



# Совместное использование нейтронного и синхротронного излучений для анализа структуры и динамики материалов

С.Б.Вахрушев

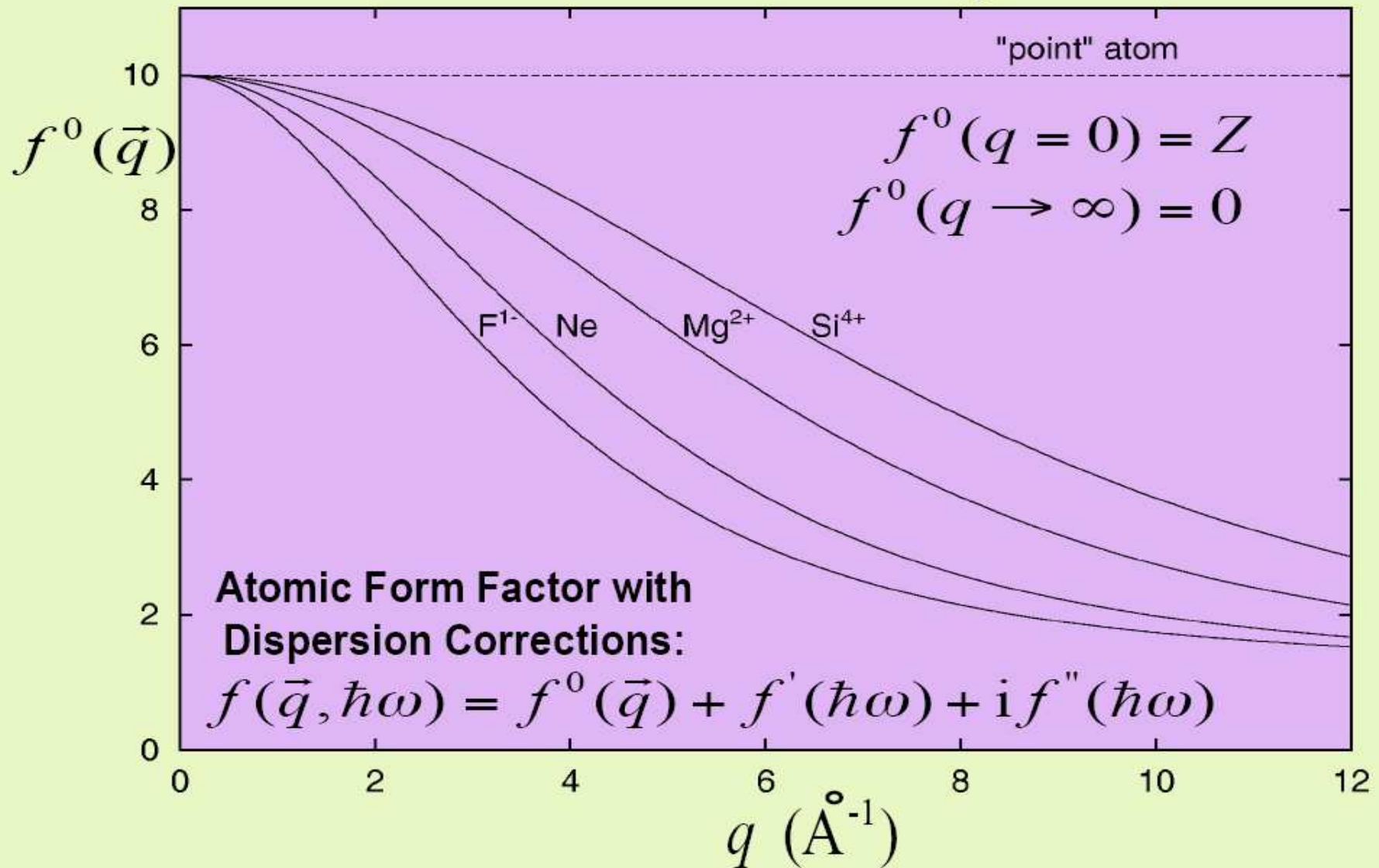
# Нейтроны и СИ



Параметр	Нейтроны	СИ
Длина волны, nm	0.025 - 3	0.01 - ?
Энергия	0.1 – 1000 meV	? – 100 KeV
Спин	1/2	1
Магнитный момент	1.913 $\mu_N$	0
Зависимость $f(\lambda)$	Для ядерного – нет, Для магнитного - есть	есть



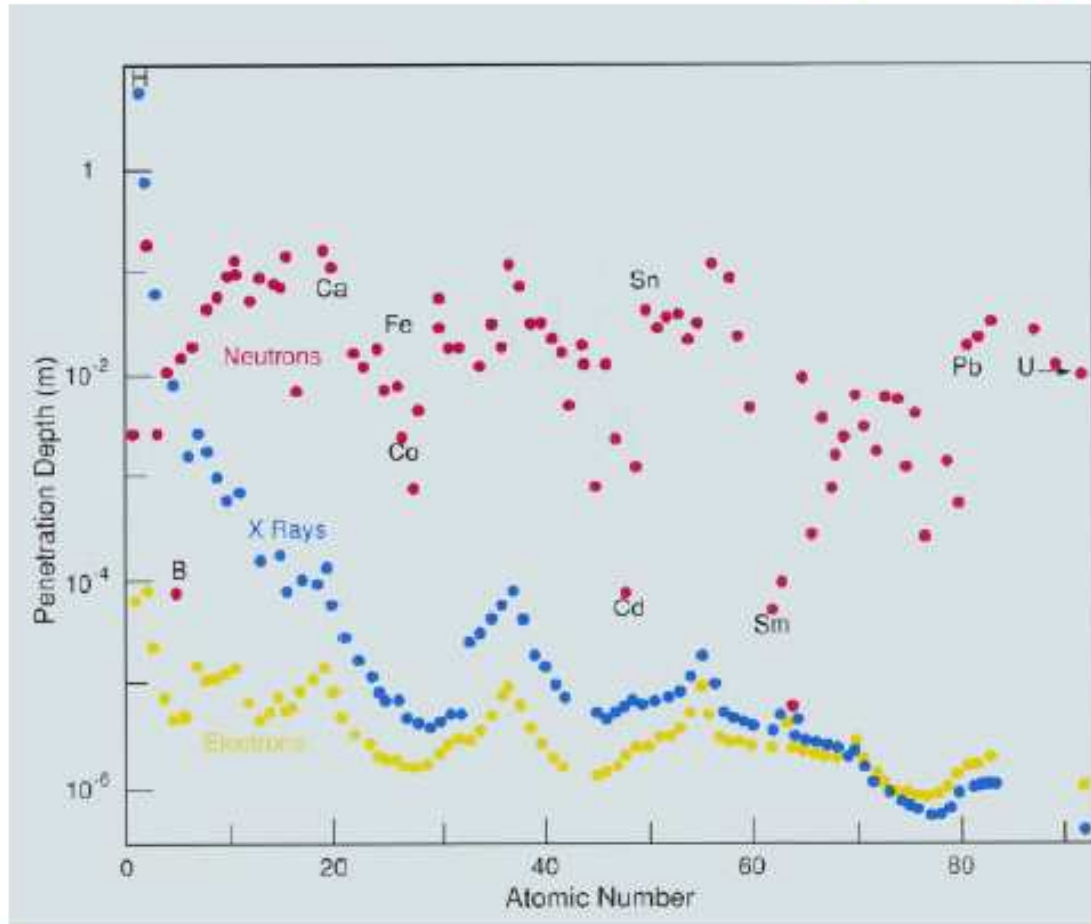
**Atomic Form Factor:**  $f^0(\vec{q}) = \int \rho(\vec{r}) e^{i\vec{q}\cdot\vec{r}} dV$



# Глубина проникновения



## Thermal Neutrons, 8 keV X-Rays & Low Energy Electrons:- Absorption by Matter



Note for neutrons:

- H/D difference
- Cd, B, Sm
- no systematic A dependence

# How a Synchrotron Works

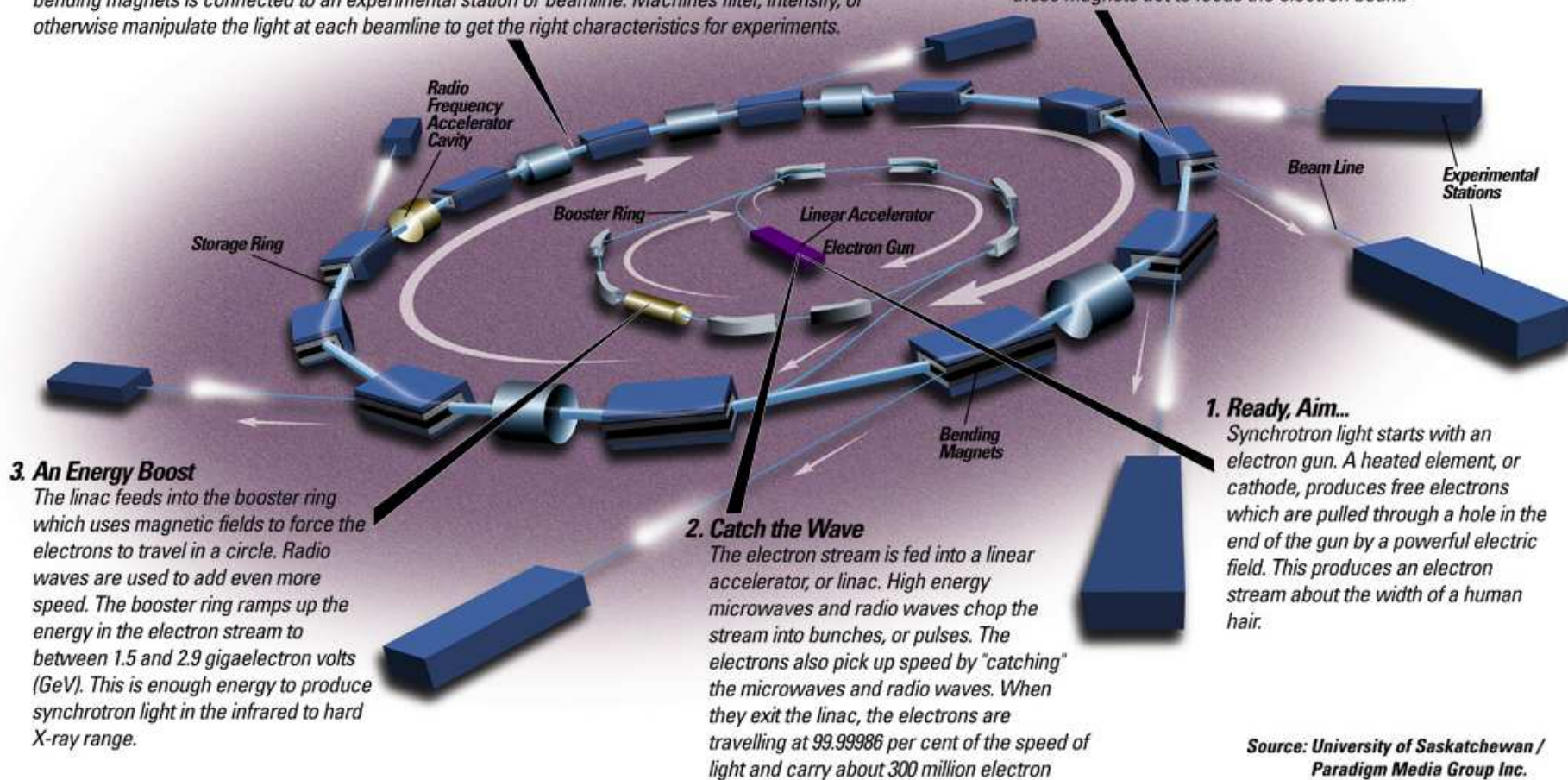
## 4. Storage Ring

The booster ring feeds electrons into the storage ring, a many-sided donut-shaped tube. The tube is maintained under vacuum, as free as possible of air or other stray atoms that could deflect the electron beam. Computer-controlled magnets keep the beam absolutely true.

Synchrotron light is produced when the bending magnets deflect the electron beam; each set of bending magnets is connected to an experimental station or beamline. Machines filter, intensify, or otherwise manipulate the light at each beamline to get the right characteristics for experiments.

## 5. Focusing the Beam

Keeping the electron beam absolutely true is vital when the material you're studying is measured in billionths of a metre. This precise control is accomplished with computer-controlled quadrupole (four pole) and sextupole (six pole) magnets. Small adjustments with these magnets act to focus the electron beam.

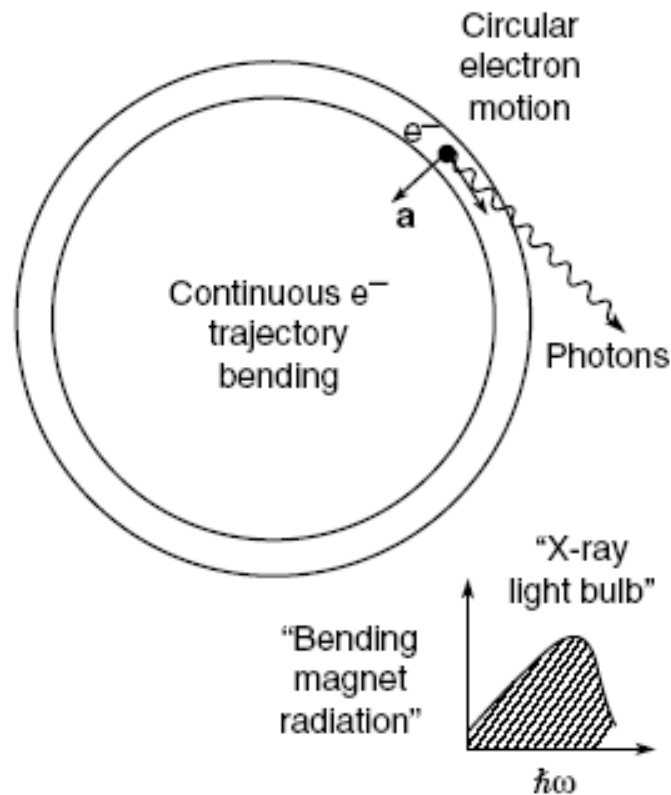


Source: University of Saskatchewan /  
Paradigm Media Group Inc.

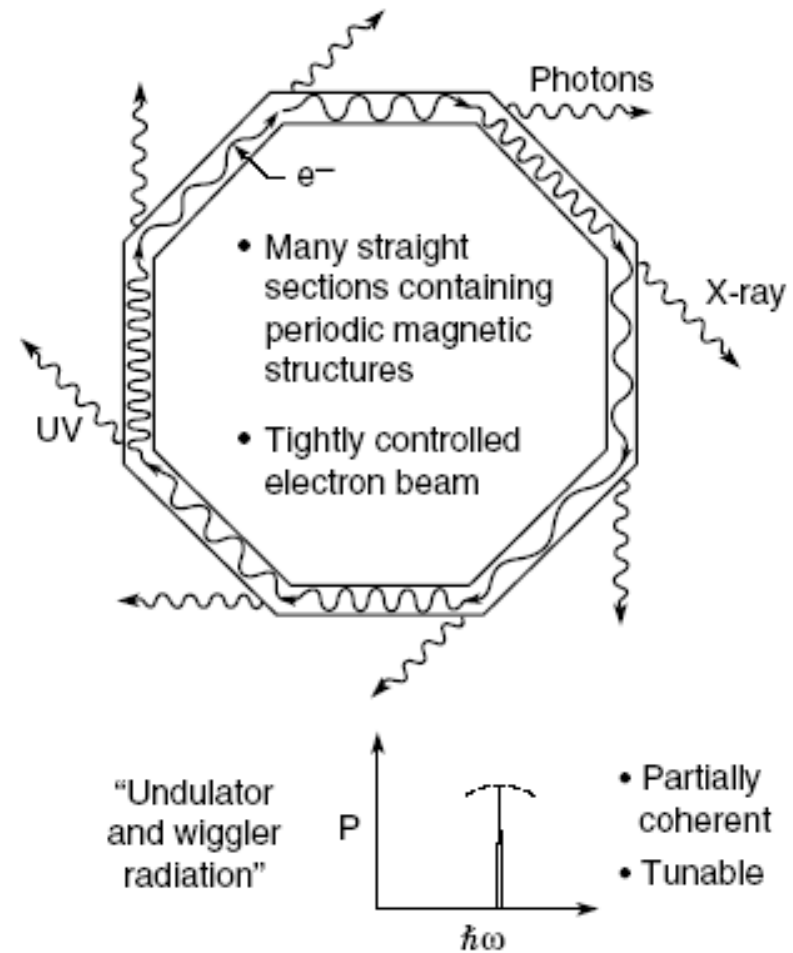


# Modern Synchrotron Radiation Facility

### Older Synchrotron Radiation Facility

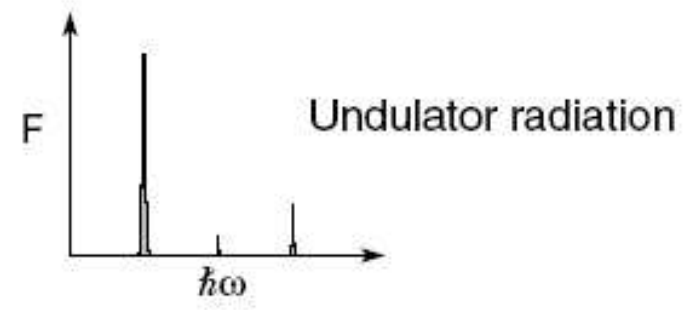
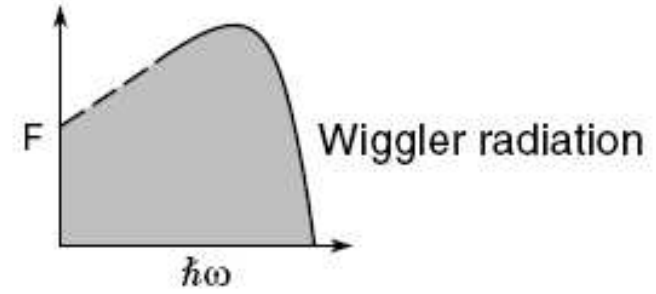
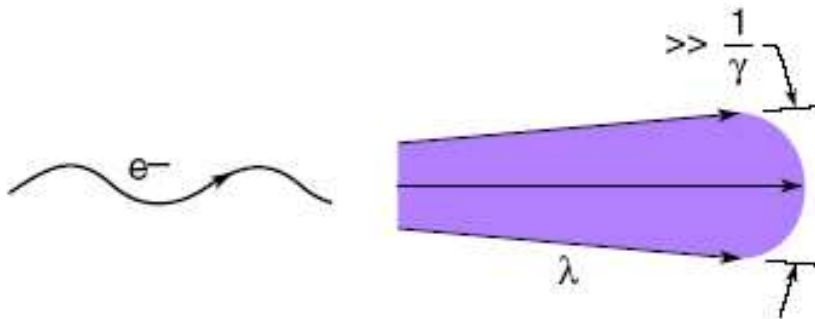
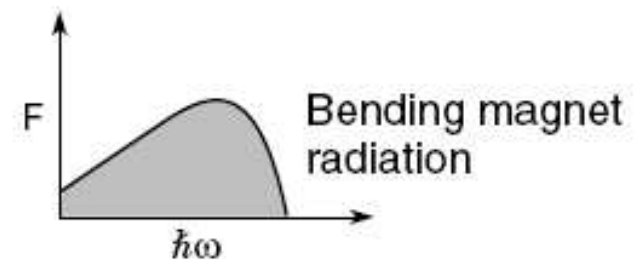
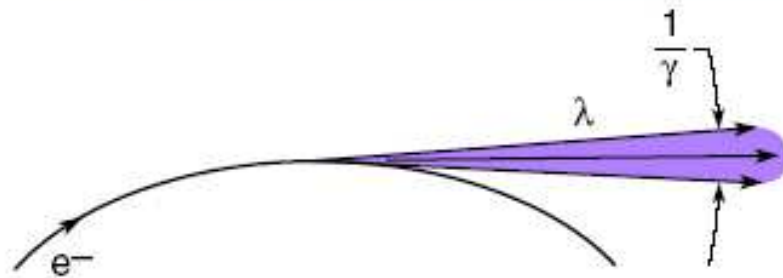


### Modern Synchrotron Radiation Facility

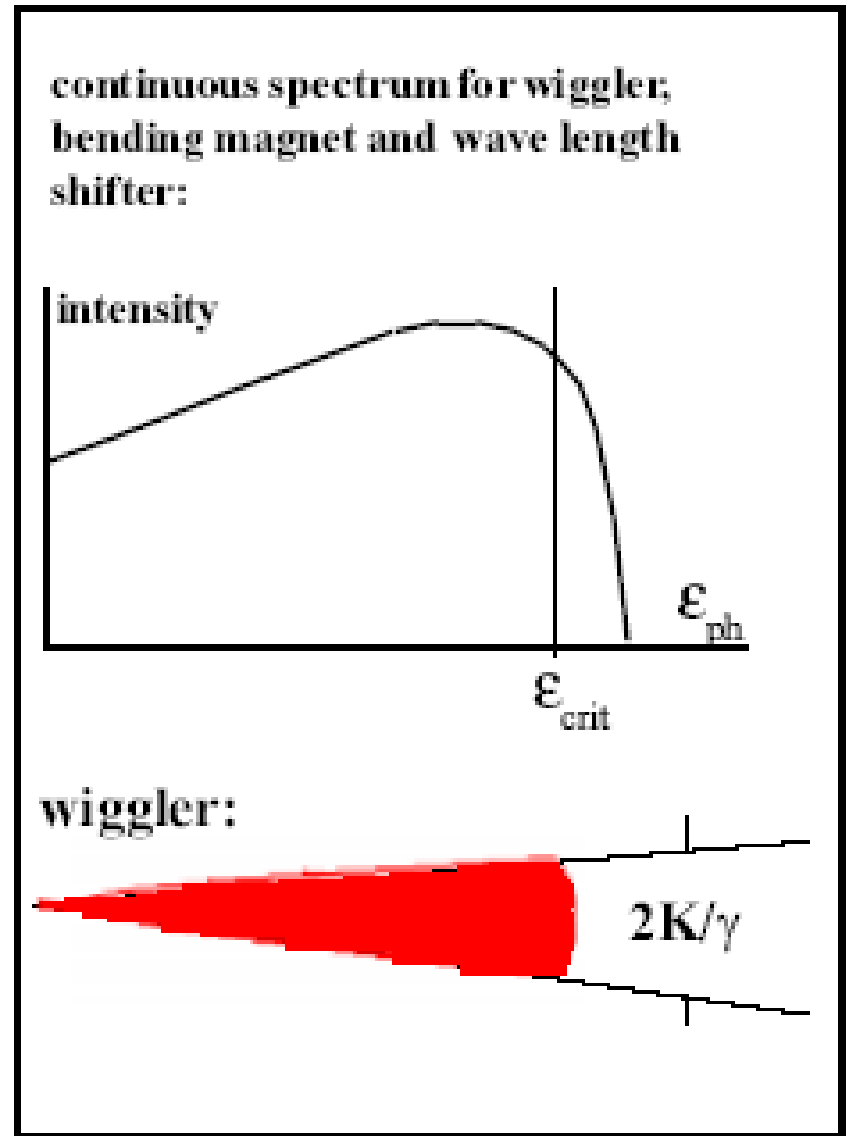
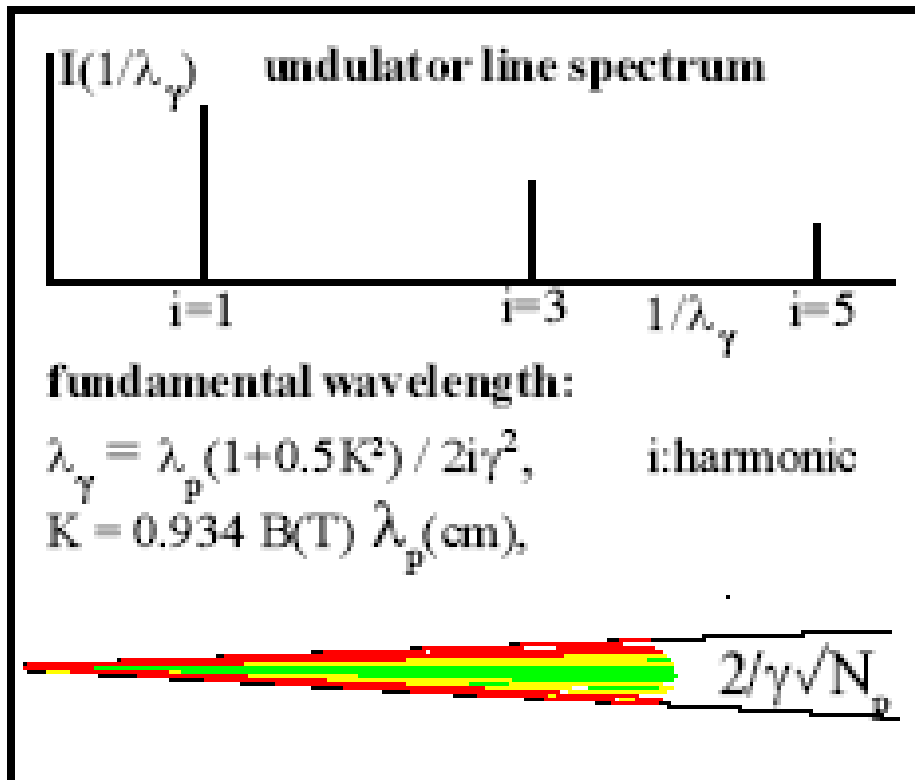




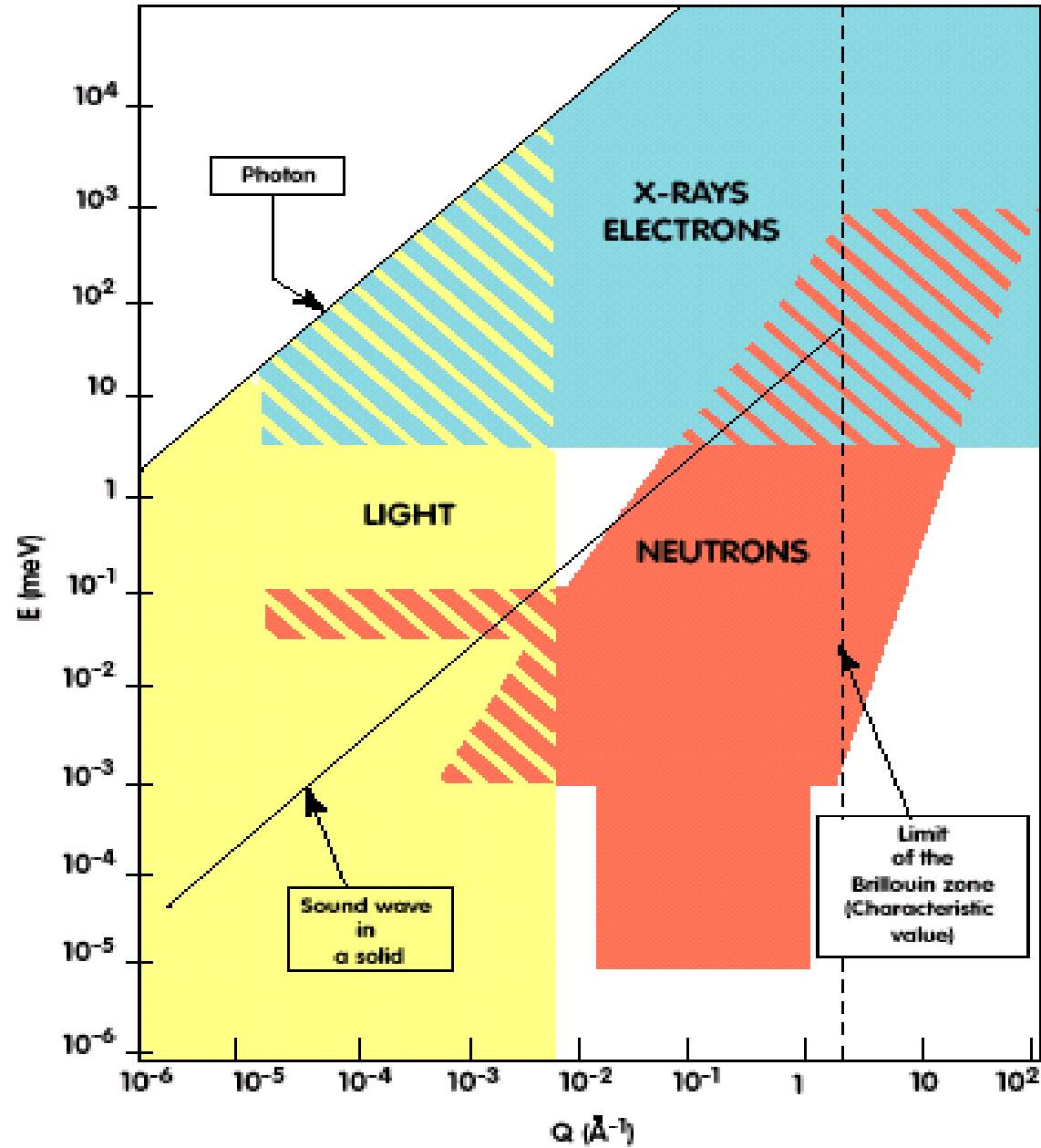
# Three Forms of Synchrotron Radiation



$$\gamma = \frac{1}{\sqrt{1 - \frac{v^2}{c^2}}}$$







# Кольцо синхротрона



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# Андулятор



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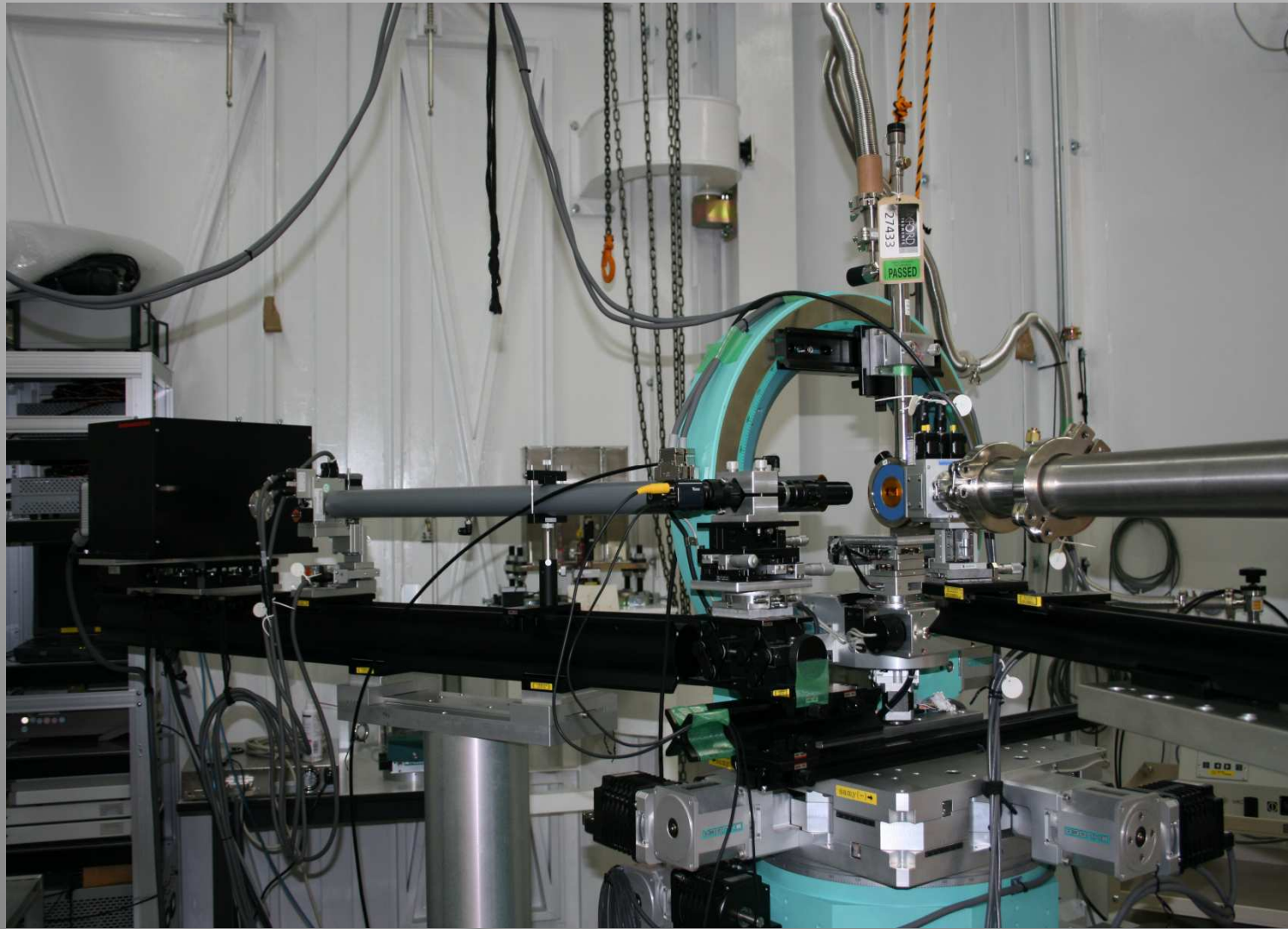
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# Вывод пучка



