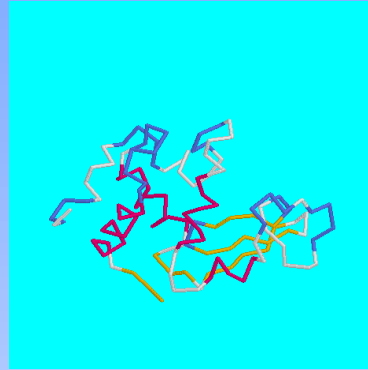
Версия программы, оптимизированная под системы PC Windows, DEC Alpha, Red Hat Linux позволяет строить модели, состоящие из 8000 остатков

Версия программы для SGI IRIX 64 и MacOSX позволяет моделировать структуры из 4000 и 2000, соответственно.

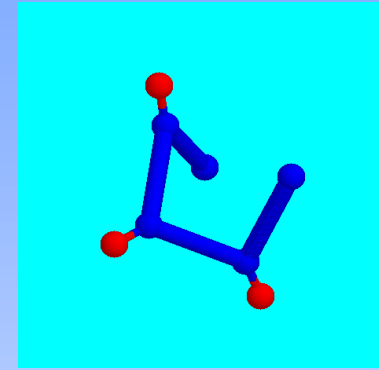
Использование дополнительной информации в GASBOR



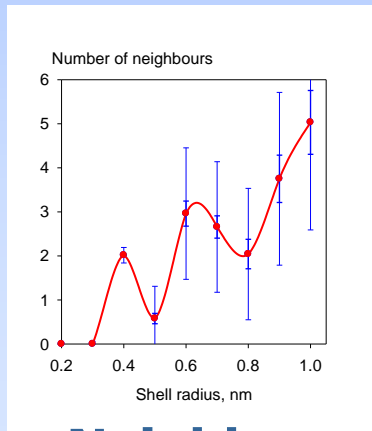
**Primary
sequence**



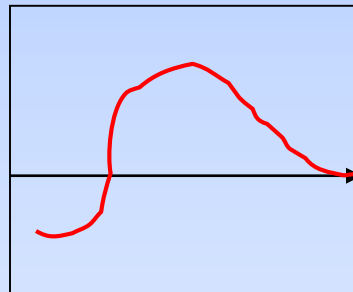
**Secondary
structure**



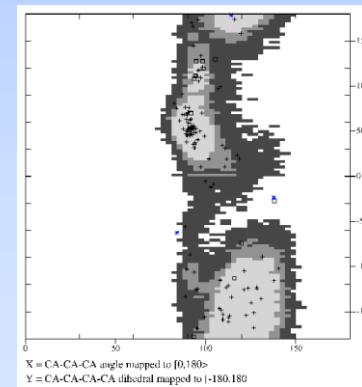
**Excluded
volume**



**Neighbors
distribution**



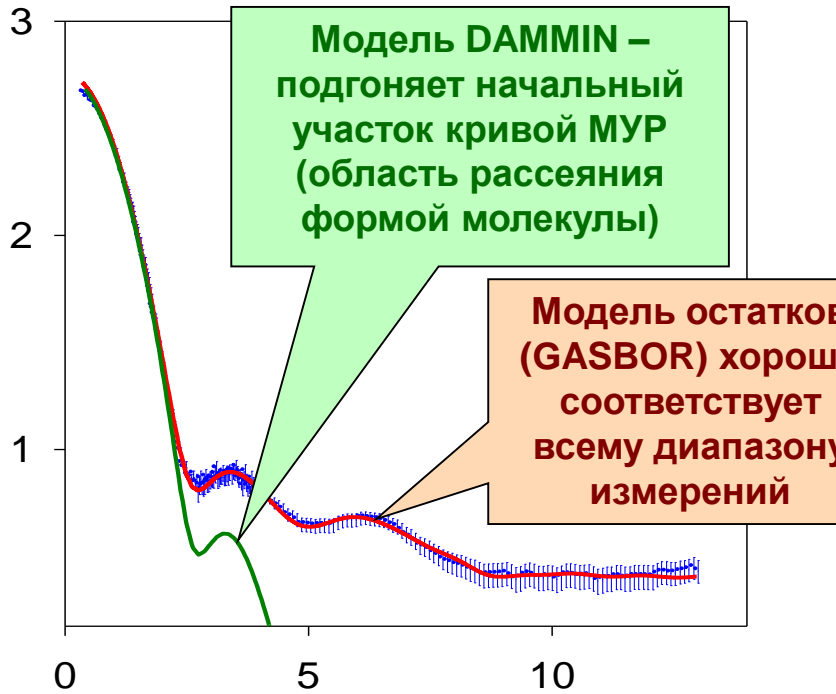
**Knowledge-based
potentials**



**Bond angles &
dihedrals distribution**

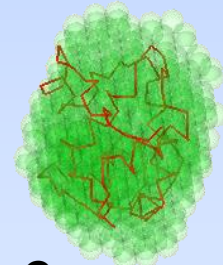
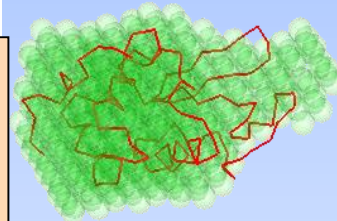
Программы DAMMIN и GASBOR: определение строения белковых молекул в растворе по данным мало- и среднеуглового рентгеновского рассеяния.

Логарифм
интенсивности

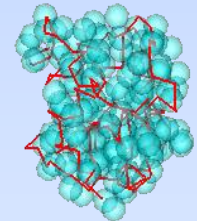
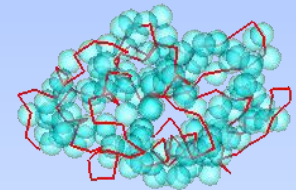
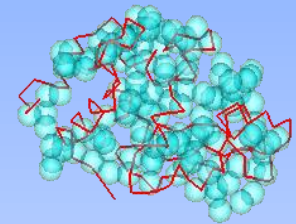
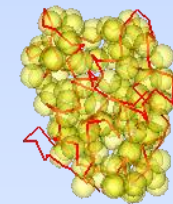
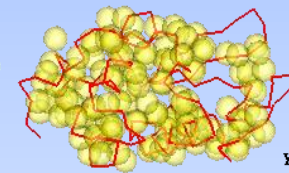
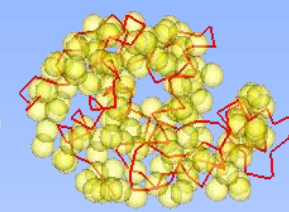


$4\pi \sin(\theta) / \lambda$, θ -угол, λ -длина волны в нм

Модель
DAMMIN
(шариковая)



Более детальные
модели GASBOR
(из аминокислотных
остатков)



