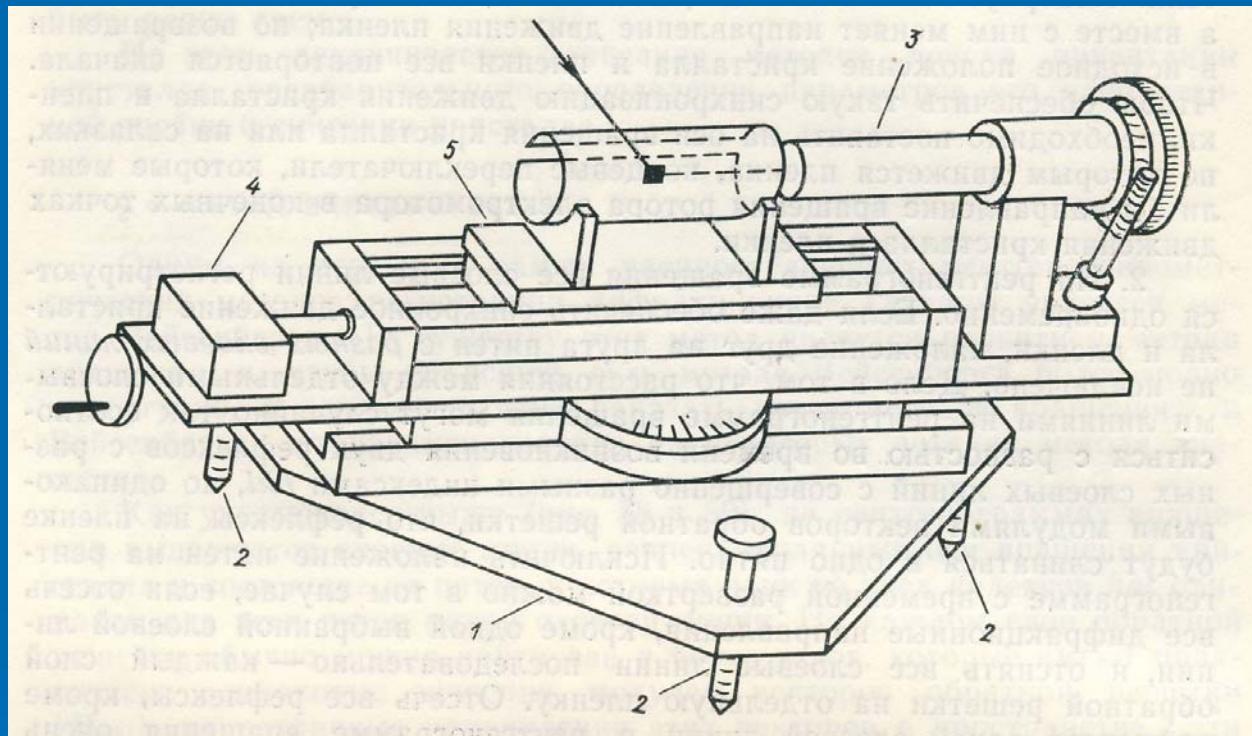
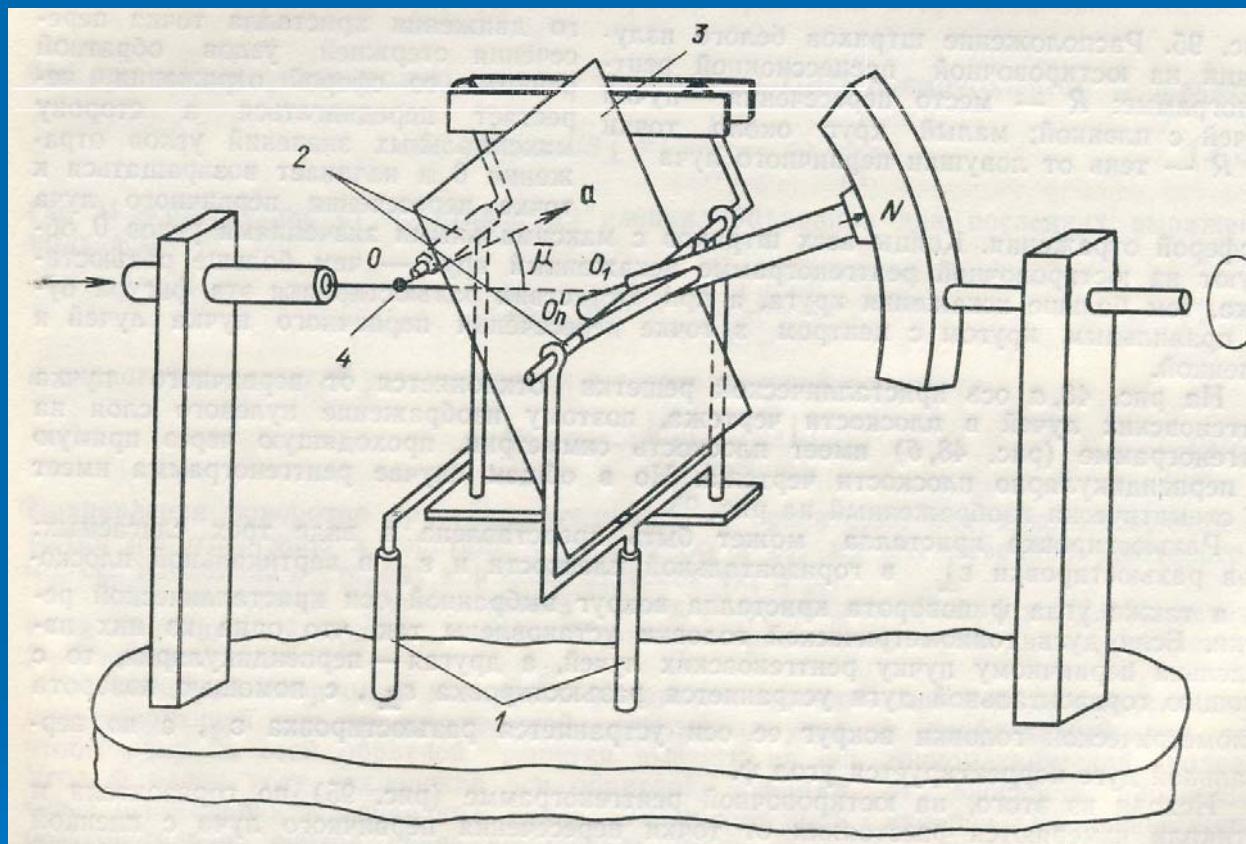
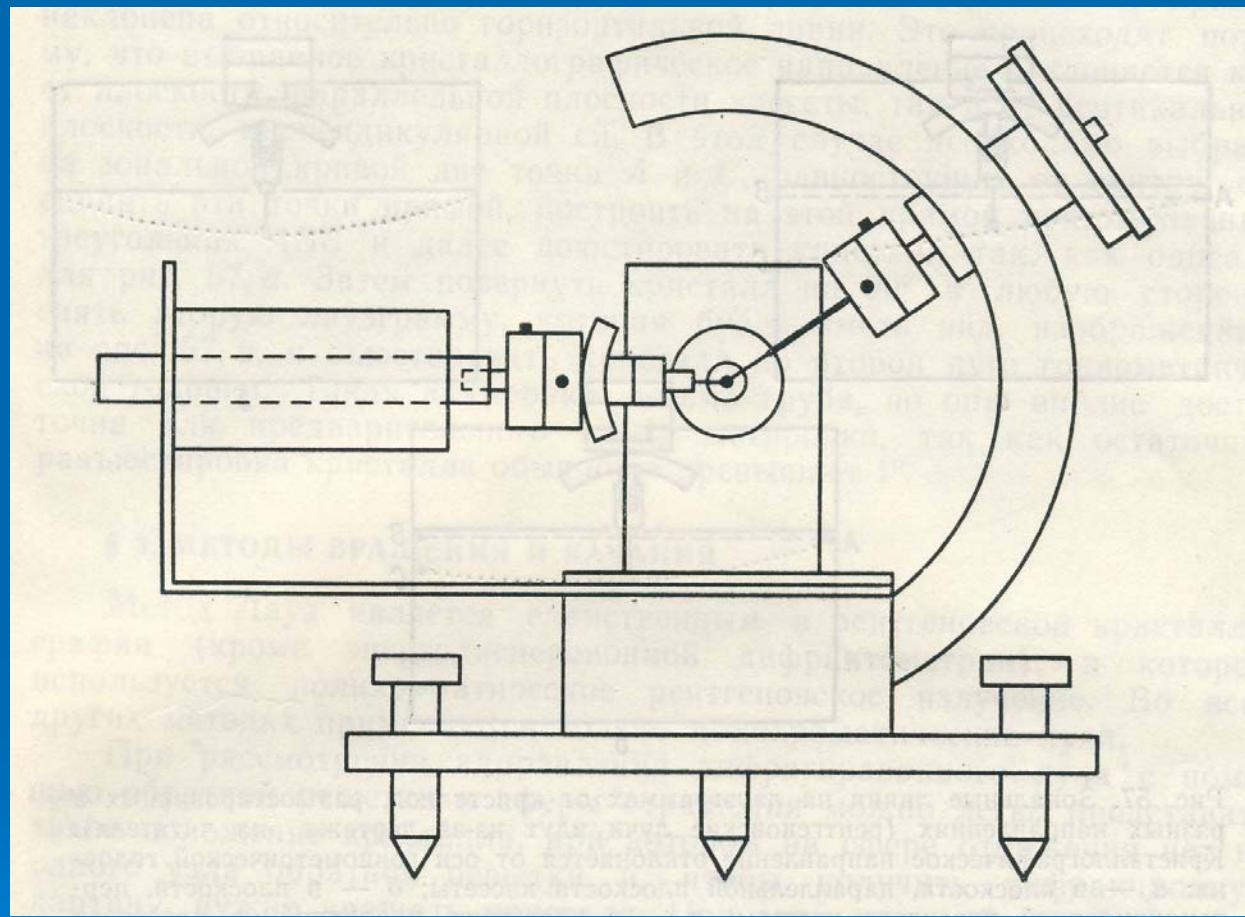