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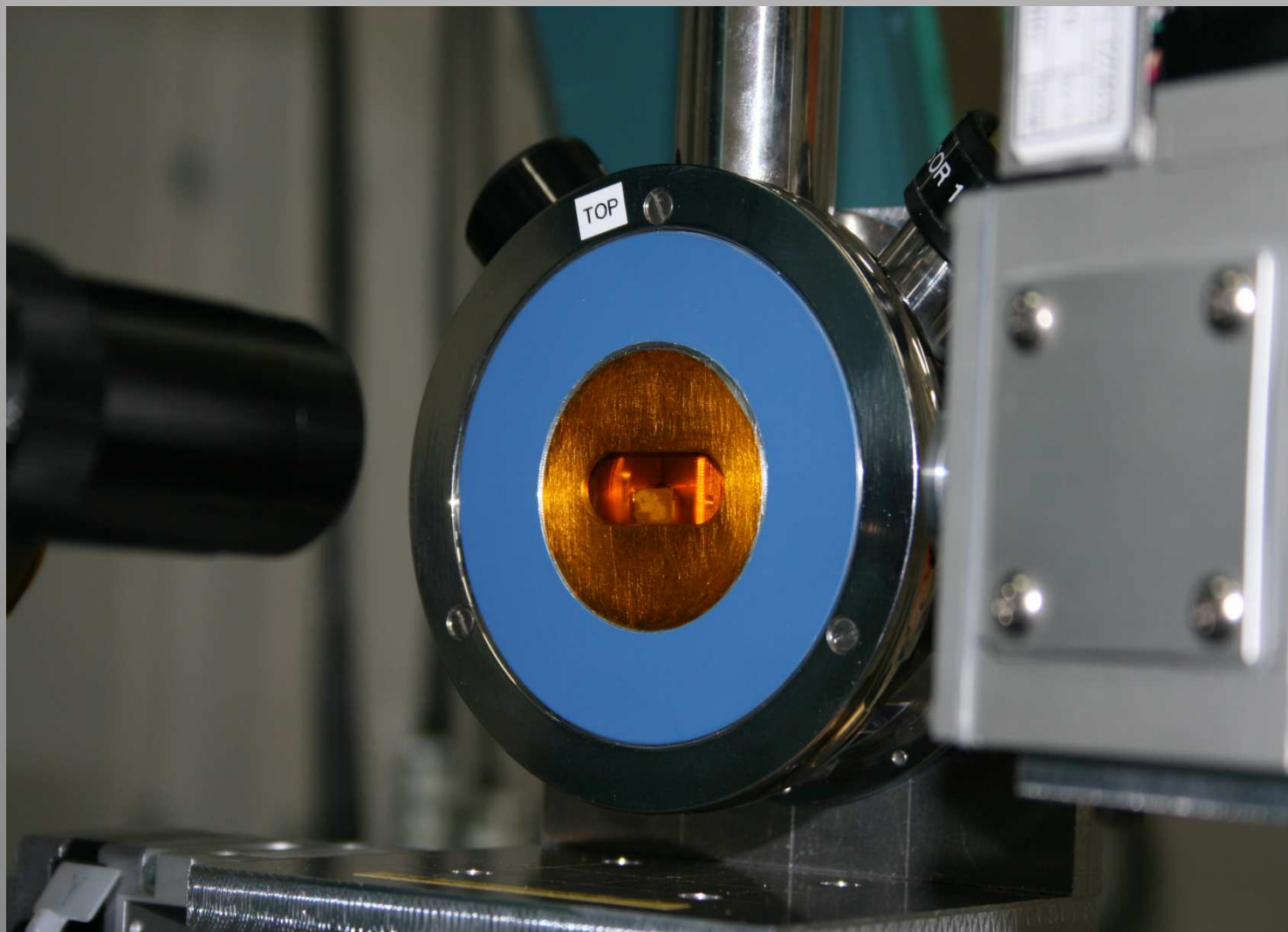
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# Криостат, вибрации $< 10\text{nm}$



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Ioffe  
Physico-  
Technical  
Institute

# Spallation Neutron Source

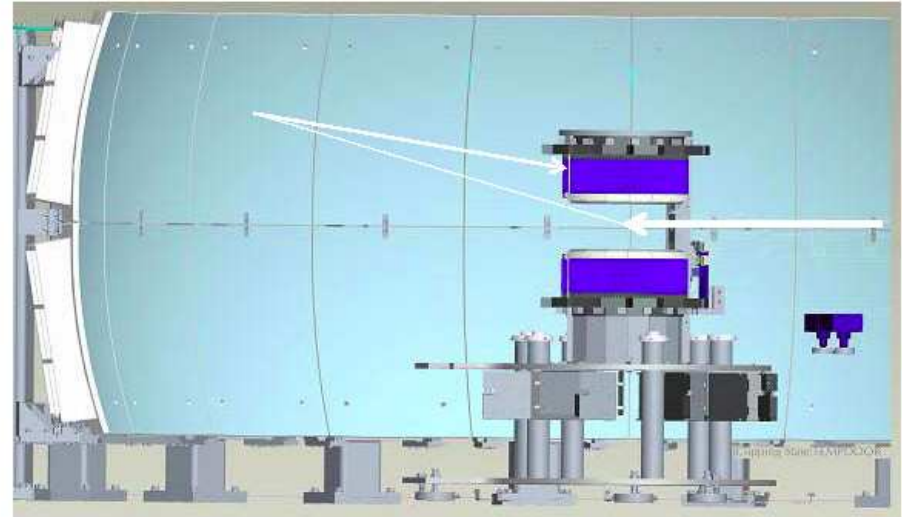


**JINS**

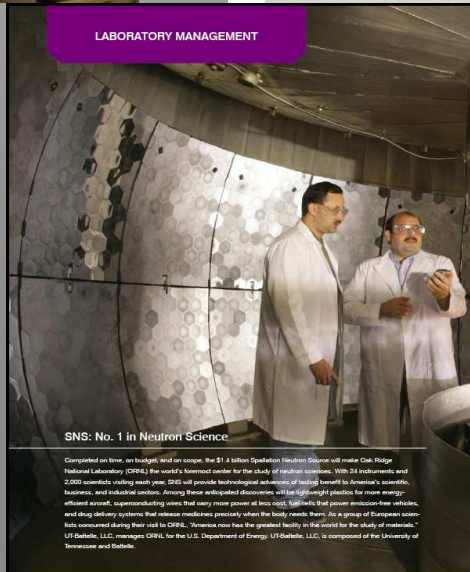
# Quasi-elastic Scattering



- BASIS-SNS



LABORATORY MANAGEMENT



SNS: No. 1 in Neutron Science

Completed on time, on budget, and on scope, the \$1.4 billion Spallation Neutron Source will make Oak Ridge National Laboratory (ORNL) the world's foremost center for the study of neutron science. With 24 instruments and 200 scientists visiting each year, SNS will provide technological advances of world renown in America's scientific, business, and industrial sectors. Among these anticipated discoveries will be lightweight plastics for more energy-efficient aircraft, superconducting wires that carry more power at less cost, magnets that power emission-free vehicles, and drug delivery systems that release medications precisely when they're needed. Says a group of European scientists concerned during their visit to ORNL, "America now has the greatest facility in the world for the study of materials." UT-Battelle, LLC, manages ORNL for the U.S. Department of Energy. UT-Battelle, LLC, is composed of the University of Tennessee and Battelle.

16.03.2009





# Почему на примере релаксоров

## Applications of Ferroelectric Single Crystals in Navy Sonar

Harold C. Robinson<sup>1</sup> and James M. Powers<sup>2</sup>

<sup>1</sup>Naval Undersea Warfare Center (NUWC) Division Newport, Newport, RI

<sup>2</sup>EDO Western Corporation, Salt Lake City, UT



		Mode	Coupling Factor	Dielectric Loss	Projector FOM	Sensor FOMs	
					Strain Energy Density (dB re PZT-8)	$g^*d$ (dB re PZT-5H)	$g^*d/\tan \delta$ (dB re PZT-5H)
PZT-8	ceramic	33	0.62	0.003	0.0	-3.3	4.9
PZT5H	ceramic	33	0.75	0.020	6.8	0.0	0.0
PZT5H	ceramic	15	0.68	0.020	6.0	2.8	2.8
PZT-4	ceramic	33	0.71	0.004	2.1	-1.8	5.2
PZT-4	ceramic	15	0.72	0.004	2.2	2.6	9.6
PMN-PT	crystal	33	0.92	0.003	11.1	6.5	14.7
PZN-8%PT	crystal	15	0.94	0.005	12.1	12.4	18.4
PZN-4.5%PT	crystal	15	0.97	0.005	16.1	16.0	22.0

Table 1. Comparison of sensor and projector material properties.

# Диэлектрическая проницаемость (I)

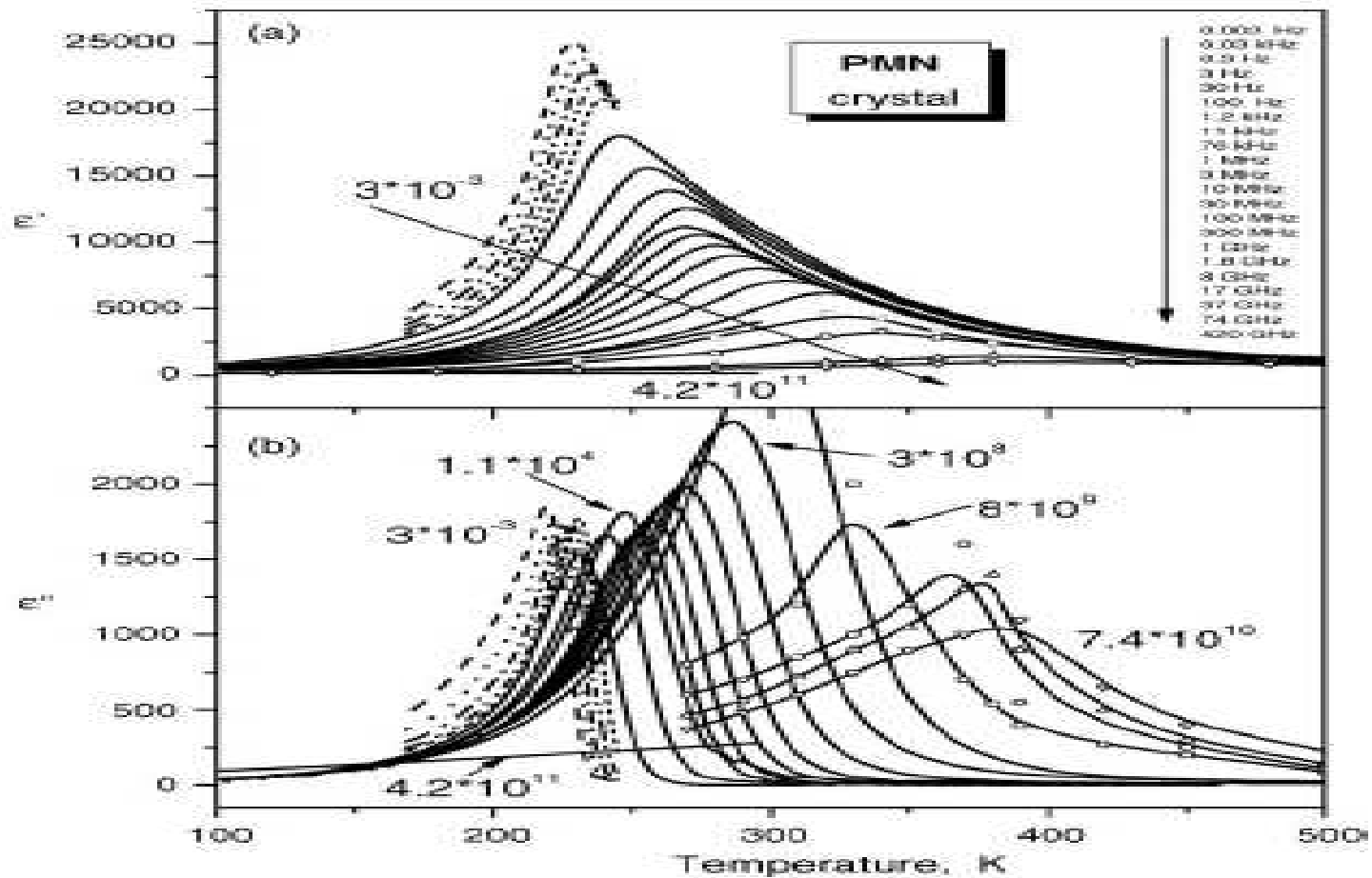
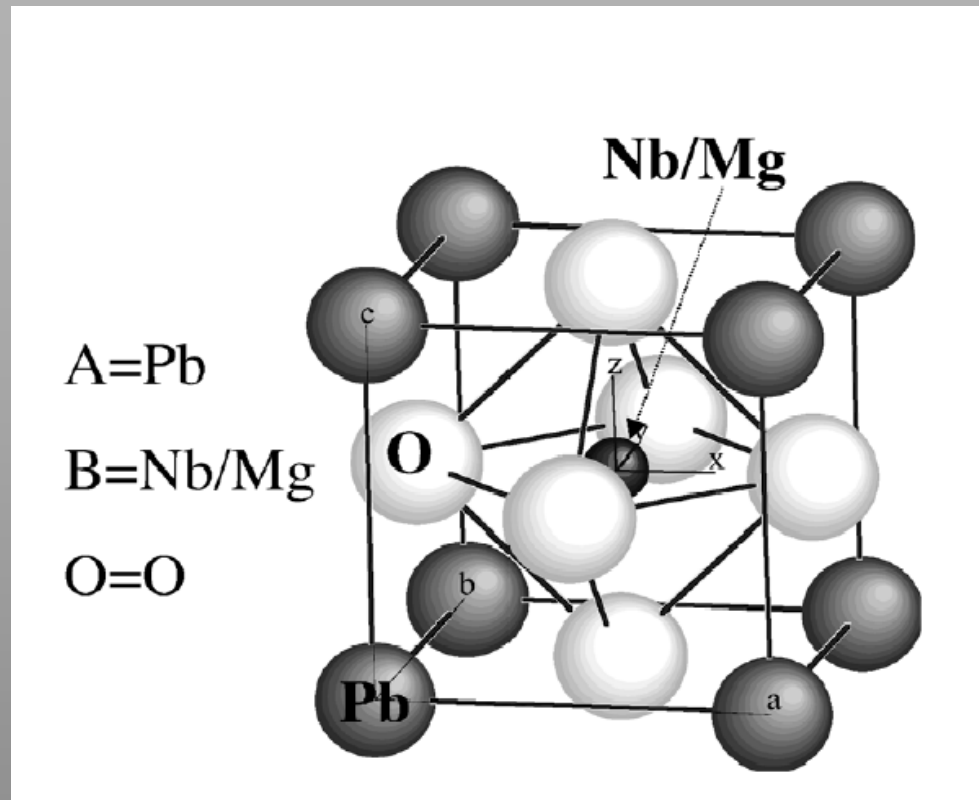


Fig. 1. Temperature dependences of dielectric permittivity  $\epsilon'$  and loss  $\epsilon''$  of PMN single crystal at various frequencies. The numbers near curves denote the frequency in Hz.

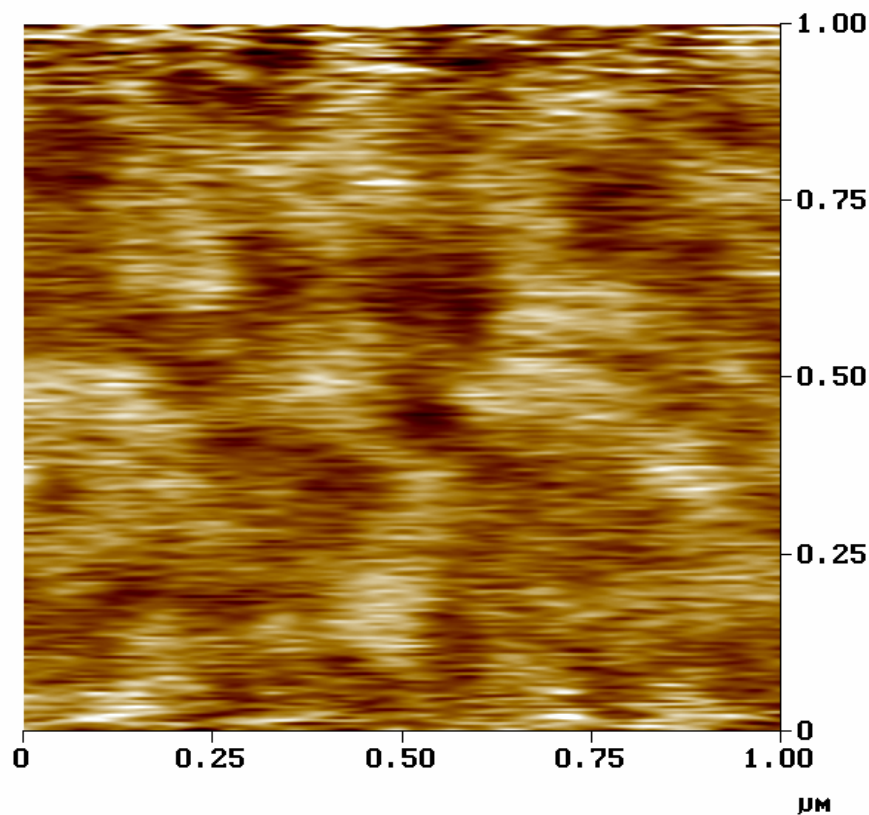
# PMN ideal structure



$\text{Nb}^{5+}$   $\text{Mg}^{2+}$  different charges, different ionic radii – **should order**  
In the compounds without lead – tripling of the cell

In the  $\text{PbB}'_{1/3}\text{B}''_{2/3}$  – **cell doubling**

# Должно быть НАНО! (нанодомены)



Digital Instruments NanoScope  
Scan size 1.000 μm  
Scan rate 0.6013 Hz  
Number of samples 256  
Image Data Aux C  
Data scale 2.000 V

рмп100\_1.084

# Структура



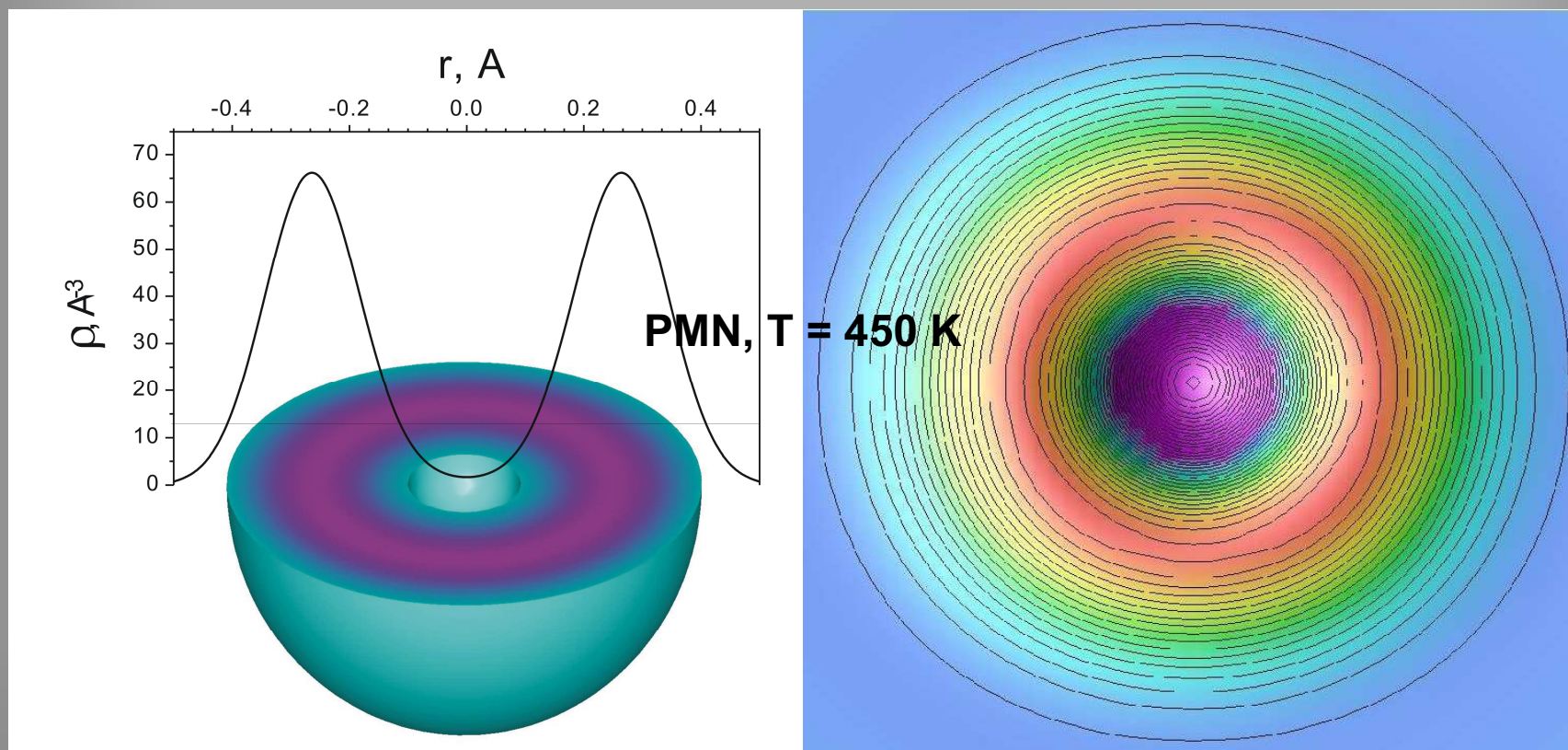
- Уточнение структуры по БРЭГГОВСКИМ ПИКАМ – неявно считаем, что упругое рассеяние доминирует, а если  $\rho(r)$ , т.е. Фурье образ  $S(Q)$ ?

# Probability density function for $\text{Pb}^{2+}$ in PMN 300K X-rays



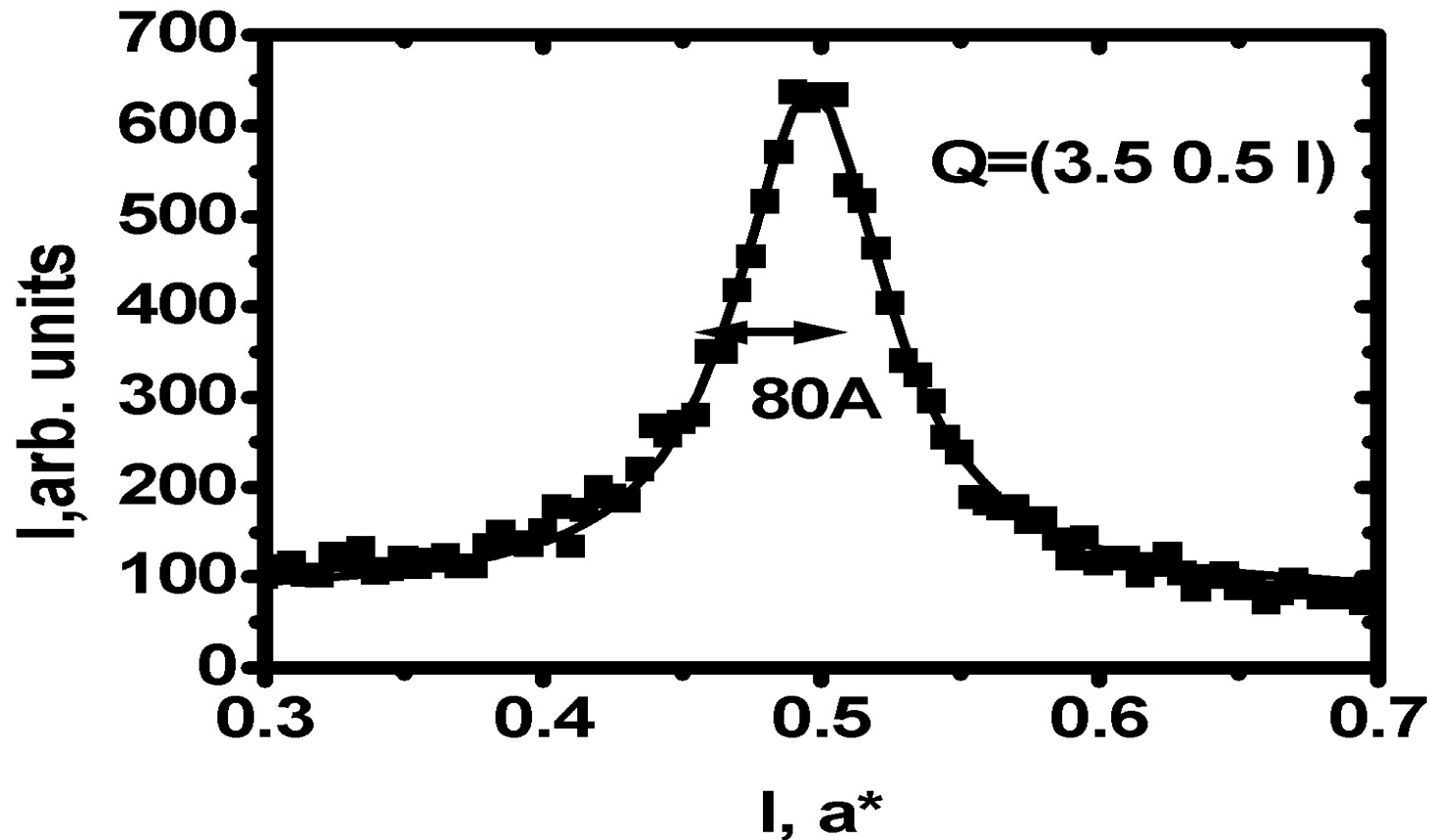
“Rotator model”

Gram-Charli expansion”



**А что с кислородом? В рентгеновском эксперименте ответа не получили**

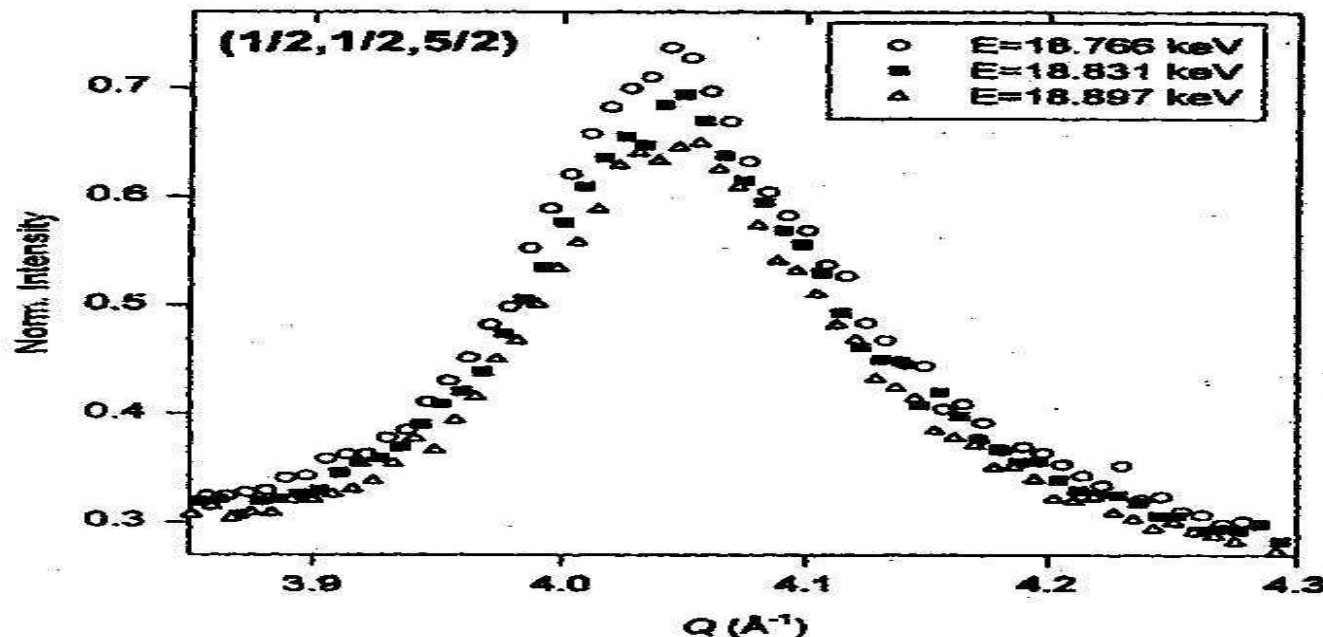
# Superstructural peak in PMN



- Superstructure in PMN measured with synchrotron radiation scattering; correlation length of compositional ordering is about 80 Å



# Anomalous X-ray scattering in PMN



$$\frac{I(Q)}{\partial I(Q) / \partial f_{Pb}} = \frac{1}{2} (f_{Nb} - f_{Pb}) + 3 \frac{Q u_O}{\alpha} f_O + \frac{Q u_{Pb}}{\alpha} f_{Pb}$$

$\alpha$  – degree of order,  $u_O$ ,  $u_{Pb}$  – displacements

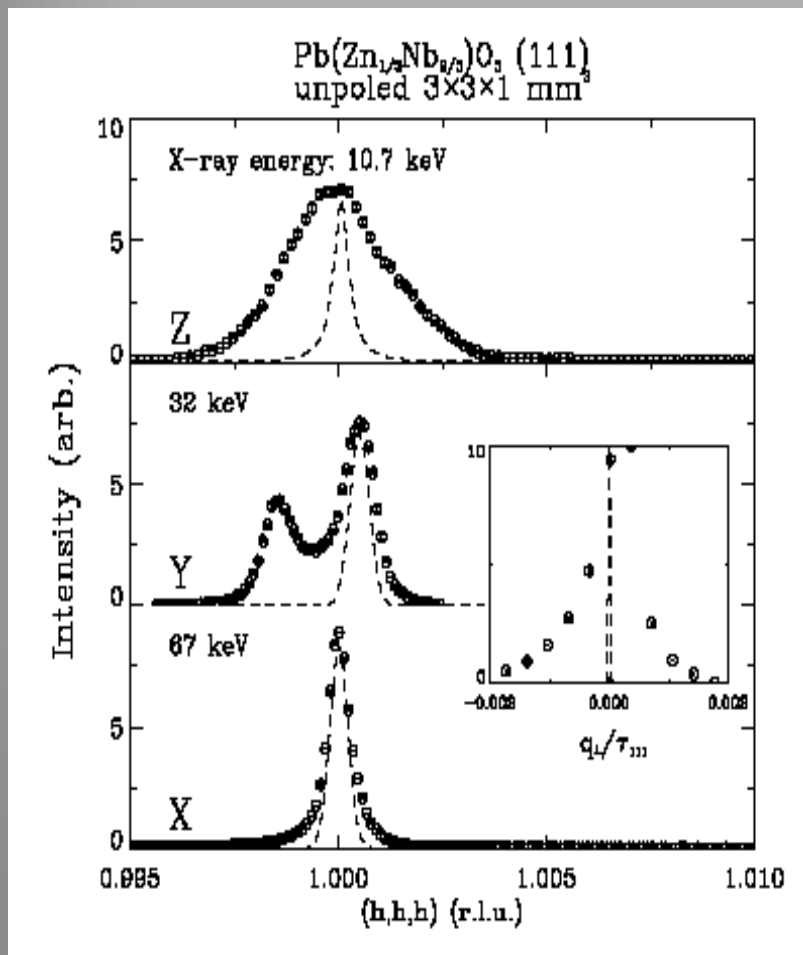
$u_{Pb}/\alpha \sim -0,07 \text{ \AA}$ ;  $u_O/\alpha \sim 0,4 \text{ \AA}$ . Positive sign – toward Nb, negative – away from Nb.