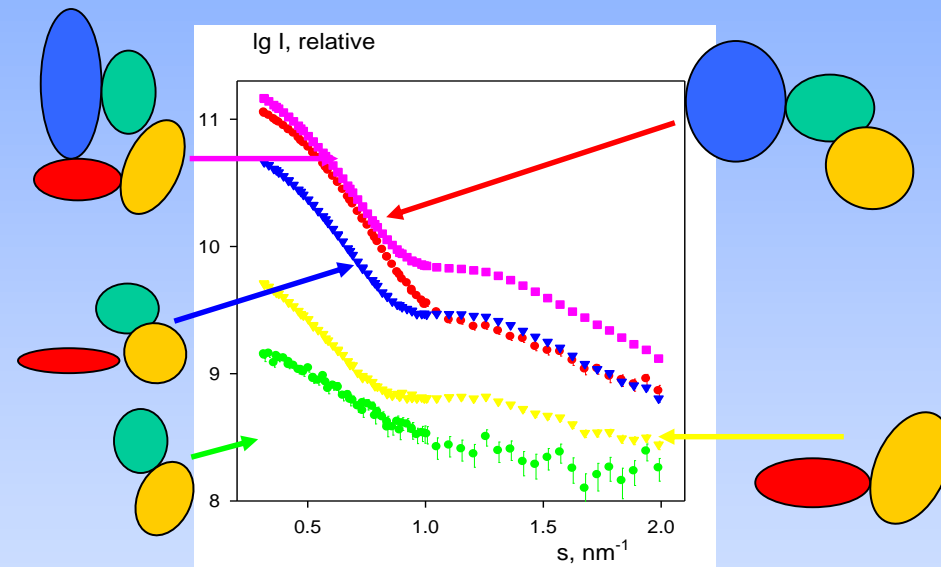
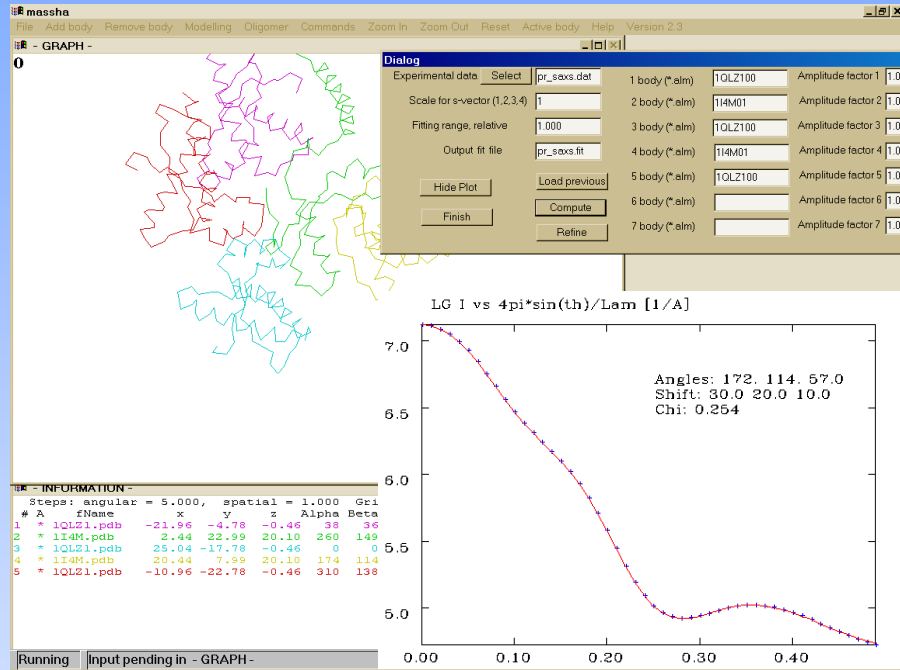
y
x
z
1 нм

Структуры даны в трех ориентациях, для сравнения линиями показаны кристаллические модели

Rigid body modelling

MASSHA/ASSA (interactive search)

SASREF (automated search, multiple data sets)

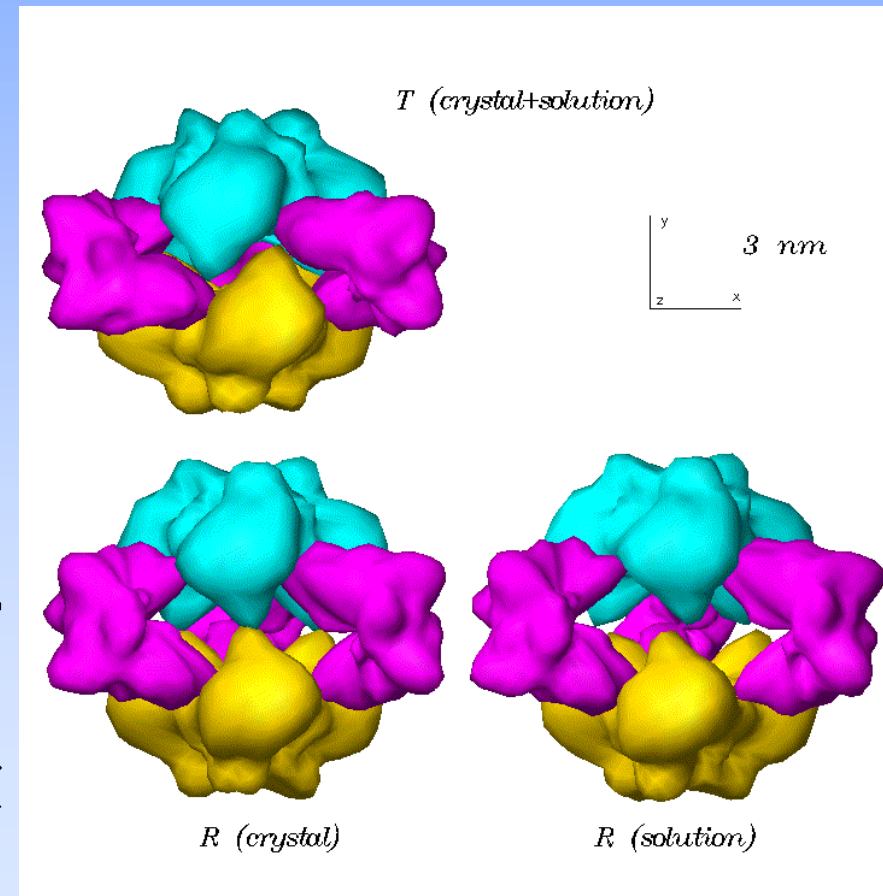
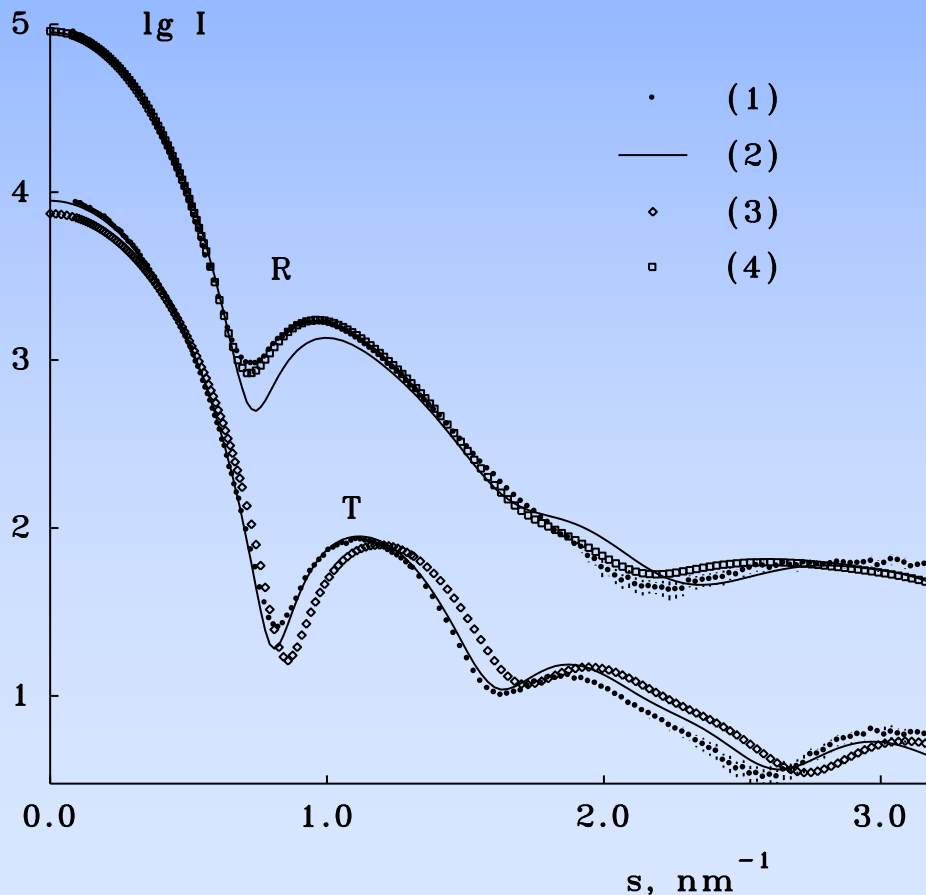