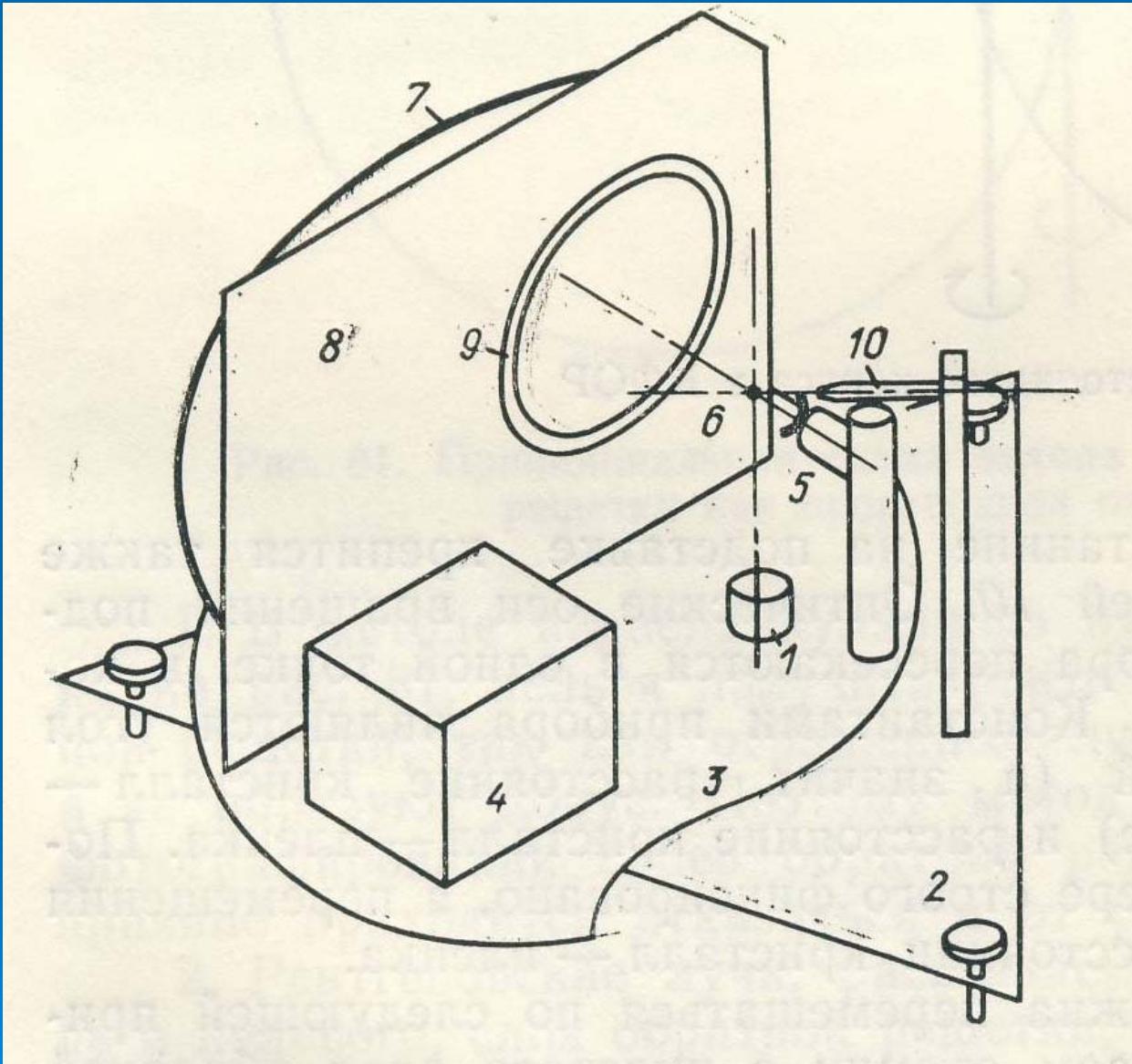
Л.А.Асланов

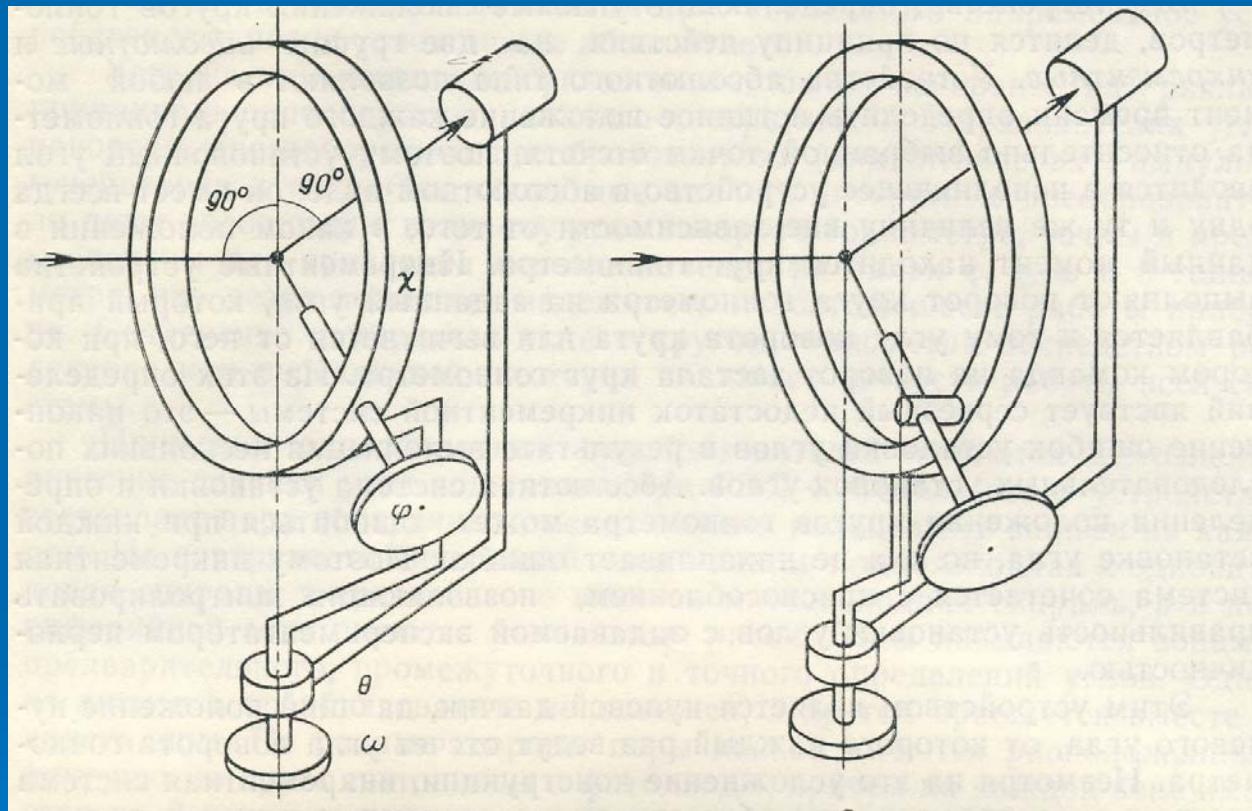
Монокристальная
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успеха, современное
состояние и перспективы