# Объём и поверхность

По материалам работ группы  
G.Shirane

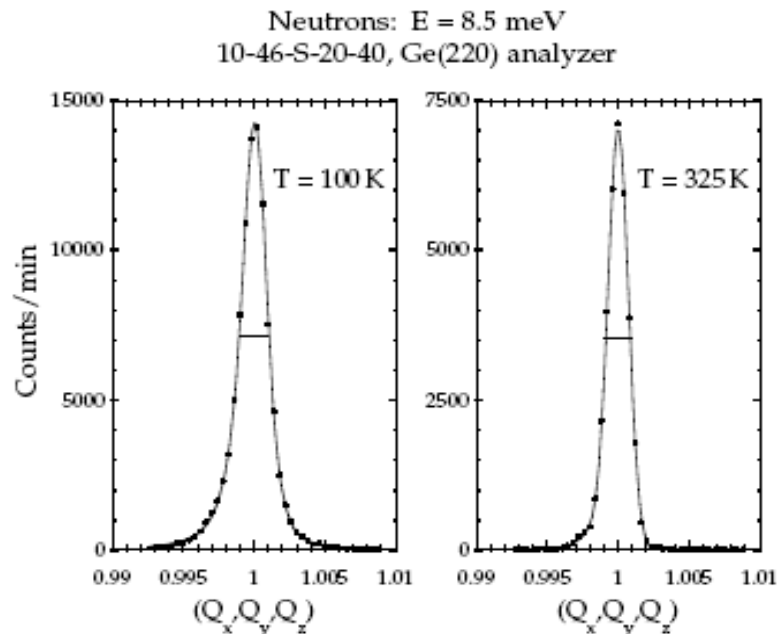
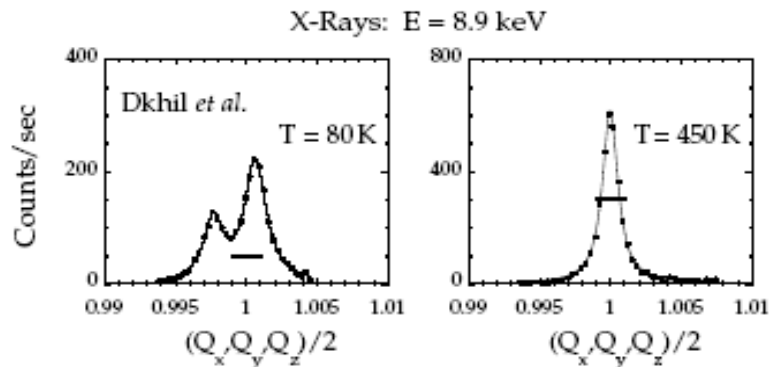
# PZN, Дифракция СИ



- Ромбоэдрические искажения наблюдаются только в поверхностном слое толщиной порядка 50 микрон

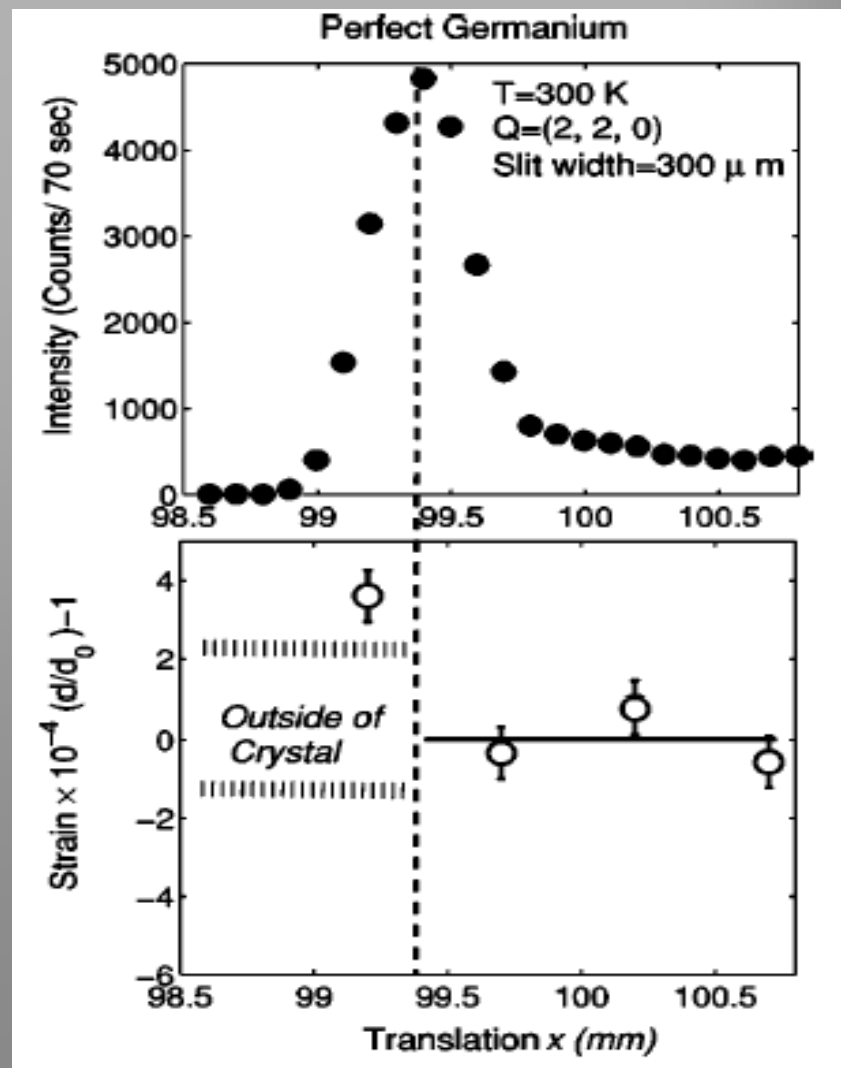
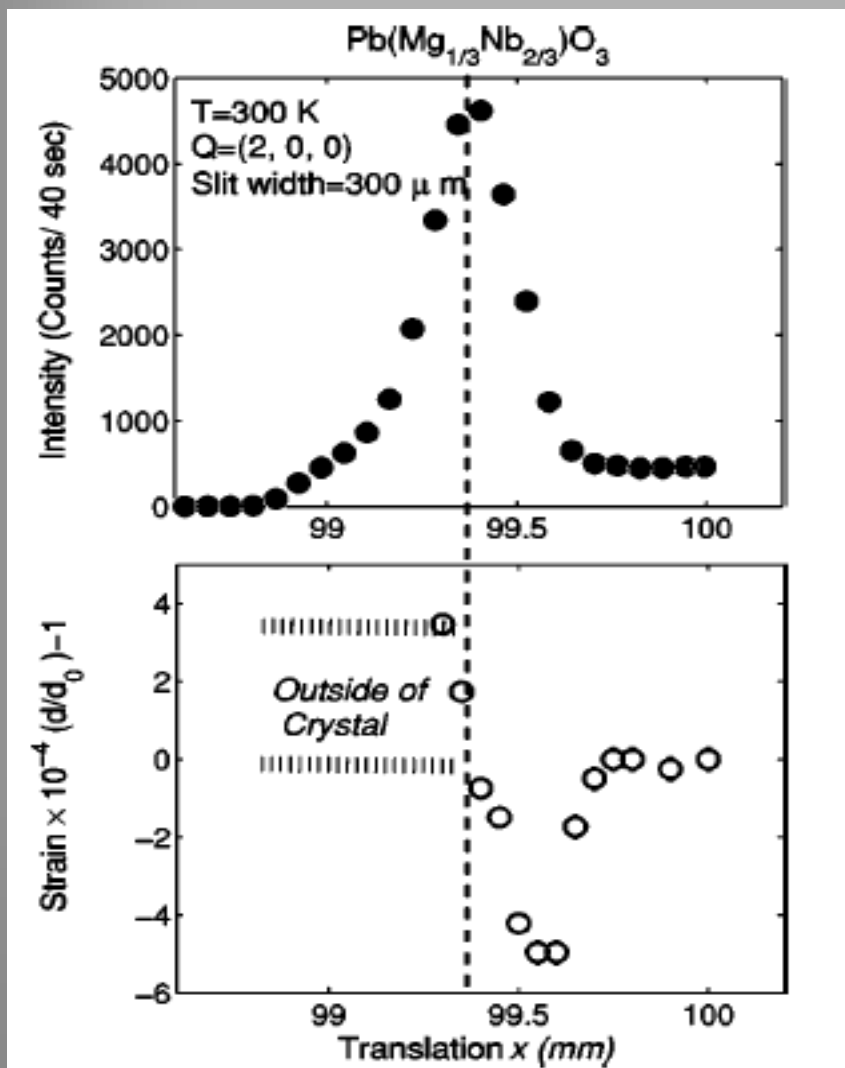
# PMNPT10

## X-rays+neutrons



- В рентгеновских экспериментах на керамике четко наблюдается ромбоэдрическая фаза (глубина проникновения  $\sim 20$  микрон).
- В нейтронном эксперименте на монокристалле кубическая фаза до 100К

# Упругие напряжения в поверхностном слое РМН

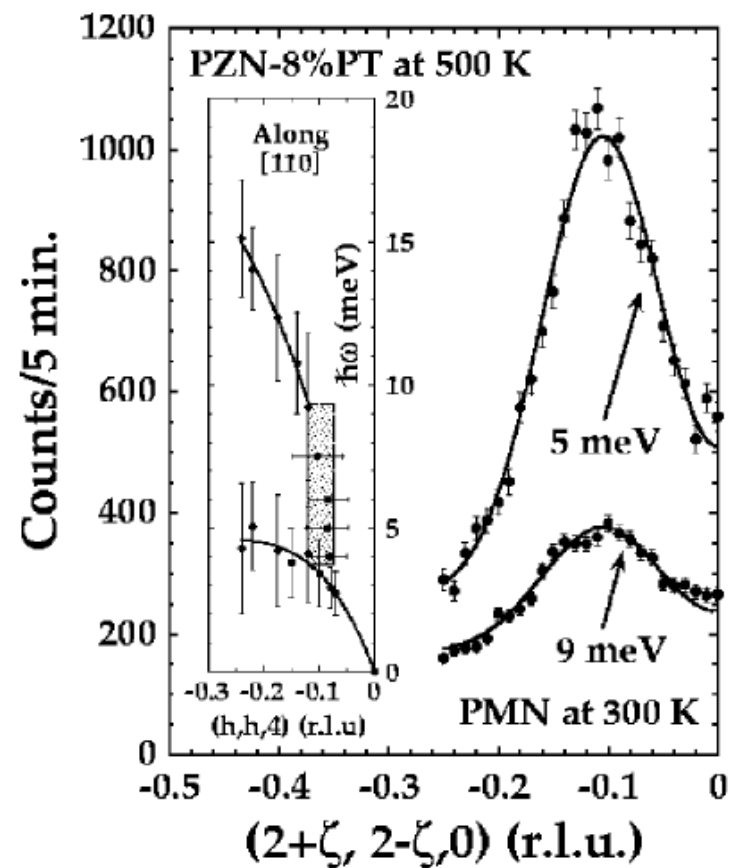
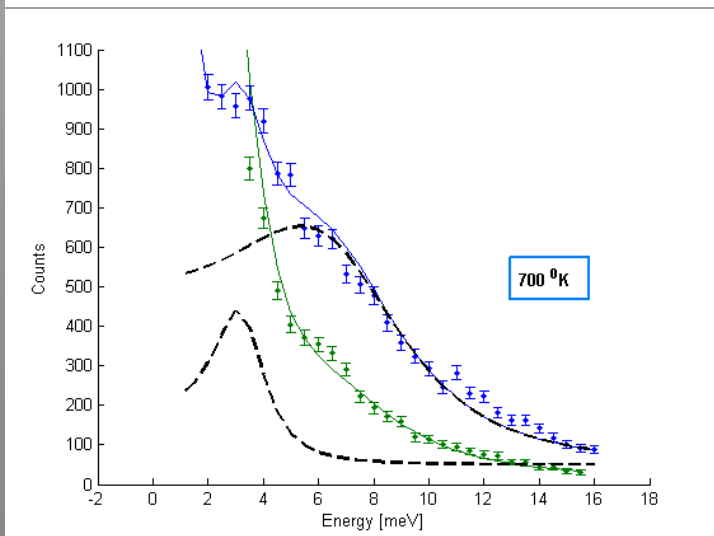
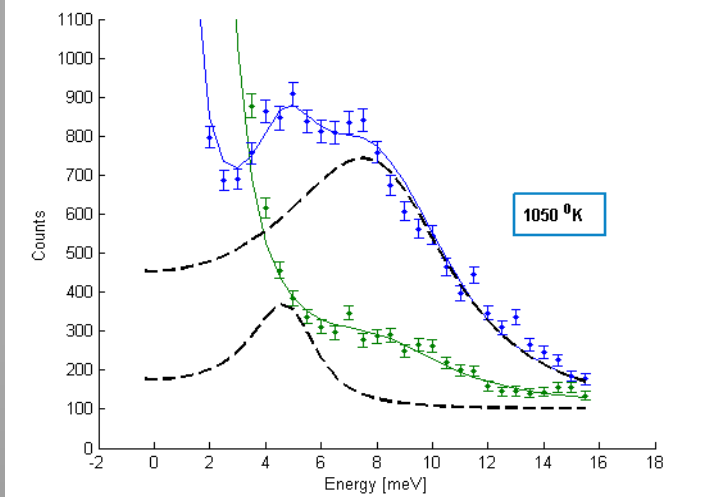




# Динамика решетки

Нейтроны

# Фононы в релаксорах



Водопад

# Central Peak

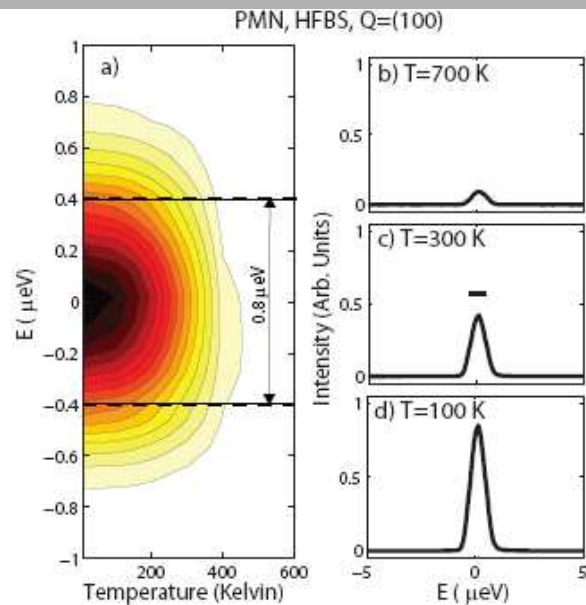


FIG. 7: (a) Contour plot of the scattering intensity as a function of energy transfer and temperature. Contours are shown on a linear intensity scale; dashed lines indicate the full-width at half-maximum (FWHM) of the peak linewidth at each temperature. The data were obtained from an integration over detectors 10-16 as illustrated in Fig. 6. Panels (b), (c), and (d) show inelastic scans at 700 K, 300 K, and 100 K. The horizontal bar in panel (c) represents the FWHM elastic energy resolution ( $2\delta E$ ) of the spectrometer.

The energy dependence of the diffuse scattering as a function of temperature is illustrated in Fig. 7. Panel (a) shows a color contour plot of the peak linewidth in energy as a function of temperature. For subtraction of a high

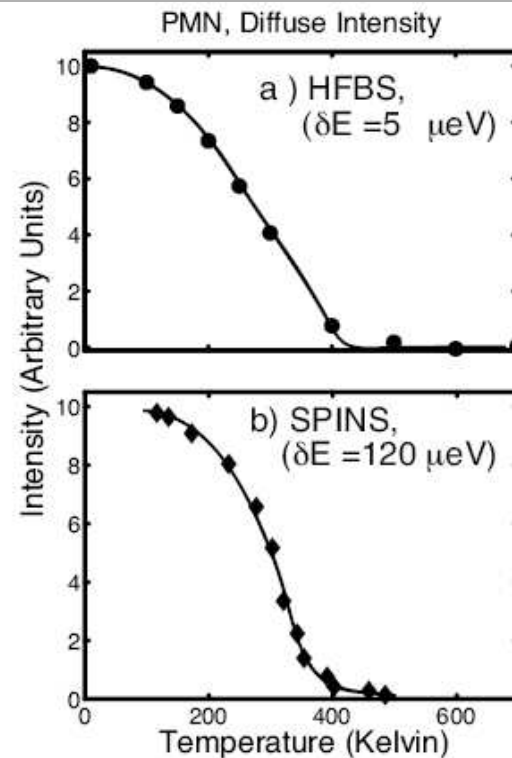


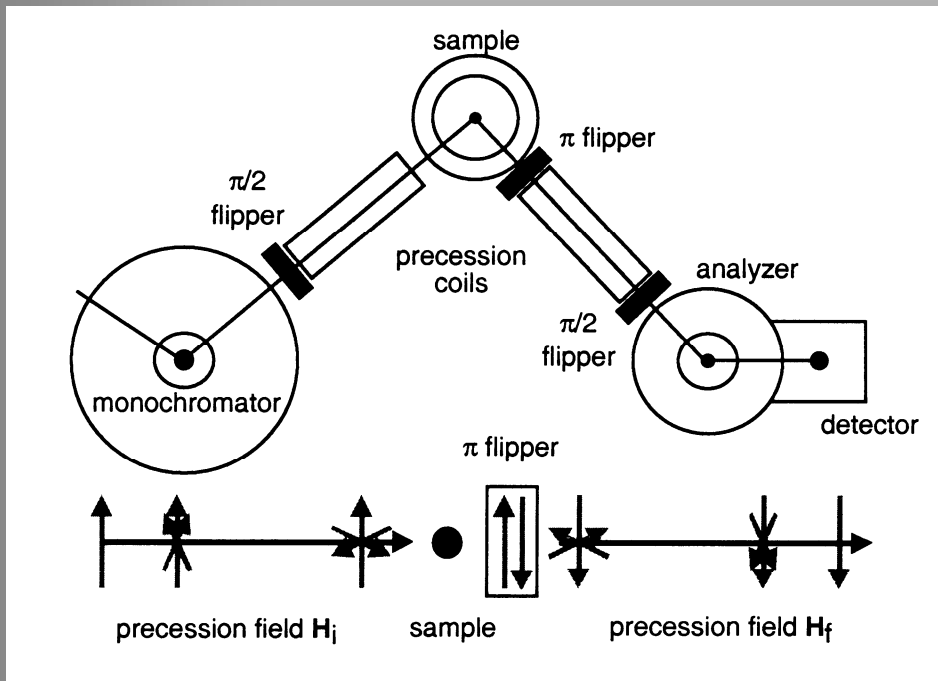
FIG. 8: (a) Temperature dependence of the diffuse scattering in PMN measured on the HFBS; data are integrated in energy from  $\pm 5 \mu eV$  and in  $Q$  over detectors 10-16 as illustrated in Fig. 6. (b) Temperature dependence of the diffuse scattering intensity in PMN measured on SPINS at  $Q = (1.05, 0.95, 0)$  by Hiraka *et al.*<sup>31</sup> The SPINS energy resolution of  $\delta E = 120 \mu eV$  HWHM provided the energy integration.



# TAS+SpinEcho

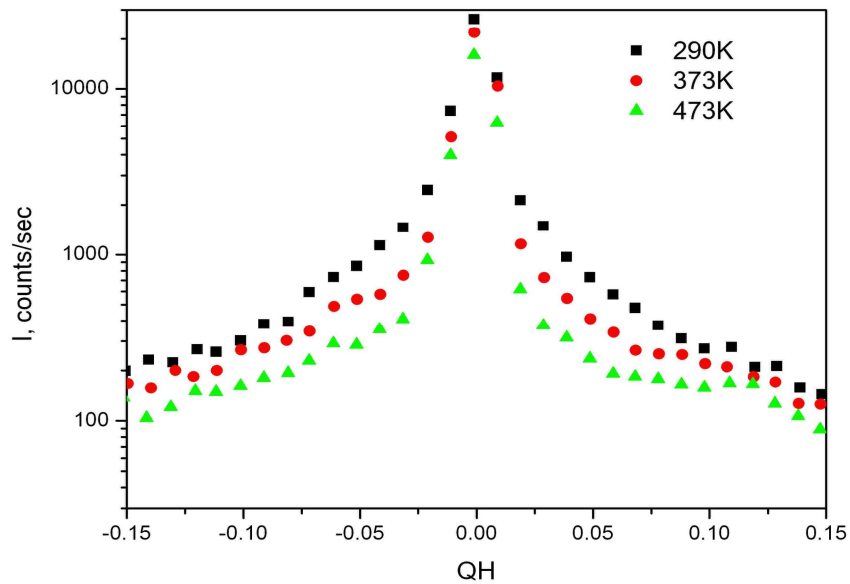


The monochromator and analyzer crystals select from the impinging beams certain energy band with defined direction of neutron polarization. If before the analyzer the neutron polarization is inclined, the intensity in the detector will be reduced.

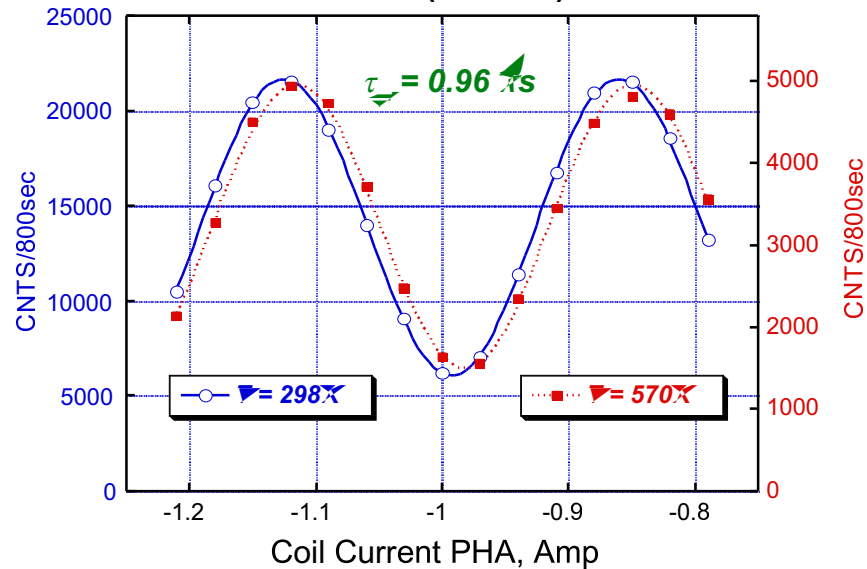


A typical experimental set-up for the precession field technique.

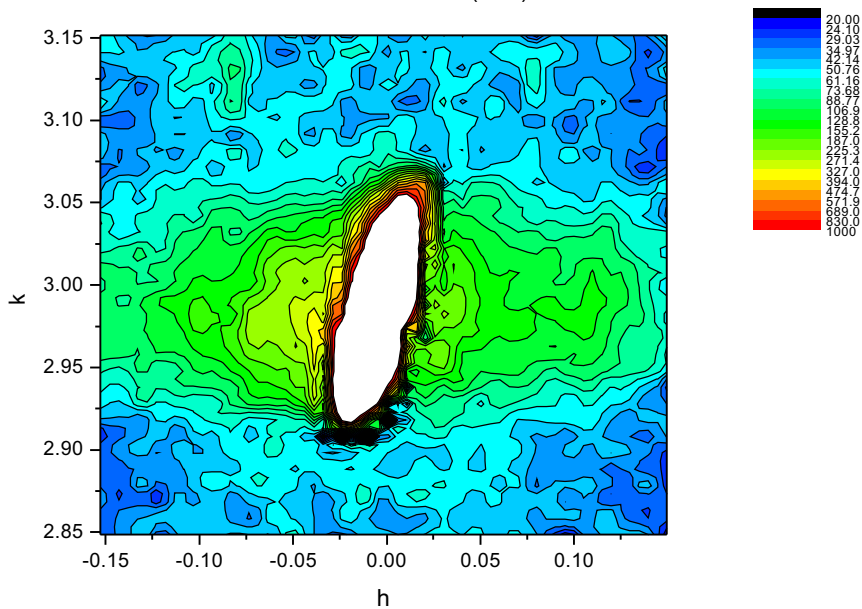
PMN IN20TASSE  $K_T=K_T=4.1A^{-1}$   $Q=(QH\ 3\ 0)$



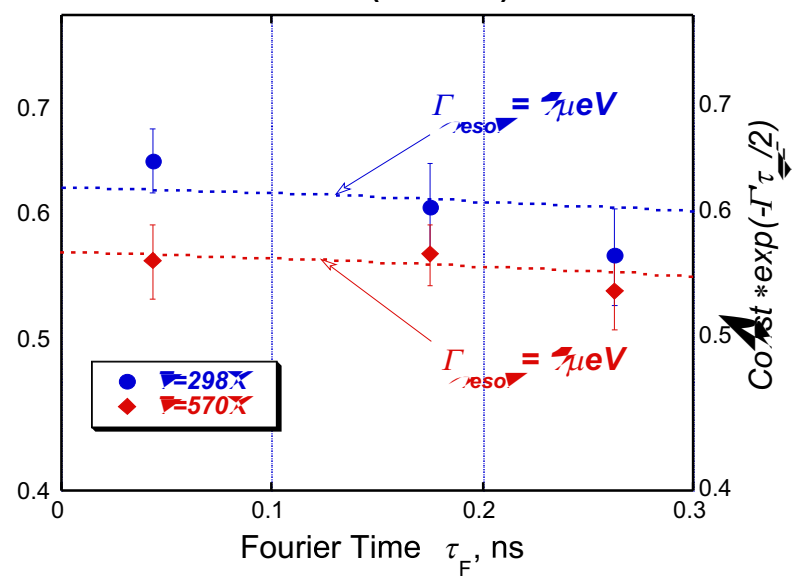
IN20 TASSE PMN  $k=4.1A^{-1}$   
diffuse  $Q=(0.05\ 3\ 0)$



PMN TASSEIN20 473K (030)mesh



IN20 TASSE PMN  $k=4.1A^{-1}$   
diffuse  $Q=(0.05\ 3\ 0)$





# Неупругое рассеяние СИ

# Адиабатическое приближение

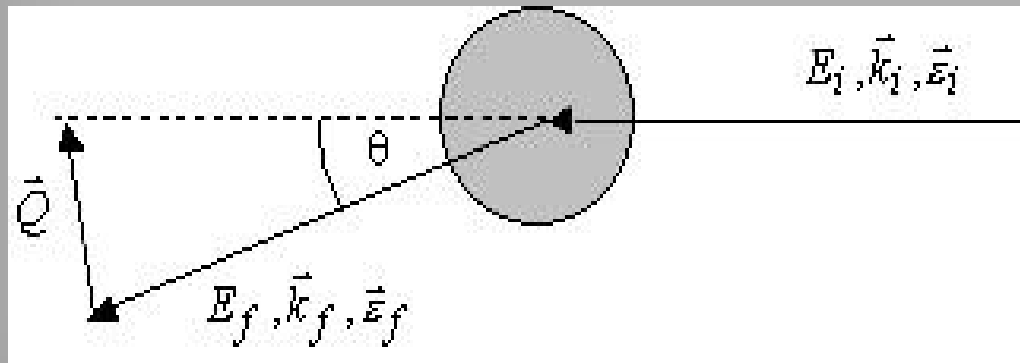


При смещении ядра атома все электроны движутся вместе с ним составляя одно целое

$$\rho(q) = \sum_i e^{-iq \cdot r_i} = \sum_\ell e^{-iq \cdot R_\ell} \left[ \sum_{i(\ell)} e^{-iq(r_i - R_\ell)} \right]$$

$$\rho(q, t) = Zf(q) \sum_\ell e^{-iq \cdot R_\ell(t)} = Zf(q) \sum_\ell e^{-iq(\ell + u_\ell(t))}$$

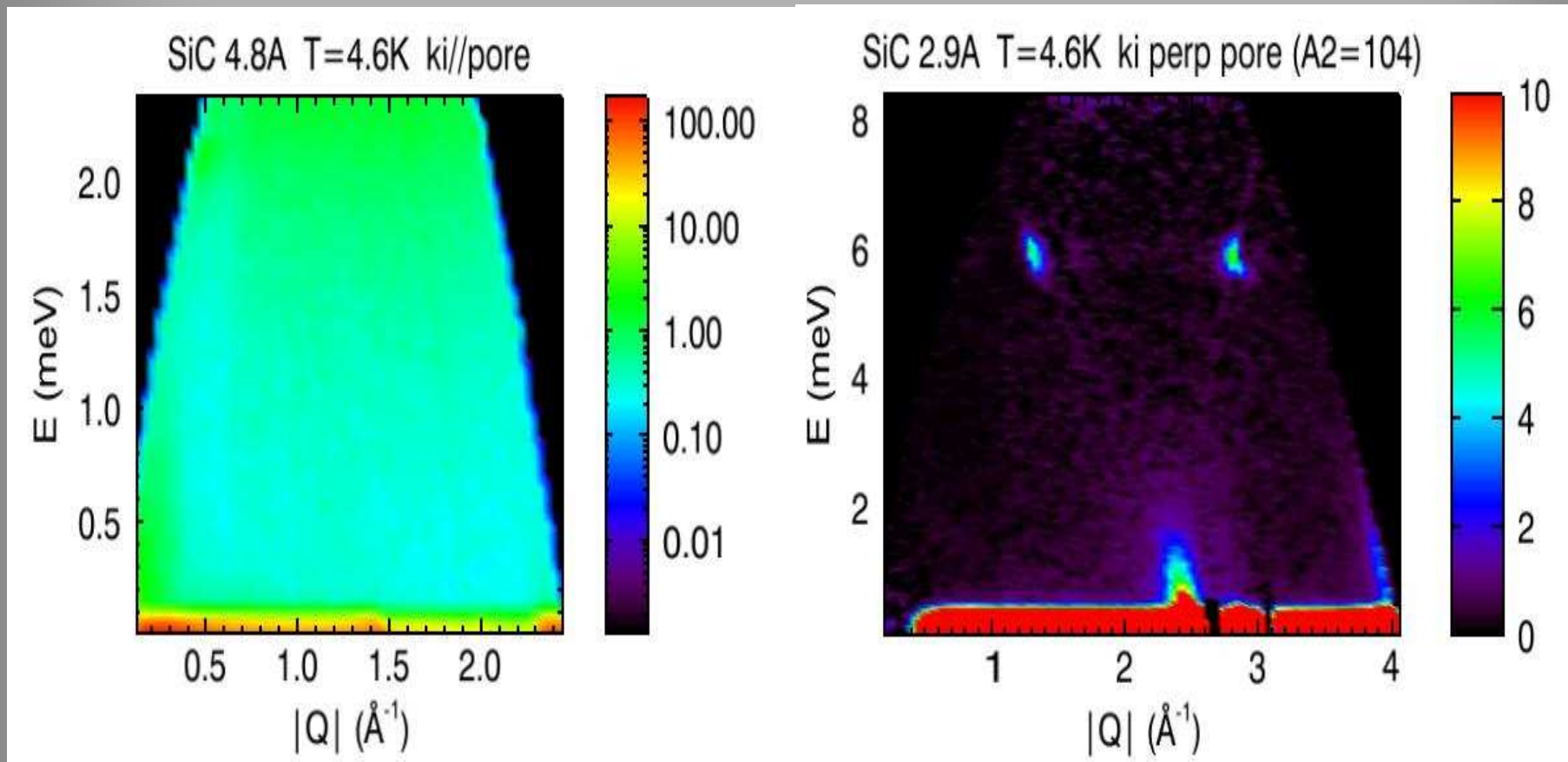
# Кинематика рассеяния



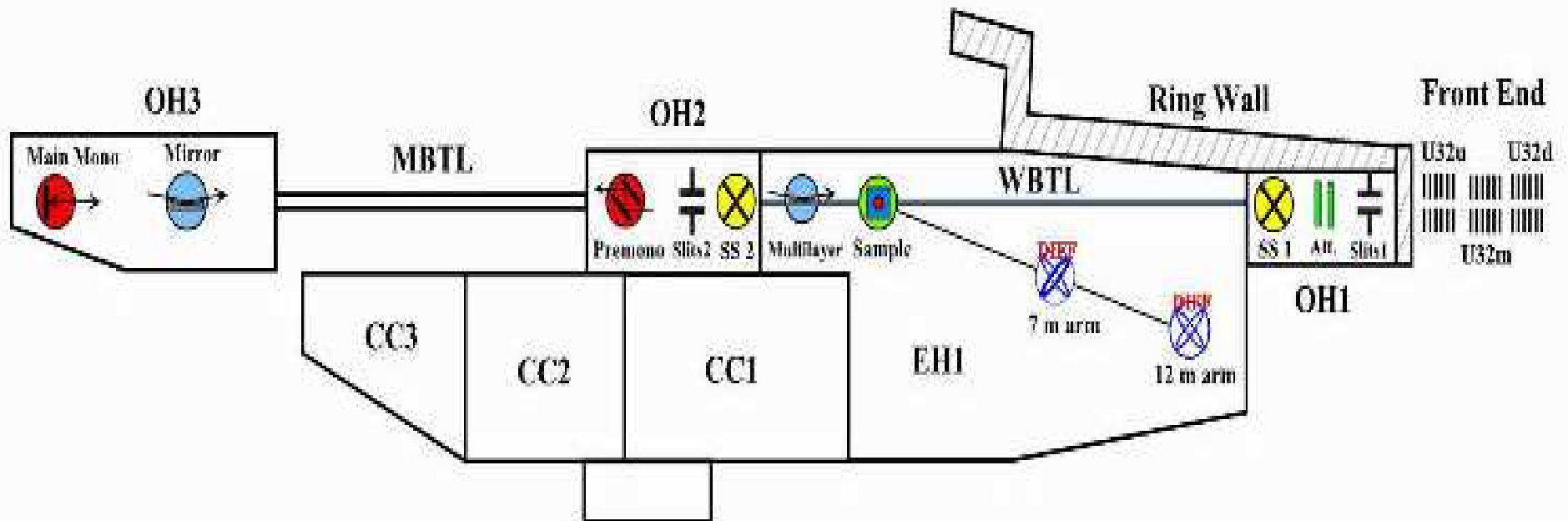
$$K_i \approx K_f; \quad (Q/K_i) = 2\sin(\theta/2)$$

**Нет ограничений на передачу энергии**

# $S(Q, \omega)$ $\lambda_i = 4.8 \text{ \AA}$ SiC NIST



# ID28 Spectrometer (ESRF)

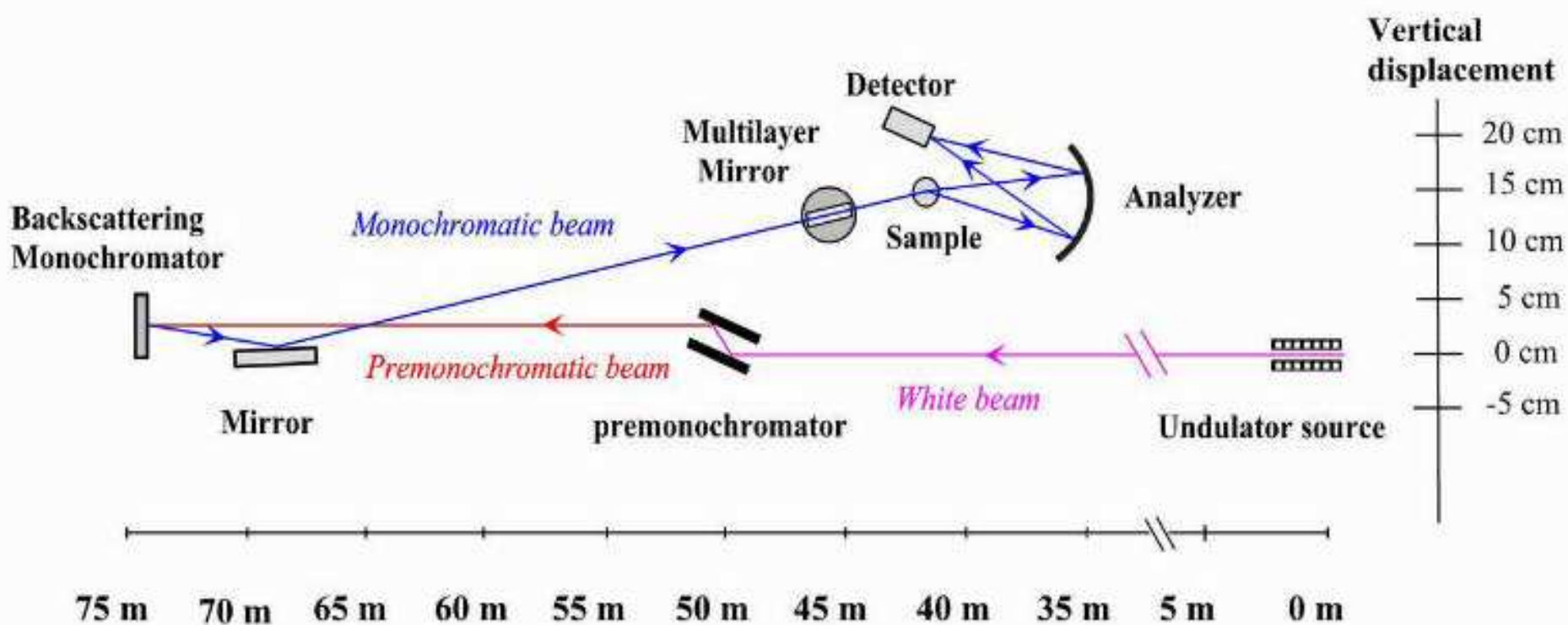


Высокое разрешение достигается за счет геометрии обратного рассеяния

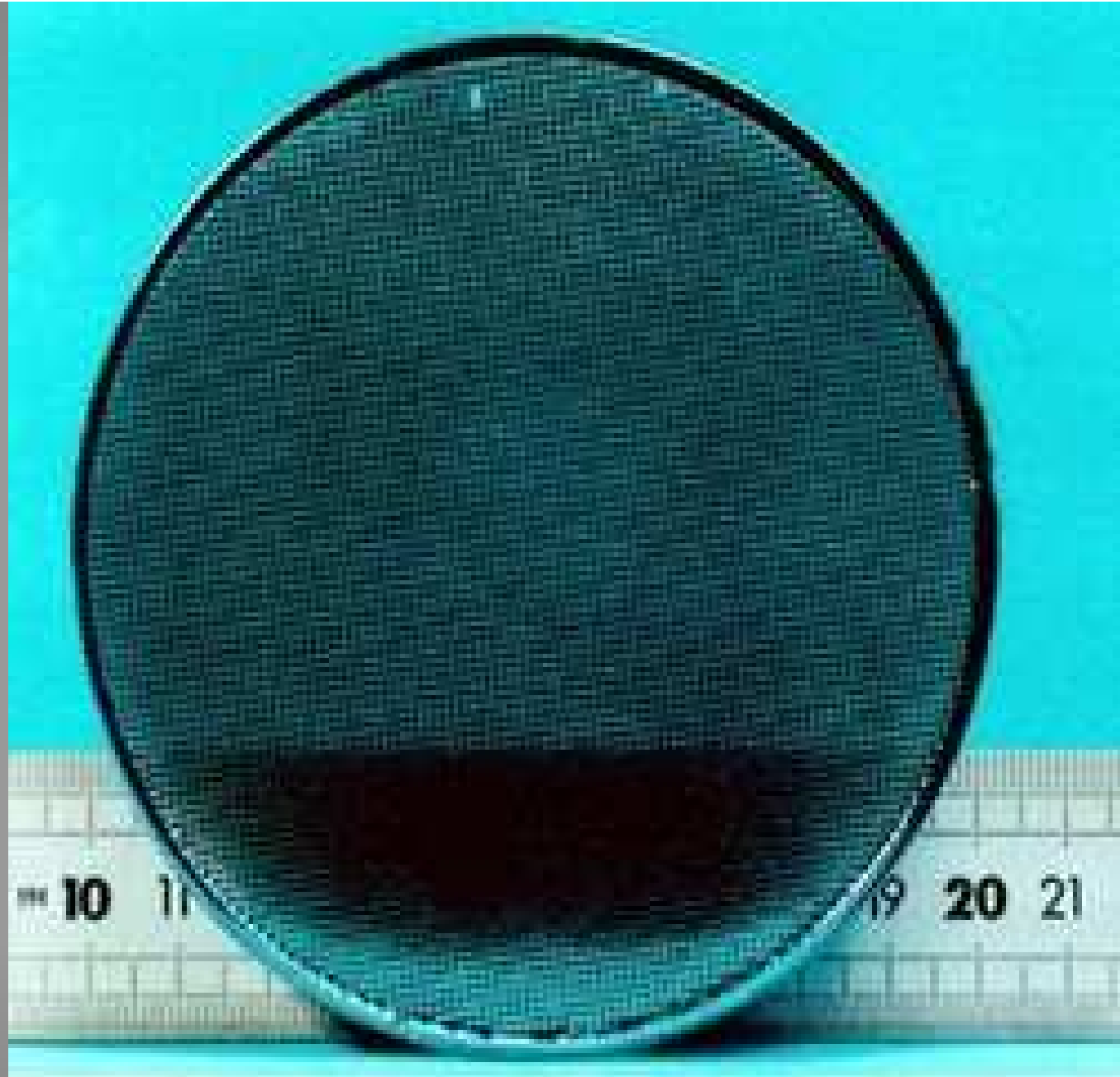
$$\lambda = 2d \sin(\Theta); \Delta\lambda/\lambda = \Delta d/d + \Delta\Theta \operatorname{ctg}(\Theta)$$