P.V. Konarev, M.V. Petoukhov & D.I. Svergun (2001). *J. Appl. Cryst.* 34, 527-532

Petoukhov, M. V. & Svergun, D. I. (2005). *Biophys. J.* 89, 1237-1250

Determination of tiny differences in protein structures: solution *versus* crystal

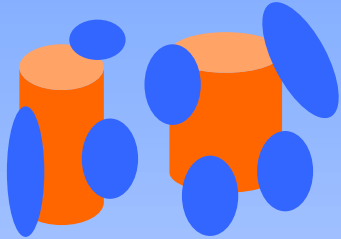
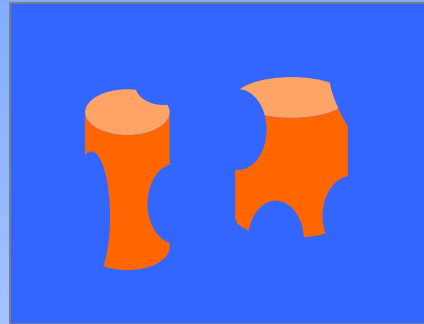
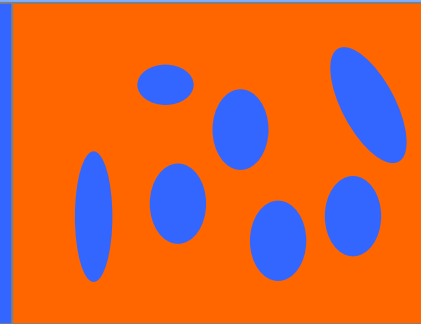
Packing forces in the crystal restrict the allosteric transition in aspartate transcarbamylase



Нейтронное рассеяние от растворов рибосомы 70S *E-Coli*: вариация контраста путем частичного дейтерирования компонентов

0% D₂O

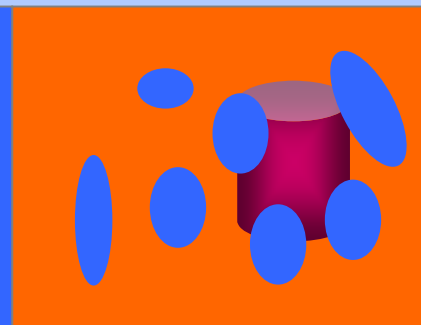
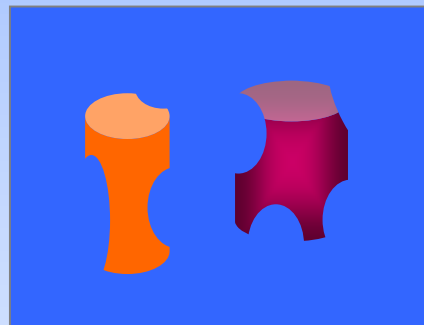
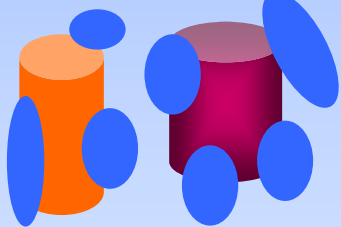
30S 50S

40% D₂O70% D₂O

Содержание
тяжелой воды в
растворителе

Протонированная 70S рибосома (НН30+НН50)

30S 50S



Компоненты:

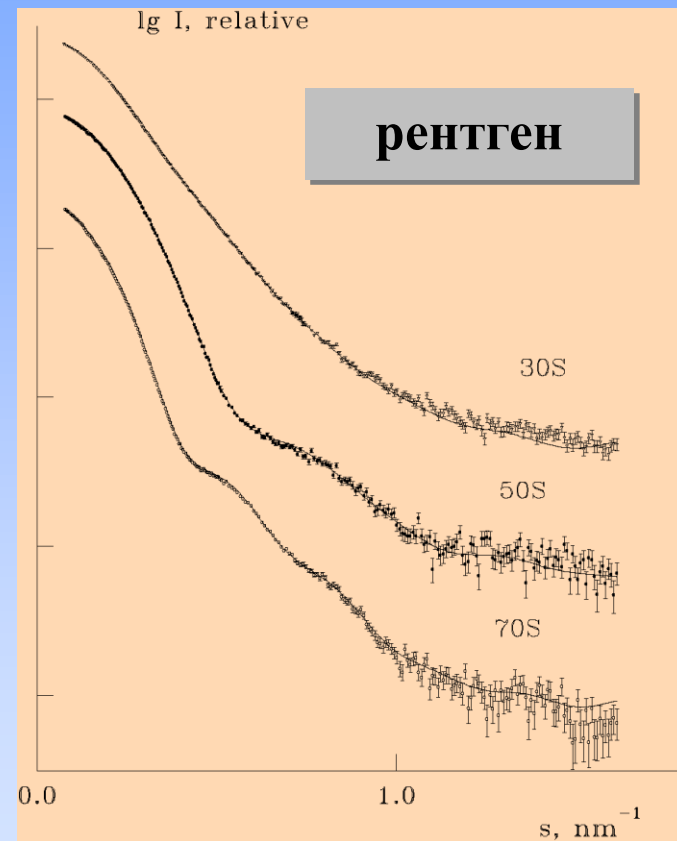
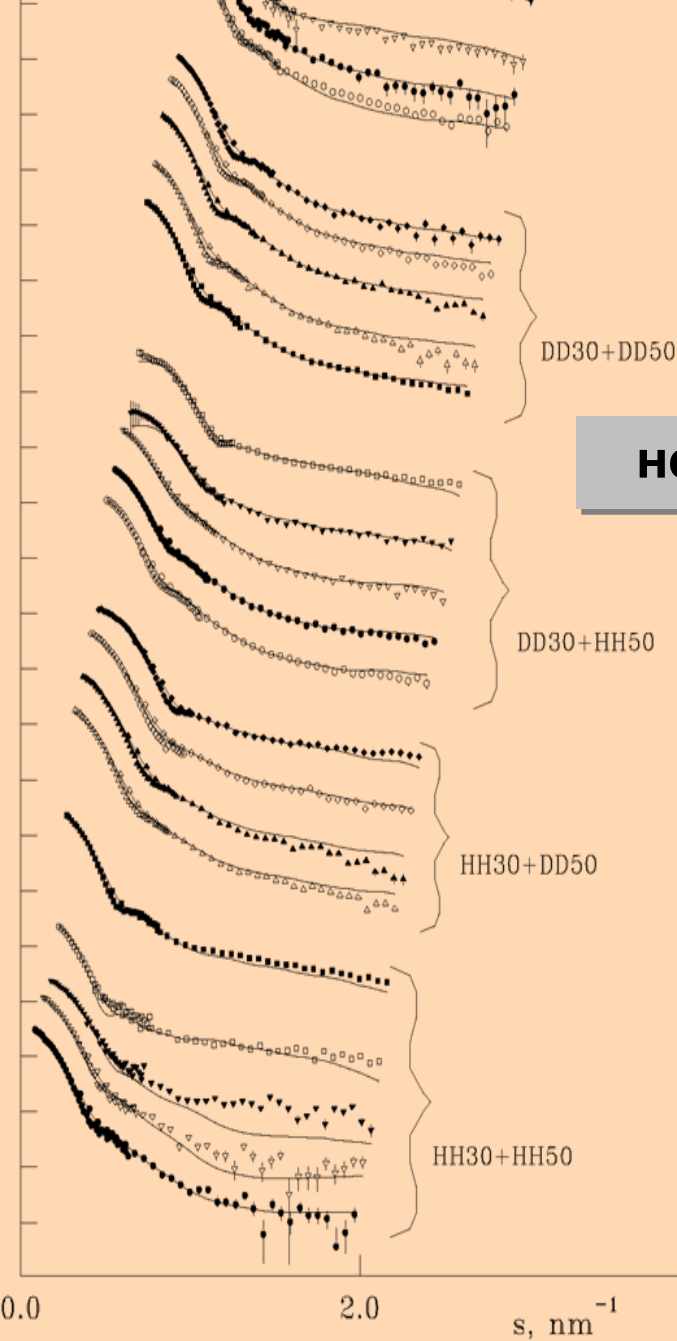
1. Белки 30S
2. РНК 30S
3. Белки 50S
4. РНК 50S

