



Incommensurate Magnetic Phases of the Multiferroic Compound MnCr_2O_4 Described with the Super-space Formalism

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Introduction

- Nowadays, chromium-based normal spinel oxides ACr_2O_4 are one of the most studied materials in the condensed matter community due to the interplay between its magnetic, electric and structural properties [1,2].
- In particular, for MnCr_2O_4 , the ground state magnetic structure is still controversial because the magnetic structures reported by different groups and investigated by independent techniques are inconsistent [1-3].

Super-space Group Formalism

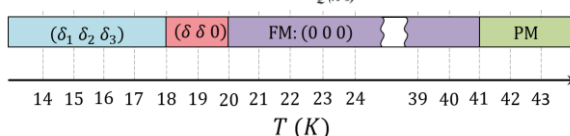
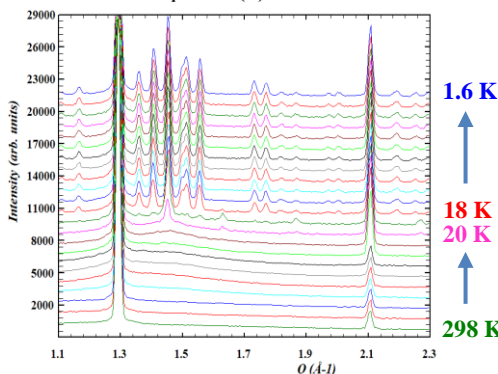
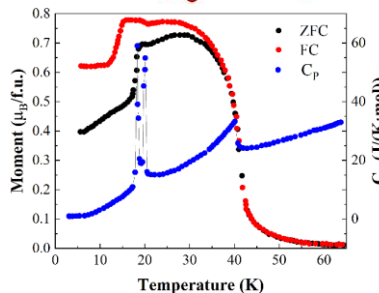
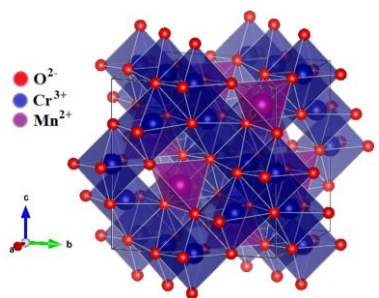
- Incommensurate structure = basic structure + modulations:

$$\vec{M}_j(x_4) = \vec{M}_{j,0} + \sum_{n=1}^{\infty} \left[\vec{M}_{j,ns} \sin(2\pi n x_4) + \vec{M}_{j,nc} \cos(2\pi n x_4) \right]$$

- Symmetry operations: space group operations + phase shifts of modulations. Determined by the magnetic super-space group.

Methods

- The magnetic structure of this compound was reinvestigated by magnetization, specific heat and neutron diffraction at different temperatures.
- The results suggested that a new magnetic phase, not previously reported, is developed under 18 K.
- The magnetic phases in this sample were:
 - Ferrimagnetic order below $T_C = 45$ K
 - Conical spin order with propagation vector $\vec{k}_{S1} = (0.62(1), 0.62(1), 0)$ below $T_{S1} = 20$ K
 - Conical spin order with propagation vector $\vec{k}_{S2} = (0.660(3), 0.600(1), 0.200(1))$ below $T_{S2} = 18$ K.



Results

- Using the super-space group approach [4], the symmetry of the nuclear and magnetic structures is determined:

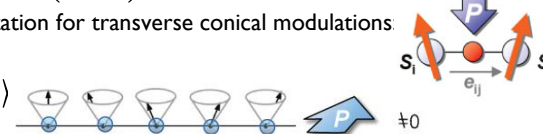
Phase	Group	Irr. Rep	\vec{k}	$\vec{M}_{j,0}$	$\vec{M}_{j,s}$	$\vec{M}_{j,c}$
PM	Fd-3m (#227)	-	-	-	-	-
FiM	Imm'a' (#74.559)	$m\text{GM}_4^+$	(0 0 0)	$\langle 1\bar{1}0 \rangle$	-	-
$\delta \delta 0$	$\text{Im}'a'2(0,0,g)0ss$ (#46.1.12.4.m245.1)	$m\text{GM}_4^+ \oplus m\text{SM}2$	(0.62 0.62 0)	$\langle 1\bar{1}0 \rangle$	$\langle 110 \rangle$	$\langle 001 \rangle$
$\delta_1 \delta_2 \delta_3$	$\text{P}1(a,b,g)0$ (#1.1.1.1.m1.1)	$m\text{GM}_4^+ \oplus m\text{GPI}$	(0.66 0.6 0.2)	$\langle 100 \rangle$	$\langle 010 \rangle$	$\langle 001 \rangle$

- Electric polarization $\vec{P} \propto \vec{r}_{ij} \times (\vec{S}_i \times \vec{S}_j)$, also can be expressed as: $\vec{P} \propto \vec{k} \times \vec{M}_z$.

- Non-zero value of polarization for transverse conical modulations:

$\delta \delta 0$ phase: $\vec{P} \parallel \langle 001 \rangle$

$\delta_1 \delta_2 \delta_3$ phase: $\vec{P} \parallel \langle 01\bar{3} \rangle$



Conclusions

- New magnetic phase, not previously reported, identified under 18 K.
- Using SGF, symmetry of nuclear and magnetic structures is determined.
- Presence of transverse conical magnetic structures in lower-temperature phases implies existence of multiferroicity.
- Through simple theoretical calculations, we derive the macroscopic electric polarization vector for each magnetic phase.

References

- [1] K. Dey et al., Journal of Magnetism and Magnetic Materials 435, 15 (2017).
- [2] K. Tomiyasu et al., Phys. Rev. B 70, 214434 (2004).
- [3] J. M. Hastings and L. M. Corliss, Phys. Rev. 126, 556 (1962).
- [4] J. Rodríguez-Carvajal and J. Villain, Comptes Rendus Physique 20, 770 (2019).