**Тепловое сканирование**

# ID28 Spectrometer (ESRF)



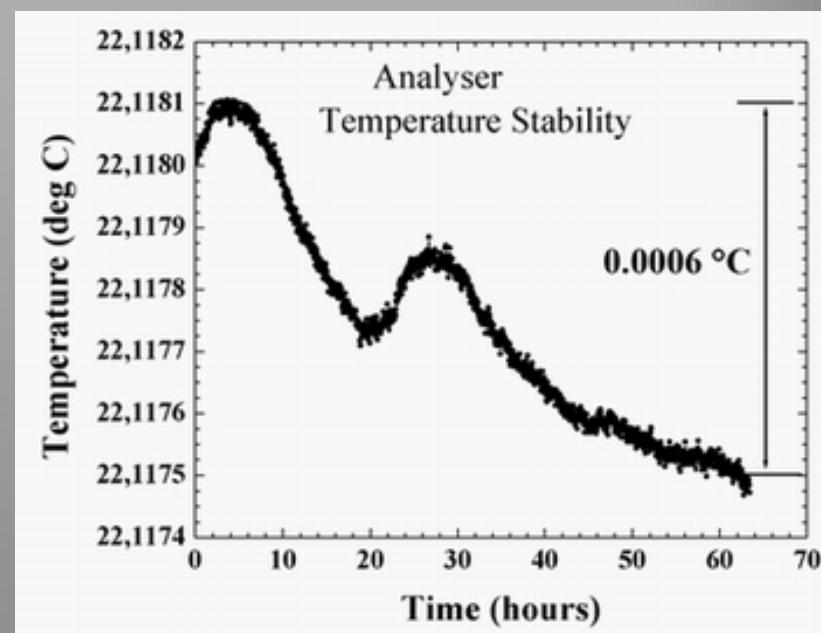
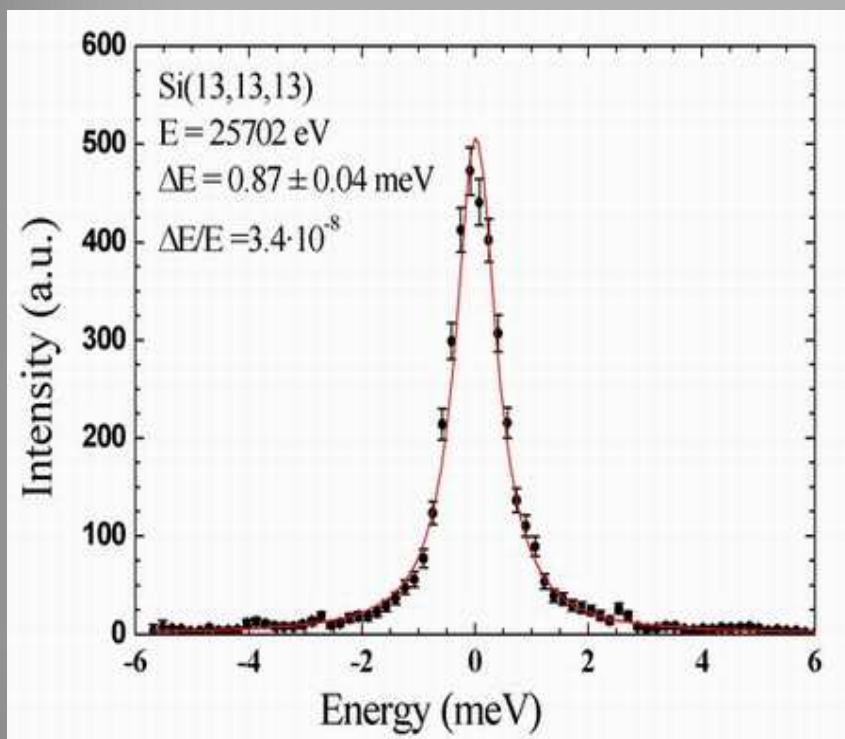




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# Сферический кристалл анализатор



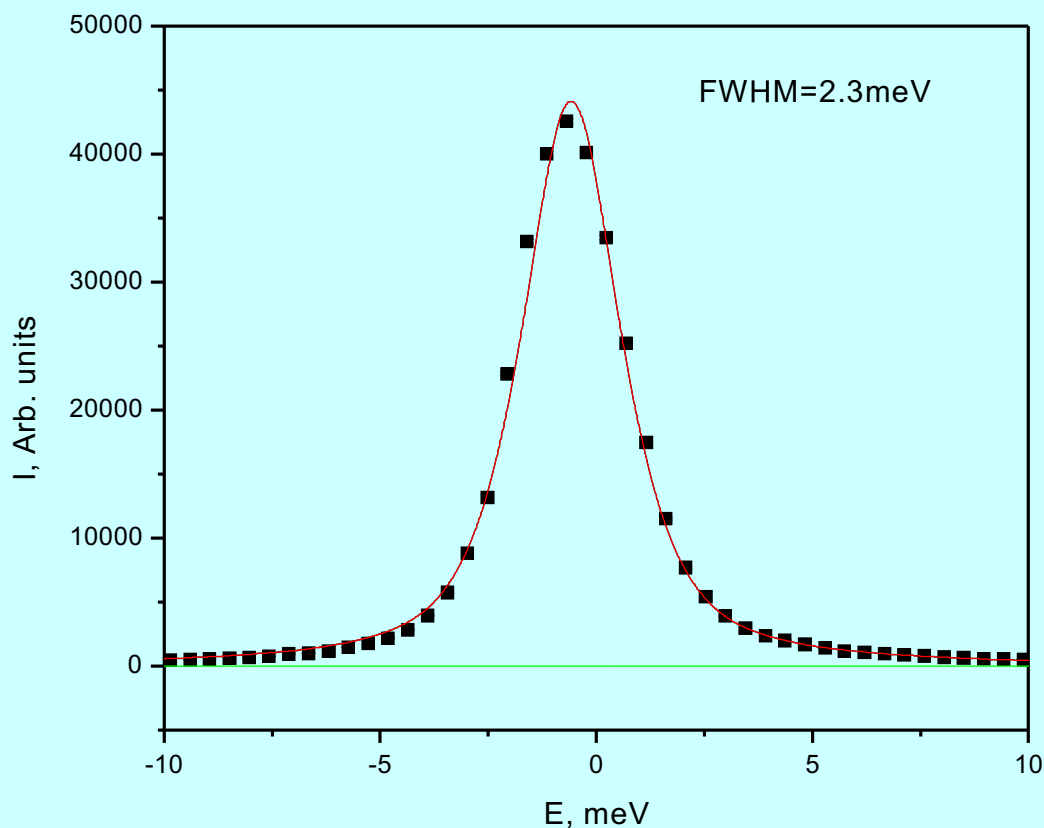
# The main characteristics of the ID28 Beamline with the 7-m arm:



Reflection	Energy [keV]	E [meV]	$Q_{\max}$ [nm <sup>-1</sup> ]	$Q_{\min}$ [nm <sup>-1</sup> ]	$\Delta Q$ [nm <sup>-1</sup> ]	Flux [ph./s/ 200 mA]
Si(7,7,7)	13.840	7.6 ± .2	64	1	1.89	10.5 · 10 <sup>10</sup>
Si(8,8,8)	15.817	5.5 ± .2	74	1	2.16	9.00 · 10 <sup>10</sup>
Si(9,9,9)	17.794	3.0 ± .2	83	1	2.43	2.70 · 10 <sup>10</sup>
Si(11,11,11)	21.747	1.5 ± .1	101	1	3.00	6.60 · 10 <sup>9</sup>
Si(12,12,12)	23.725	1.3 ± .1	111	1	3.24	5.85 · 10 <sup>9</sup>
Si(13,13,13)	25.704	1.0 ± .1	120	1	3.50	1.47 · 10 <sup>9</sup>

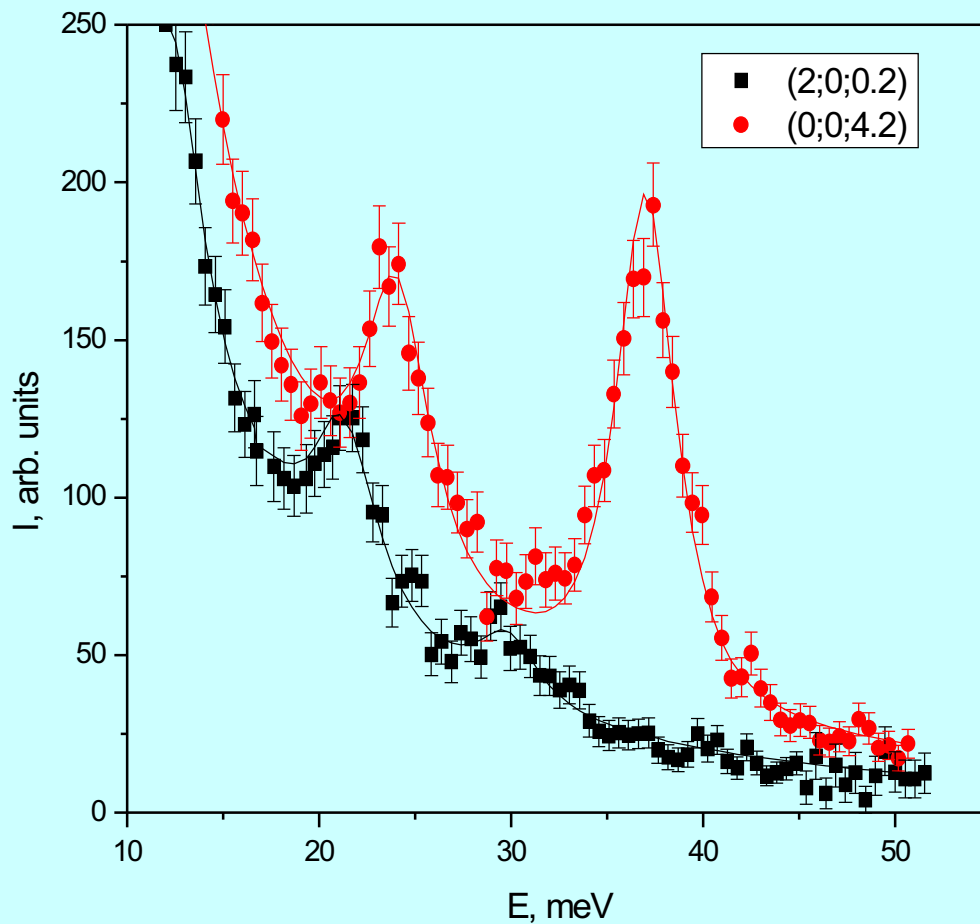
Photon **Flux** values are measured at the sample goniometer with the following experimental conditions: two 1.6 m U32 undulators; ring current: 200 mA; primary slits aperture: 1.6 mm (horizontal) x 0.7 mm (vertical); secondary slits aperture: 2.4 mm (horizontal) x 1.0 mm (vertical). The **Qmin** depends strongly from the beam divergence (40μrad hor. x 20μrad ver.) and from the aperture of the slits in front of the first analyser. The **focal spot size at the sample** is 250μ hor. x 80μ ver. using the toroidal part of the focussing mirror and 25μm hor. x 60μm ver. using the cylindrical part of the mirror for the vertical focussing and the multilayer mirror for the horizontal focussing

# Эксперимент твердый раствор CdS/CdSe

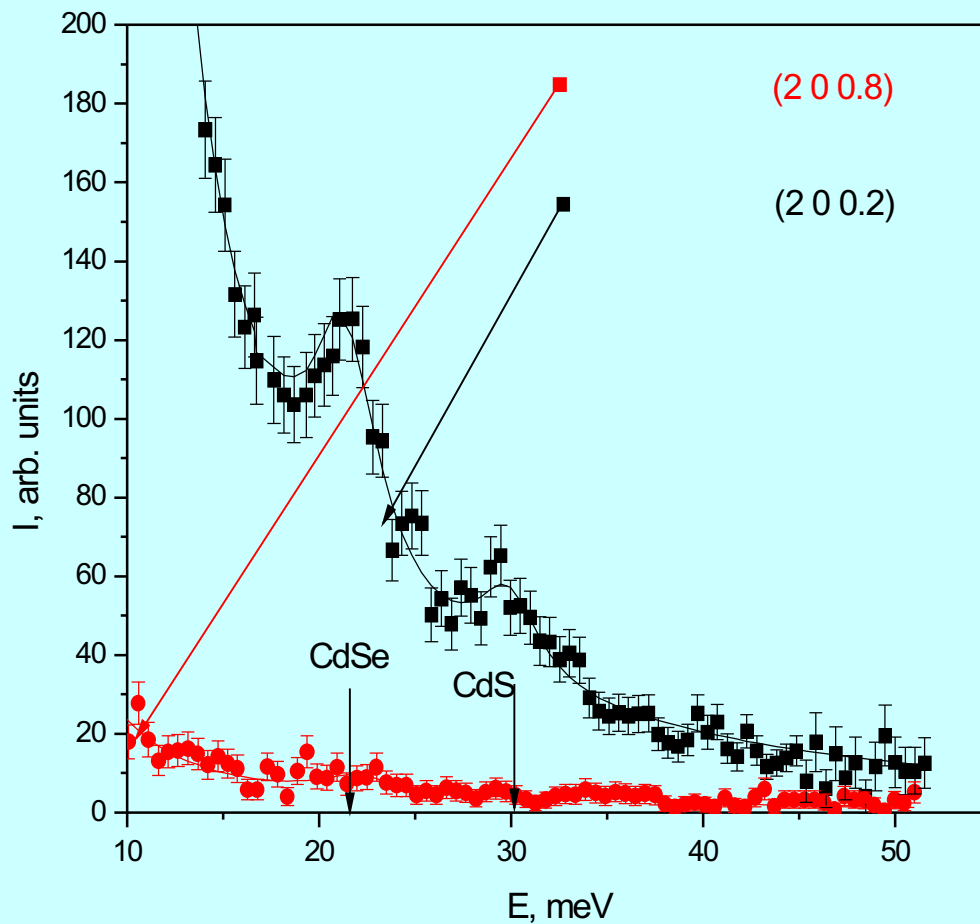


- Монохроматор: Si(999)
- $E=17.8\text{keV}$
- $\Delta E=2.3\text{meV}$
- Room temperature

# продольных и поперечных фононах



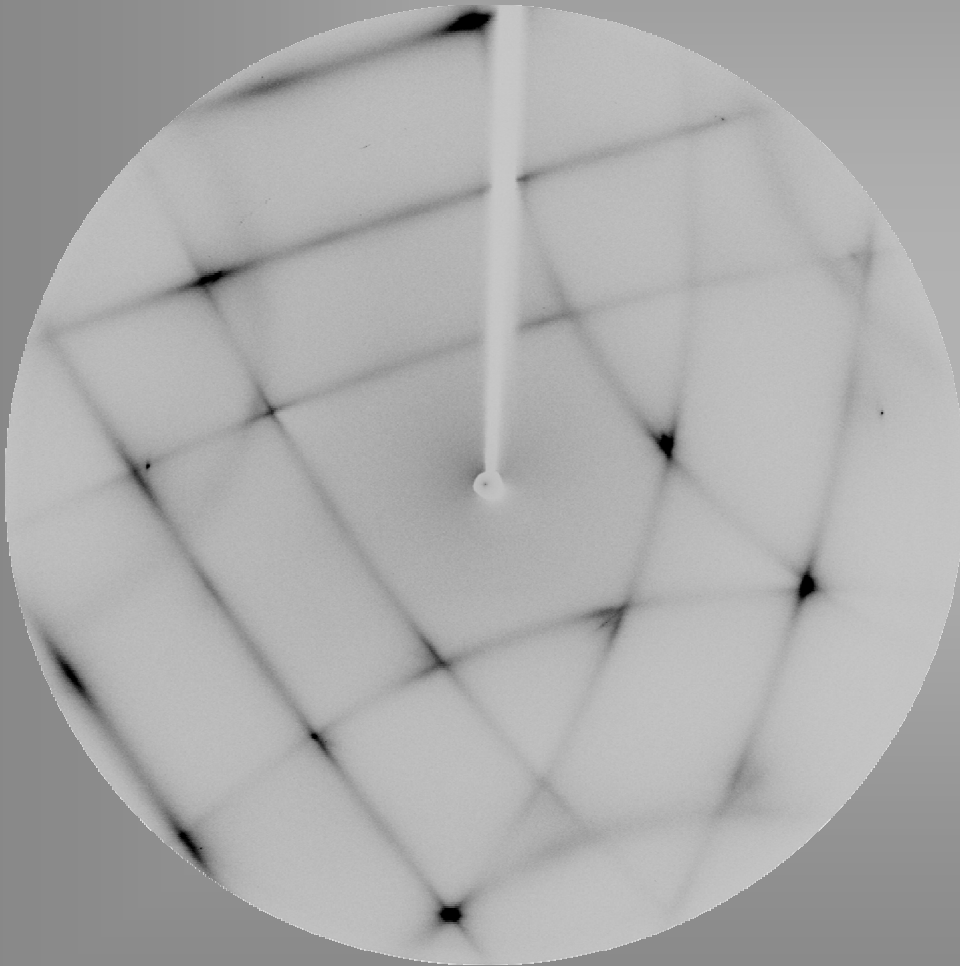
# ЗАВИСИМОСТЬ ОТ ВЕКТОРА ОБРАТНОЙ РЕШЕТКИ



# diffuse scattering in perovskite



Piezoelectrics  $\text{Li}_x(\text{K}_{0.5}\text{Na}_{0.5})_{1-x}\text{NbO}_3$



Collaboration:

A. Bosak

*ESRF*

D. Chernyshov

*SNBL*

D. Damjanovic

*EPFL, Lausanne*

M. Korablev-Dyson

*SpbGPU, St. Petersburg*

S.Vakhrushev

*A.F. Ioffe PTI, St. Petersburg*

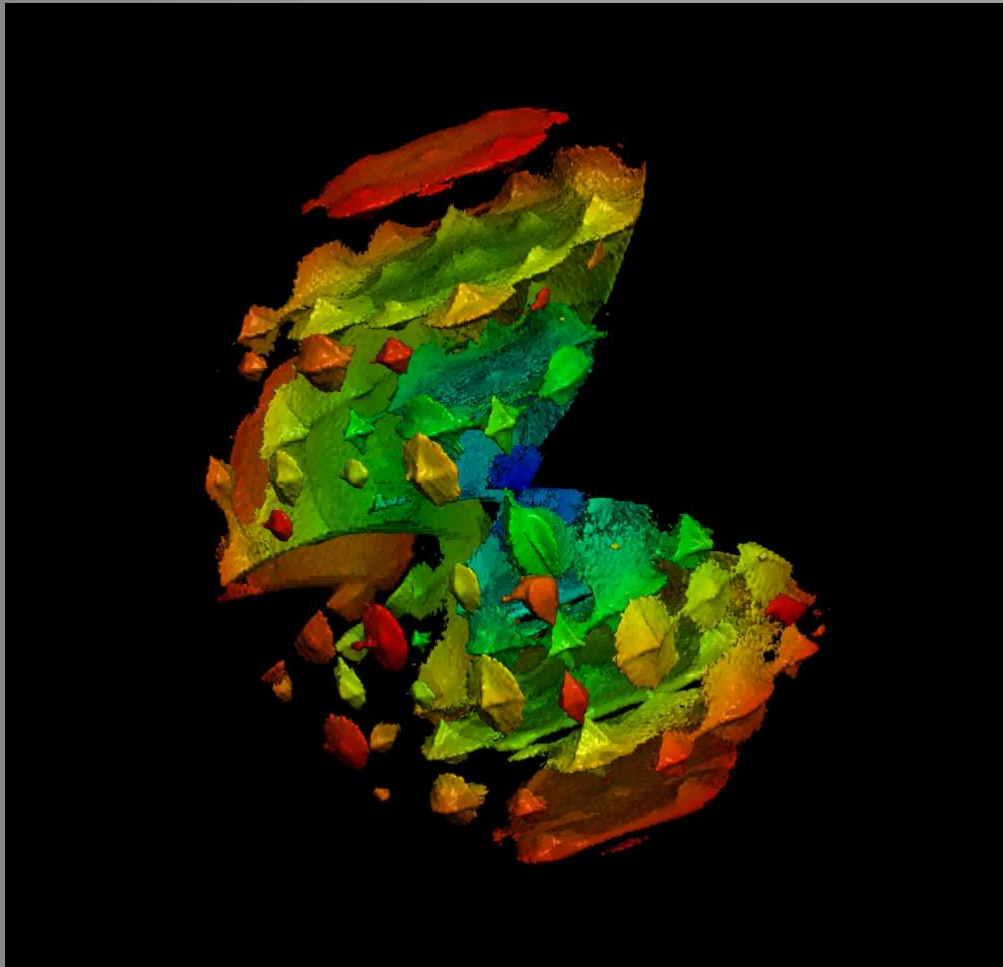
**High temperature:**

cubic phase, three families of  
diffuse planes normal to  
 $\langle 100 \rangle$ ,  $\langle 010 \rangle$ ,  $\langle 001 \rangle$

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 $\langle 100 \rangle$ ,  $\langle 010 \rangle$ ,  $\langle 001 \rangle$



# Двумерное распределение интенсивности в NBT ДН-2 Дубна

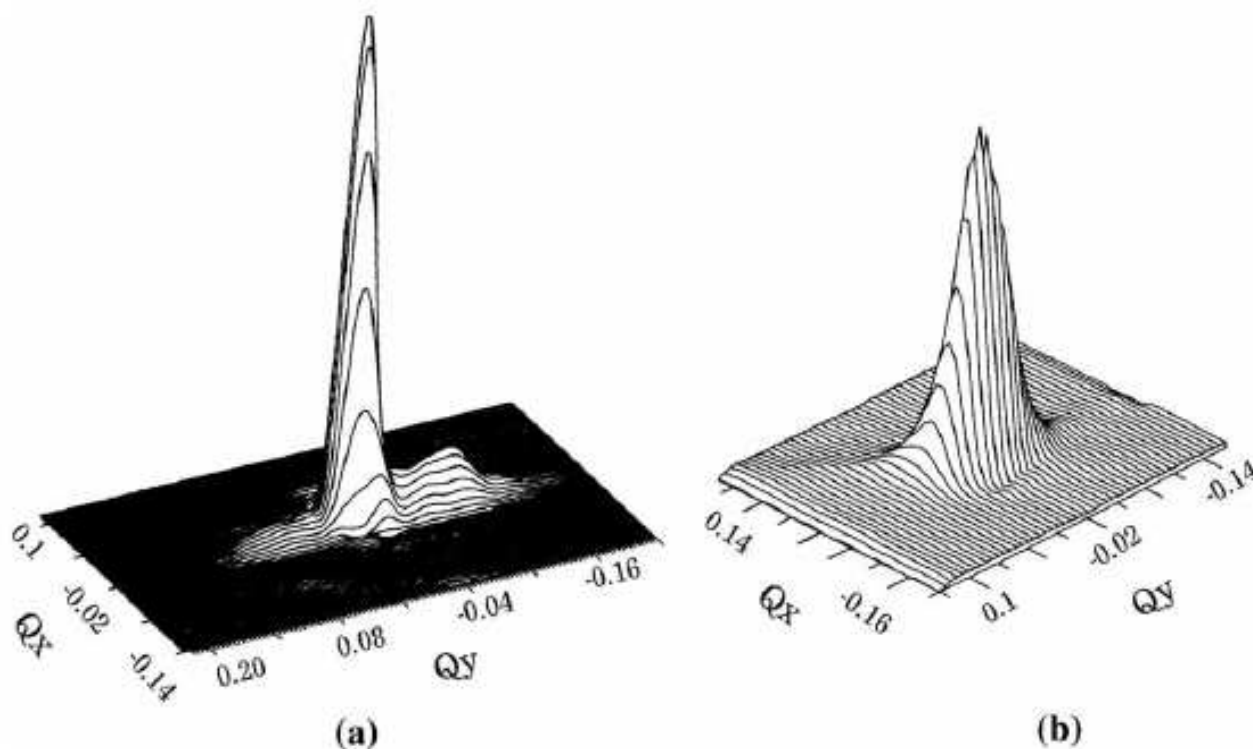


Figure 6. The experimental two-dimensional spectra of neutron scattering intensity in NBT near the point (1.5, 0.5, 0.5) for scans of (a) ( $Q_x \parallel [310]$ ,  $Q_y \parallel [001]$ ) and (b) ( $Q_x \parallel [301]$ ,  $Q_y \parallel [010]$ ).



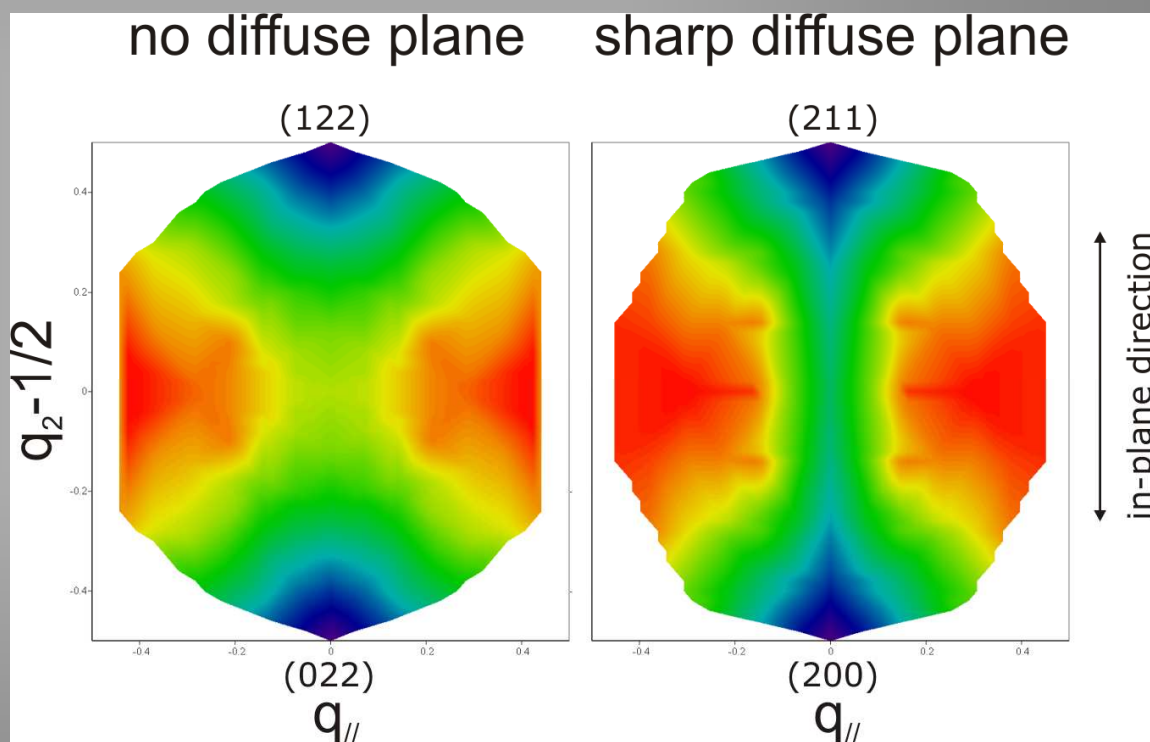
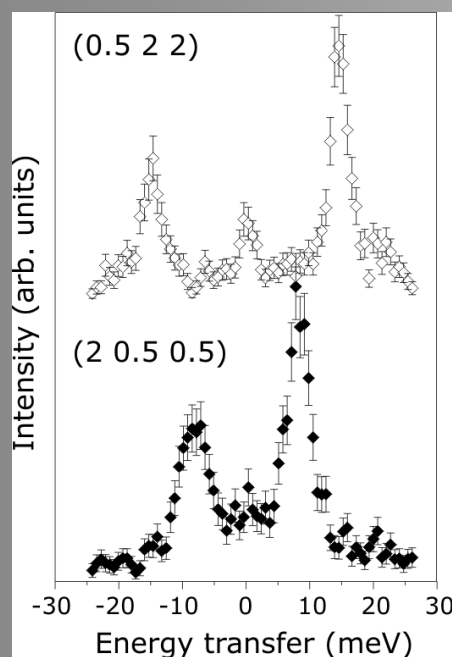
# Phonons only: no static disorder

**Ambient temperature:**

orthorhombic phase, only one family of diffuse planes normal to  $\langle 001 \rangle$  survives

elastic or inelastic?

IXS @ ID28!



sharp diffuse features correspond to strong phonon softening



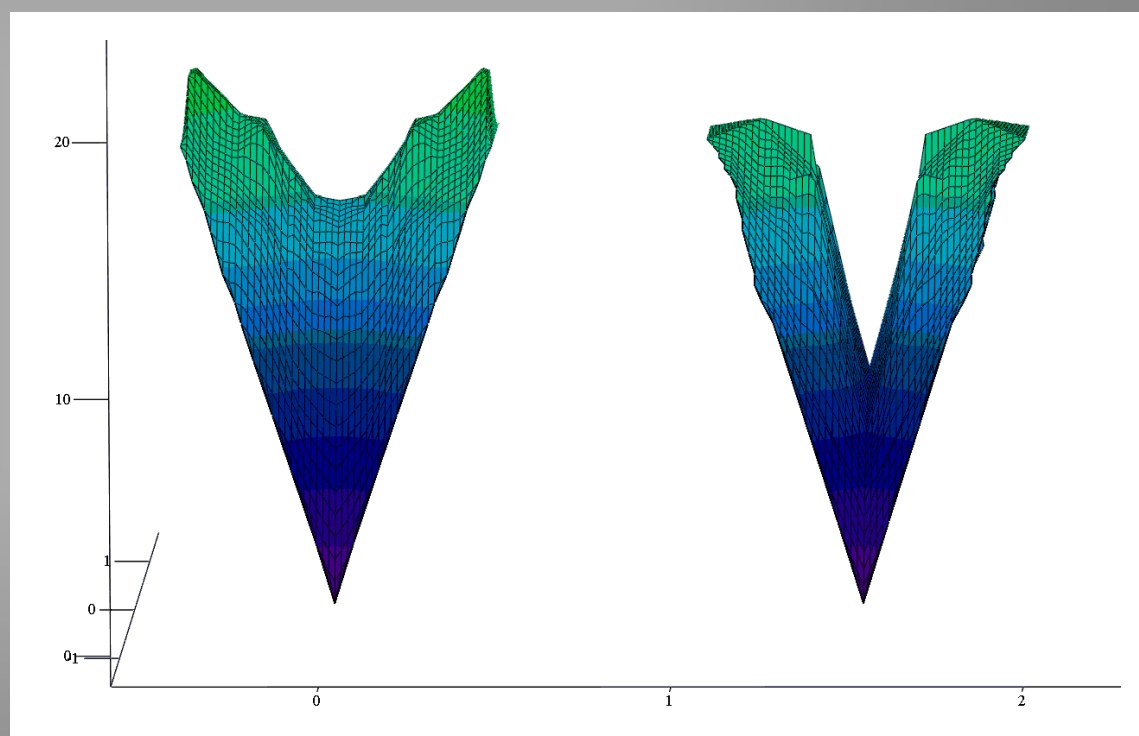
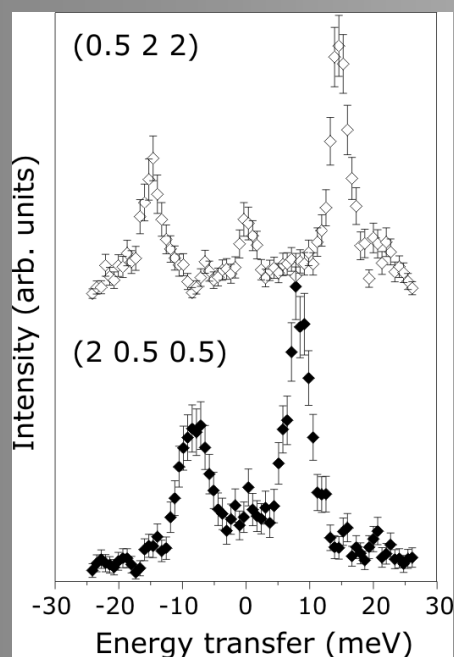
# Phonons only: no static disorder

**Ambient temperature:**

orthorhombic phase, only one family of diffuse planes normal to  $\langle 100 \rangle$  survives

elastic or inelastic?

IXS @ ID28!



sharp diffuse features correspond to strong phonon softening



# ПЛЕНКИ

# Phonons in 100nm film



PMN film (0.25 2 0) "large" tilt (inside film?)

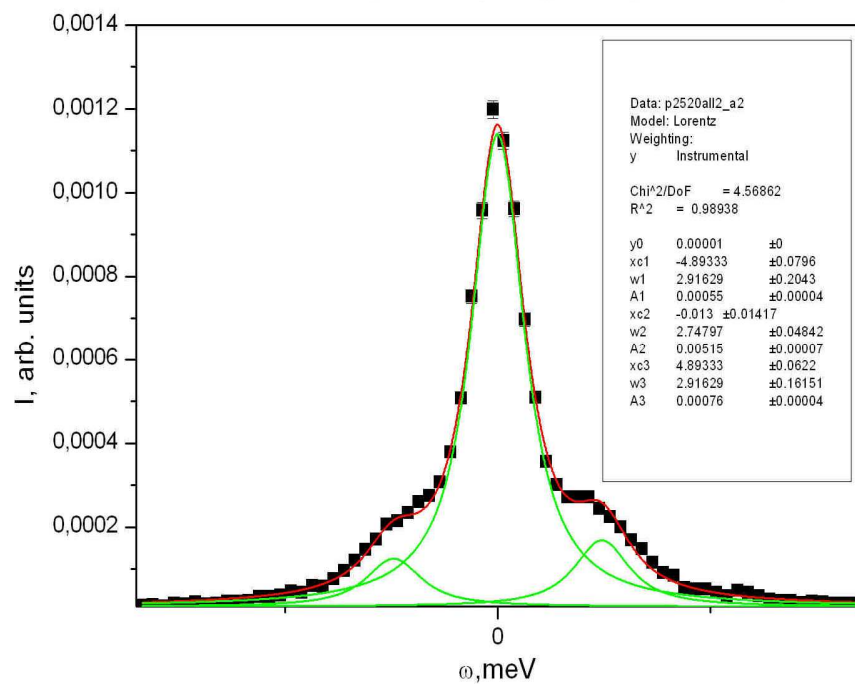


Figure 1

PMN film (0.25 2 0) small tilt (near surface?)