Гибридная 70S, 23S РНК дейтерирована (НН30+НД50)

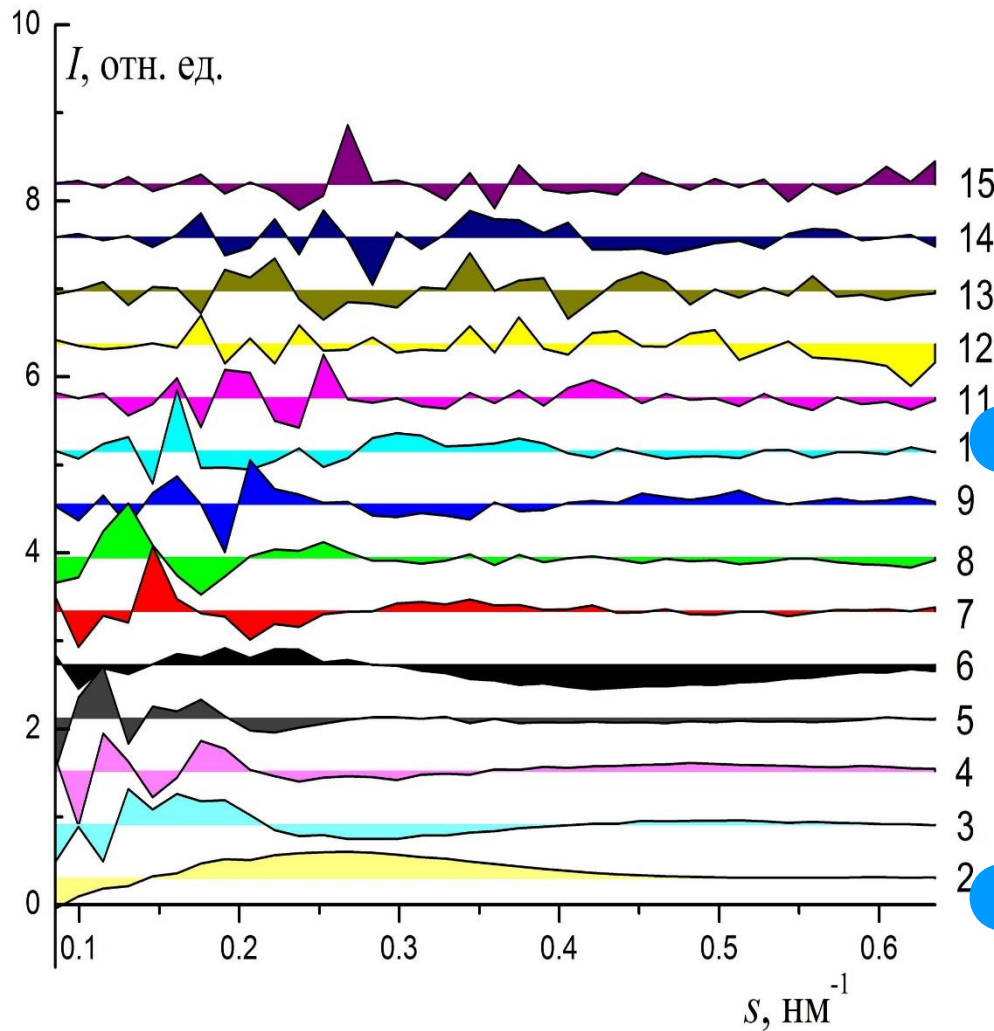
$$I(s) = \sum_{n=1}^4 (\Delta\rho_n)^2 I_{nn}(s) + 2 \sum_{n>k} \Delta\rho_n \Delta\rho_k I_{nk}(s)$$

Рассеяние от 4-х компонентной частицы
есть сумма интенсивностей от каждой
компоненты плюс 6 перекрестных членов.

Данные малоуглового рассеяния от образцов рибосомы 70S *E.coli*



Оценка числа компонентов в матрице данных рассеяния по левым сингулярным векторам



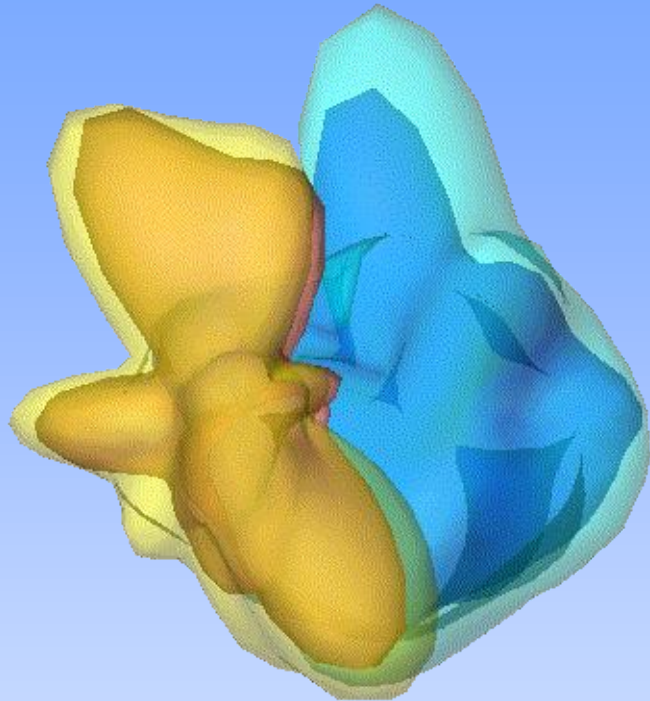
Первые 15 сингулярных векторов матрицы данных нейтронного рассеяния, представленные в виде контуров относительно вектора рассеяния.