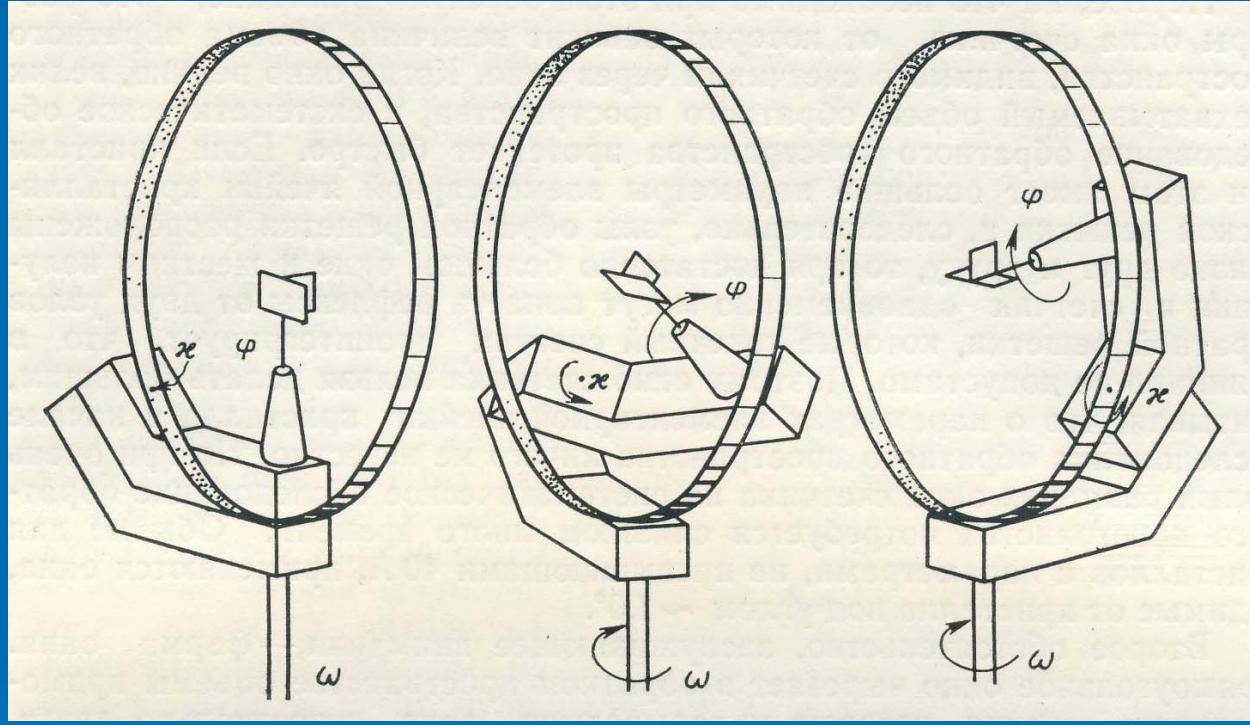




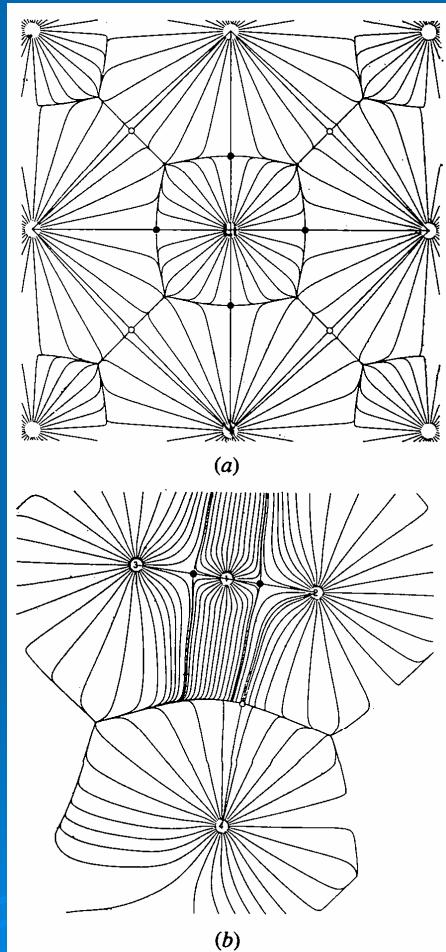




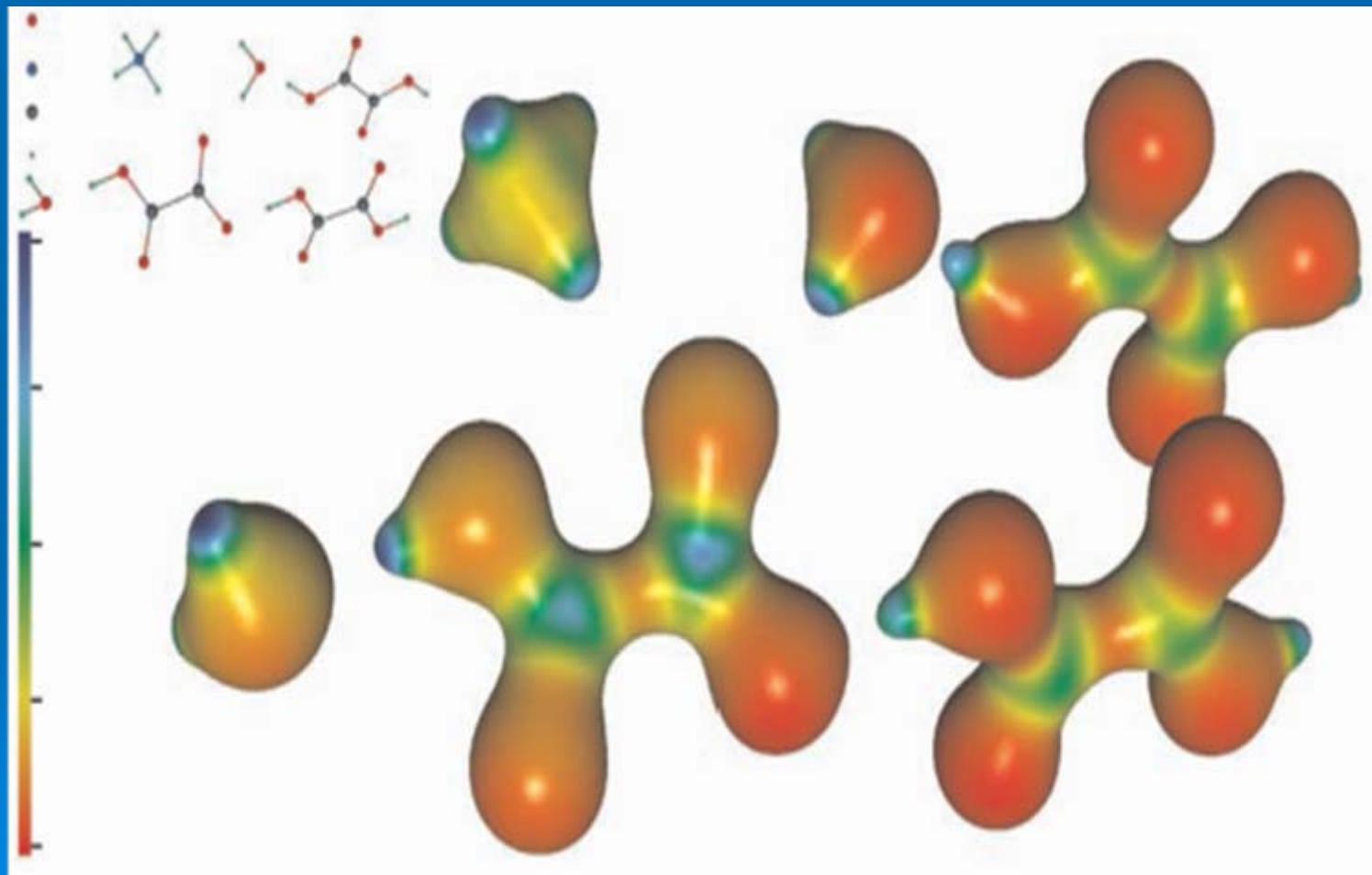




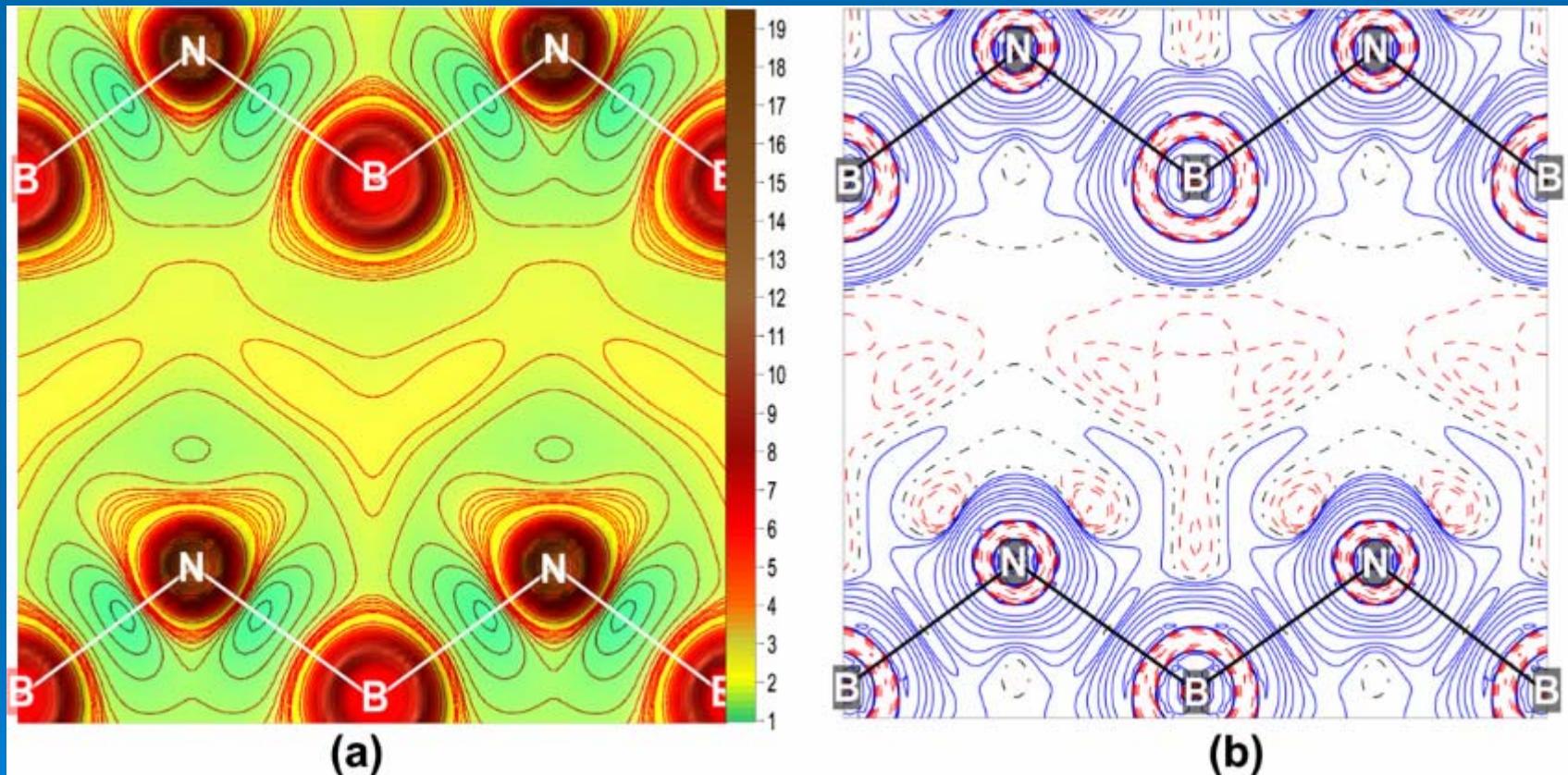
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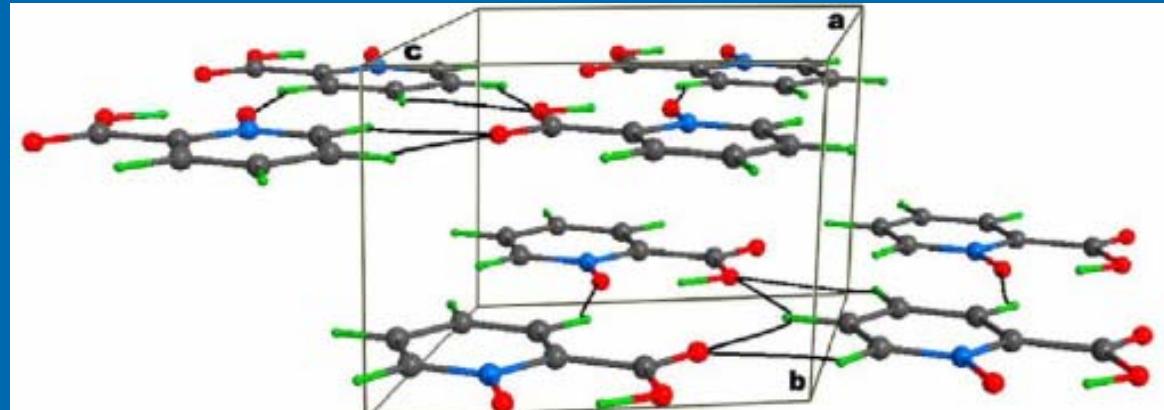
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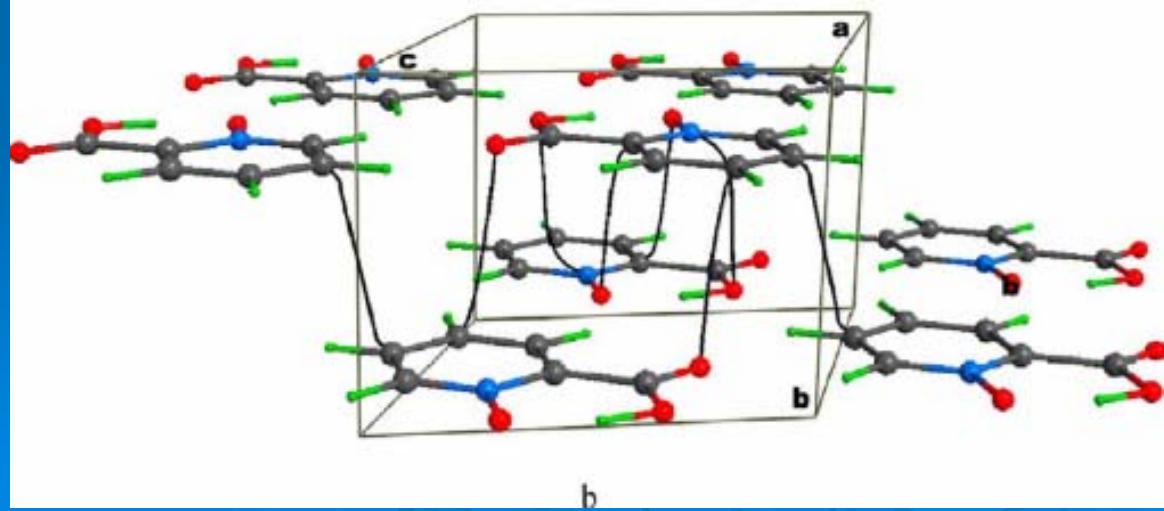
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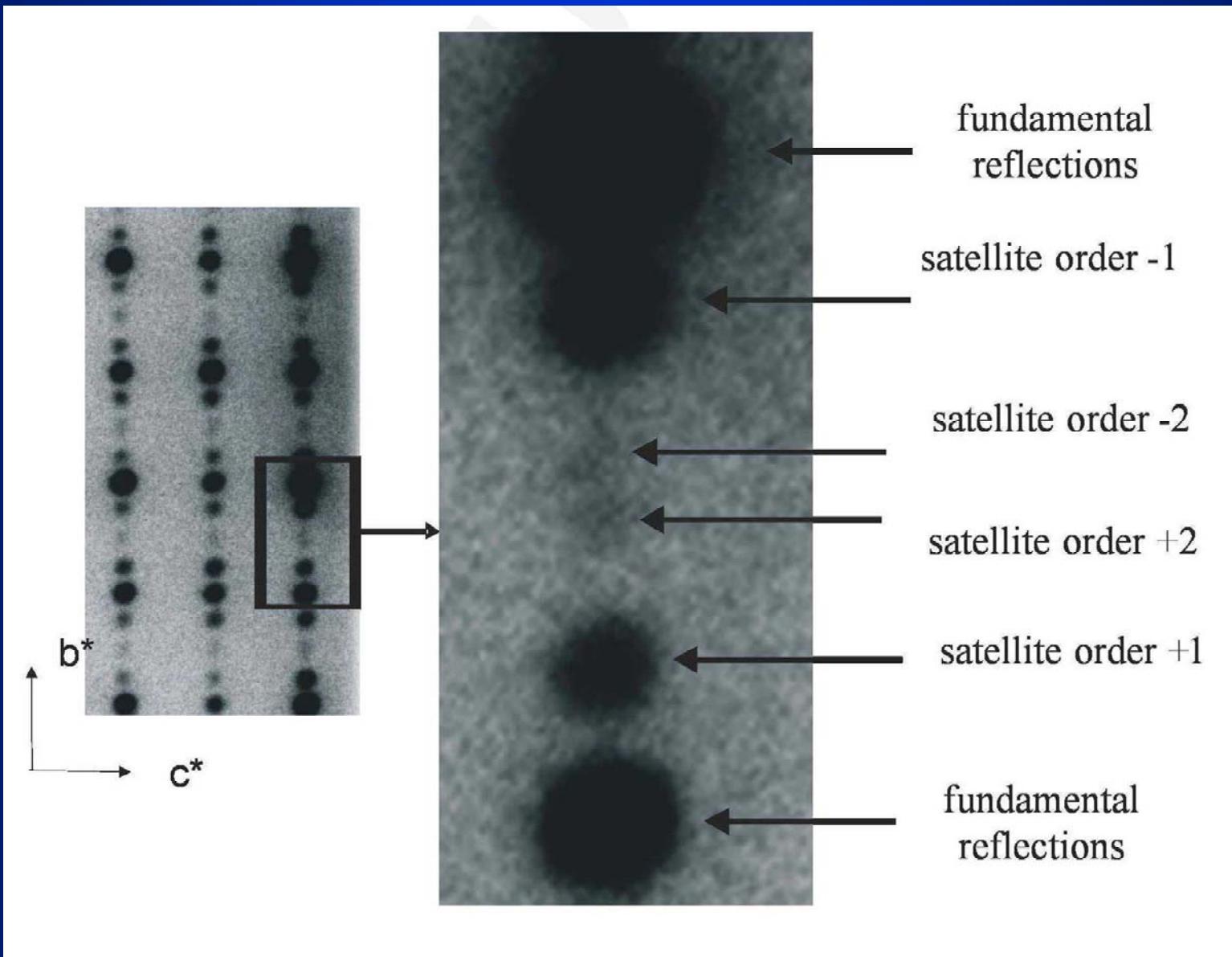
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a



b



The incommensurately modulated crystal structure of β -Pb₂BiVO₆
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Diffraction pattern of a modulated single crystal contains satellite reflections in the interstitials of the reciprocal lattice

$$\mathbf{H}(hkl) = h\mathbf{a}^* + k\mathbf{b}^* + l\mathbf{c}^* \leftarrow \text{a main reflection}$$

$$\mathbf{q}(\alpha\beta\gamma) = \alpha\mathbf{a}^* + \beta\mathbf{b}^* + \gamma\mathbf{c}^* \leftarrow \text{a modulation vector}$$

$$\mathbf{S}(hklm) = \mathbf{H}(hkl) + m\mathbf{q} \leftarrow \text{a satellite}$$