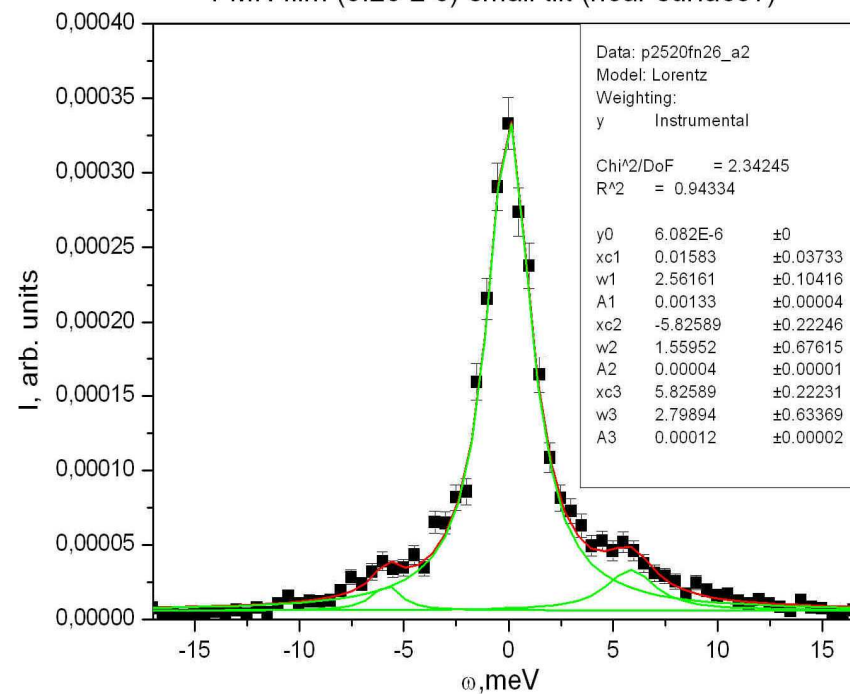


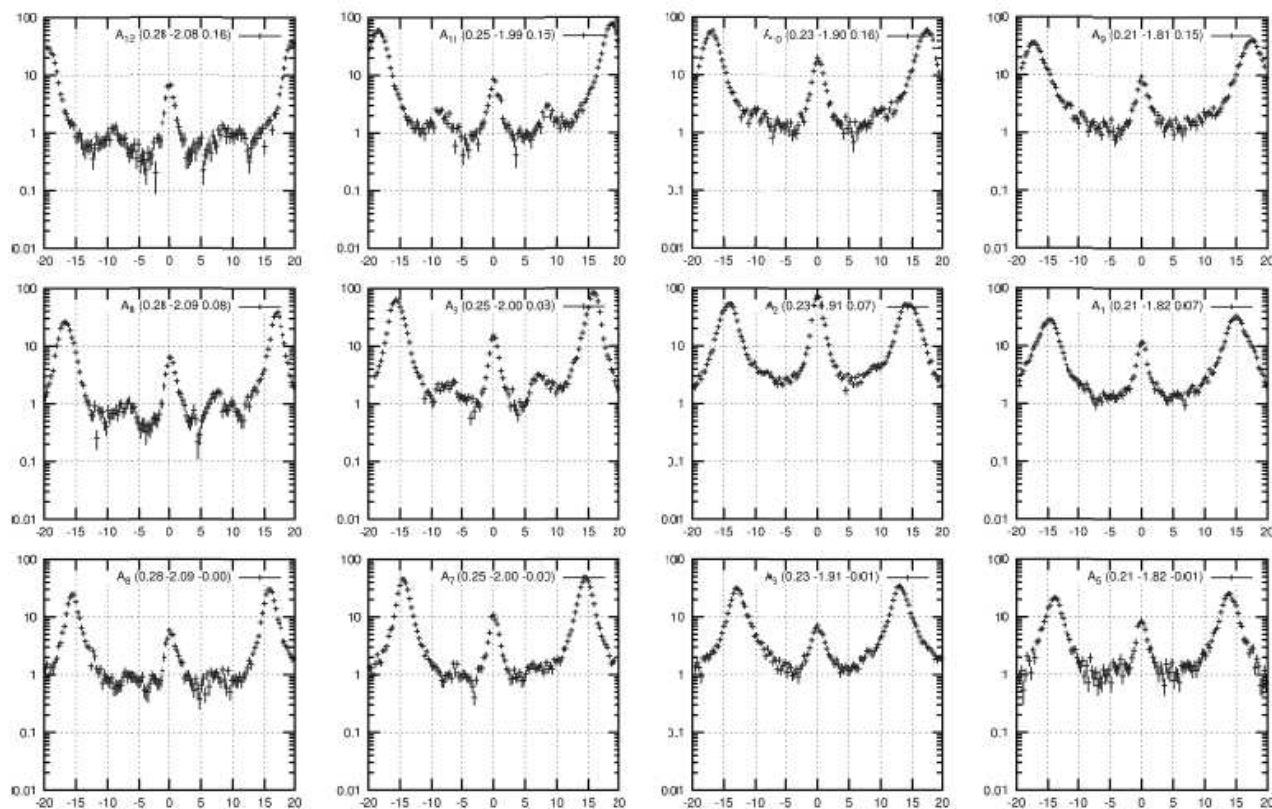
Figure 2

# PMN film 80nm

## BL35XU $V=800\mu^3$



PBMN 600C (0.25 2 0)  $dQ = (0.007\ 0.07\ 0.45)$  horizontal slit opened





# Локальная Структура и динамика



# Static PDF

- Dynamic structure factor:

$$S(\mathbf{Q}, \omega) = \frac{1}{N \langle b \rangle^2} \sum_{\nu, \mu} b_{\nu} b_{\mu} \int \left\langle \left\langle e^{i\mathbf{Q} \cdot (\mathbf{R}_{\nu}(0) - \mathbf{R}_{\mu}(t))} \right\rangle \right\rangle e^{-i\omega t} dt$$

- Elastic structure factor ( $\omega = 0$ ) describes the average structure:

$$S(\mathbf{Q}, 0) = \frac{1}{N \langle b \rangle^2} \sum_{\nu, \mu} b_{\nu} b_{\mu} \left\langle \left\langle e^{i\mathbf{Q} \cdot (\mathbf{R}_{\nu} - \mathbf{R}_{\mu})} \right\rangle \right\rangle$$



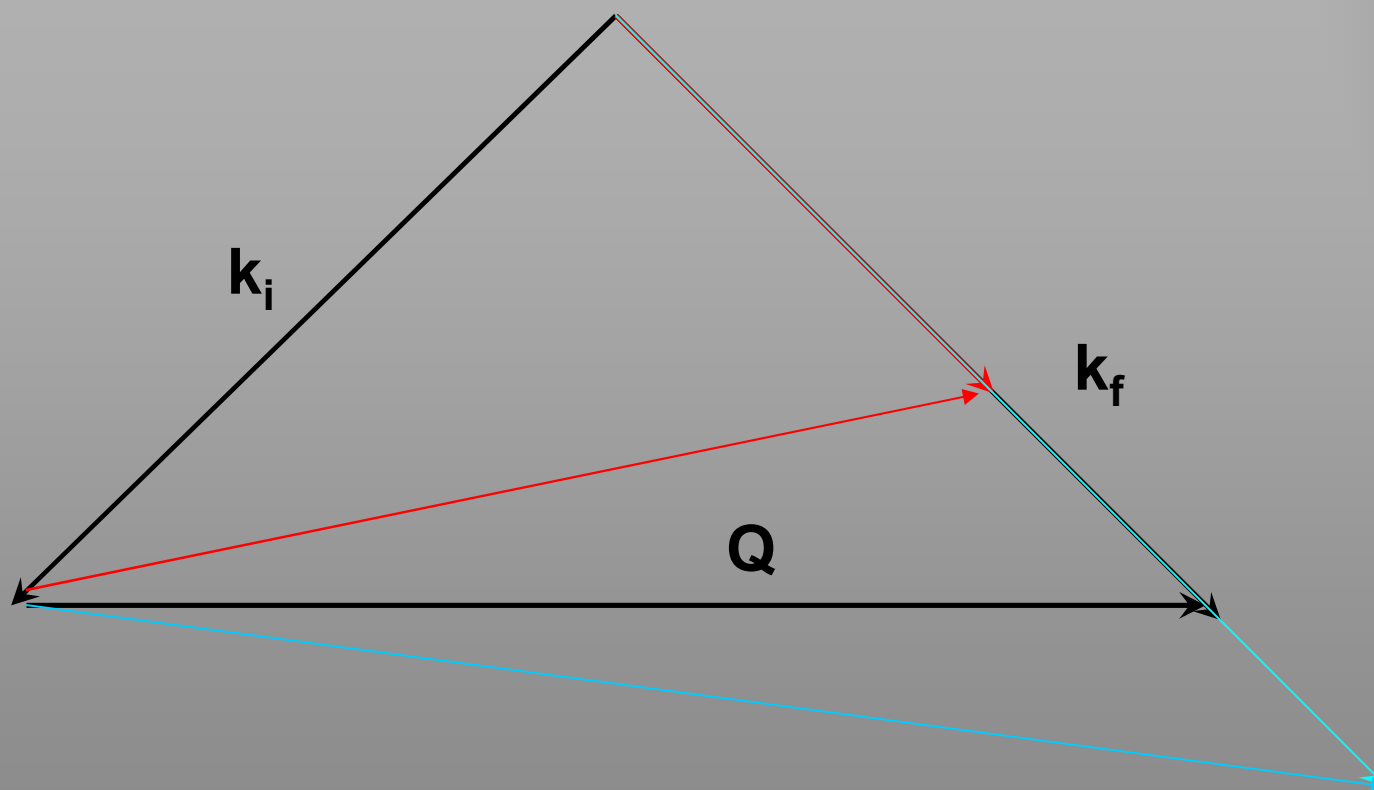


# Instantaneous PDF

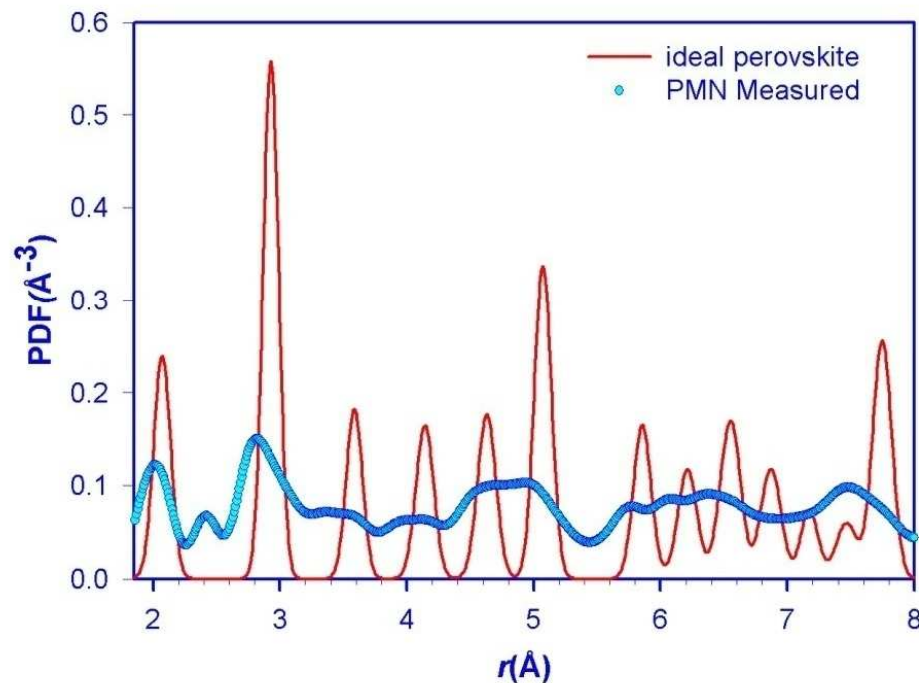
- Energy integrated structure factor describes the instantaneous (snap-shot) structure:

$$\begin{aligned}
 S_{total}(\mathbf{Q}) &= \int_{-\infty}^{\infty} S(\mathbf{Q}, \omega) d\omega \\
 &= \frac{1}{N\langle b \rangle^2} \sum_{\nu, \mu} b_{\nu} b_{\mu} \iint \left\langle \left\langle e^{i\mathbf{Q} \cdot (\mathbf{R}_{\nu}(0) - \mathbf{R}_{\mu}(t))} \right\rangle \right\rangle e^{-i\omega t} dt d\omega \\
 &= \frac{1}{N\langle b \rangle^2} \sum_{\nu, \mu} b_{\nu} b_{\mu} \left\langle \left\langle e^{i\mathbf{Q} \cdot (\mathbf{R}_{\nu}(0) - \mathbf{R}_{\mu}(0))} \right\rangle \right\rangle
 \end{aligned}$$

# Дифракция без анализа по энергии



# Pb polarization



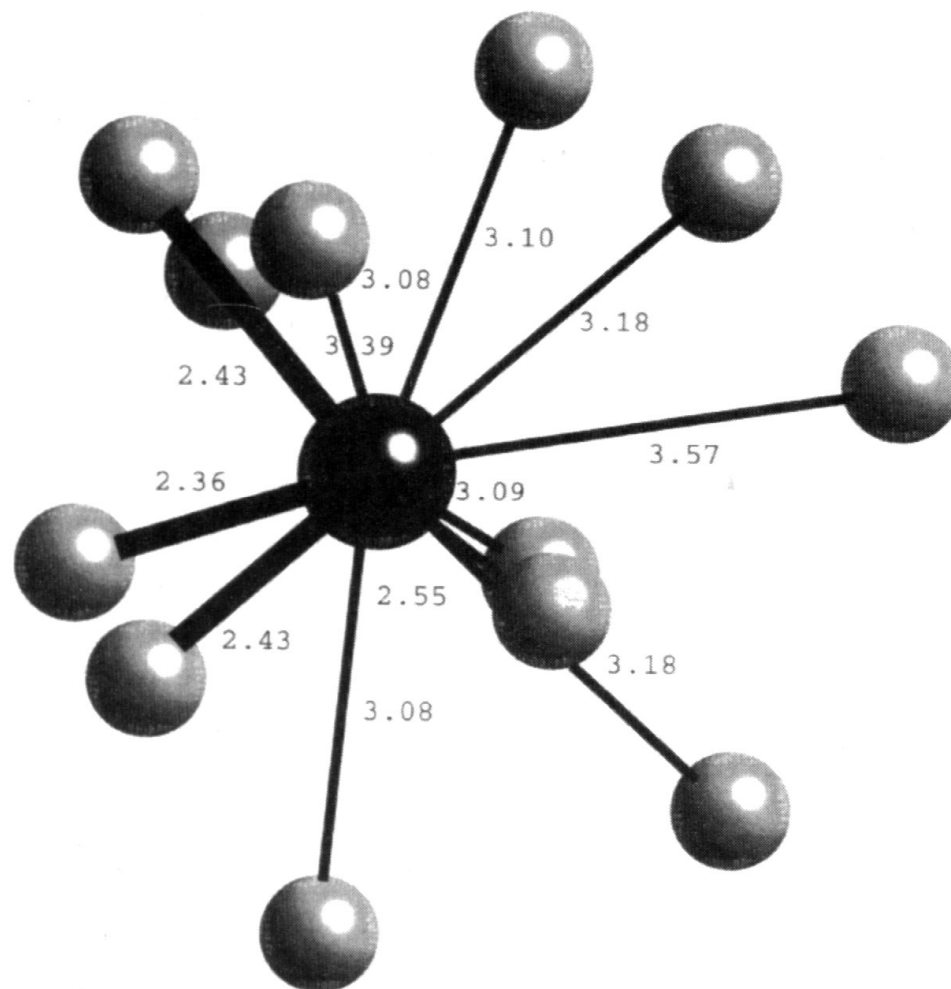
- PDF of PMN



## $\text{Pb}^{2+}$ in $\text{PbZrO}_3$

Pb is off-centered by  $0.5 \text{ \AA}$  in the  $\text{O}_{12}$  cage

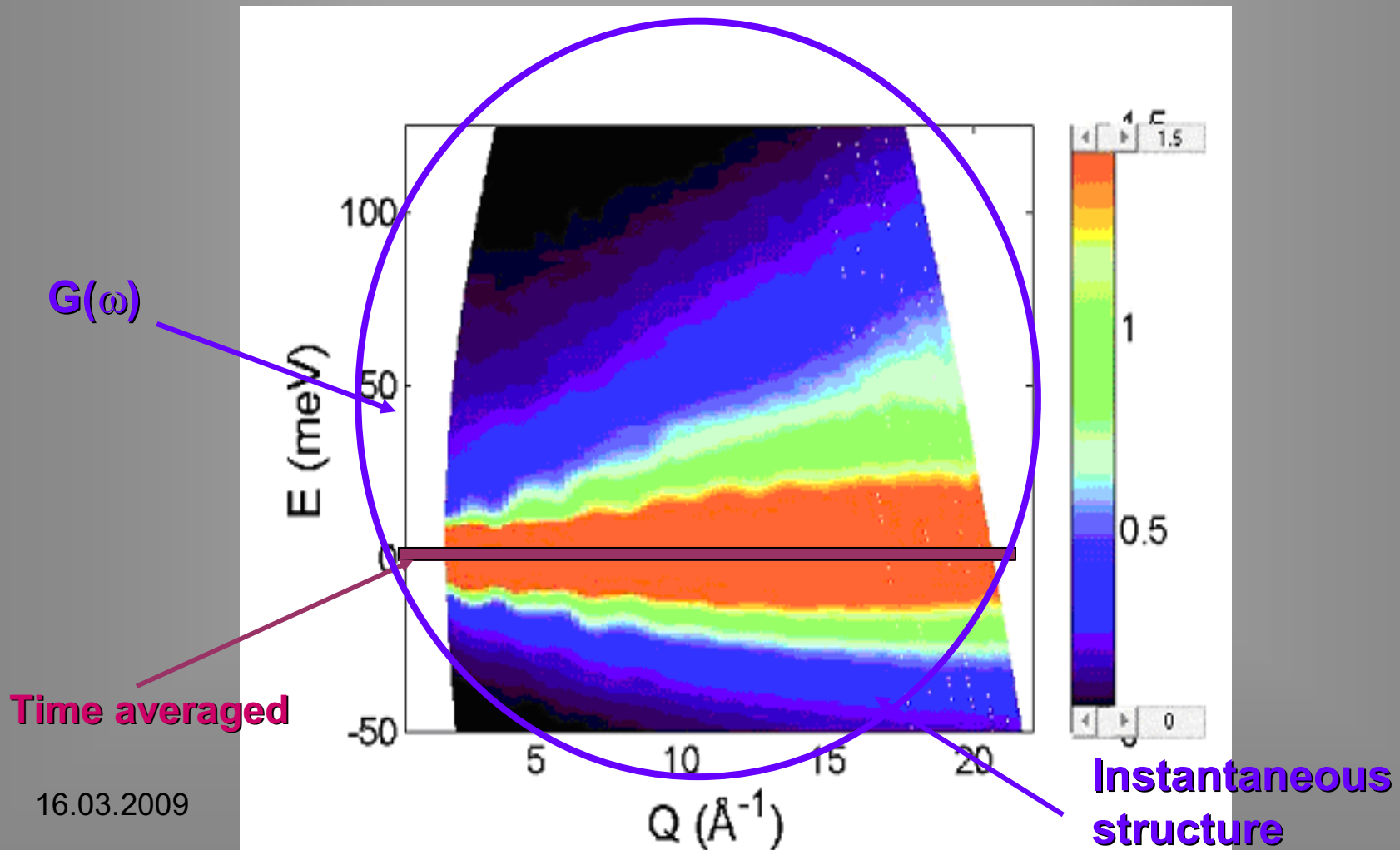
Lone-pair  $s$ - $p$   
electrons of Pb



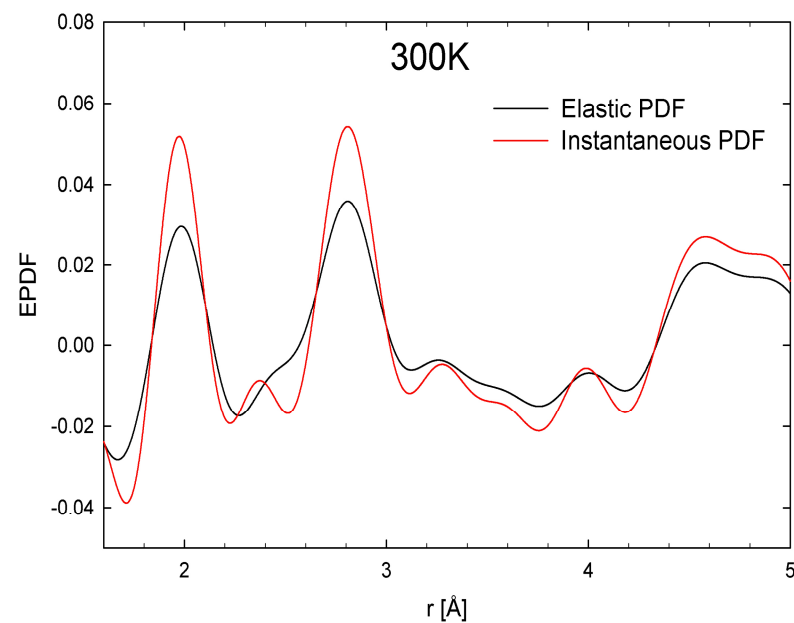
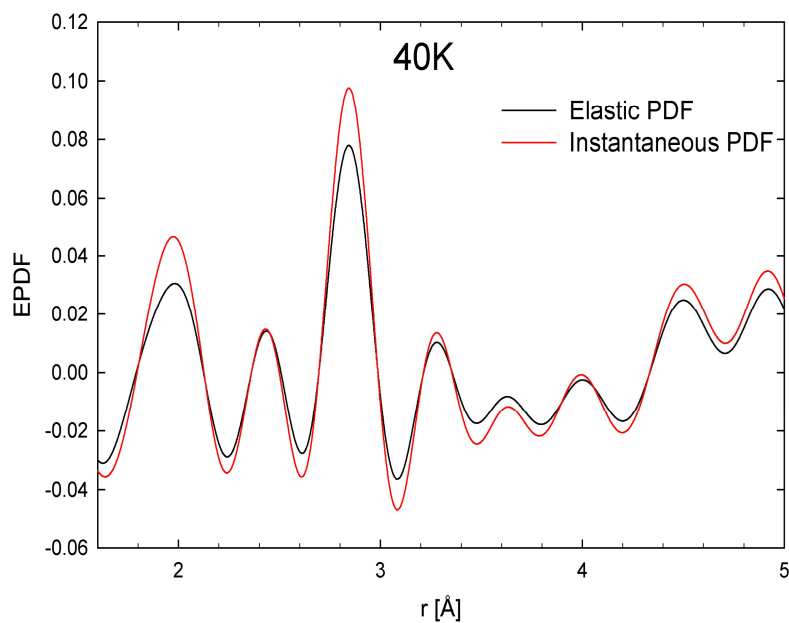
# $S(Q, \omega)$ PMN, $T = 450$ K



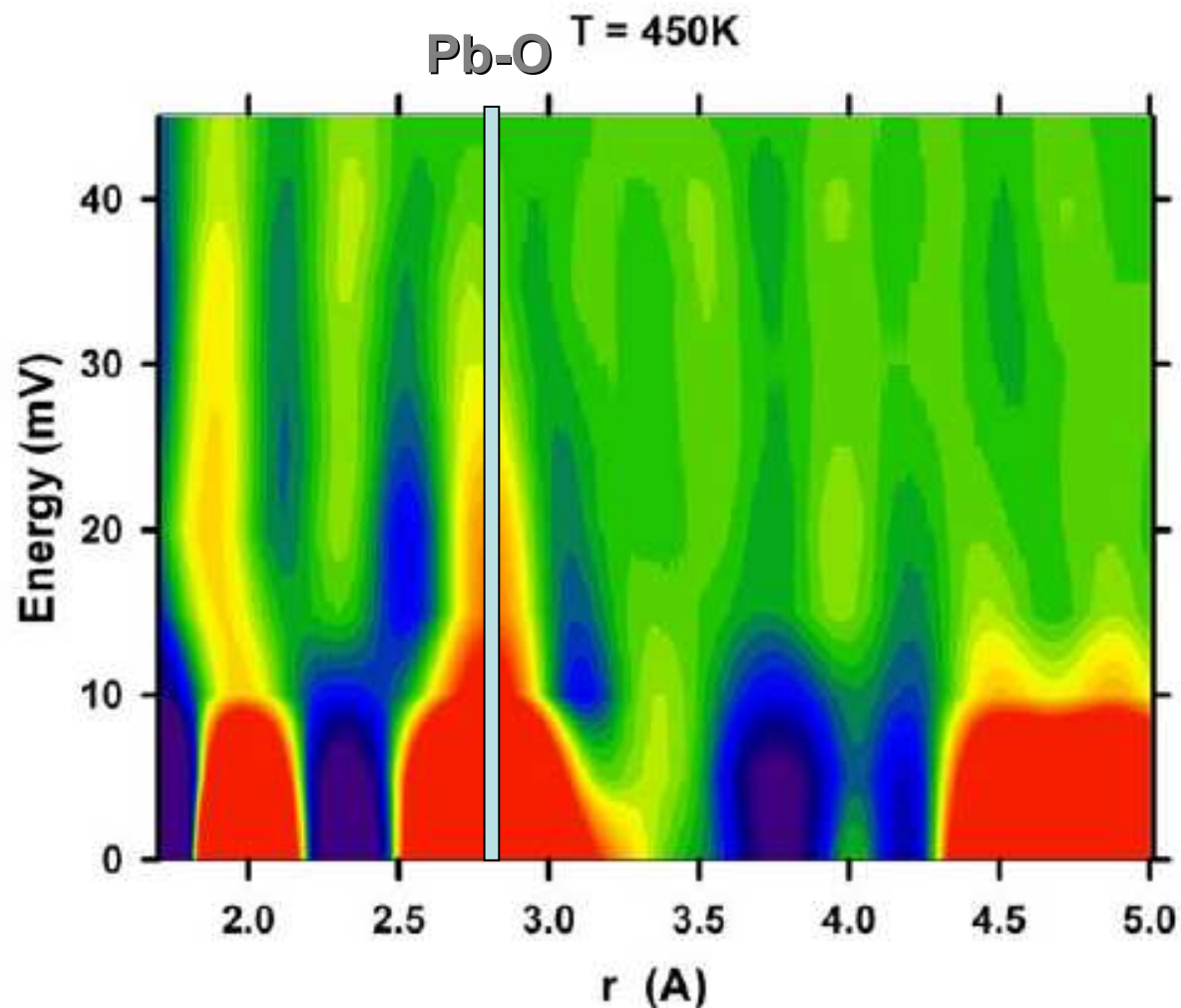
Usually it is implicitly supposed that **time-averaged** and **instantaneous** structures are equivalent



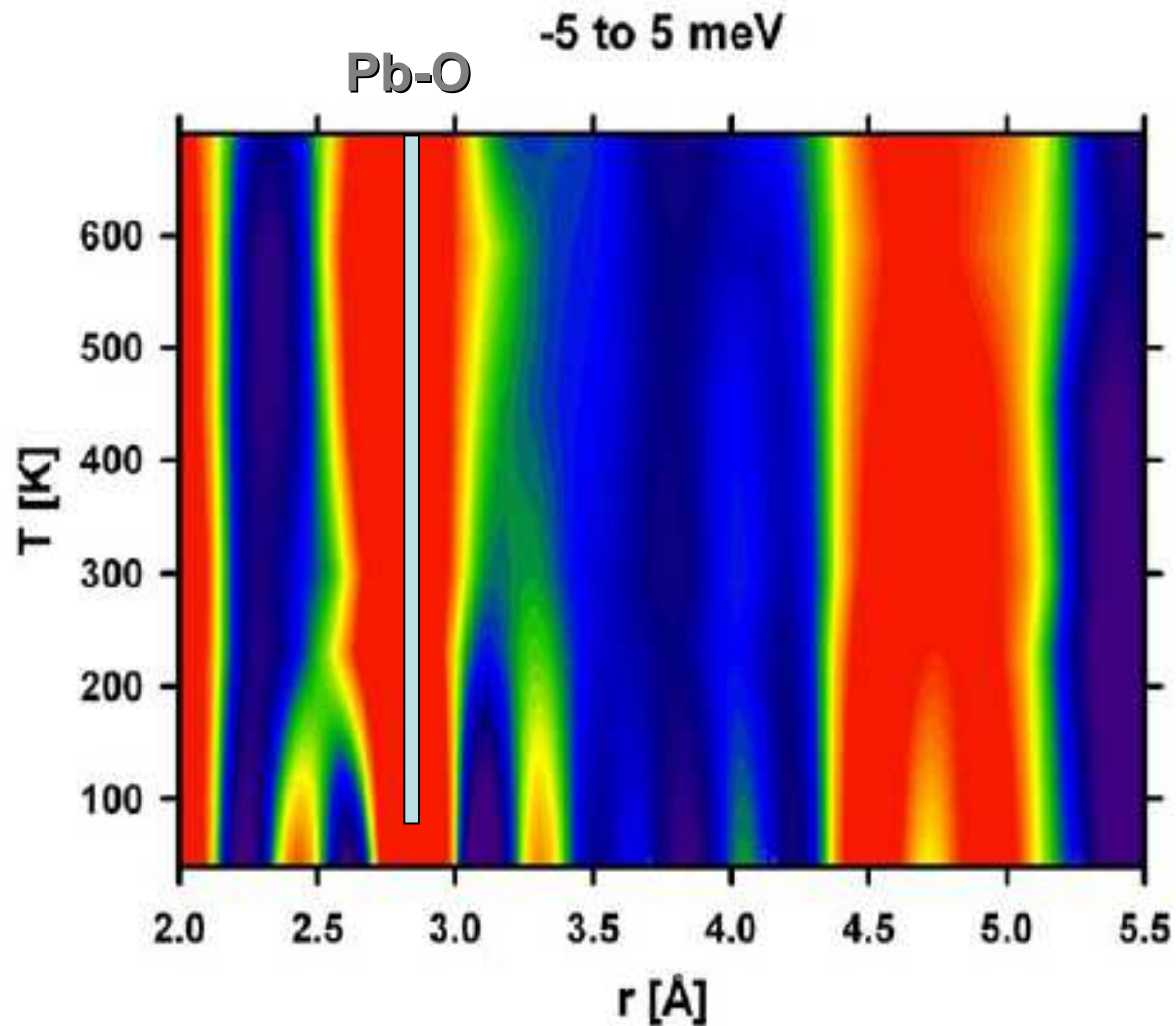
# Elastic (average) and energy-integrated (instantaneous) pair distribution functions for Pb in PMN



# Dynamic PDF of PMN at 450 K.

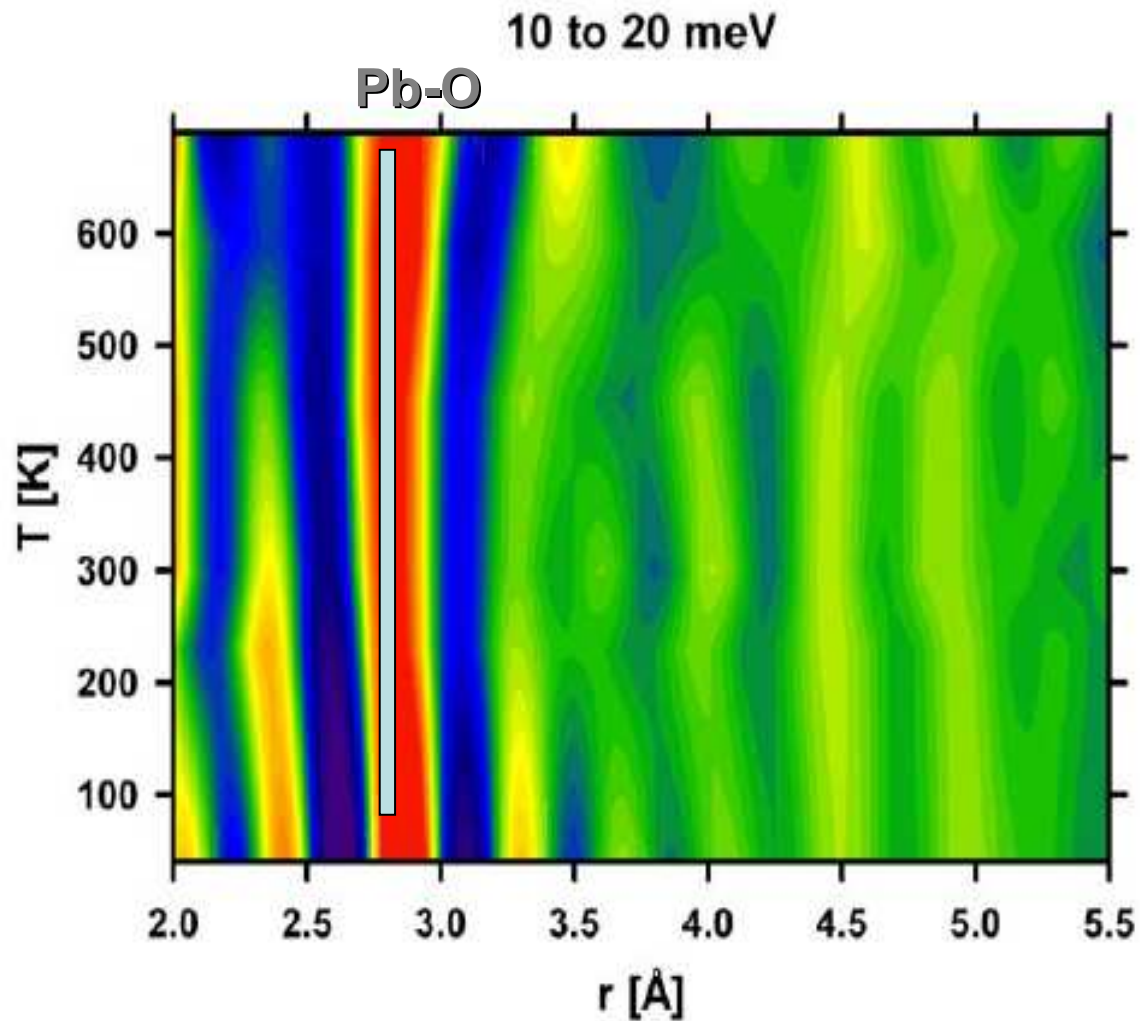


# Temperature evolution of average local structure





# Temperature evolution of the dynamic structure



# Мезоструктура. Почему рассеяние



- Макроскопические методы не дают микроскопической картины
- Оптическая микроскопия – не дает достаточного разрешения и не чувствительна к смещениям отдельных ионов
- Электронная микроскопия – только тонкие слои и нарушает структуру
- PFM – сильные поля

# Немного о рассеянии



$$\left( \frac{d\sigma}{d\Omega} \right)_{li} = \frac{k}{k_o N} \sum_v^N \sum_{v'}^N b_v b_{v'} \langle i | e^{iQ\hat{r}_v} | l \rangle \langle l | e^{-iQ\hat{r}_{v'}} | i \rangle$$

в кристалле мы можем записать:

$$\hat{r}_v \equiv \hat{r}_{nj} = \mathbf{R}_n + \boldsymbol{\rho}_j + \hat{u}_{nj}$$

Тогда, после усреднения:

$$\left( \frac{d\sigma}{d\Omega d\omega} \right)_{coh} = \frac{1}{m} \sum_j^m \sum_{j'}^m b_{jcoh} b_{j'coh} e^{iQ(\boldsymbol{\rho}_j - \boldsymbol{\rho}_{j'})} \frac{1}{N} \sum_n^N \sum_{n'}^N e^{iQ(\mathbf{R}_n - \mathbf{R}_{n'})} \varphi_{vv'}(T)$$

$$\left( \frac{d\sigma}{d\Omega d\omega} \right)_{inc} = \frac{1}{m} \sum_j^m b_{jinc}^2 \frac{1}{N} \sum_n^N \varphi_{vv}(T)$$

# От какого объема мы получаем картину рассеяния?



- На самом деле суммирование ведется НЕ ПО ОБЪЕМУ ОБРАЗЦА и НЕ ПО РАЗМЕРУ ПУЧКА, а по некому «когерентному объему» определяемому параметрами пучка излучения.