Из рисунка видно, что систематическое поведение контуров заметно до 10 вектора включительно.

Критерий Дарбина-Ватсона наличия автокорреляции в матрице остатков F^0 после учета первых 10 компонентов в кривых рассеяния был $1.7 > 1.5$, что говорит о приемлемости оценки числа базисных функций и о числе компонентов рибосомы = 4

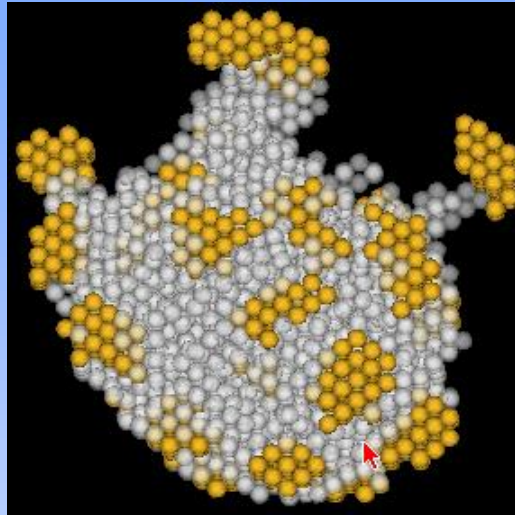
$$F^0 = D - D^0, \quad D^0 = U_{j=1,..K} \cdot \Lambda \cdot V_{j=1,..K}^T$$

Структура рибосомы 70S и 50S *E.coli* в растворе по данным рентгеновского и нейтронного малоуглового рассеяния

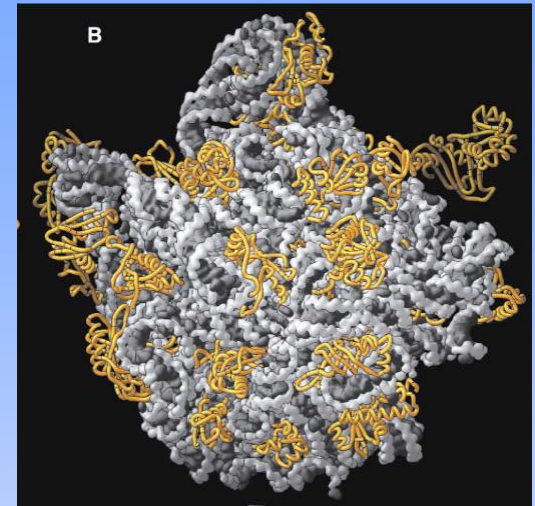


10 nm

D.I.Svergun, N.Burkhardt,
J.Skov Pedersen, M.H.J.
Koch, V.V.Volkov,
M.B.Kozin, et al. J. Mol.
Biol. (1997),. 271, 588-601



Шариковая модель
субъединицы 50S
рибосомы 70S *E.coli* с
разрешением 1 nm по
данным МУР (Svergun
& Nierhaus, May 2000)

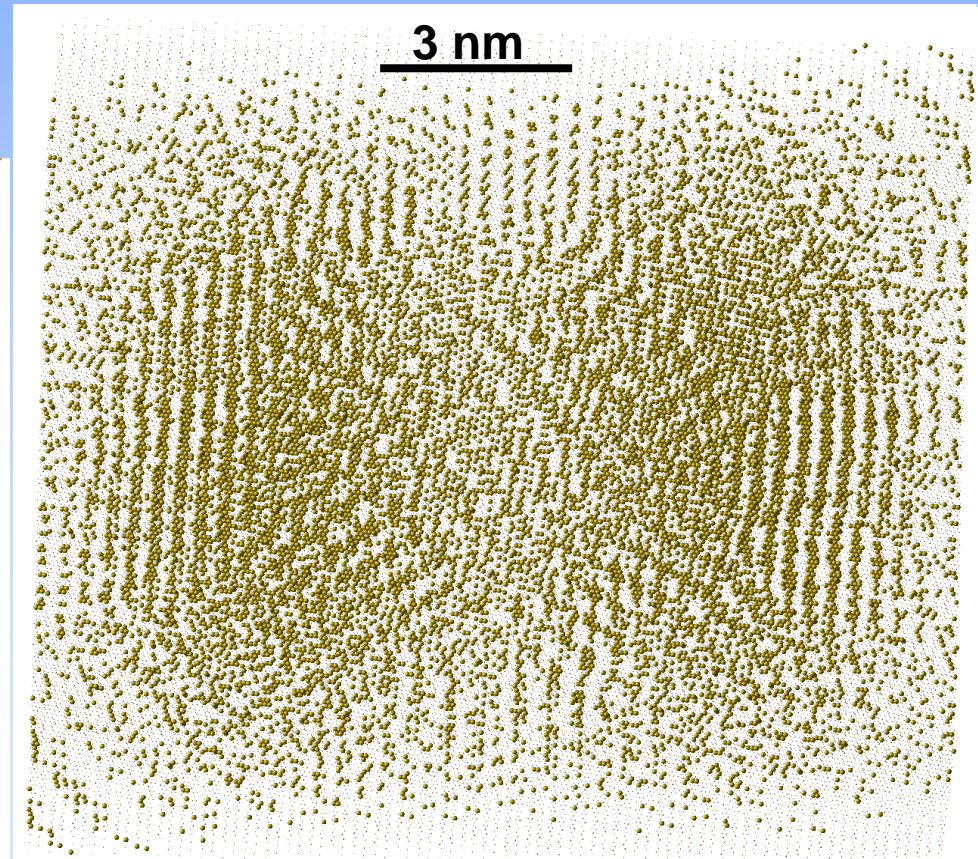
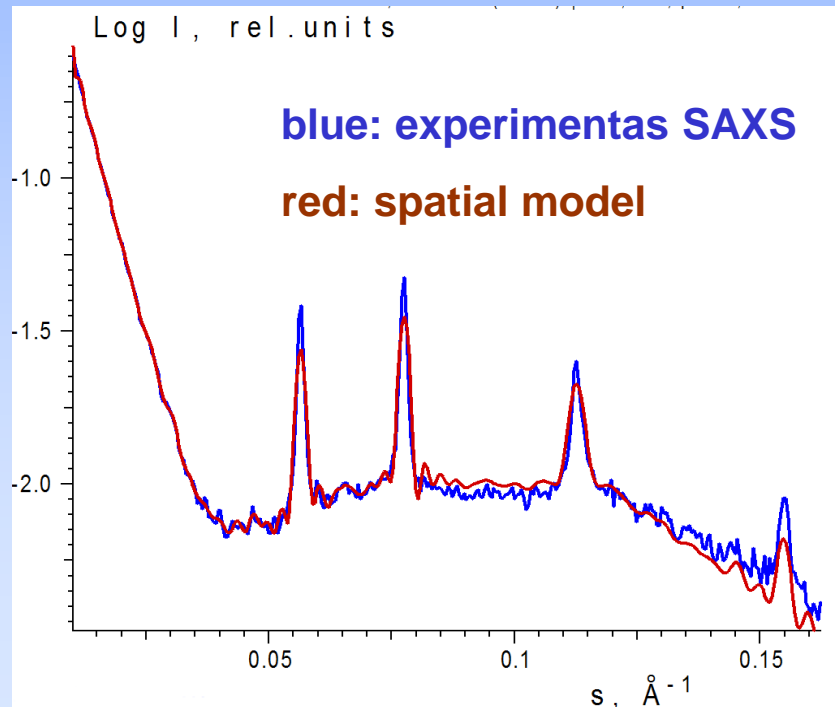