$$= (h \pm m\alpha)\mathbf{a}^* + (k \pm m\beta)\mathbf{b}^* + (l \pm m\gamma)\mathbf{c}^*$$

There are different kinds of the structure modulation:

Displacive modulation:

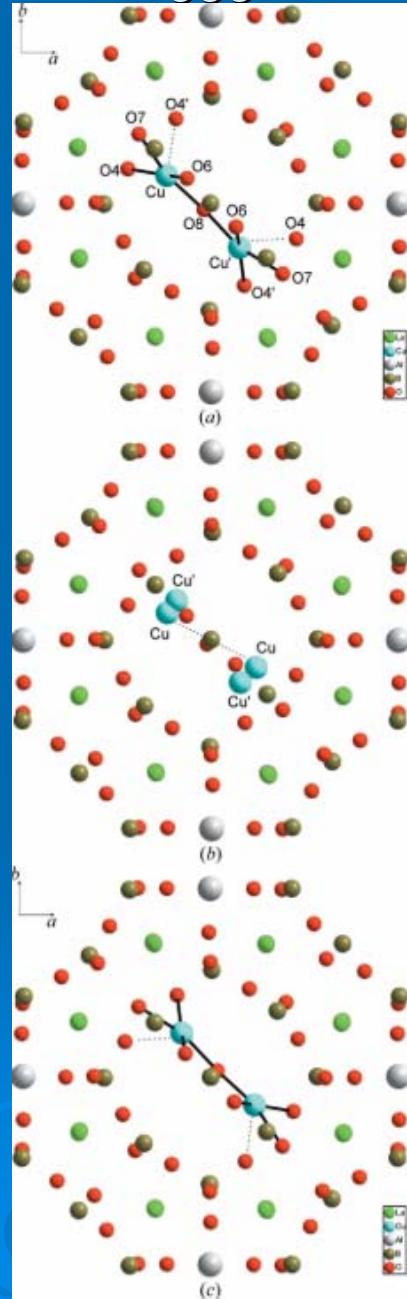
$$\mathbf{r} = \mathbf{r}^0 + \mathbf{n} + \sum_k \{\mathbf{s}_k \sin[2\pi k \mathbf{q} \cdot (\mathbf{r}^0 + \mathbf{n})] + \mathbf{c}_k \cos[2\pi k \mathbf{q} \cdot (\mathbf{r}^0 + \mathbf{n})]\}$$

Occupation modulation:

$$p = p^0 + \sum_k \{sp_k \sin[2\pi k \mathbf{q} \cdot (\mathbf{r}^0 + \mathbf{n})] + cp_k \cos[2\pi k \mathbf{q} \cdot (\mathbf{r}^0 + \mathbf{n})]\}$$

Since translational symmetry is broken, atomic coordinates depend on the lattice position. We should select a unit cell of the periodic lattice as an origin; \mathbf{n} is a translation between the origin and the cell under consideration; $\mathbf{r}^0(x^0, y^0, z^0)$ are basic atomic coordinates and the last term defines atomic displacement.

A modulation function can be expand into Fourier series as here. Legendre polynomials can also been used to expand the stepwise functions such as **crenels** and **saw-tooth** functions.