### 4.2.2. Пространственная когерентность и площадь когерентности

Теперь рассмотрим вкратце интерференционный эксперимент типа опыта Юнга, используя квазимонохроматический свет от протяженного источника  $\sigma$  (рис. 4.2). Предположим, что  $\sigma$  представляет собой тепловой источник, такой, как раскаленное вещество или газовый разряд. Для простоты рассмотрим симметричную схему с источником в форме квадрата со стороной  $\Delta s$ . Если отверстия  $P_1$  и  $P_2$  расположены достаточно близко к оси симметрии, вблизи центральной точки  $P$  в плоскости наблюдения  $\mathcal{A}$  будут наблюдаться интерференционные полосы. Возникновение полос является, как говорят, проявлением пространственной когерентности между двумя пучками, приходящими в точку  $P$  от двух отверстий  $P_1$  и  $P_2$ , поскольку контраст между полосами зависит от расстояния между этими отверстиями (расстояние  $P_1P_2$ ). Экспериментально установлено, что при достаточно большом расстоянии между источником и плоскостью  $\mathcal{A}$ , в которой расположены отверстия, интерференционные полосы вблизи  $P$  будут наблюдаться в том случае, если

$$\Delta\theta\Delta s \leq \bar{\lambda}, \quad (4.2.5)$$

где  $\Delta\theta$  — угол, под которым виден отрезок  $P_1P_2$  из источника, и  $\bar{\lambda} = c/\bar{\nu}$  — средняя длина волны. Если через  $R$  обозначить расстояние между источником и плоскостью, в которой расположены отверстия, то оказывается, что для наблюдения полос вблизи  $P$  отверстия должны быть расположены на плоскости  $\mathcal{A}$  в пределах области с центром в точке  $Q$  и площадью

$$\Delta A \sim (R\Delta\theta)^2 \sim \frac{R^2\bar{\lambda}^2}{S}, \quad (4.2.6)$$

где  $S = (\Delta s)^2$  — площадь источника. Эта область называется площадью когерентности света в плоскости  $\mathcal{A}$  вблизи точки  $Q$ , а квадратный корень от площади когерентности иногда называют поперечной длиной когерентности. Следует отметить, что согласно (4.2.6) площадь когерентности будет тем больше, чем

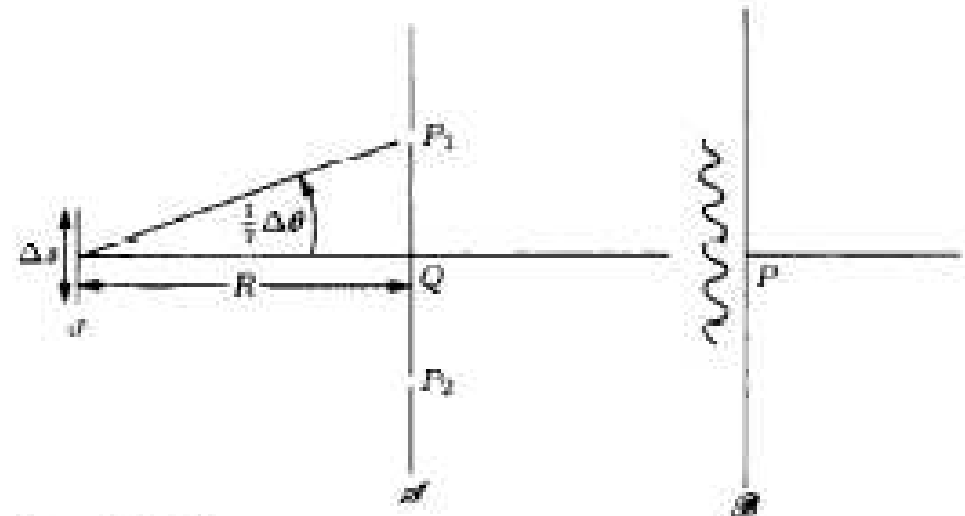


Рис. 4.2. Пространственная когерентность, иллюстрируемая интерференционным опытом Юнга для света от теплового источника  $\sigma$

For classical X-ray scattering experiments, the diffraction of large beams with many coherence volumes is observed. In each coherence volume  $\mathcal{D}_i$ , a wave  $A_i(\mathbf{q})$  is diffracted. Only an incoherent sum of the intensities over a large number of domains  $N$  is measured:

$$I(\mathbf{q}) = \sum_{i \in N} |A_i(\mathbf{q})|^2. \quad (1)$$

With the new synchrotron sources, the high brilliance and the small source size open the possibility of obtaining coherent X-ray beams of reasonable intensity and of nearly macroscopic spatial extension. As the X-ray source is not coherent, the method consists in selecting, in the two transverse directions, a part of the incoherent beam which fulfils the conditions for diffraction:

$$\sigma\sigma' \simeq \lambda/4\pi, \quad (2)$$

where  $\sigma'$  is the r.m.s. divergence of the beam and  $\sigma$  is the r.m.s. beam size. The equality in equation (2) corresponds to fully coherent Gaussian beams. Equation (2) is in fact another version of the Heisenberg equation, if one estimates  $\Delta p = 2\pi\hbar\sigma'/\lambda$  and  $\Delta x = \sigma$ . In practice, owing to optics,



Характерное значение для рентгеновского излучения  
 $\sigma = 1.5 \cdot 10^{-1} / 4\pi / 10^{-3} = 13 \text{ nm}$



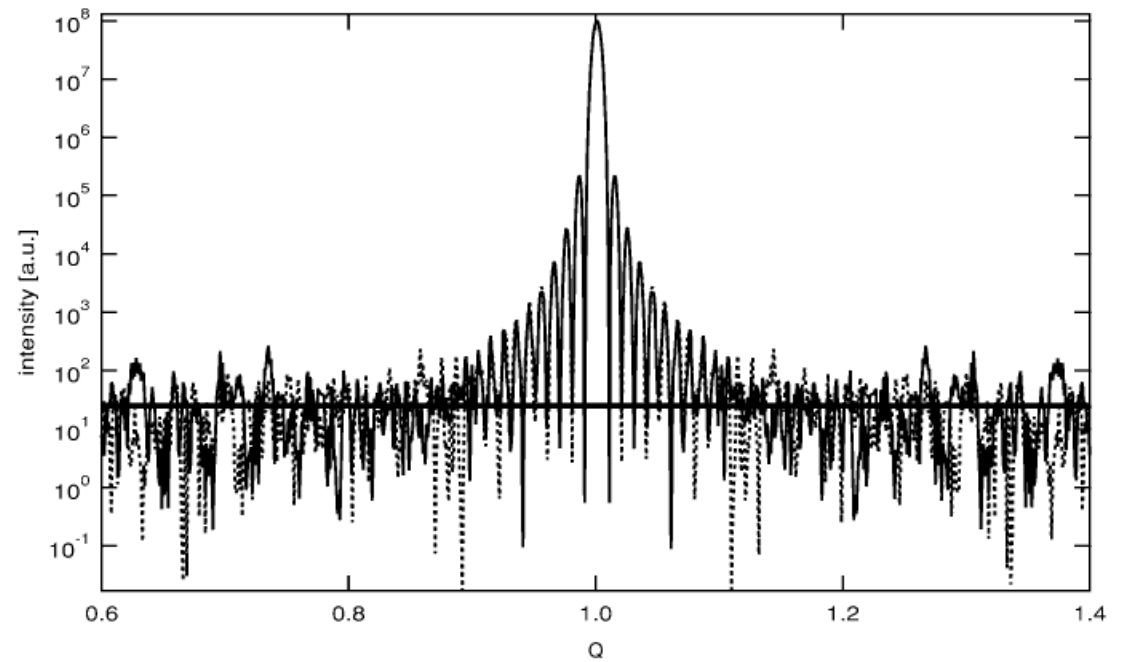
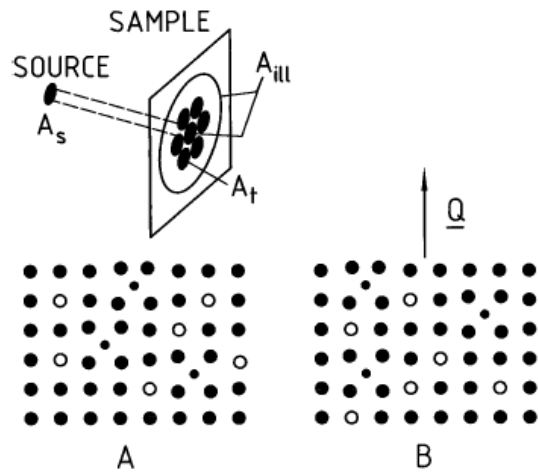
Along the longitudinal direction, the diffracted waves can interfere if the FWHM path-length distribution of the waves in the irradiated sample  $\Delta\mathcal{L}$  fulfils

$$\Delta\mathcal{L} \leq \Lambda_l = \lambda^2 / 2\delta\lambda, \quad (4)$$

where  $\Lambda_l$  is the longitudinal (temporal) coherence length. The optics determines the experiment monochromaticity  $\delta\lambda$ . One

Характерное значение для рентгеновского излучения  
 $\Lambda = 0.15 / 2 / (d\lambda/\lambda = 2 \cdot 10^{-4}) = 400 \text{ nm}$

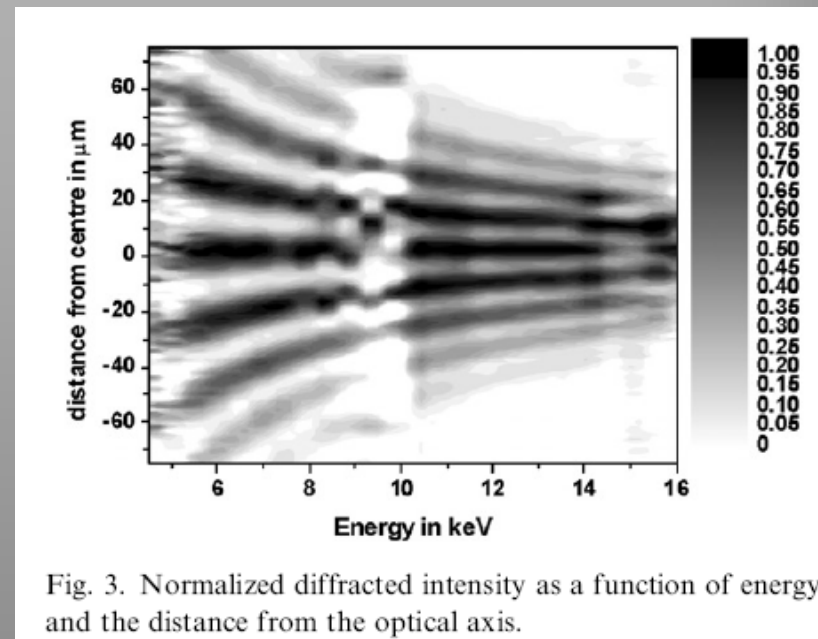
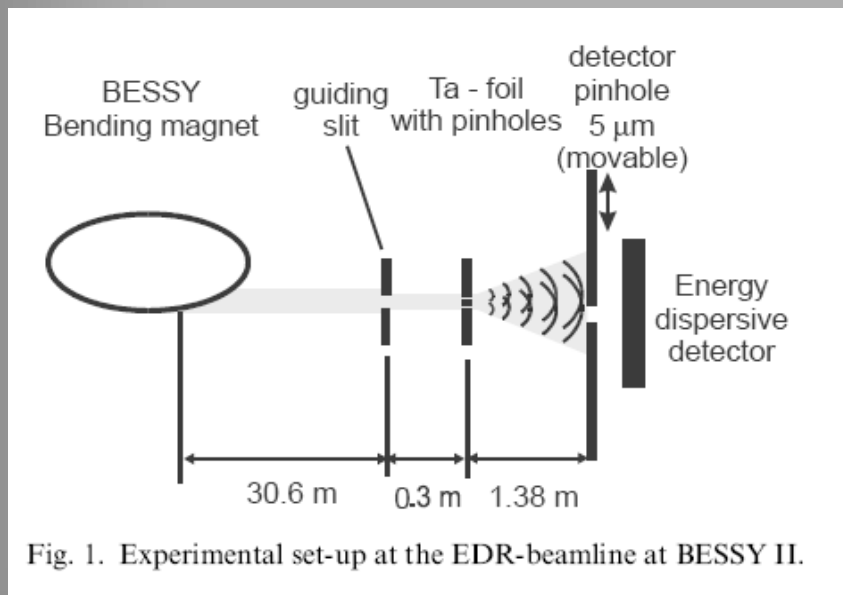
Для пучка размером  $10 \cdot 10$  микрон мы должны иметь расходимость  
Порядка  $10^{-5}$  радиана и монохроматичность порядка  $10^{-5}$



**Fig. 4** Two sample areas with equal average periodic lattice, equal defect densities, equal short and long-range order but different individual arrangement of the defects. The *upper part* shows the transverse coherence area  $A_T$  and two illuminated areas of different size



# Double pinhole diffraction of white synchrotron radiation



*W. Leitenberger et al. / Physica B 336 (2003) 63–67*

# Double pinhole diffraction of white synchrotron radiation

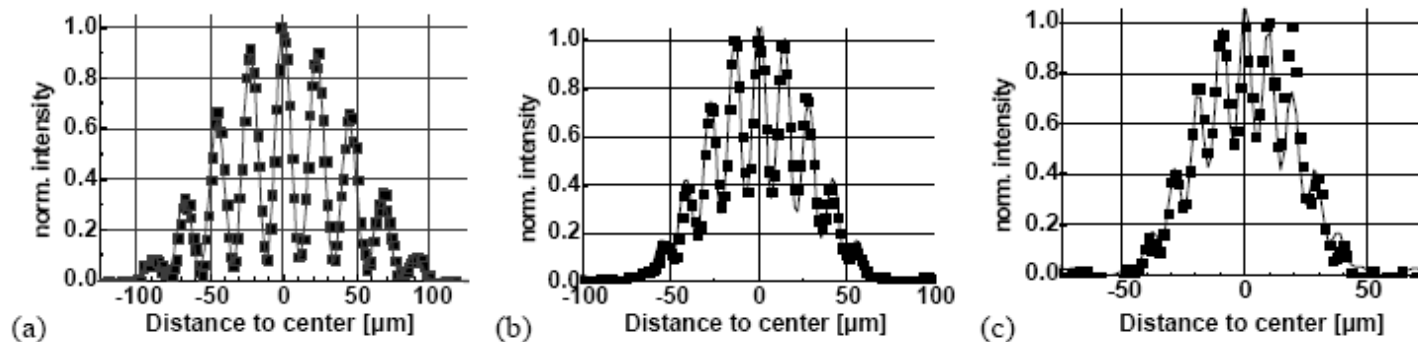
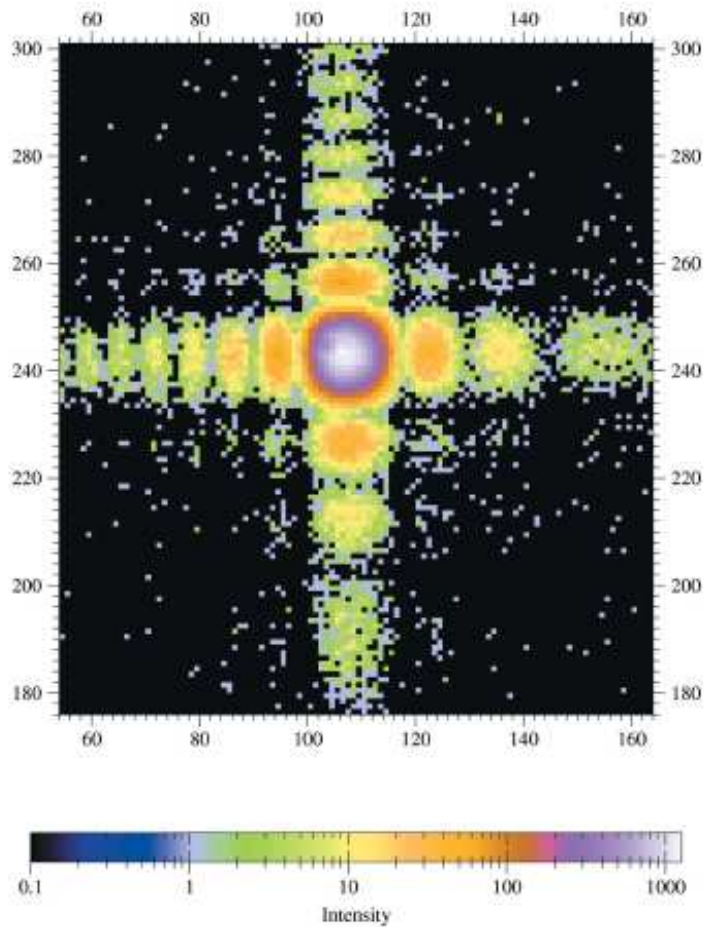
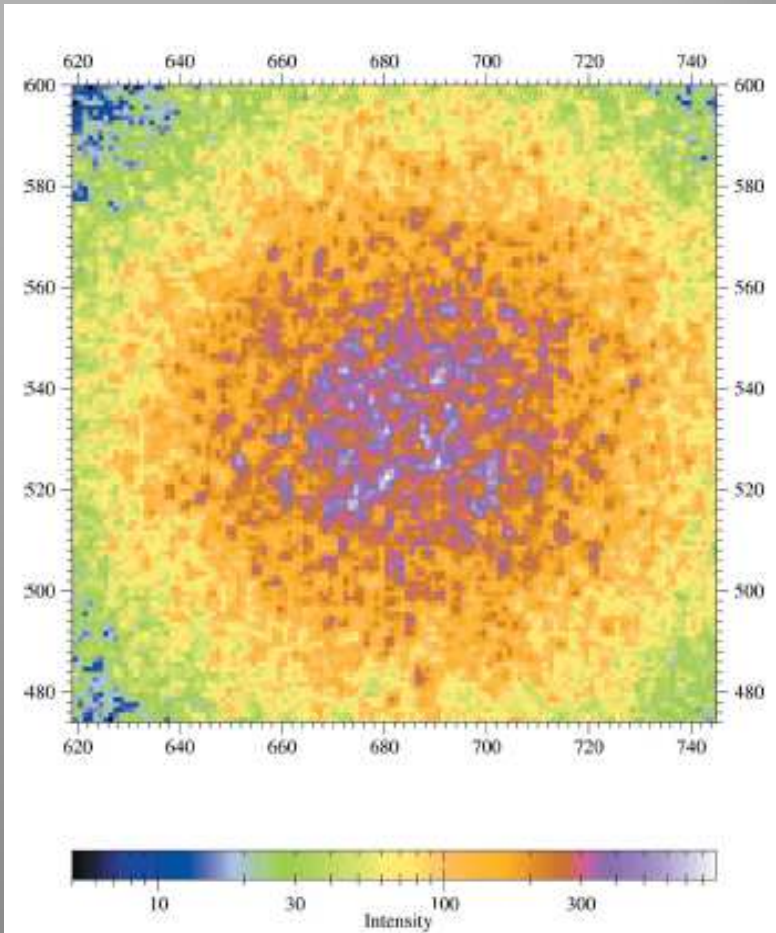


Fig. 4. Normalized interference fringes obtained with the double pinhole at three different energies (a)–(c) 6 keV, 10 keV and 14 keV. The squares indicate the measured data from Fig. 3 and the lines indicate the results of the best fit of Eq. (1).

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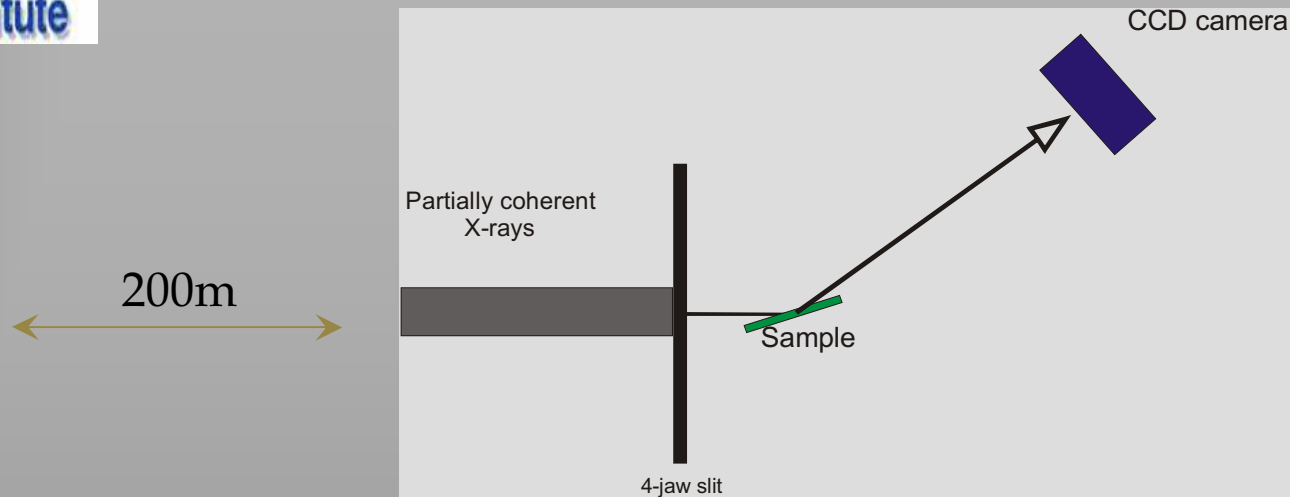


**Figure 8**  
Diffraction from 1  $\mu\text{m}$  asymmetric square slits,  $\lambda = 1.58 \text{ \AA}$ , detector with 22  $\mu\text{m}$  pixels at 1.25 m. Slit edges are 1 mm distant along the beam path (unpublished results from the BM2 beamline of ESRF).



**Figure 9**  
Diffraction from an ordered AuAgZn<sub>2</sub> alloy at the  $(\frac{111}{523})$  Bragg superstructure position.  $\lambda = 1.58 \text{ \AA}$ , 12  $\mu\text{m}^2$  slits, detector with 22  $\mu\text{m}$  pixels at 2 m (unpublished results from the ID10 beamline of ESRF).

# Coherent X-ray scattering

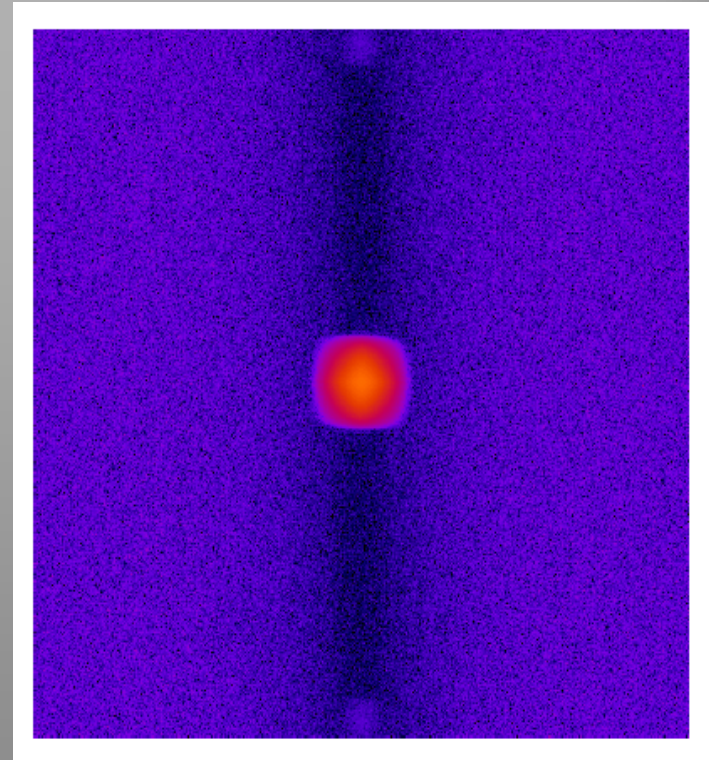
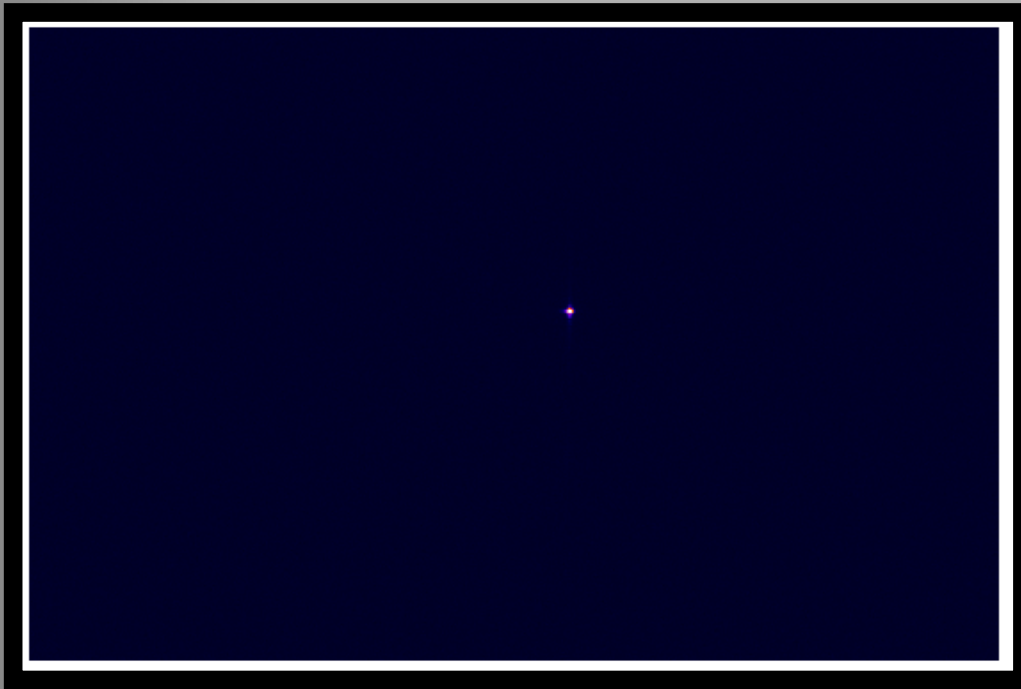


$$\gamma(x) = \frac{\int_{-\infty}^{\infty} \mathcal{T}^*(x' + x) \mathcal{T}(x') dx'}{\int_{-\infty}^{\infty} \mathcal{T}^*(x') \mathcal{T}(x') dx'}$$

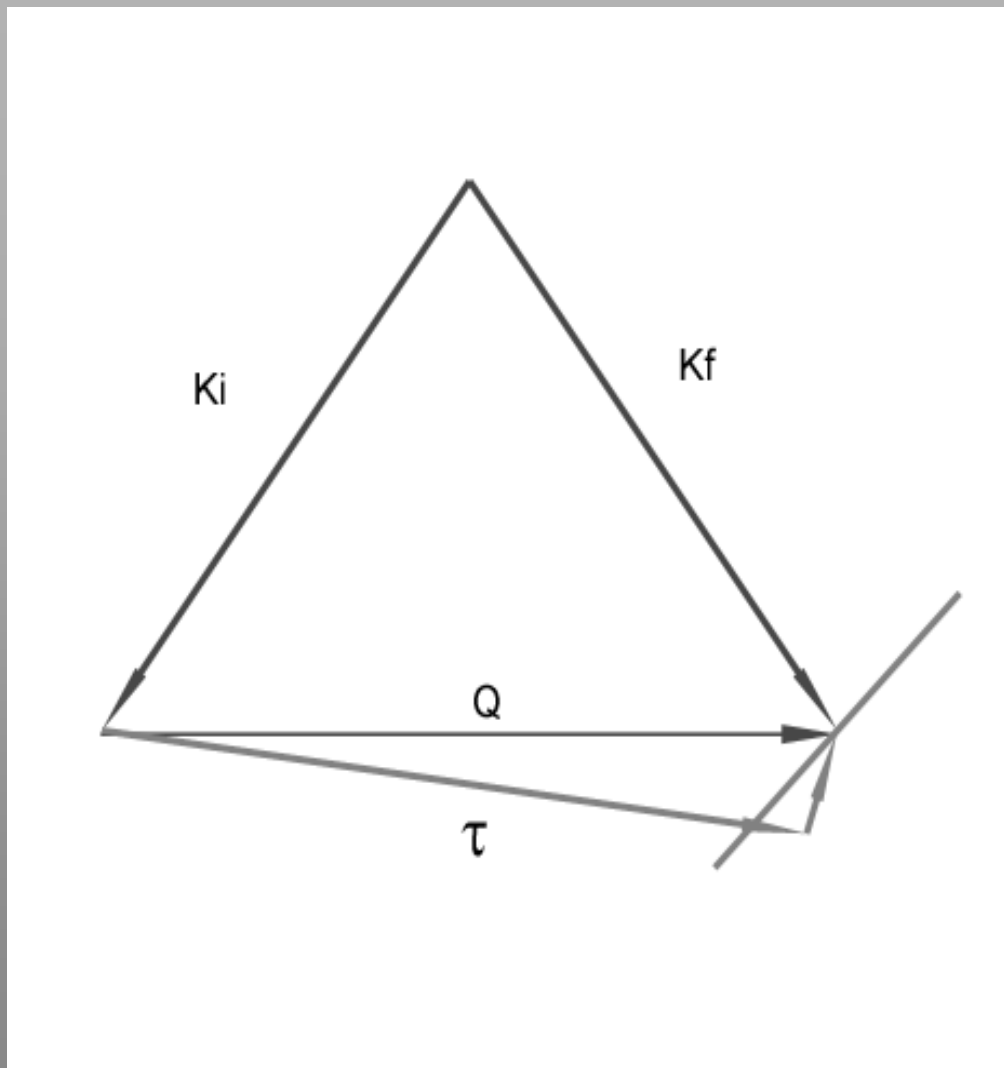
**Simplified** (Following R.Z.Tai et al., PRL 89,257602 (2002))

$$\gamma(x) = \mathbf{F}(I(q)) / \mathbf{F}(I_{sp}(q))$$

# Diffraction image from perfect crystal and its FFT

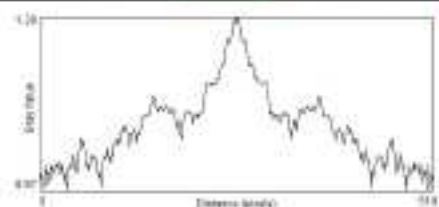
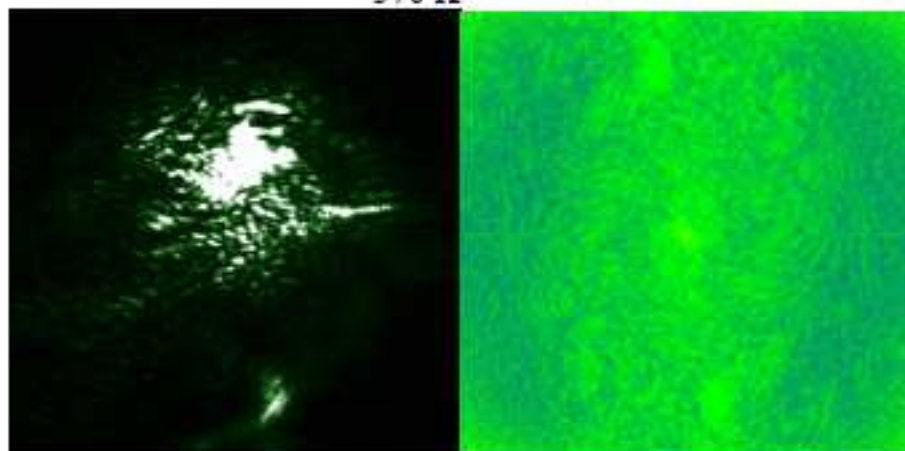


# Геометрия рассеяния

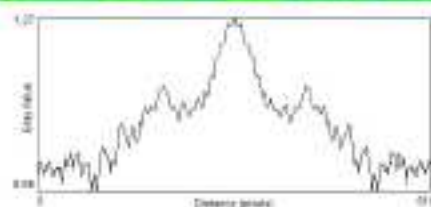




Бреговское рассеяние  
370 К

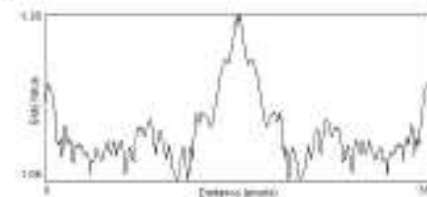
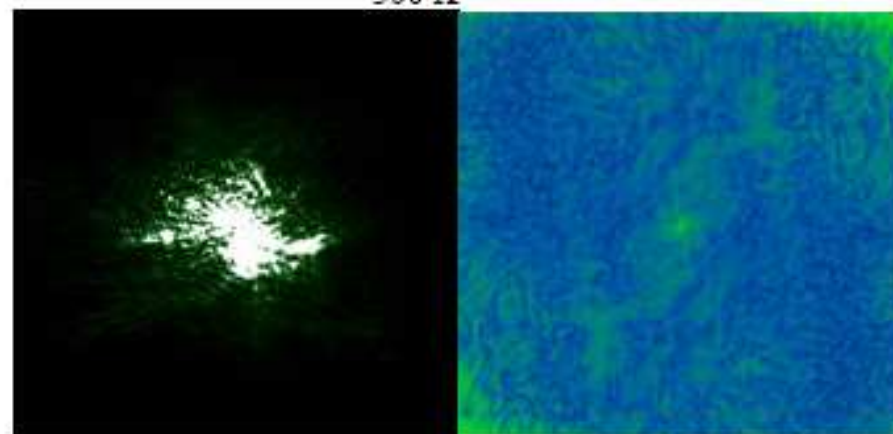