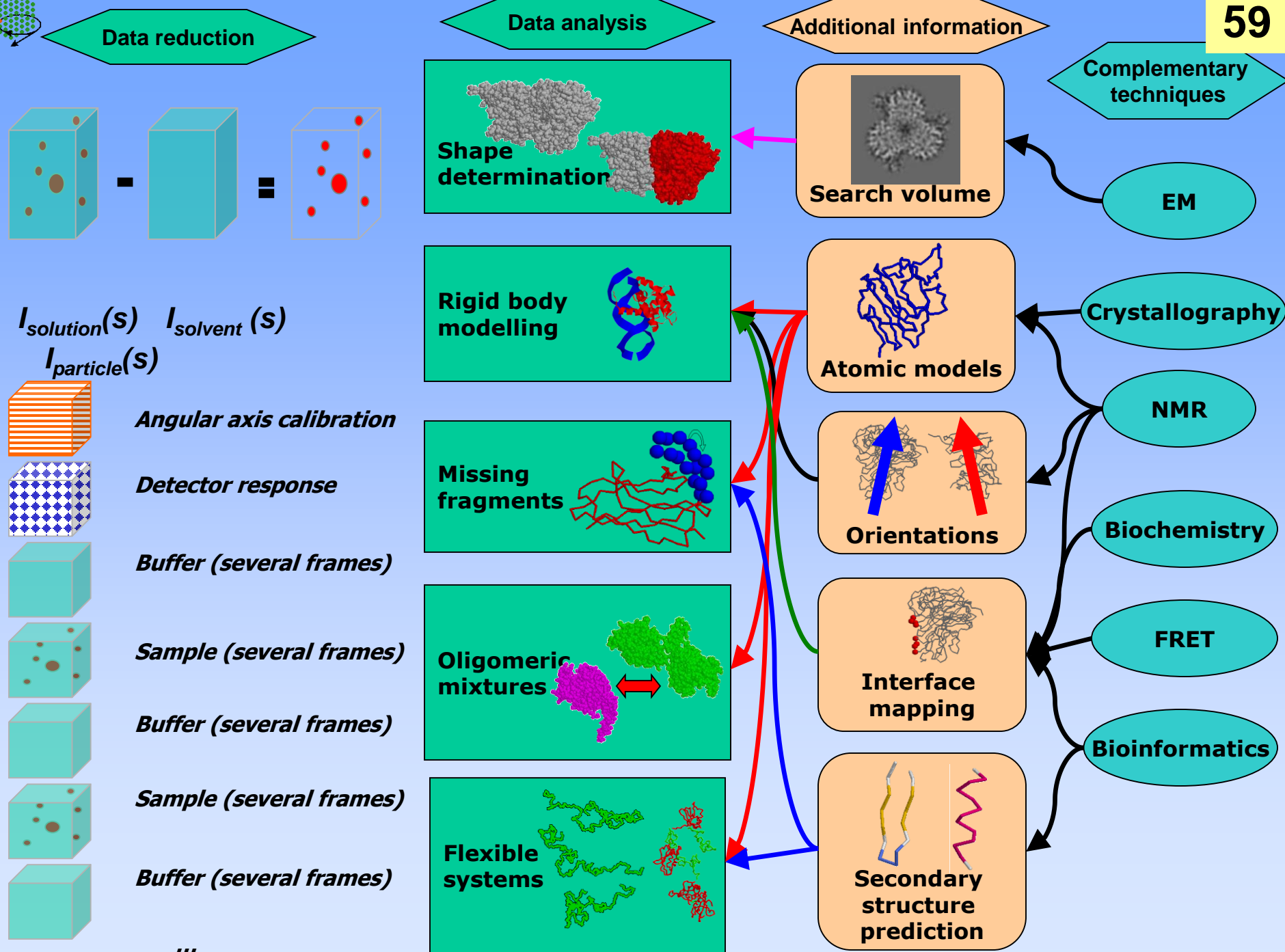
Для сравнения:
кристаллическая
модель
субъединицы 50S
H.marismortui (Steitz
group, August 2000)

Direct space modeling:

- program DAMMIN (new version)
- large amount of space nodes (here: 150 000)
- direct fit to experimental data
- use of wide angular range is possible

Modeling of precipitate
cytochrome-C + cardiolipin at
pH 7.3, phosphate buffer







Outline of ATSAS



Polydisperse & interacting systems:

OLIGOMER

(Volume fractions of components)

MIXTURE

(Modelling multi-component systems)

PEAK

(Evaluating peak positions)

EOM

(Unfolded or flexible proteins)

Database for rapid protein characterization:

DARA

Ab initio structure analysis:

DAMMIN/DAMMIF

(Bead modelling)

SASHA

(Shape determination using envelope functions)

GASBOR

(Dummy residues modelling)

MONSA

(Multiphase bead modelling)

Data regularization & overall structural parameters:

GNOM, AUTOGNOM

Data Reduction and Processing:

PRIMUS, AUTORG

(Primary analysis and manipulations with small-angle scattering data)

Addition of missing fragments to high resolution models:

CREDO

Rigid body modelling:

MASSHA

(Manual & automated refinement)

ASSA

(Manual rigid body refinement/UNIX)

GLOBSYMM

(Quaternary structure determination of symmetric oligomers)

SASREF

(Multisubunit complexes modelling)

BUNCH

(Multidomain proteins modelling v.s. multiple data sets)

Computation of solution scattering from atomic models:

CRYSOL

(X-ray scattering)

CRYSON

(Neutron scattering)

Models averaging:

SUPCOMB

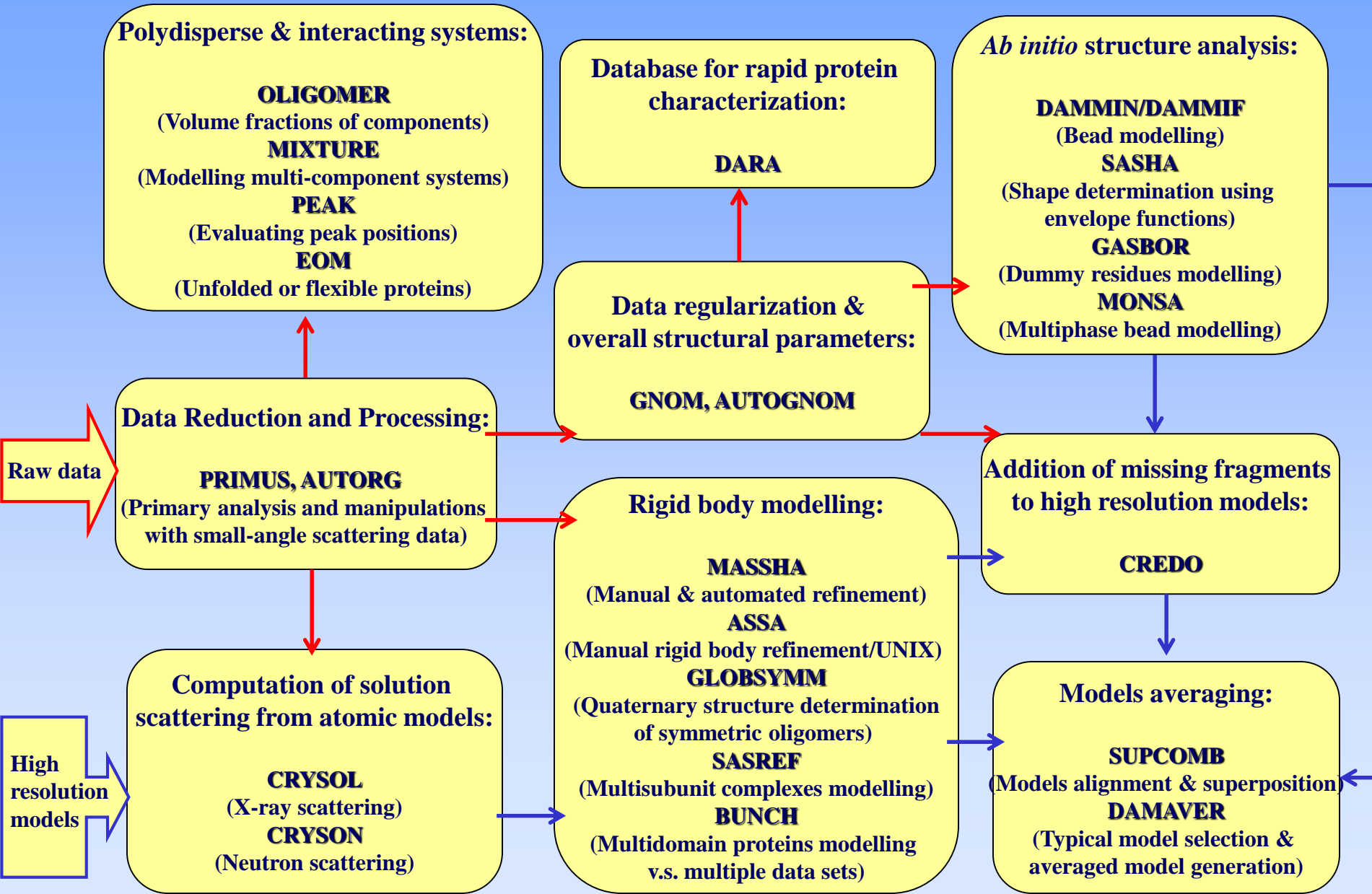
(Models alignment & superposition)

DAMAVER

(Typical model selection & averaged model generation)

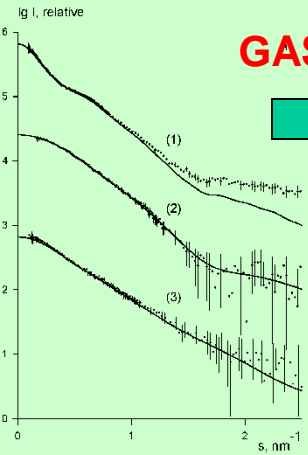
Raw data

High resolution models

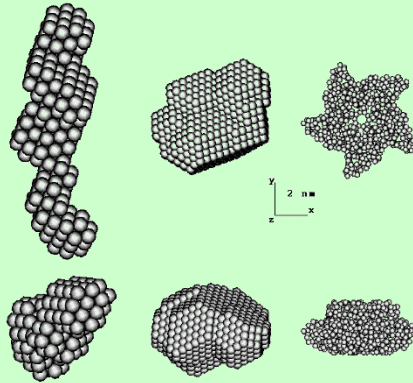


Thank you for attention!

Сочетание различных методов: структура вертексного комплекса бактериофага PRD1

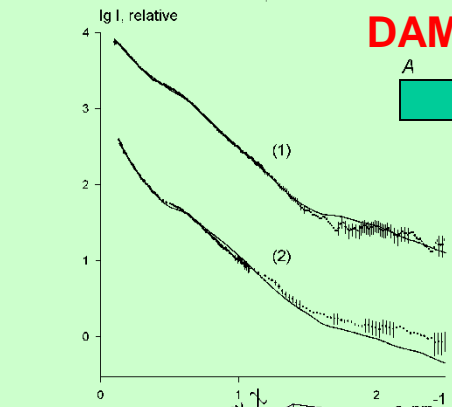


GASBOR

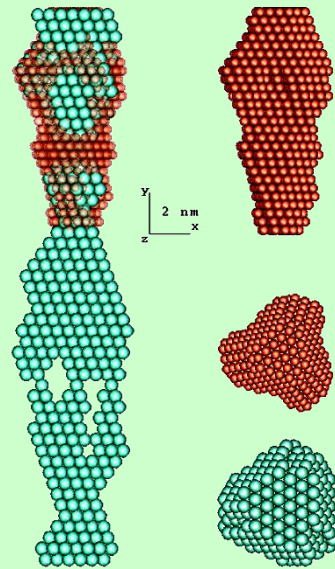
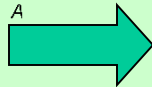


PRD1 has an icosahedral capsid similar to that of adenovirus

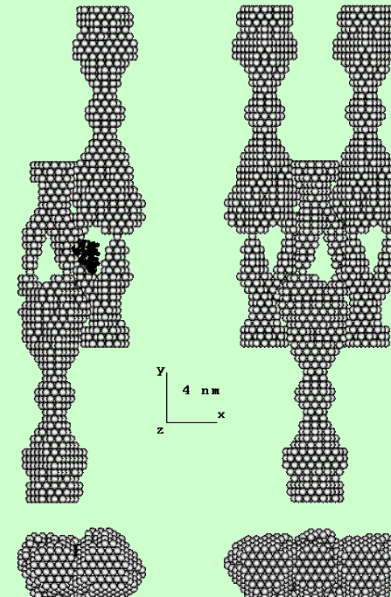
Sokolova, A. et al. (2001) *J. Biol. Chem.* 276, 46187.