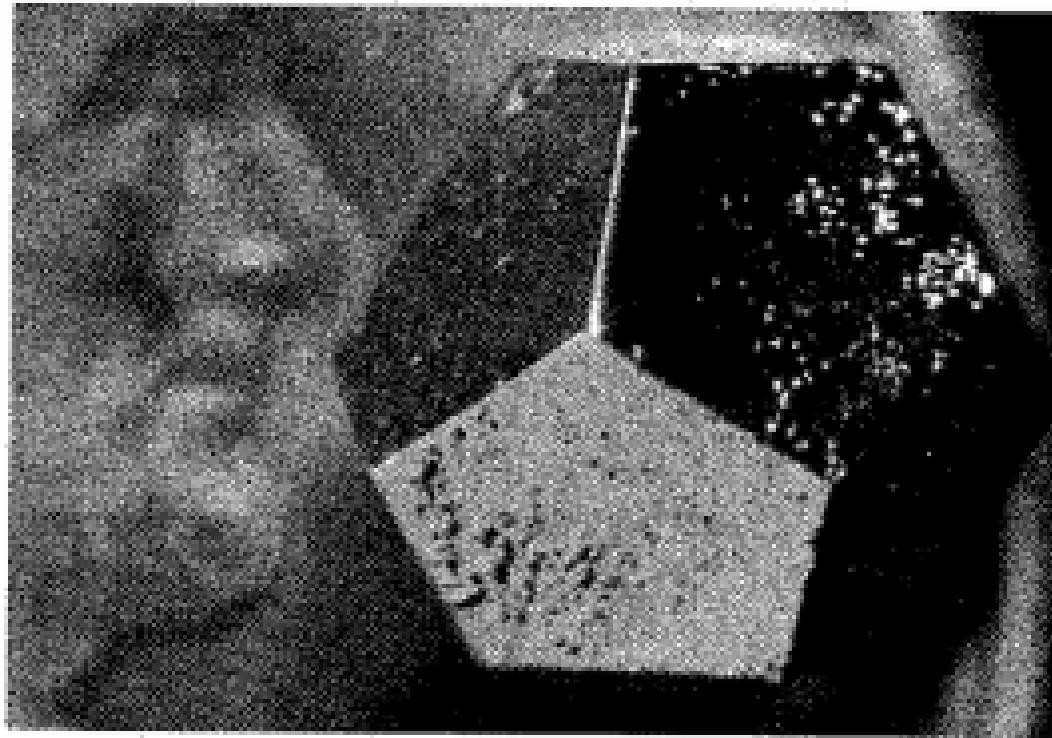
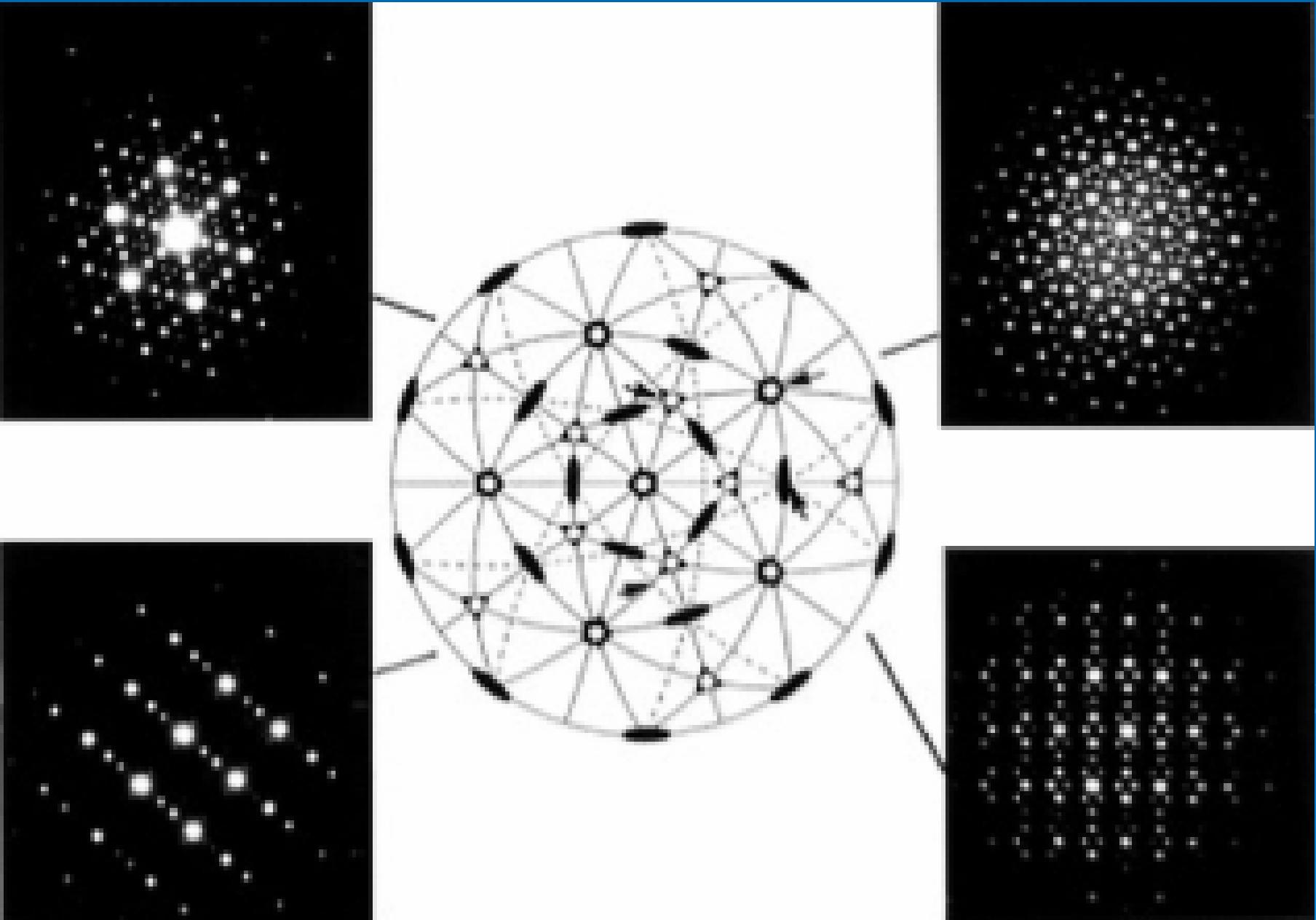
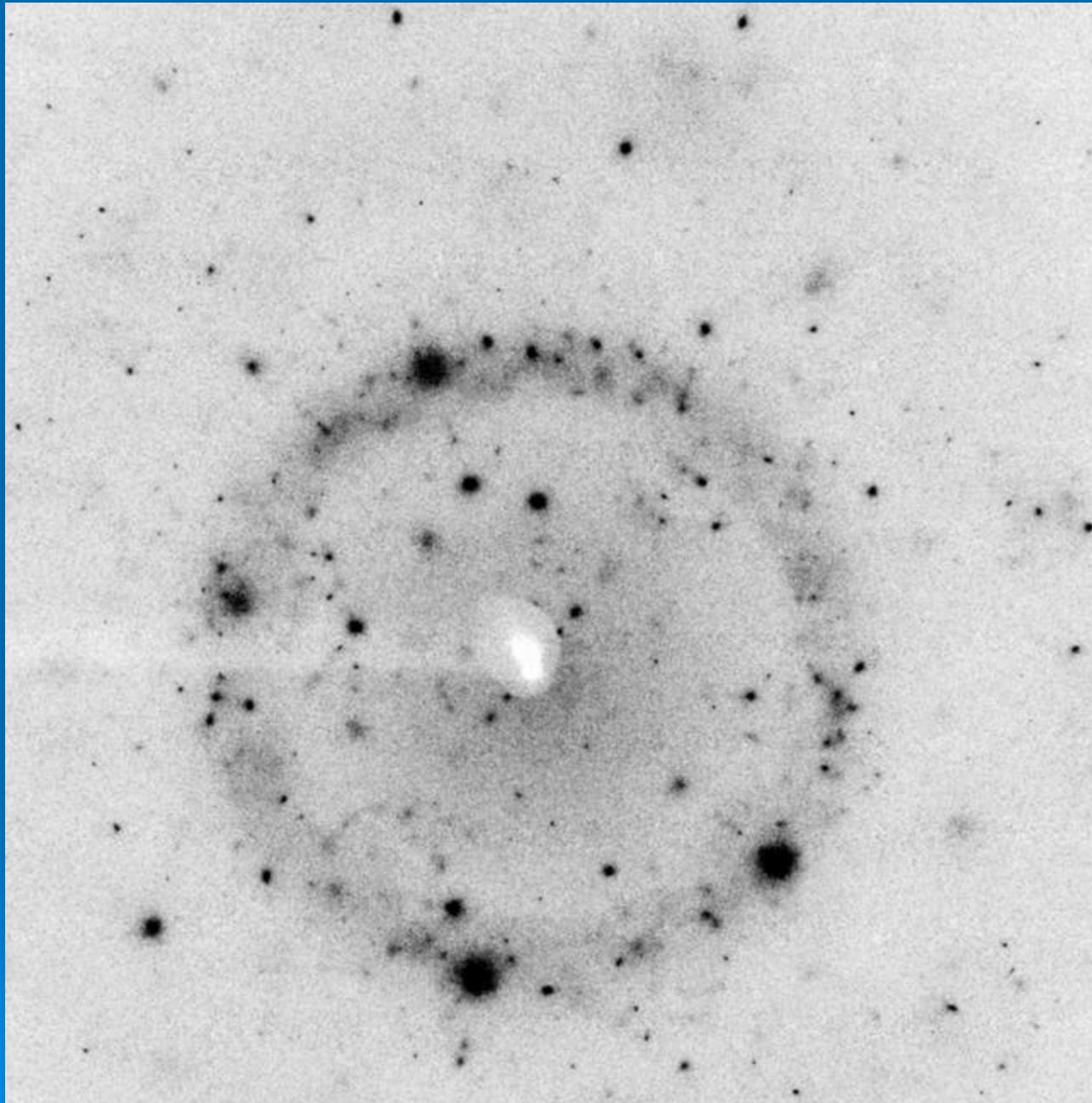
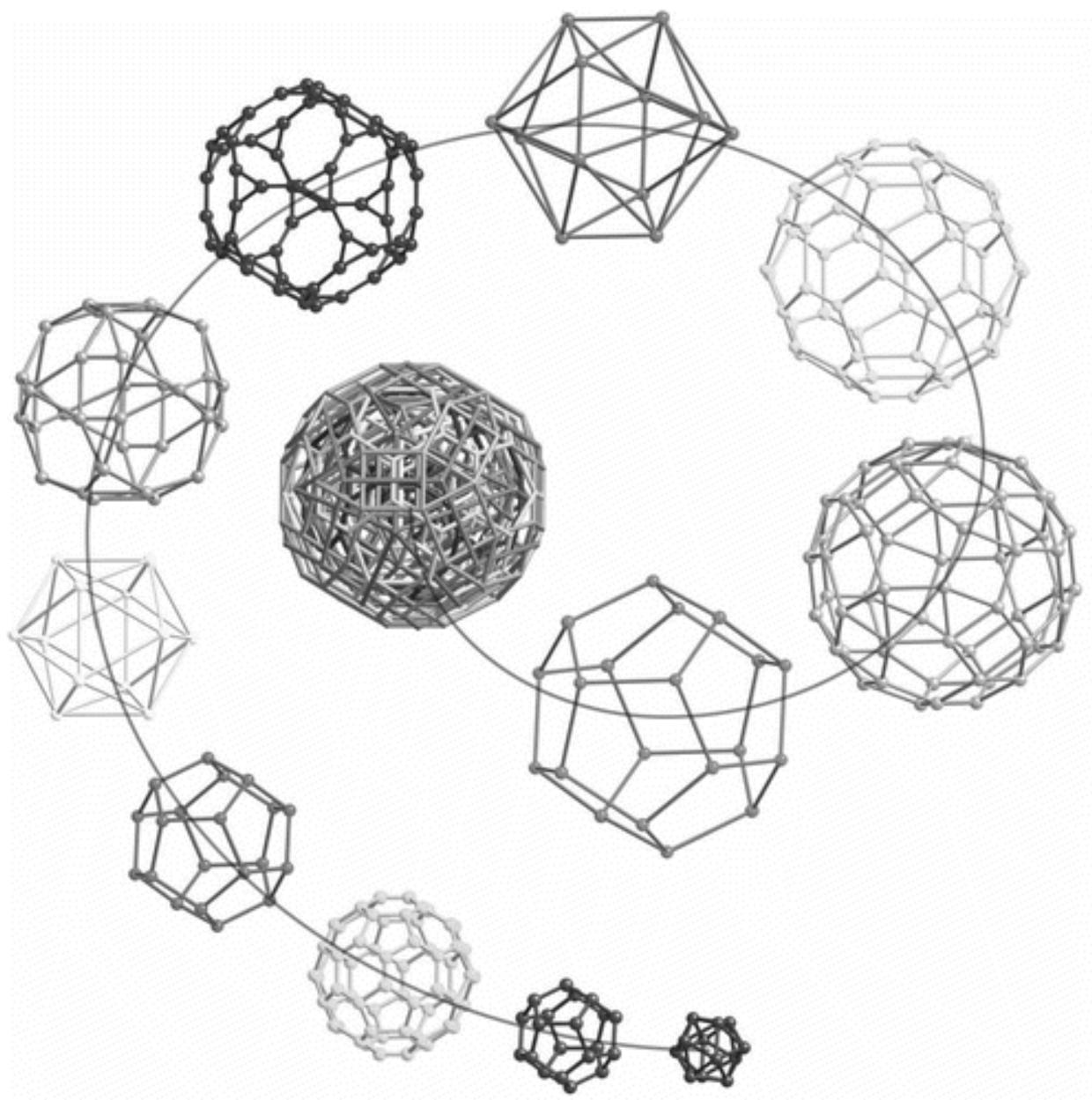
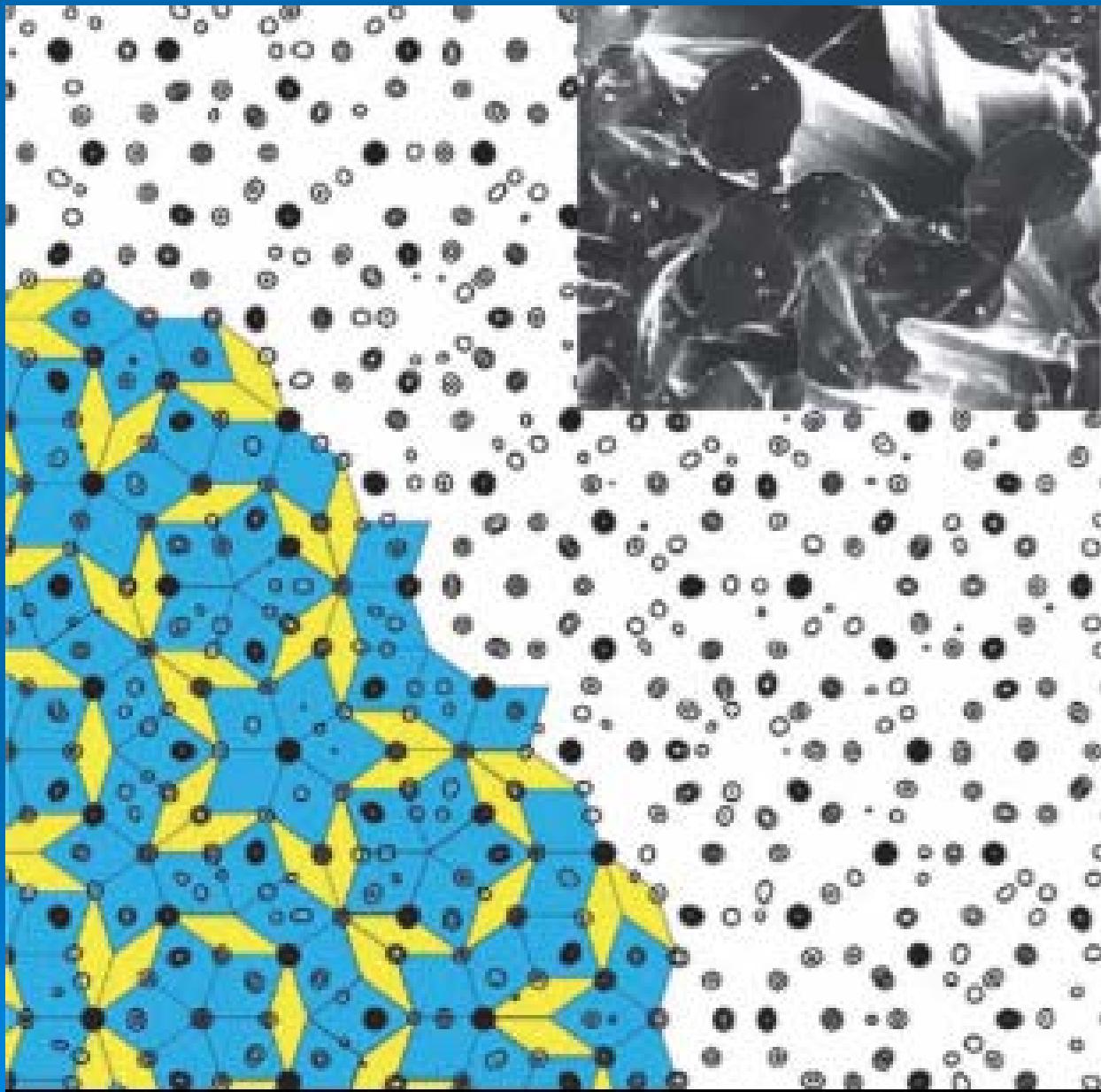