0°

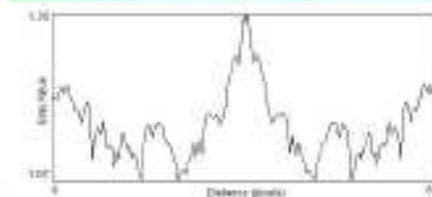


-15°

Бреговское рассеяние  
300 К



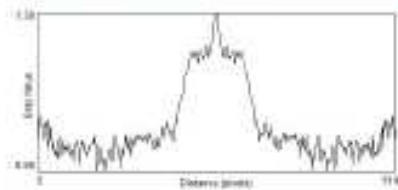
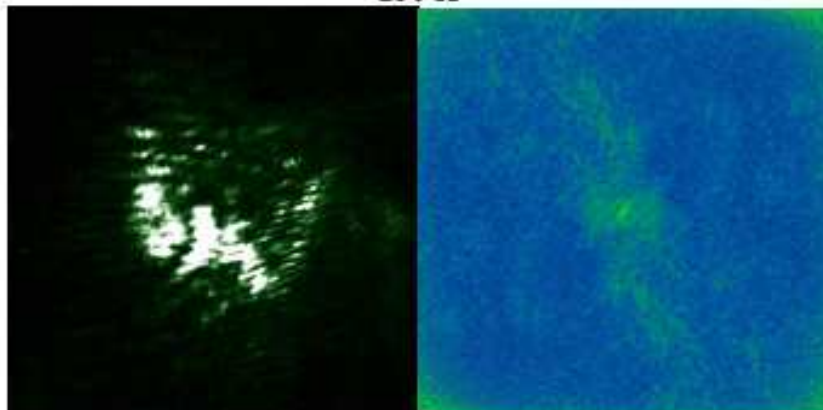
0°



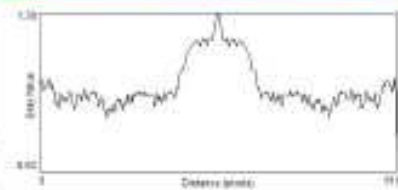
10°



Бреговское рассеяние  
250 К

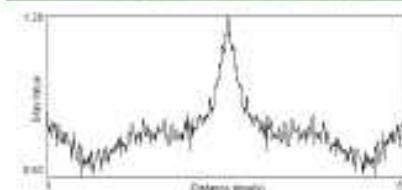
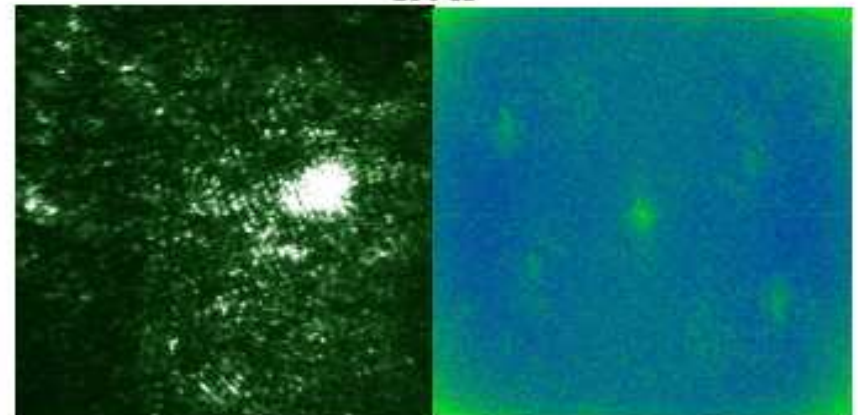


0°

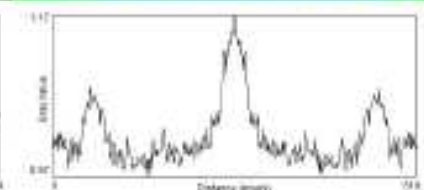


5°

Бреговское рассеяние  
230 К



0°

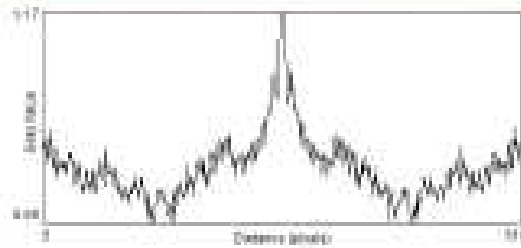
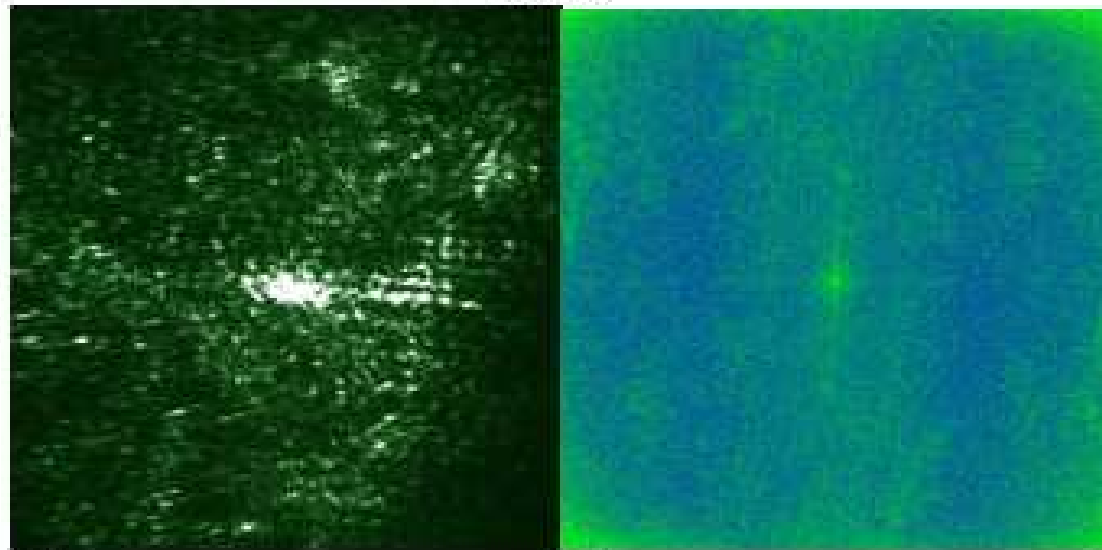


-35°

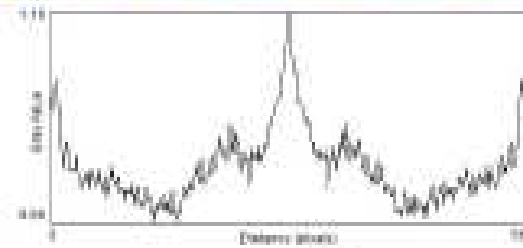




Бреговское рассеяние  
200 К



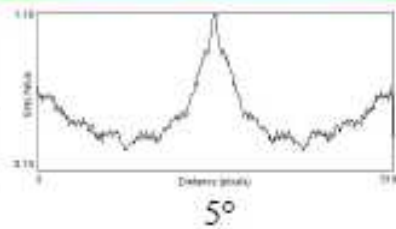
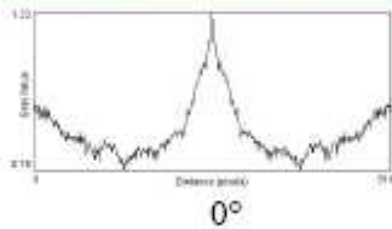
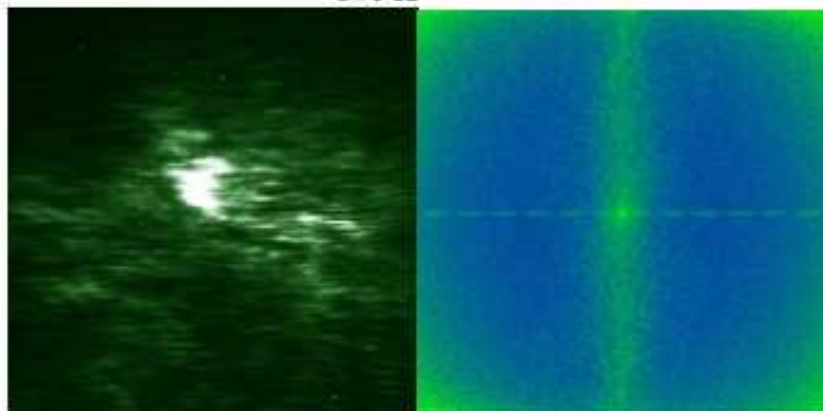
0°



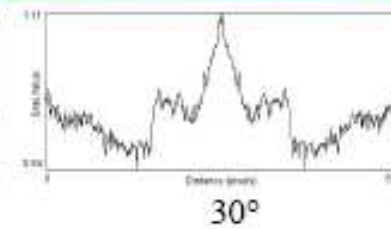
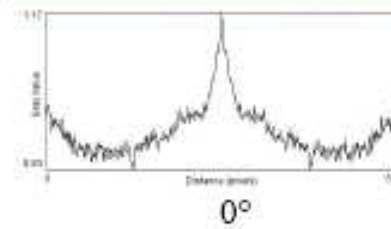
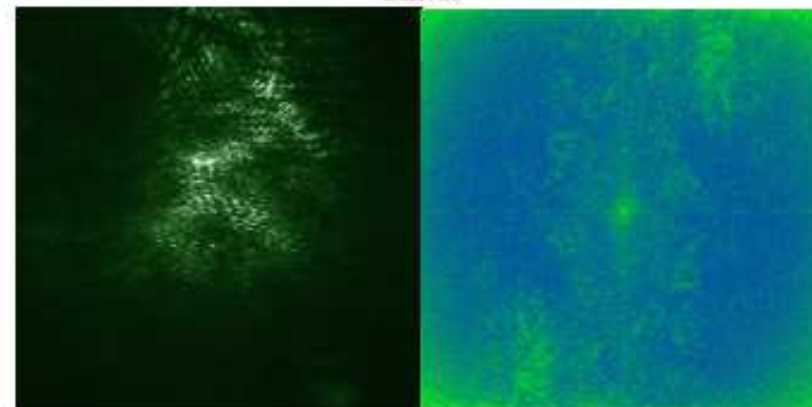
-10°



Диффузное рассеяние  
370 К

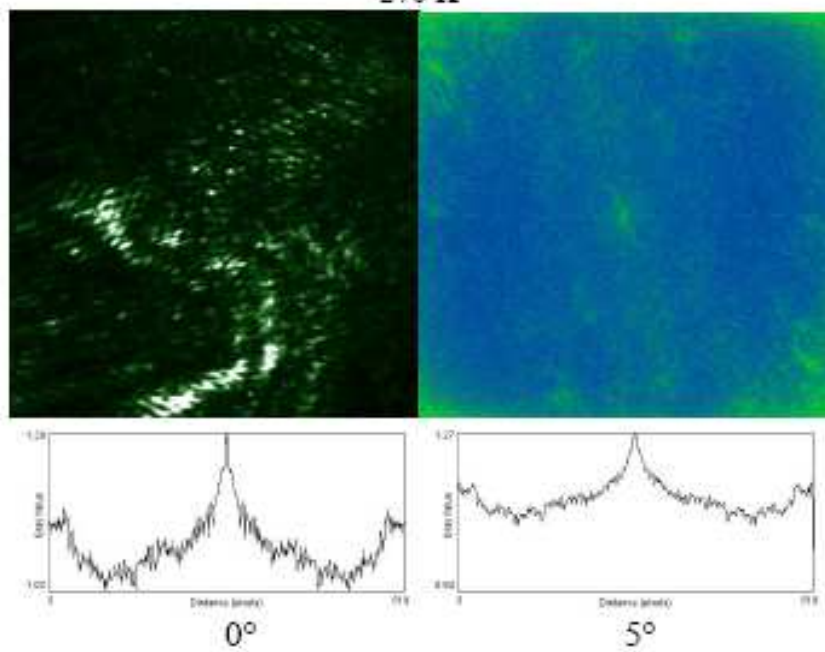


Диффузное рассеяние  
320 К

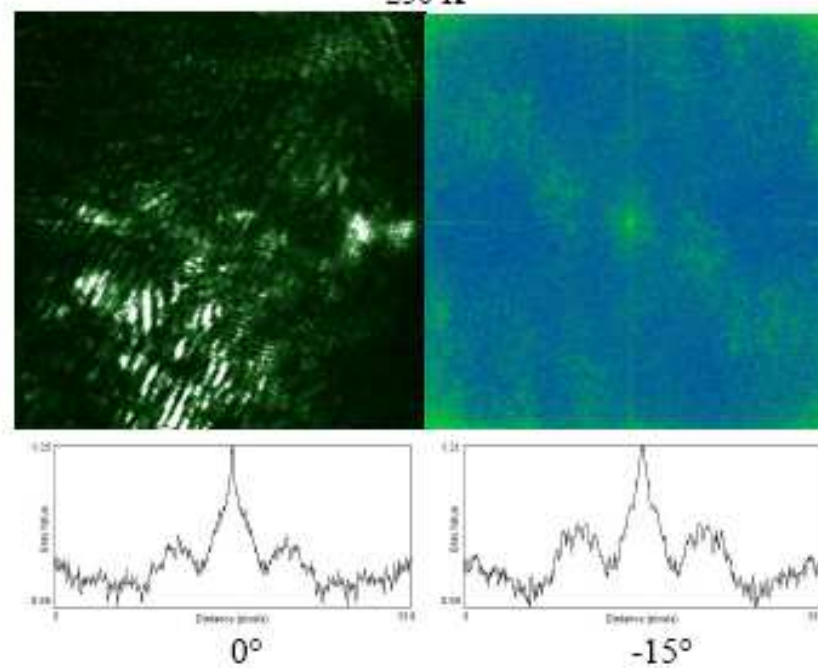




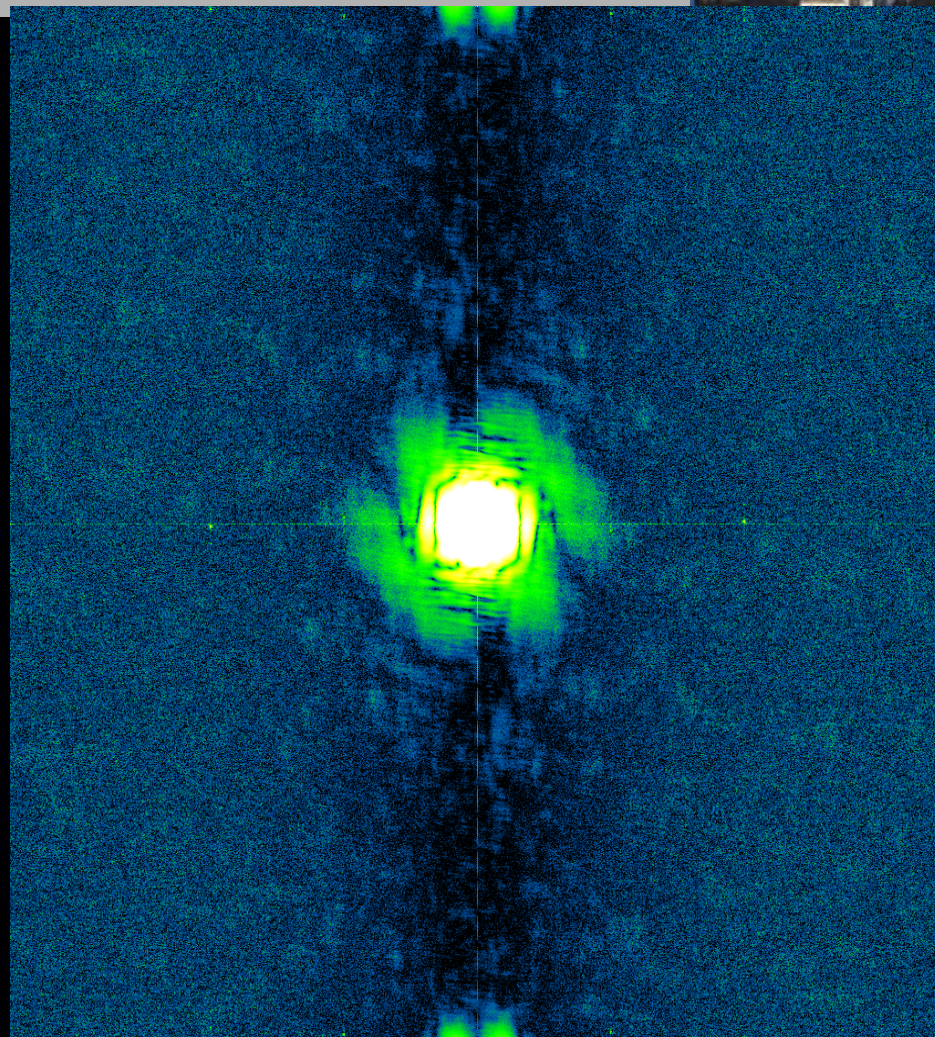
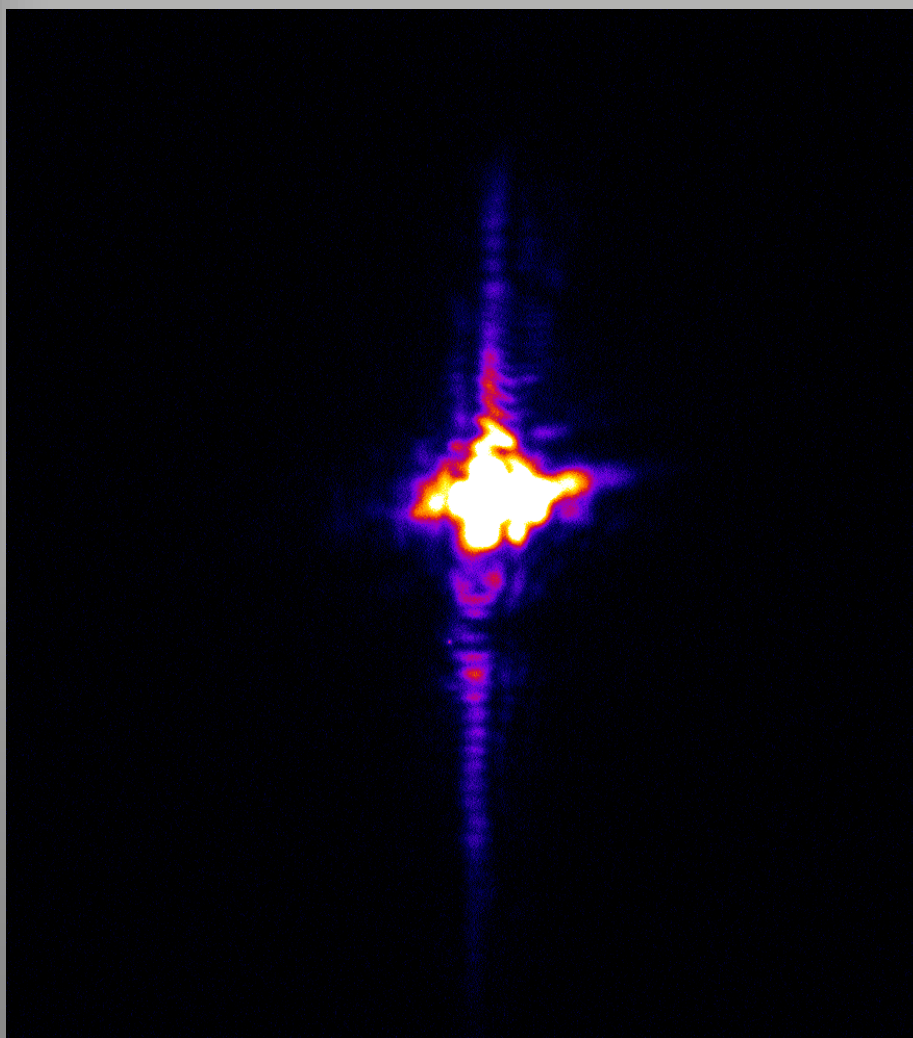
Диффузное рассеяние  
270 К



Диффузное рассеяние  
250 К



# SBN61 480K брэгговский пик

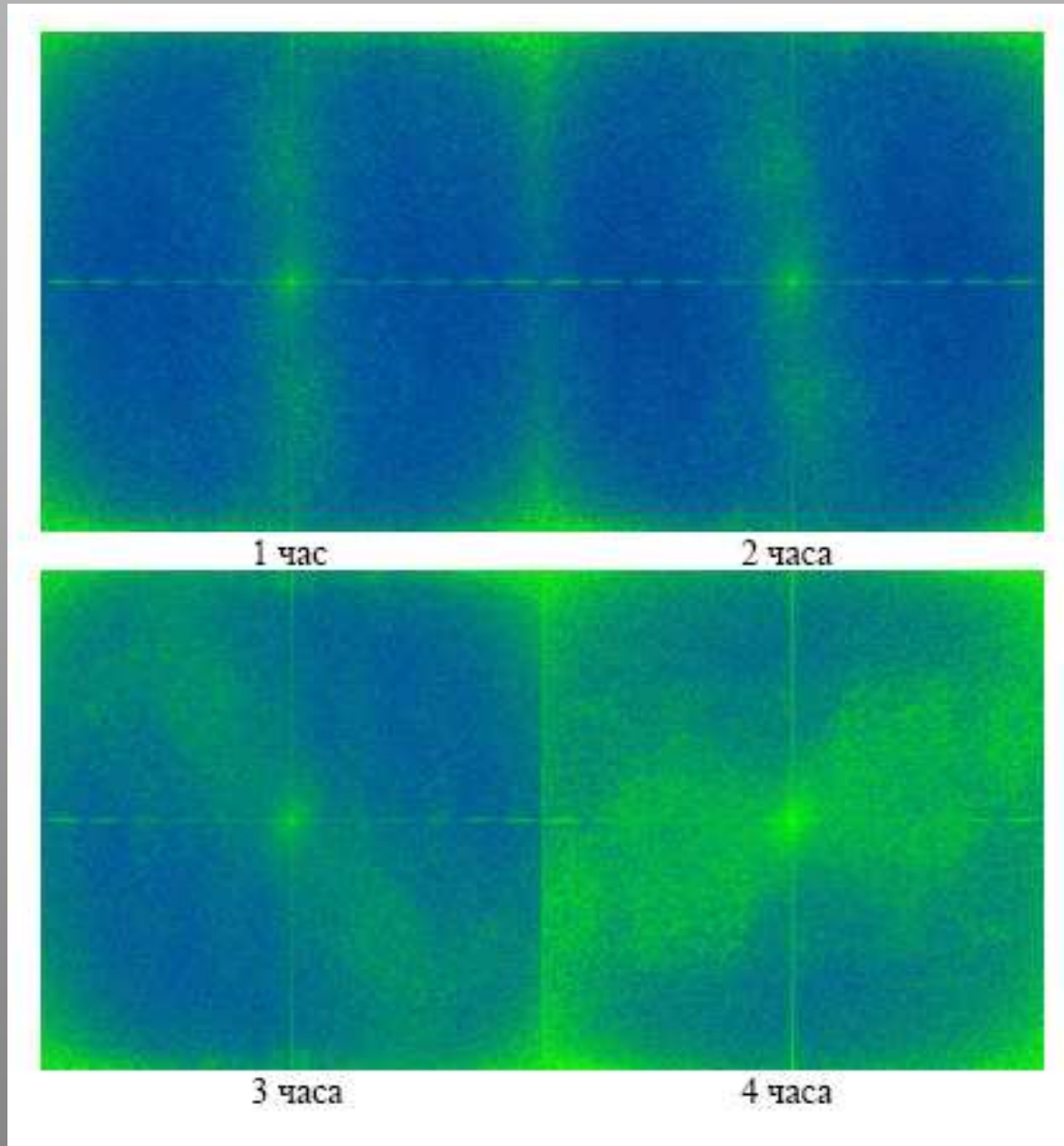


Дифракция на щели в вертикальном  
направлении  
16.03.2009

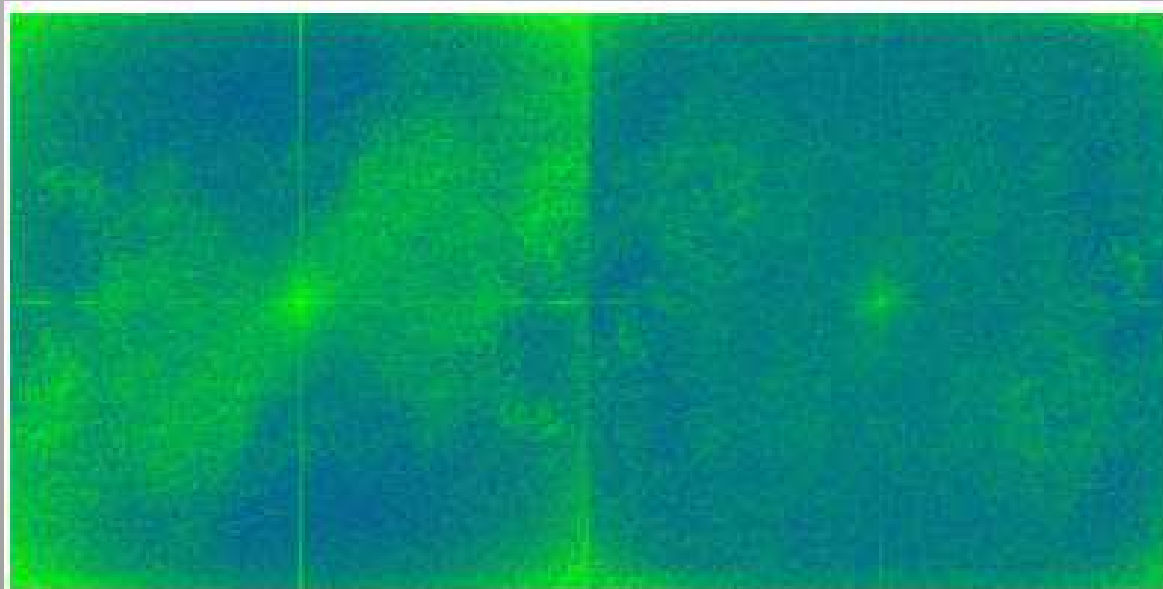
ШКОЛА ПИЯФ

Фурье образ

# 230 K diffuse

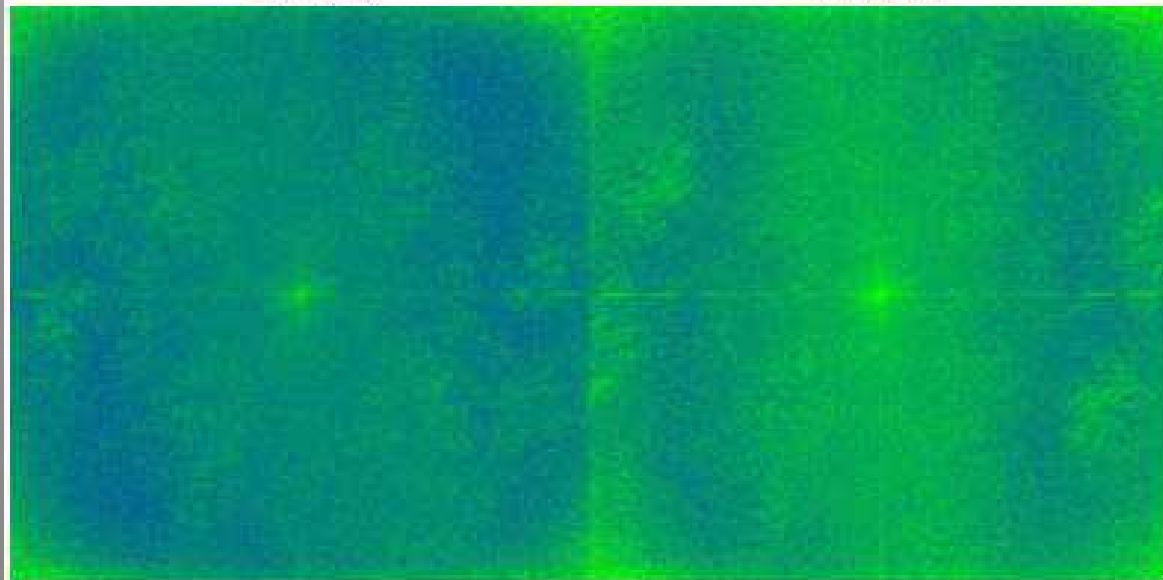


# 230K diffuse



5 часов

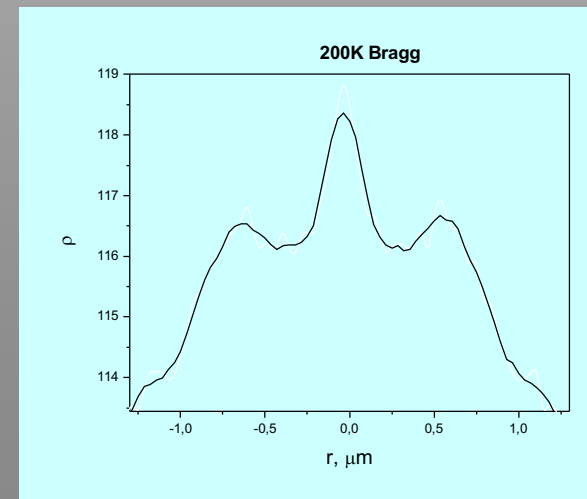
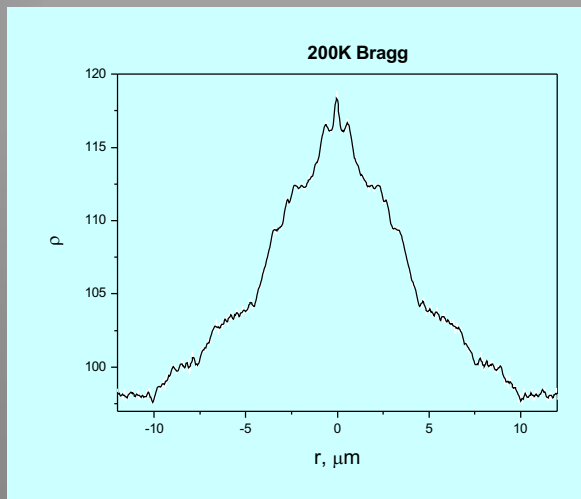
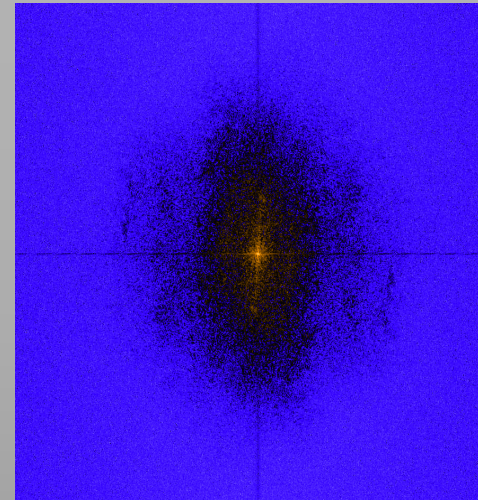
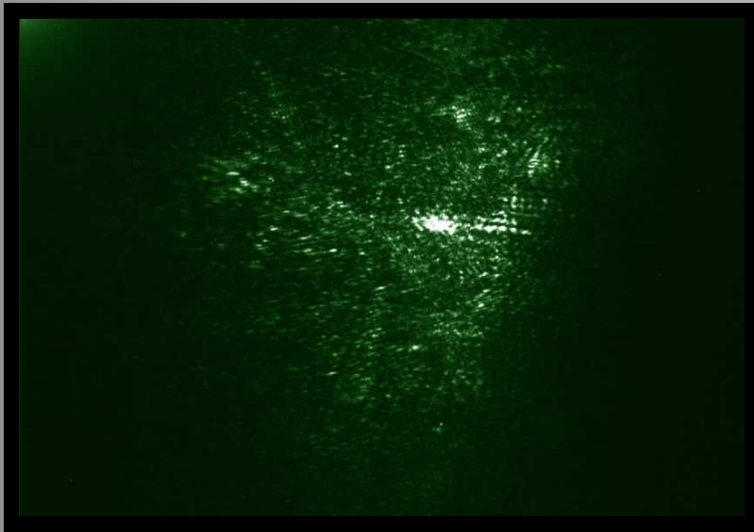
6 часов