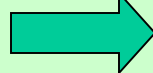
DAMMIN



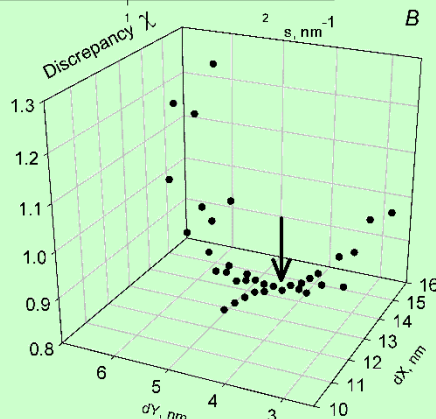
EM, Xtal, Hydro



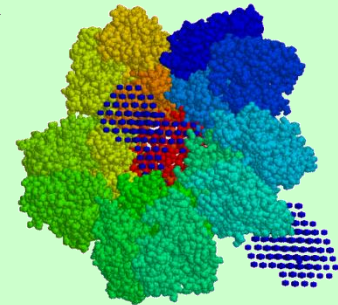
MASSHA



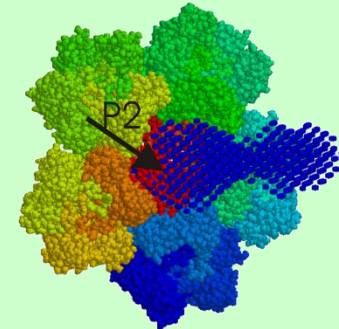
OLIGOMER



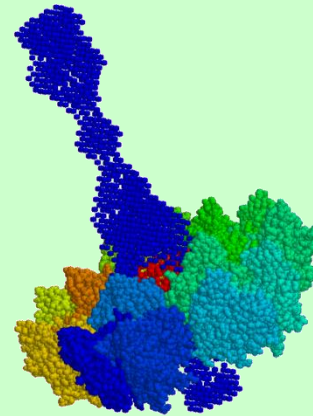
A



B

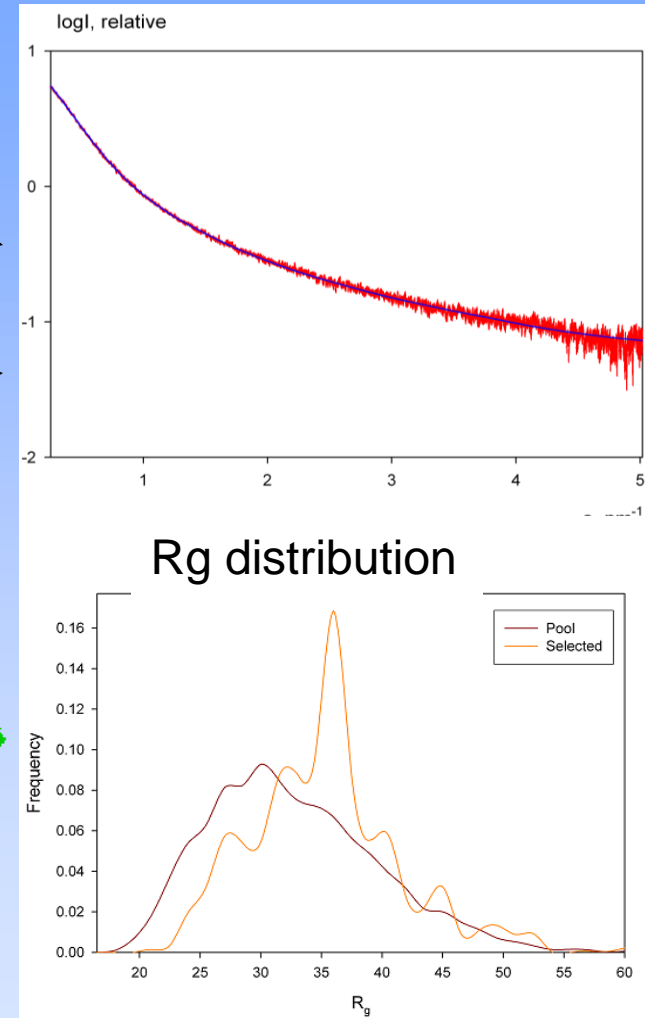
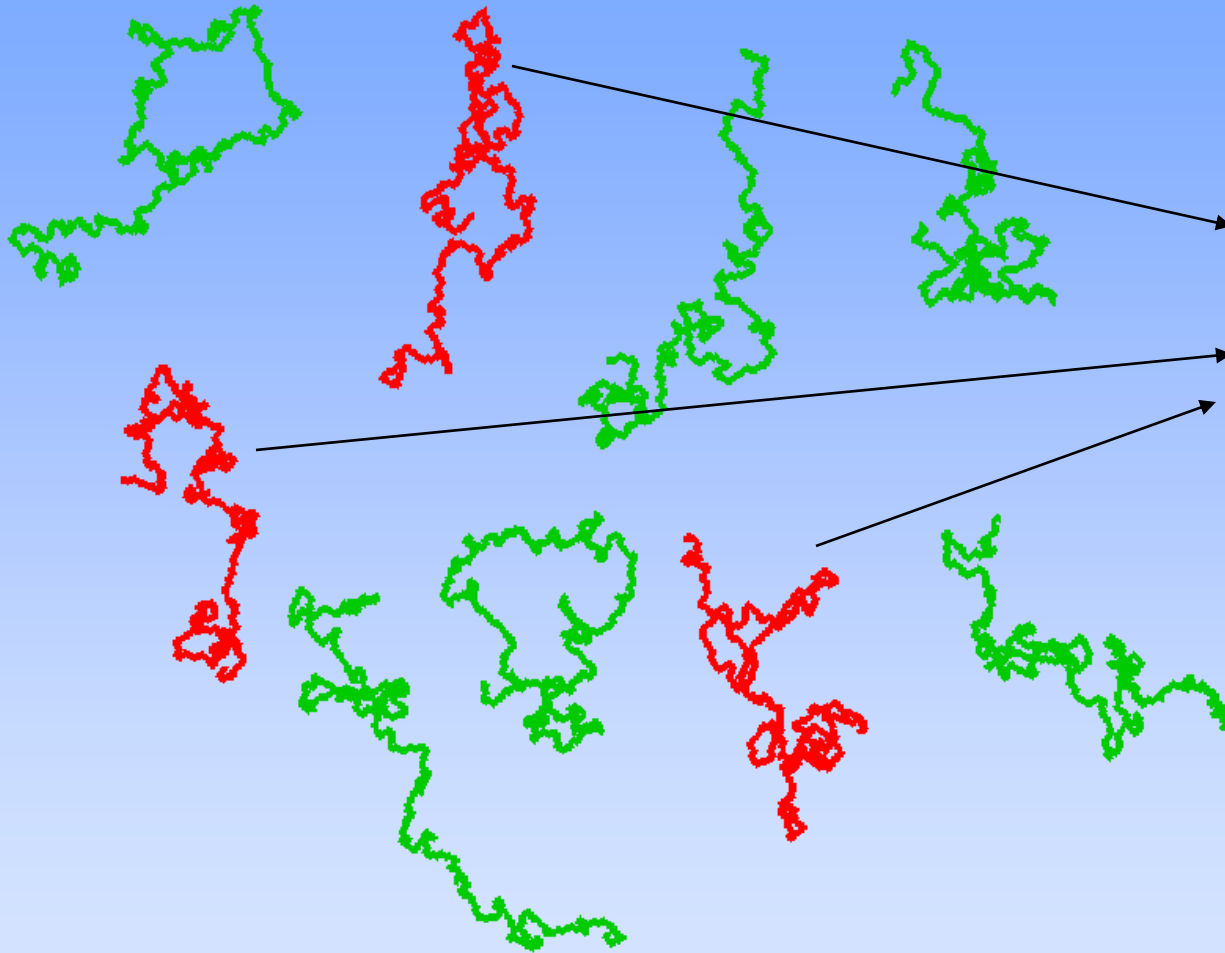


C





EOM – Ensemble optimization method



P. Bernado, E. Mylonas, M. V. Petoukhov, M. Blackledge & D. I. Svergun (2007)
JACS, 129, 5656-5664