Fig. 1.17. Specimen of icosahedral HoMgZn. Quasicrystals may have the shape of a dodecahedron. Six Miller indices are needed in this case. Photograph courtesy of I. R. Fisher (Stanford) and P. C. Canfield (Ames Laboratory)

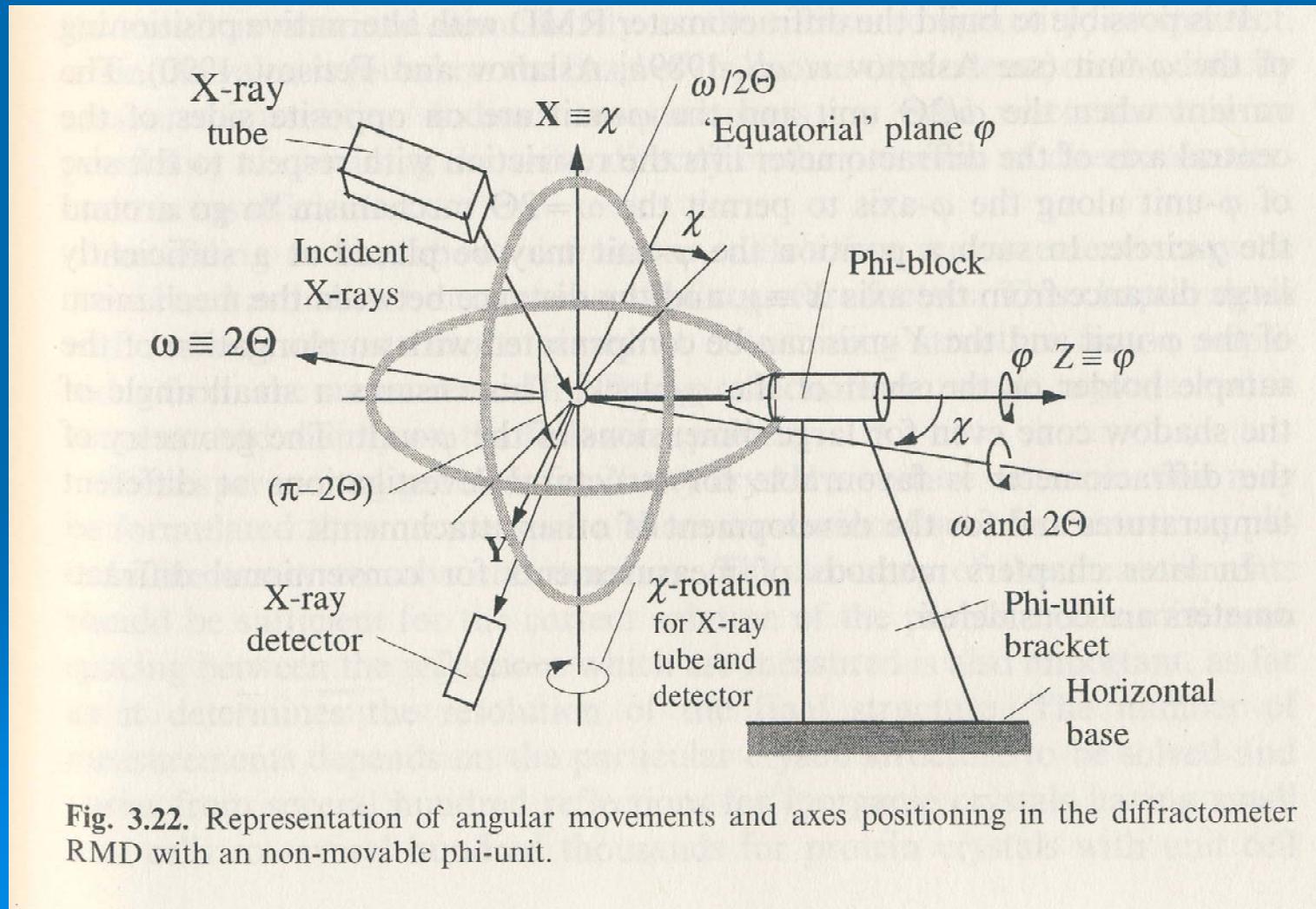


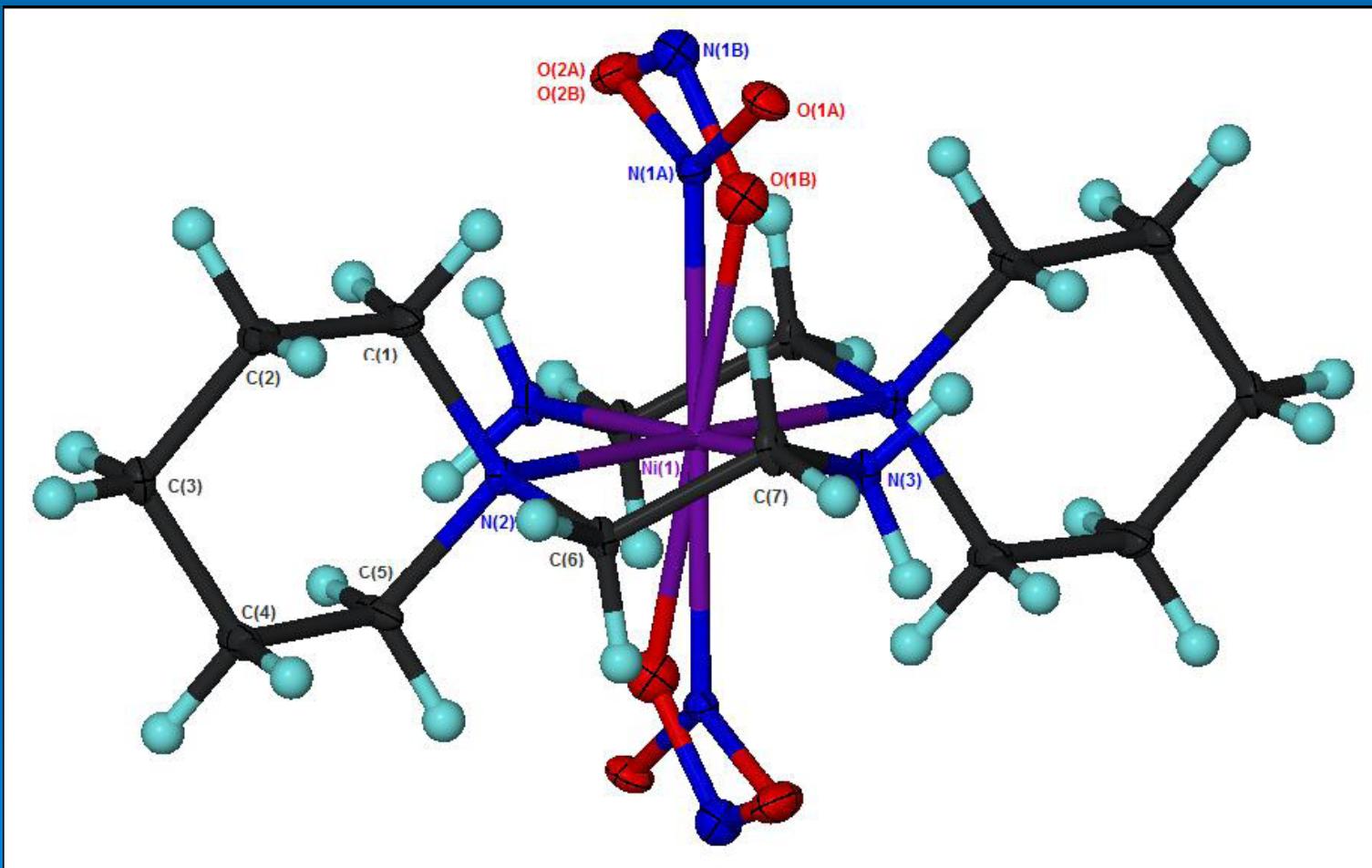


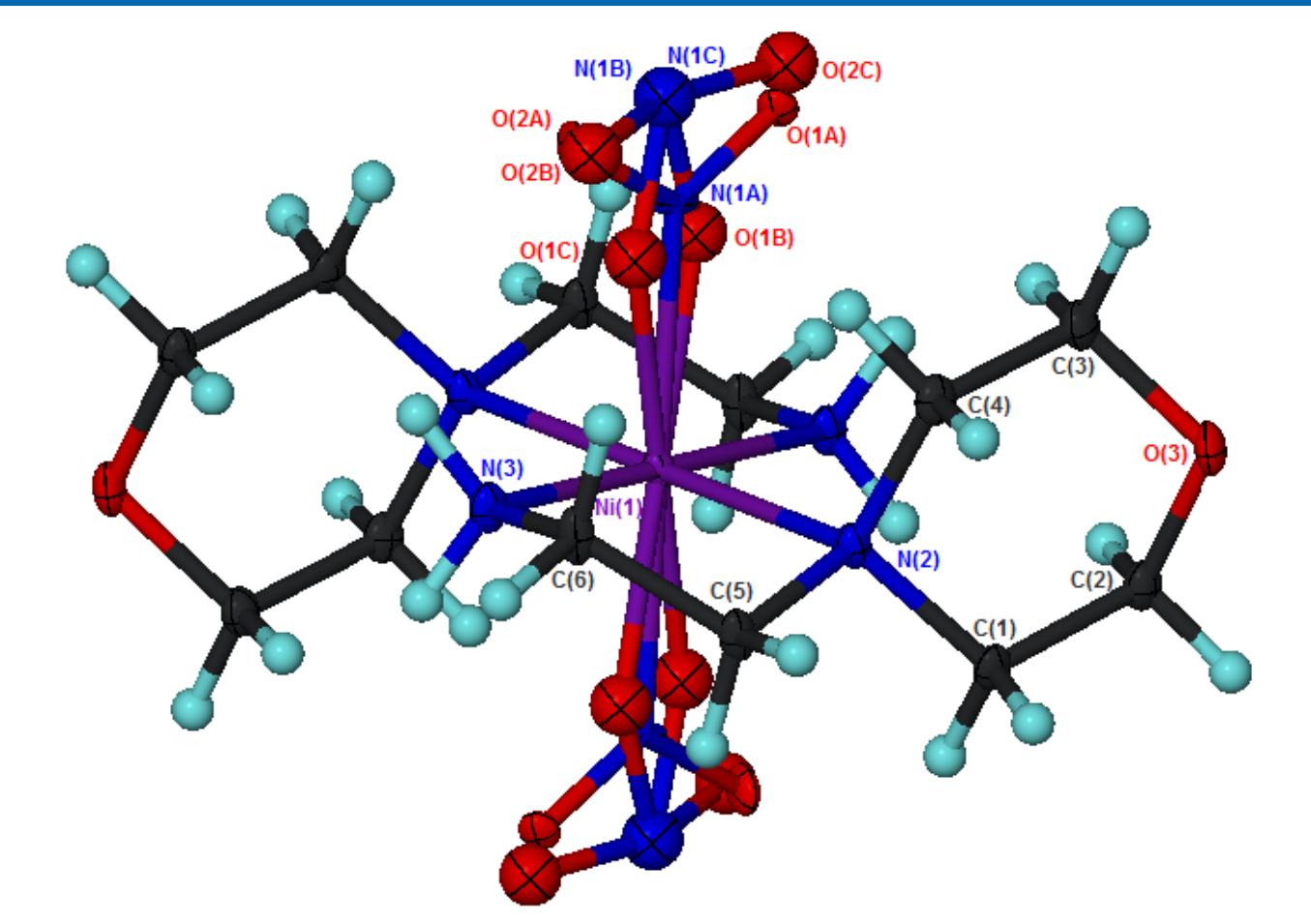




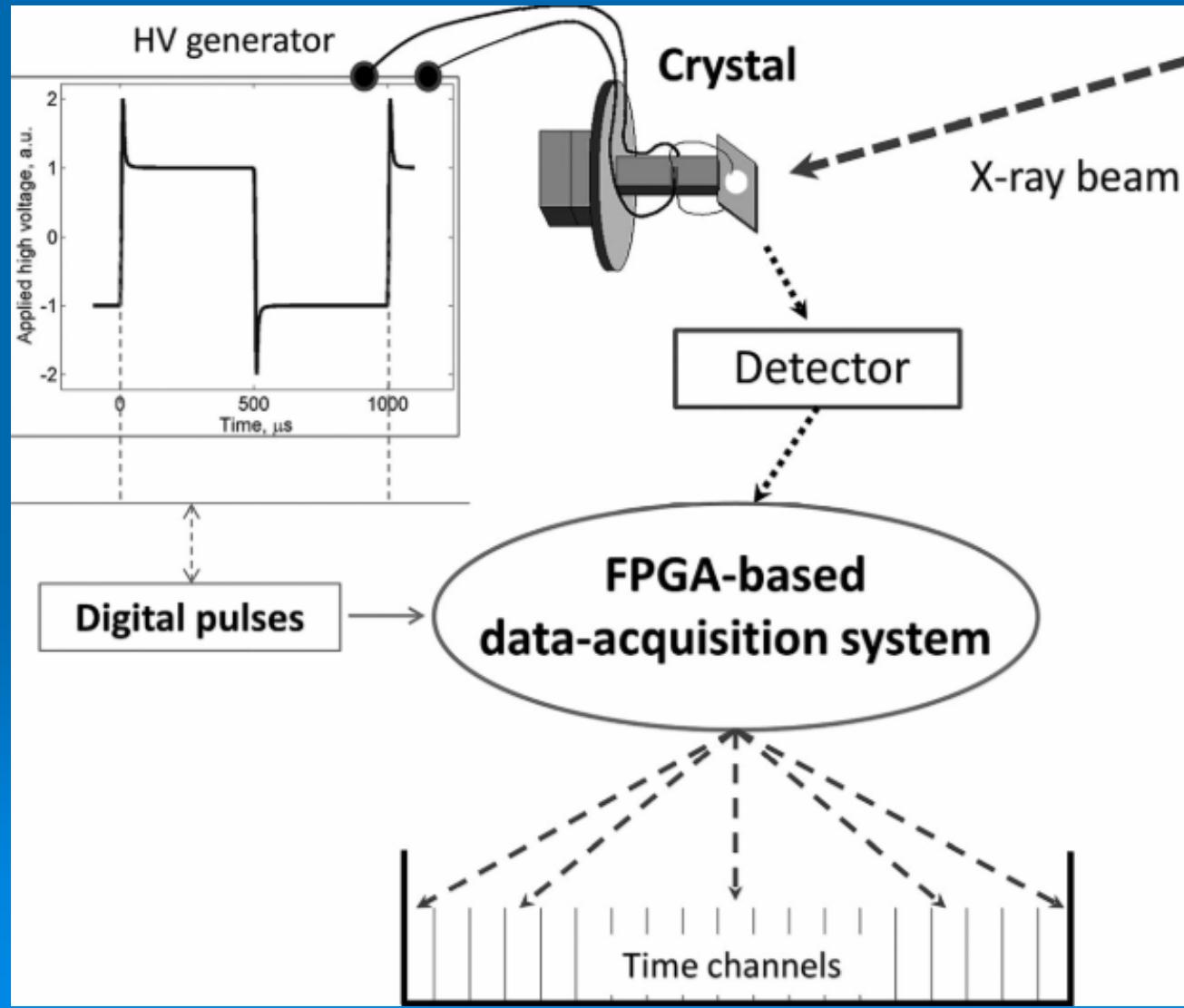
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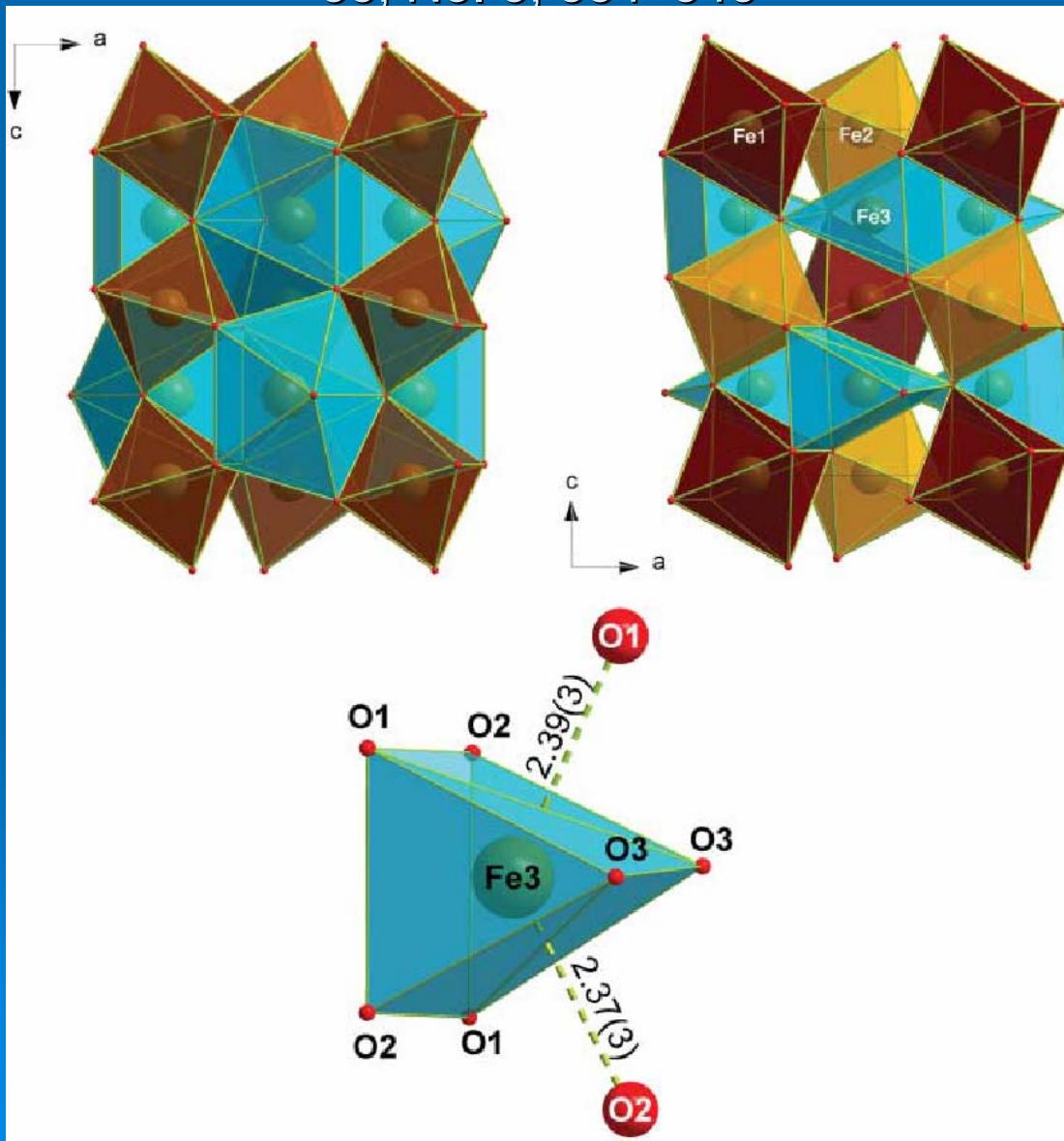