7 часов

8 часов

# Bragg diffraction image 200K





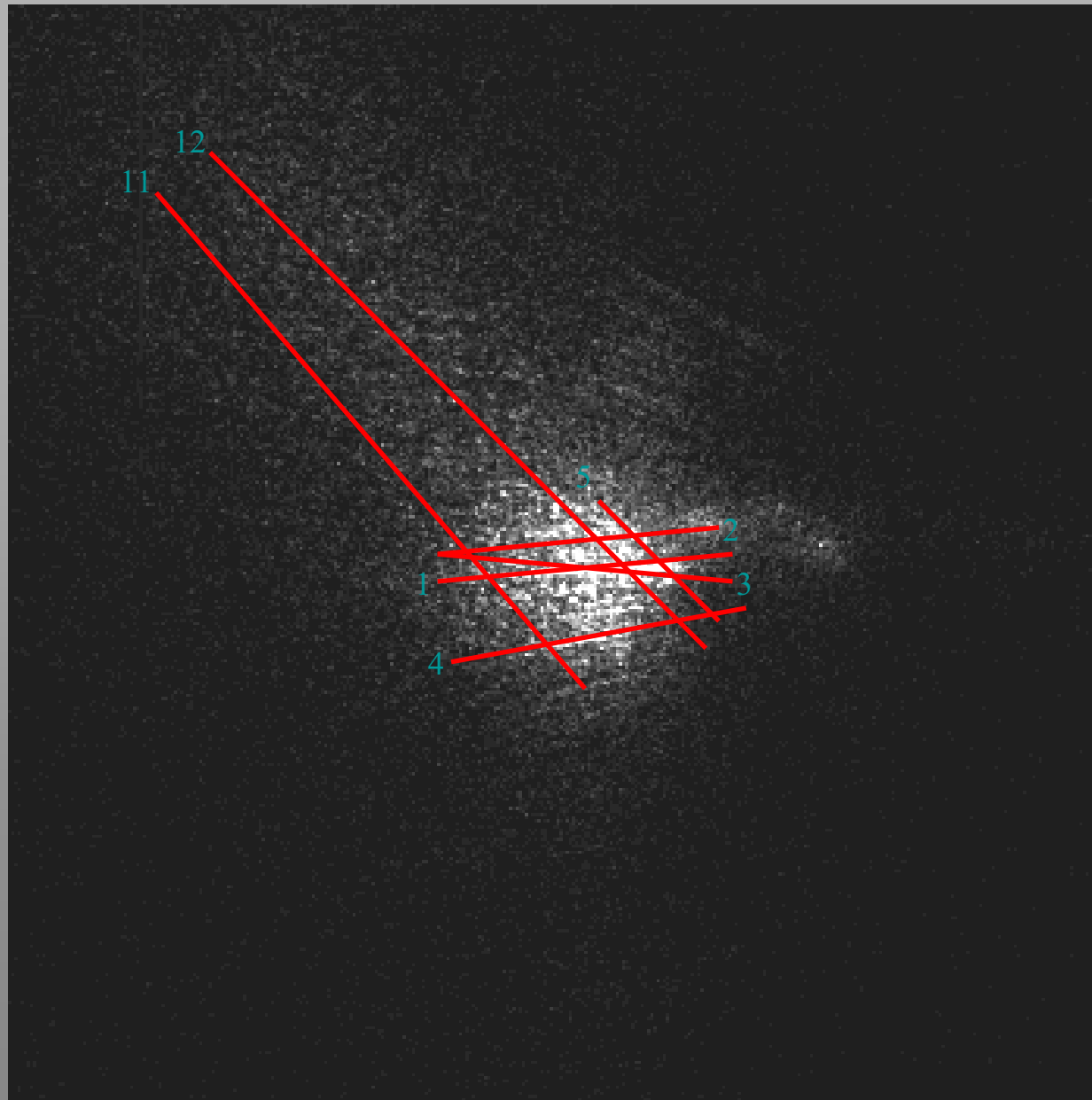
# ХРПС

## Рентгеновская фотонная корреляционная спектроскопия

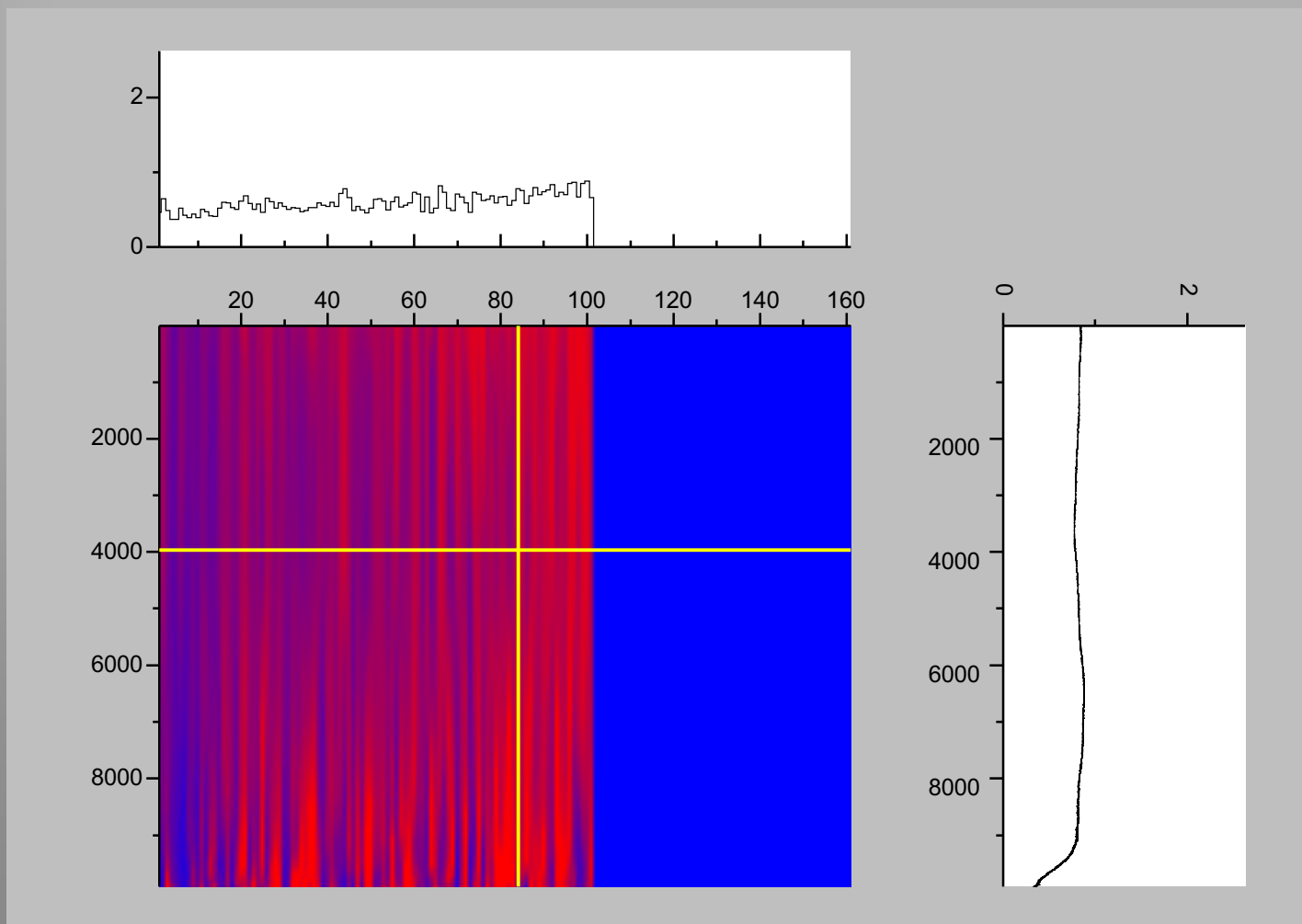
$$1 + \beta(q)g^{(2)}(q, t) = \langle \langle I(\mathbf{q}, t)I(\mathbf{q}, t + t') \rangle \rangle_{\mathbf{q}} / \langle \langle I(\mathbf{q}, t) \rangle \rangle_{\mathbf{q}}^2,$$



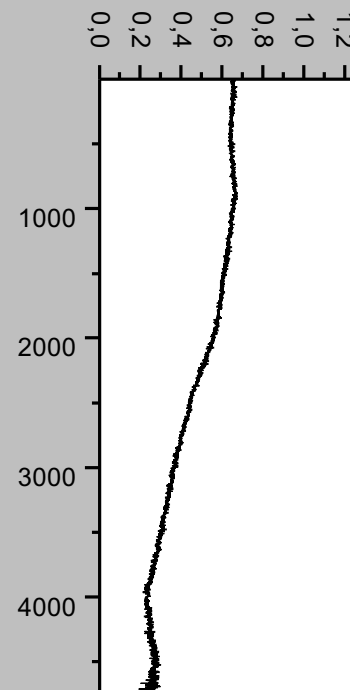
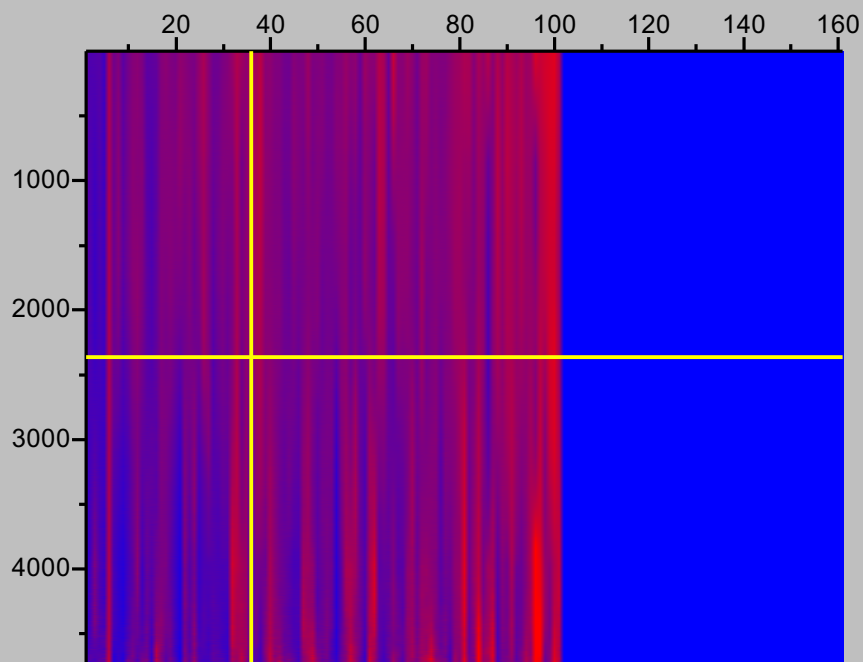
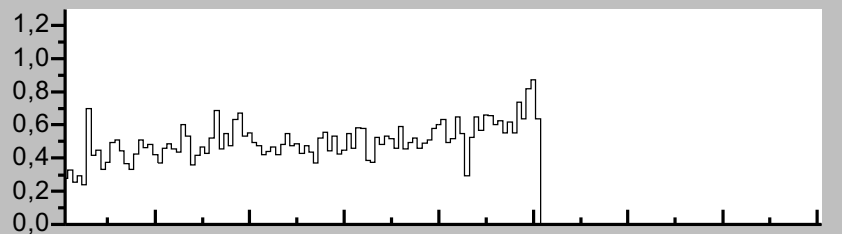
# Slices position



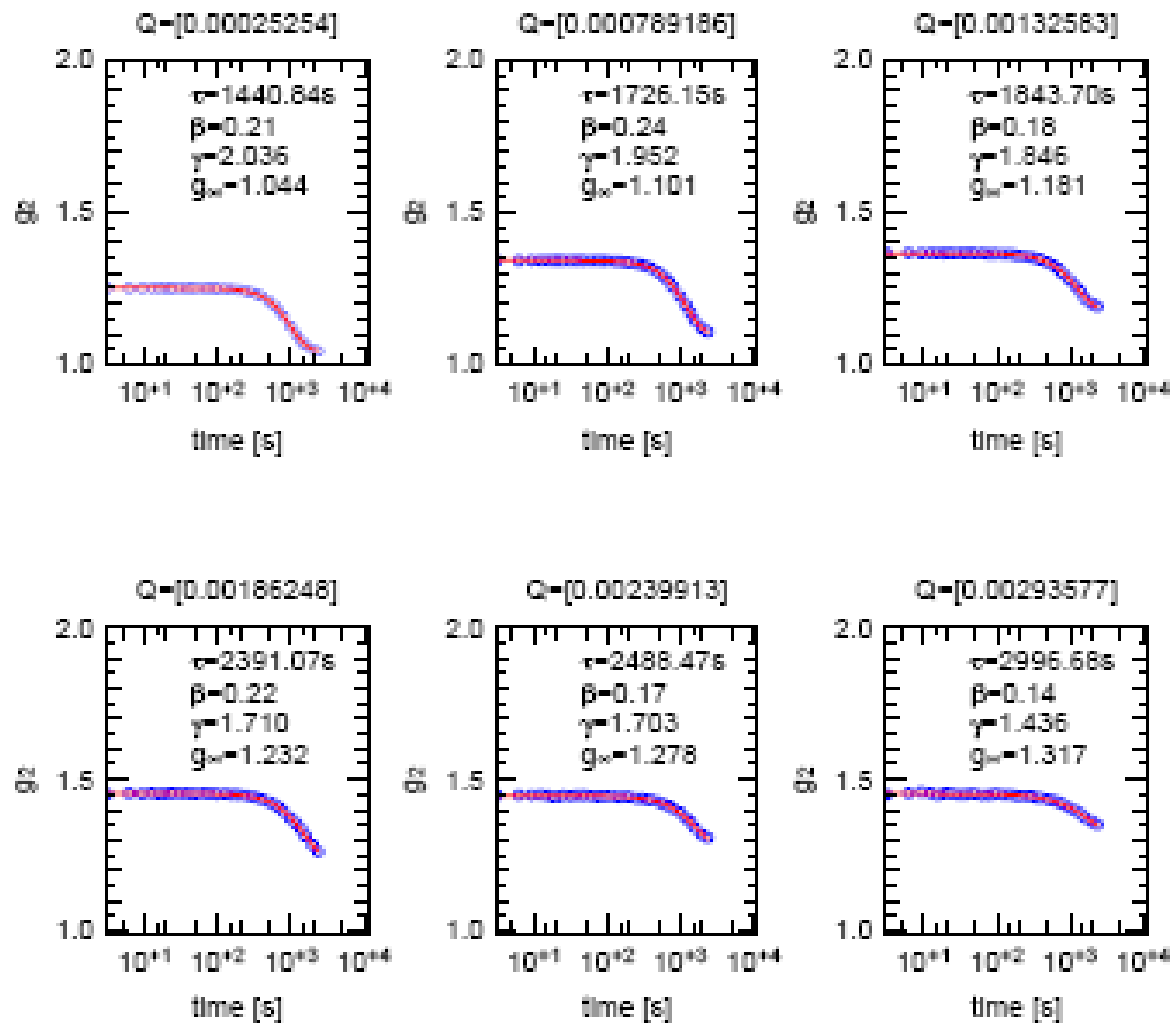
# 360K



# 340K



# PMNPT10 XPCS 210K





# Вода

# Нейтроны - диффузия

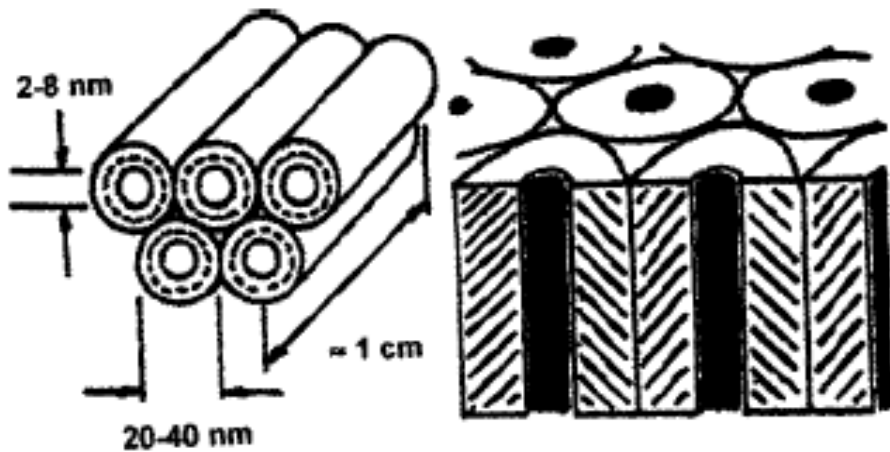


FIG. 1. A schematic picture of a bundle of chrysotile asbestos fibers.

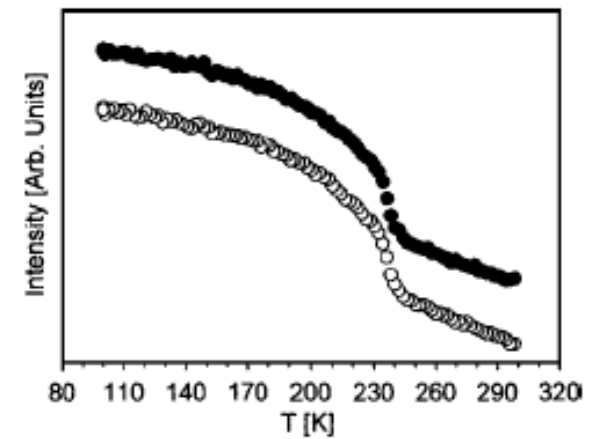


FIG. 2. The elastic scattering intensity measured in the fixed-window mode as a function of temperature and summed up over all  $Q$  values. Open circles: “ $Q$ -parallel” orientation. Filled circles: “ $Q$ -perpendicular” orientation. An arbitrary vertical offset of the baselines is applied for clarity. The increase in the elastic scattering at about  $T=237$  K is due to the freezing of water in the fibers.

# Замедление динамики больше чем на порядок

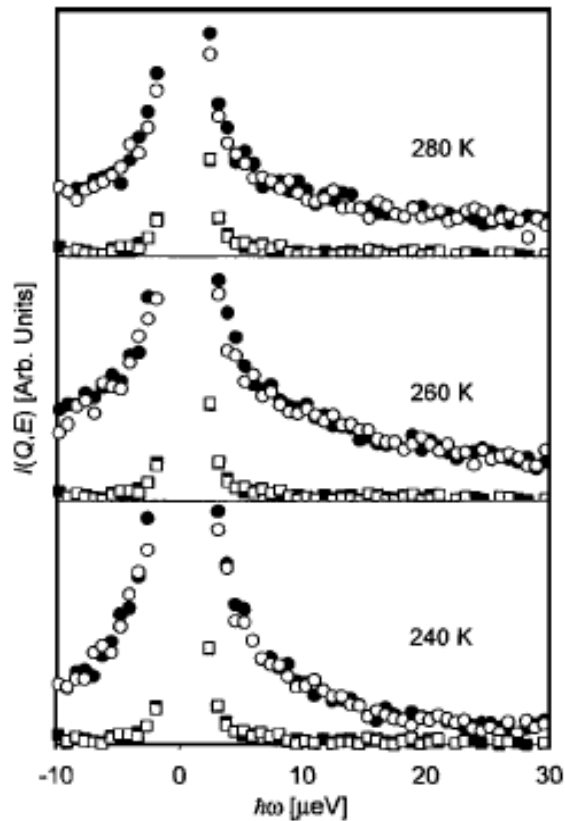


FIG. 3. The scattering intensities measured in the energy space at the  $90^\circ$  detector ( $Q=1.42 \text{ \AA}^{-1}$ ). The elastic peaks at zero energy transfer are truncated to better demonstrate the quasielastic signal. The 100 K data used as a resolution function are plotted on every graph and shown with squares. Open symbols: “ $Q$ -parallel” orientation. Filled symbols: “ $Q$ -perpendicular” orientation.

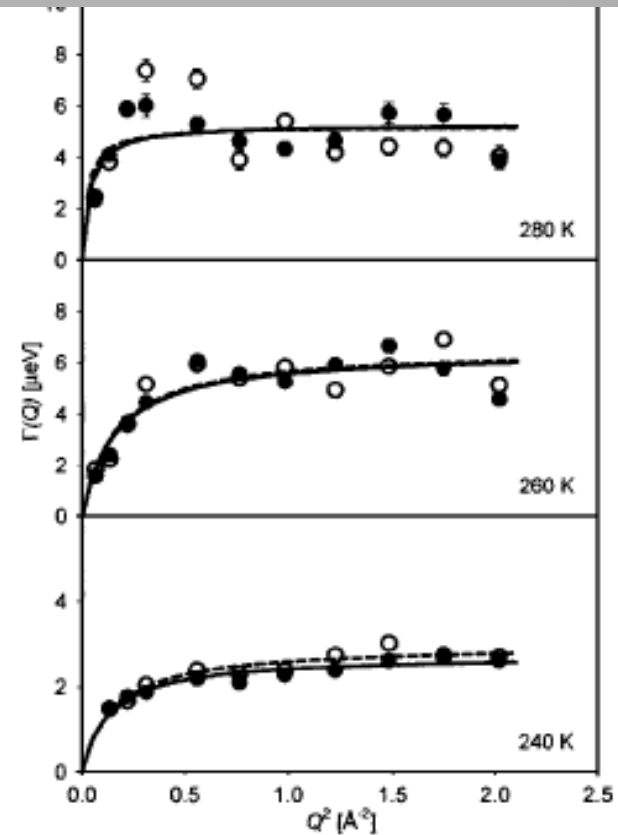
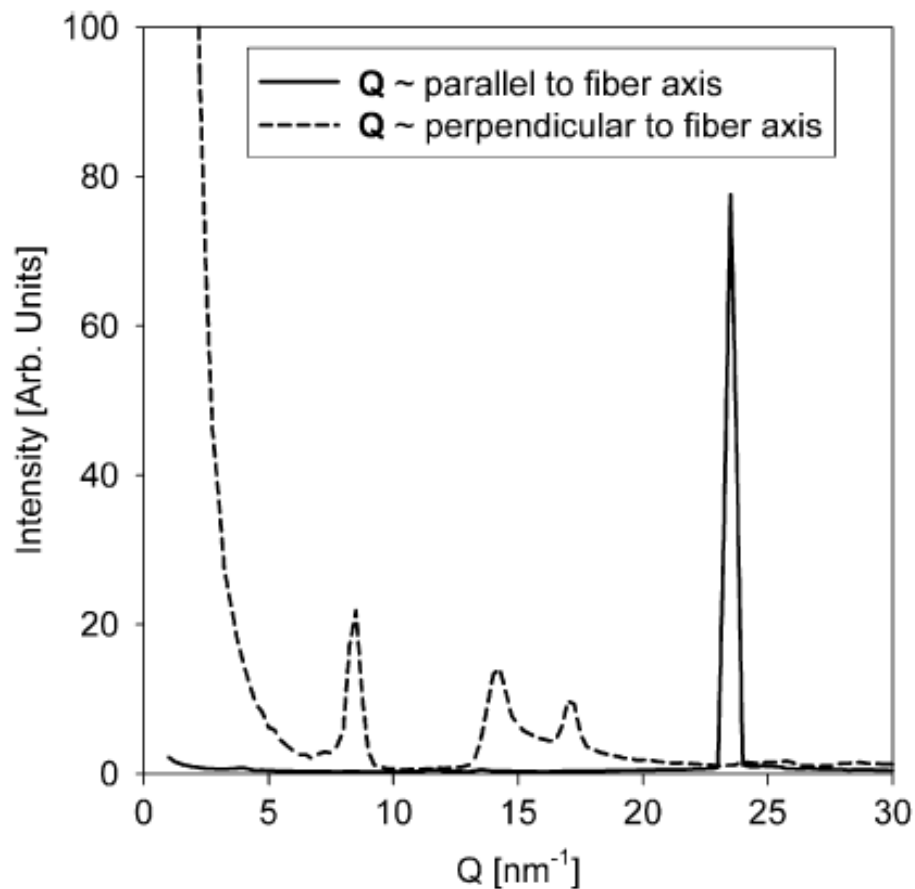


FIG. 4. The  $Q$  dependence of the parameter  $\Gamma(Q)$  obtained from fitting the data using Eqs. (1) and (2) and its fit with Eq. (3). Open circle data points and dashed line fitting curves: “ $Q$ -parallel” orientation. Filled circle data points and solid line fitting curves: “ $Q$ -perpendicular” orientation.

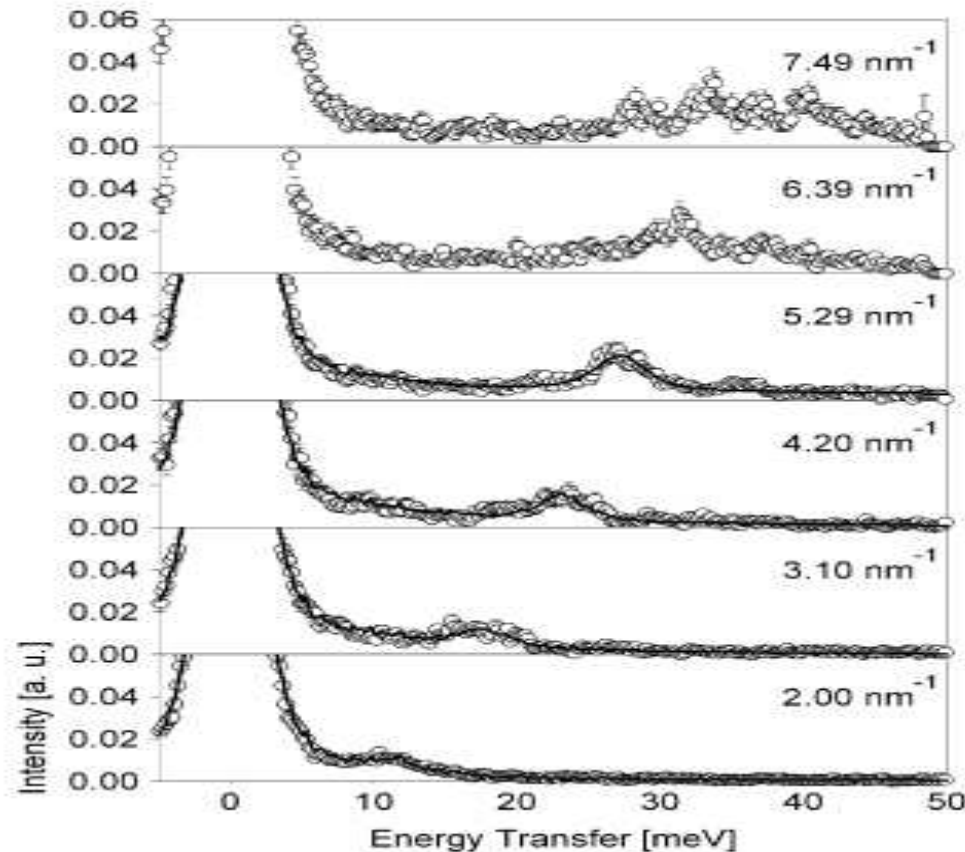
# Дифракция СИ в асбесте



**Fig. 2.** Diffraction patterns measured with the scattering vector aligned nearly parallel and perpendicular to the long axis of the chrysotile asbestos fiber.



# Неупругое рассеяние СИ

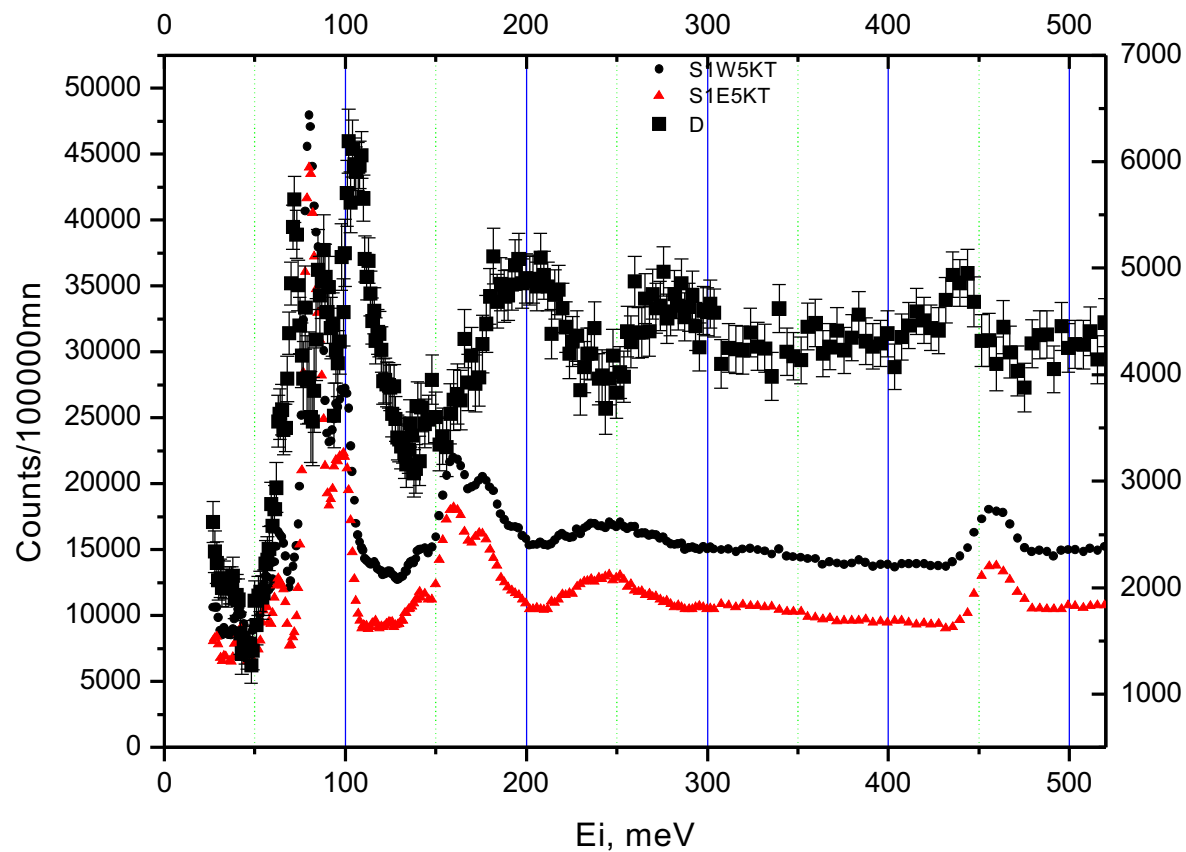


**Fig. 3.** Symbols: Inelastic x-ray scattering spectra measured with the scattering vector aligned along [1 0 0] direction of the reciprocal lattice (that is, nearly parallel to the long axis of the chrysotile asbestos fiber, which coincides with [1 0 0] direction of the direct lattice). Lines: Fits with Eqs. (1) and (2) (for the four lowest  $Q$  values). The spectra are normalized to have the same height of the elastic peak at all  $Q$  values.

# IN1 вода в асбесте

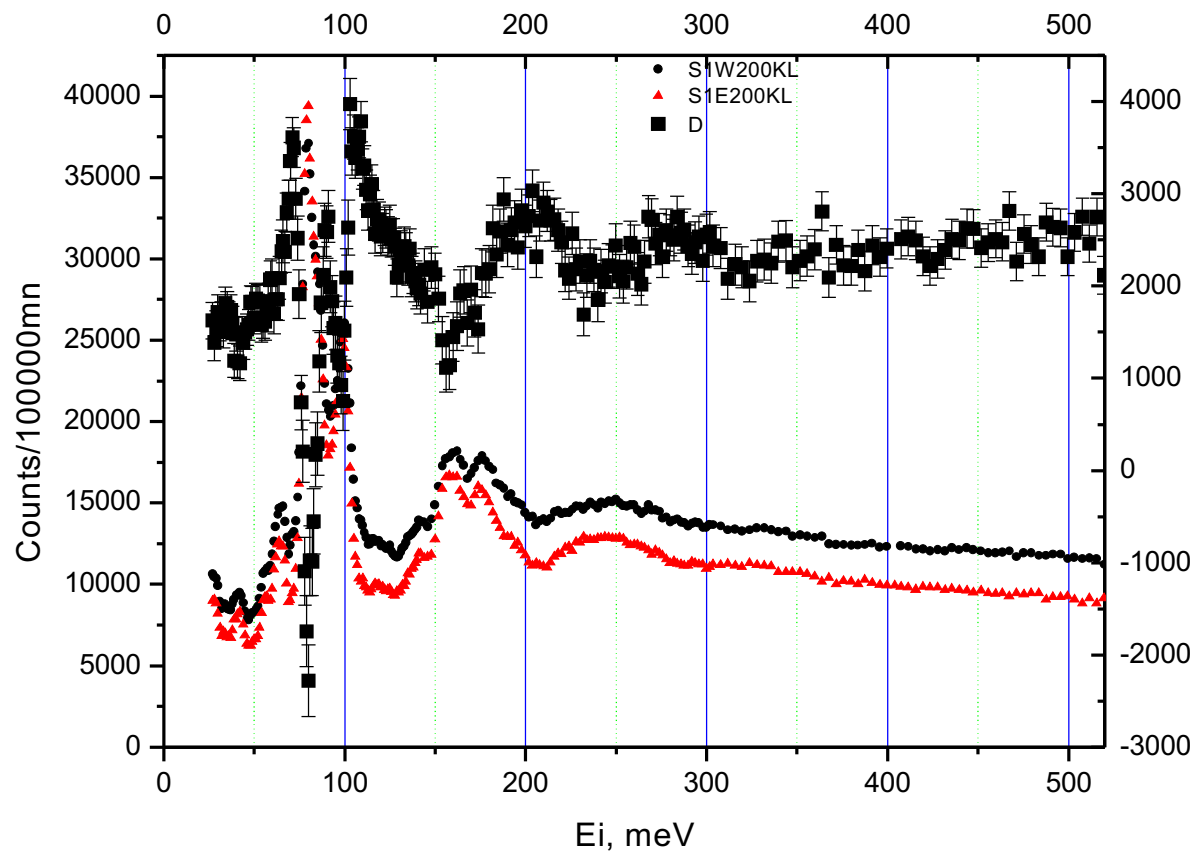


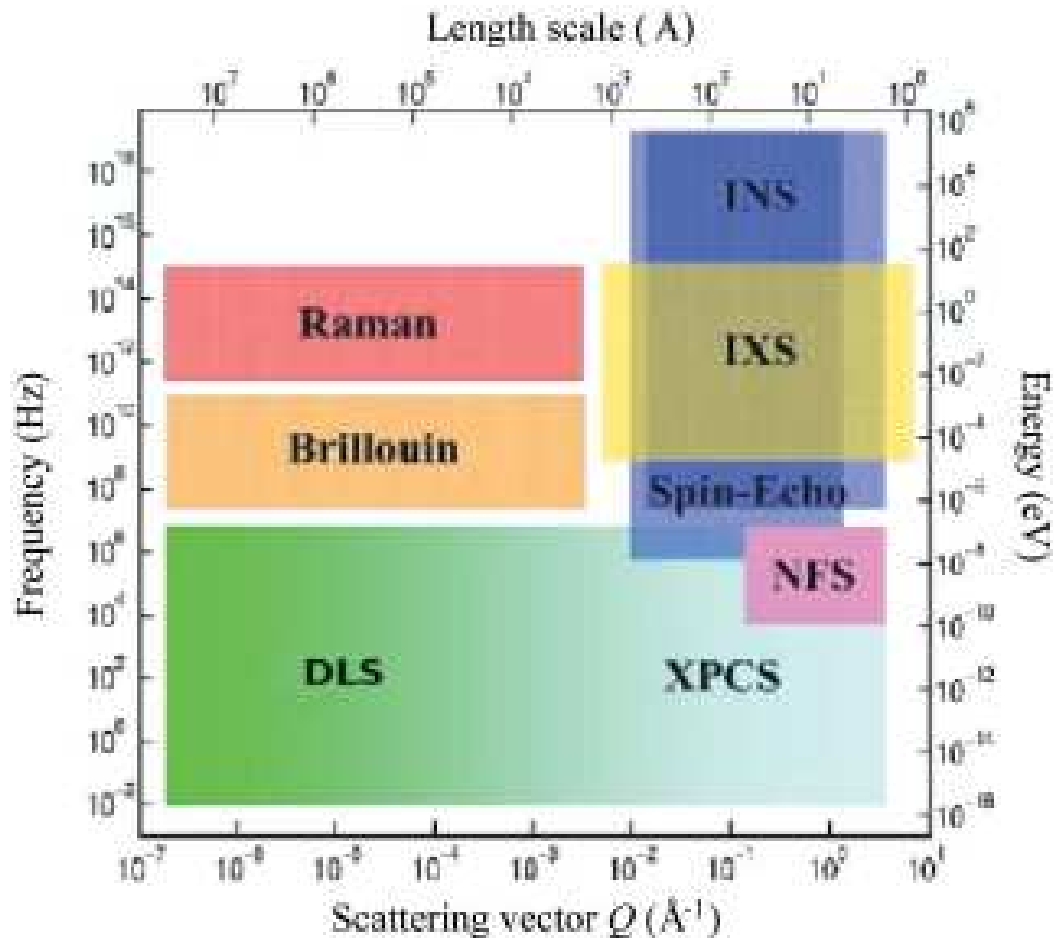
S#1 5K  $\alpha_3=98$  (perp Ki) Cu220





### S#1 200K $a_3=8$ (along Ki) Cu220





**Figure 1**

The frequency-scattering vector domains of available techniques for dynamic studies [adapted from Grübel & Zontone (2004)]. The XPCS domain can be extended down to  $q \simeq 3 \times 10^{-4} \text{\AA}^{-1}$  and  $\nu \simeq 10^{-4} \text{ Hz}$ , overlapping with DLS. The other techniques are inelastic neutron scattering (INS), inelastic X-ray scattering (IXS) and nuclear forward scattering (NFS).