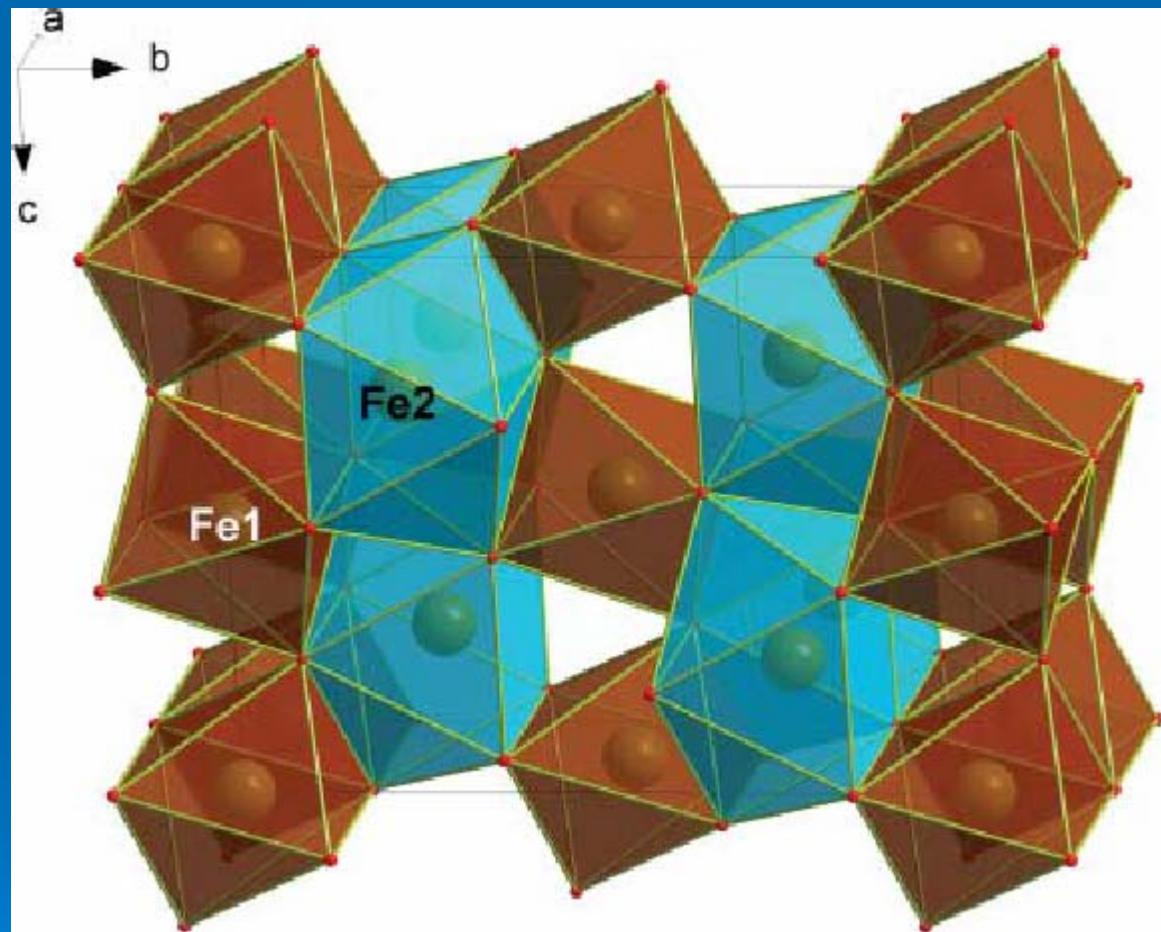


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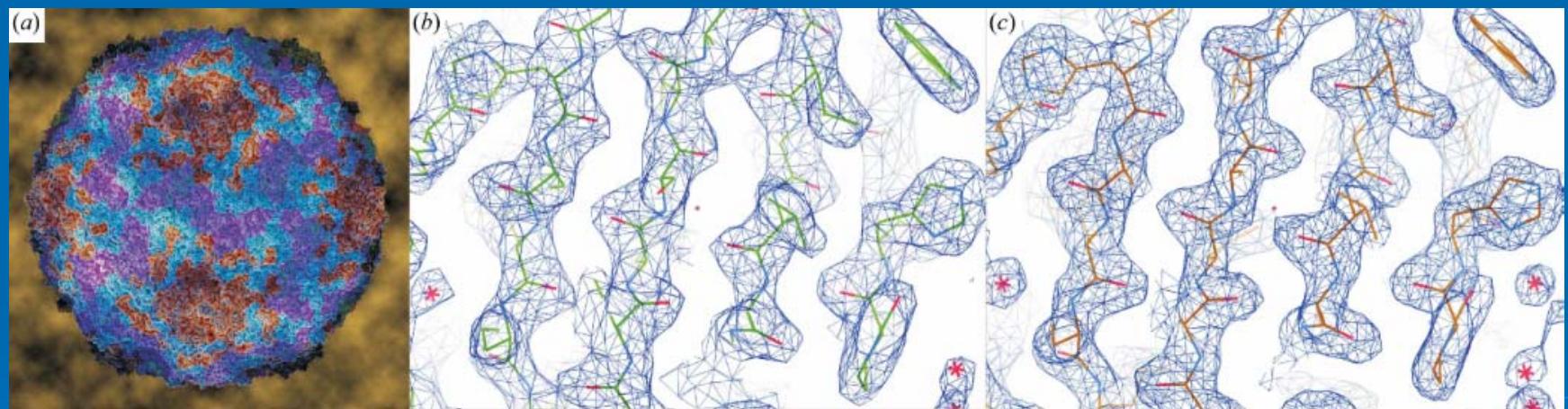


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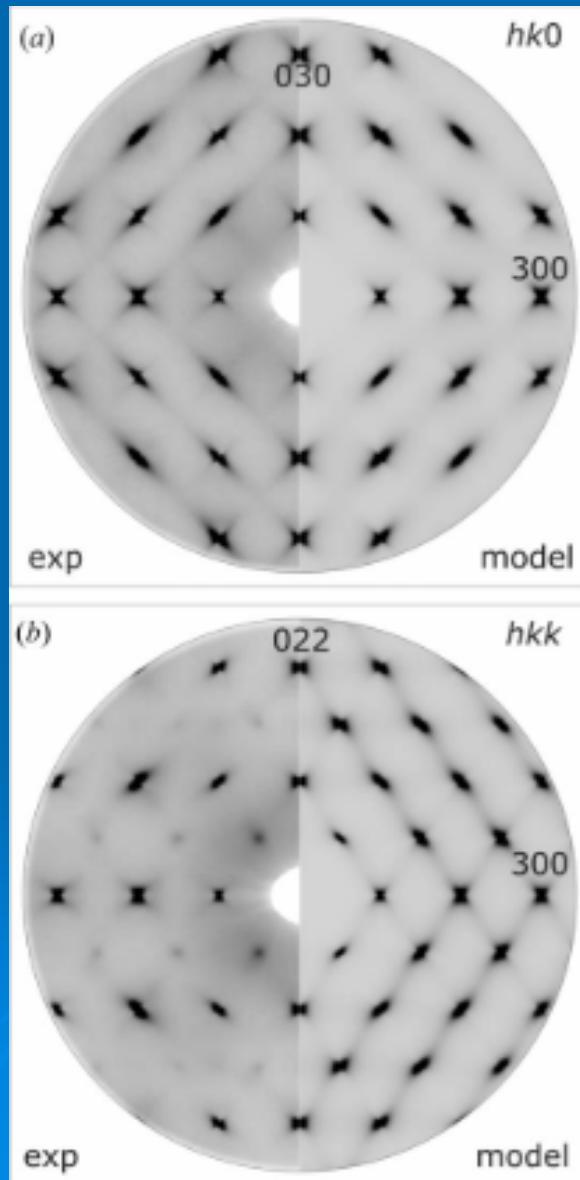




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E.E. Fry, D.I. Stuart, A. Meents. *Acta Cryst.* (2013). D69, 308–312



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(2012). A68, 117–123



$c^*/5$  $a^*/5$ 

002



111



211

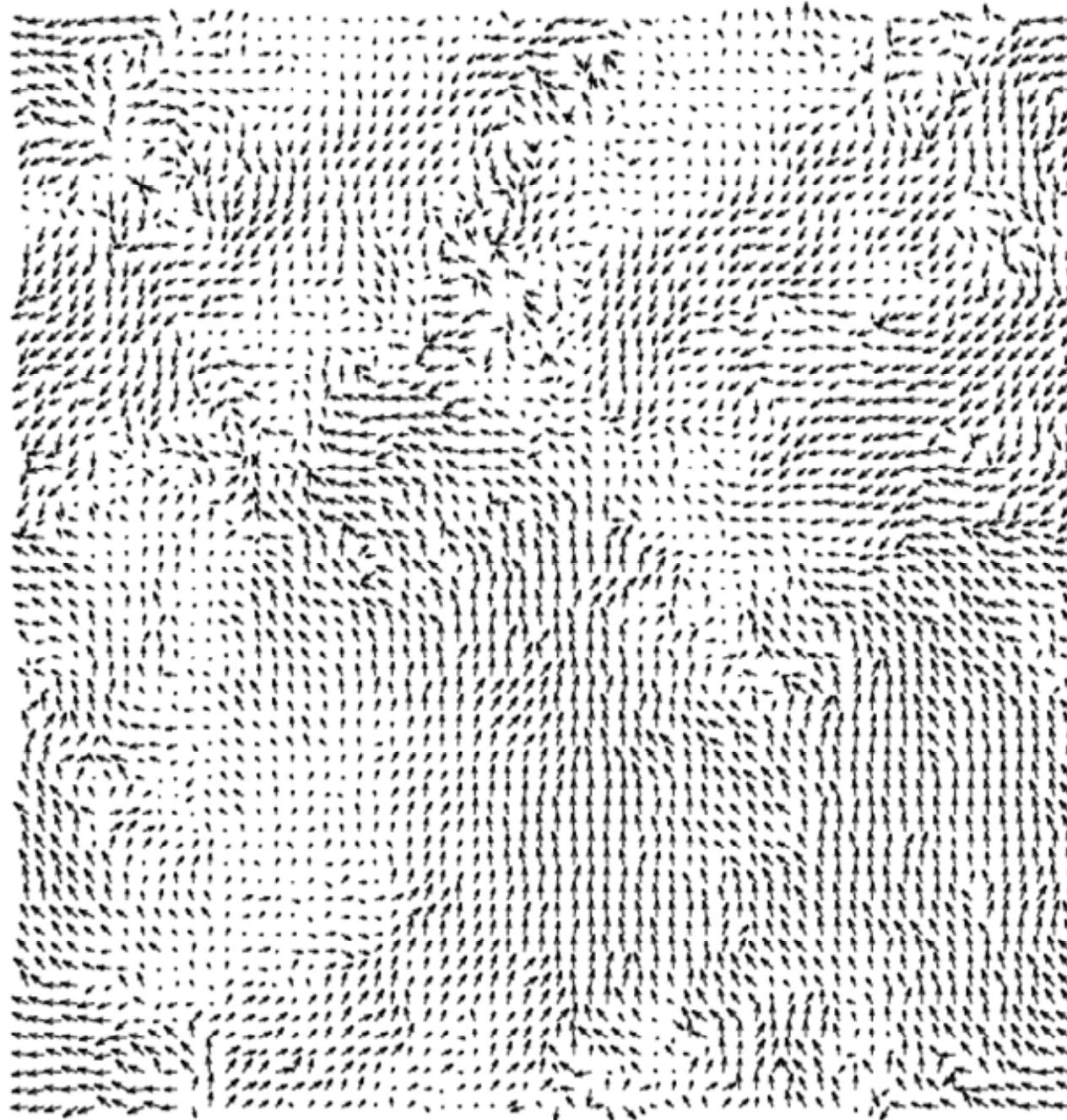
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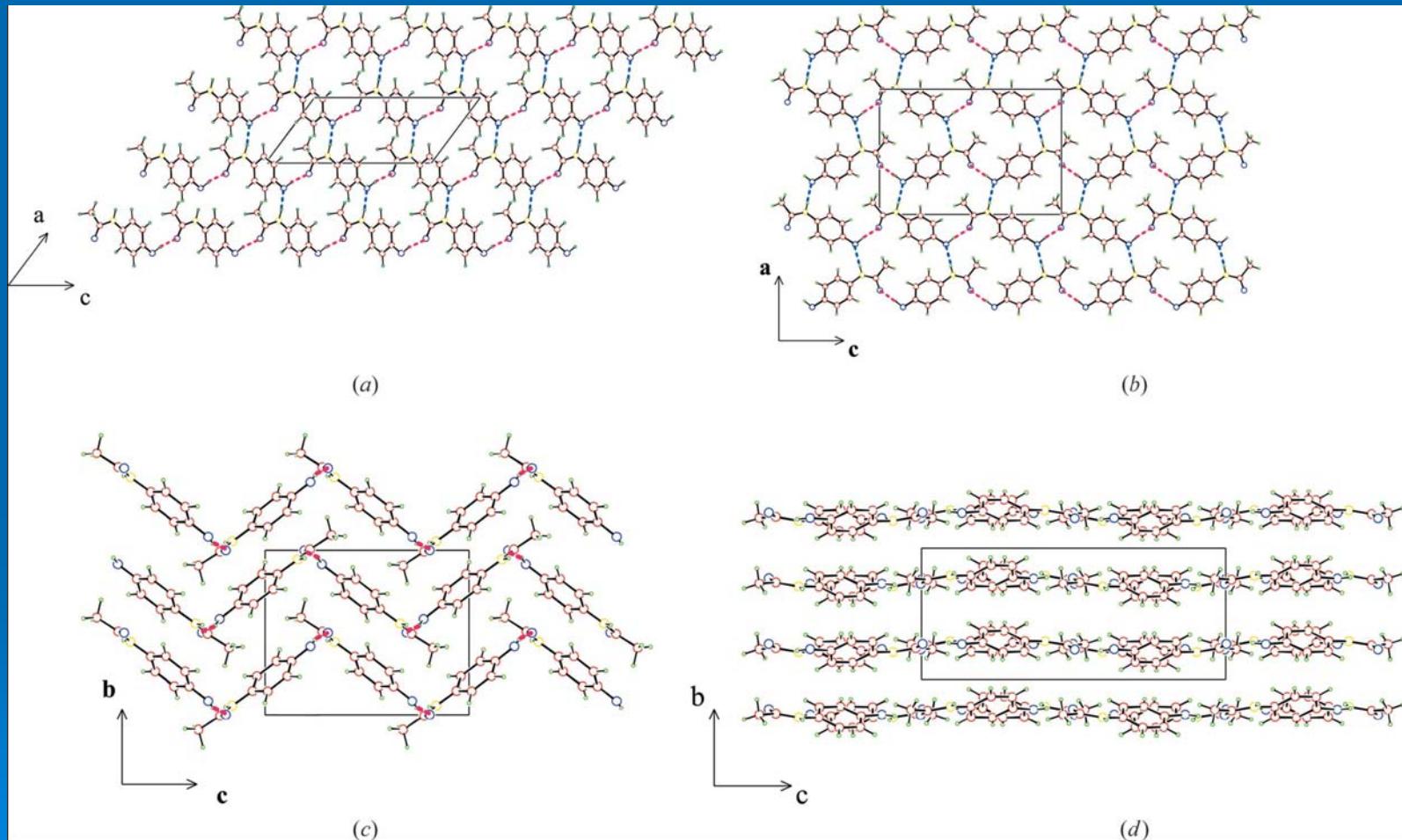
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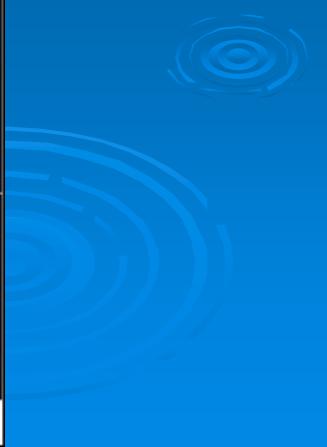
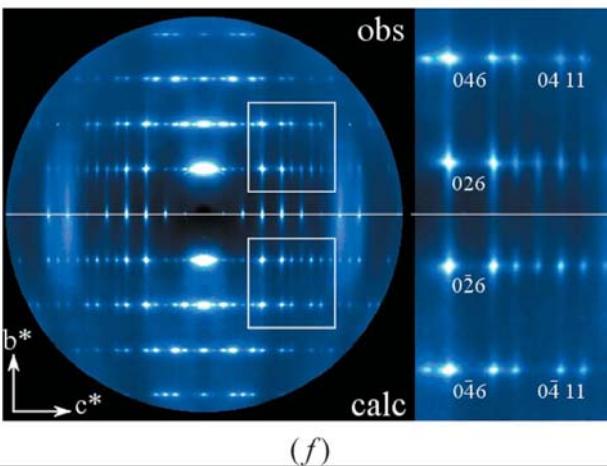
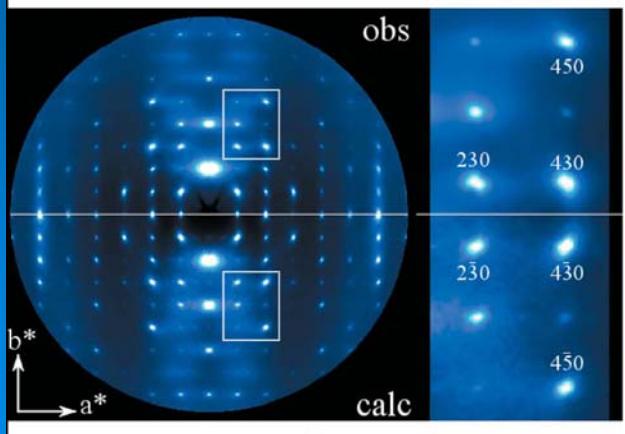
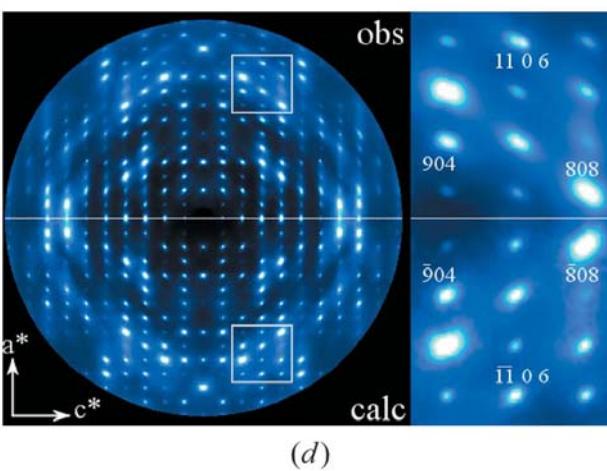
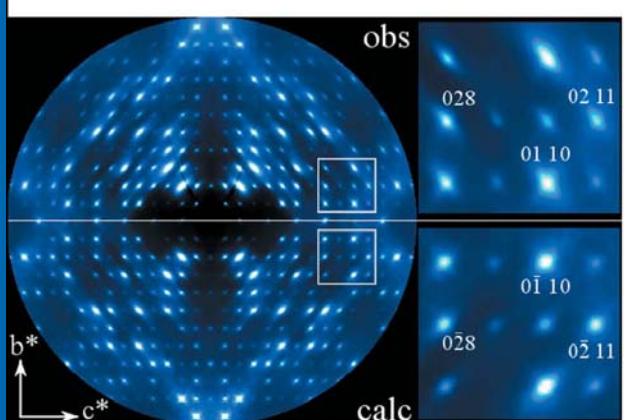
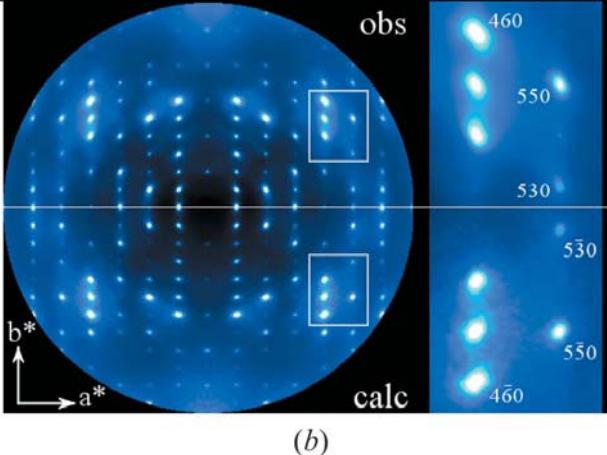
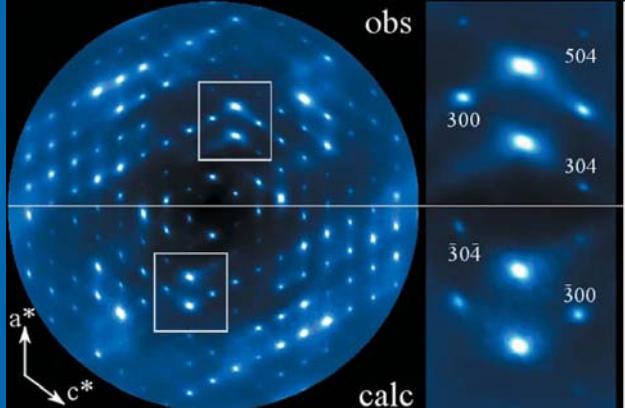
(c)

(d)

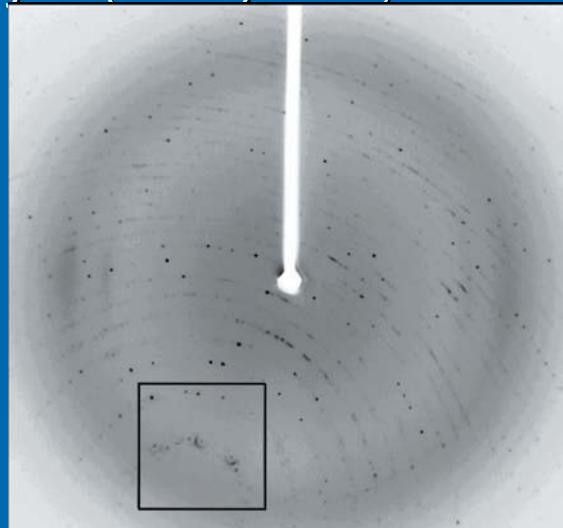
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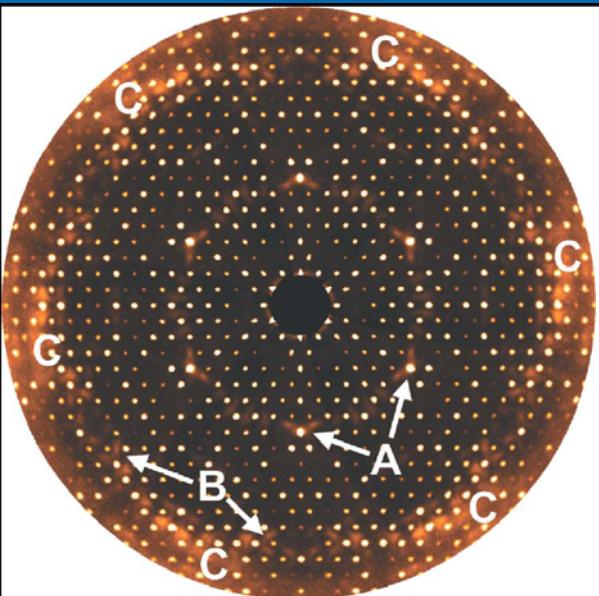
T. R. Welberry, A. P. Heerdegen, D. C. Goldstone, Ian A. Taylor. *Acta Cryst.* (2011). B67, 516–524



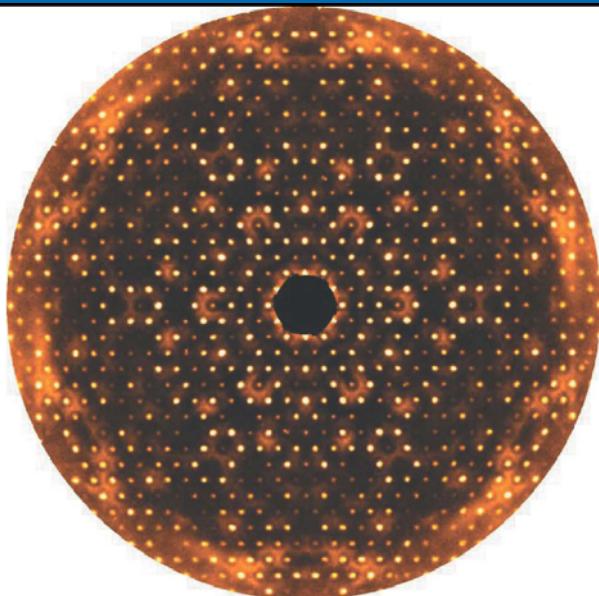
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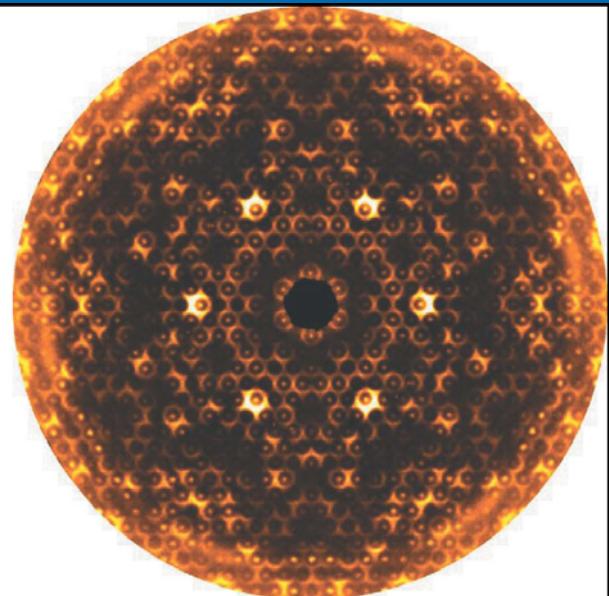
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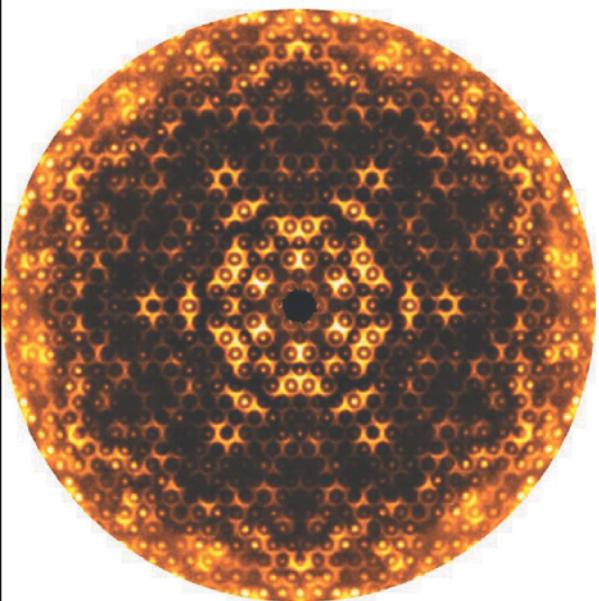
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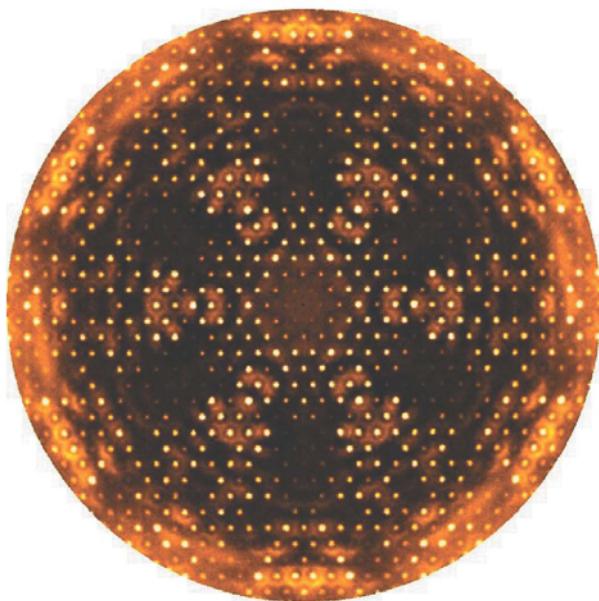
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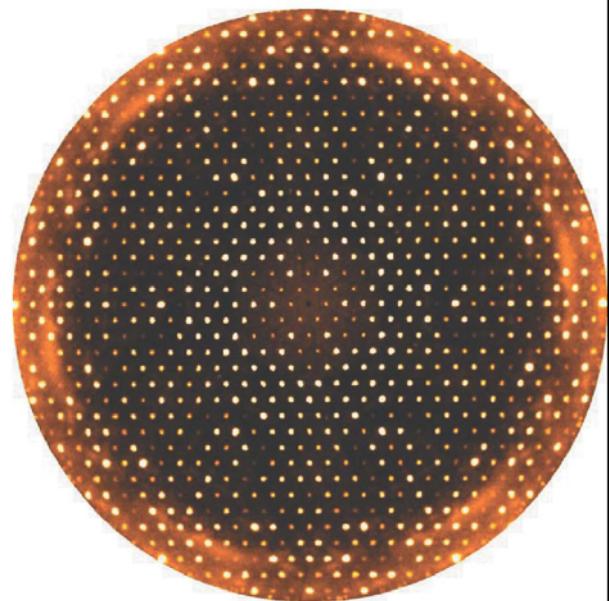
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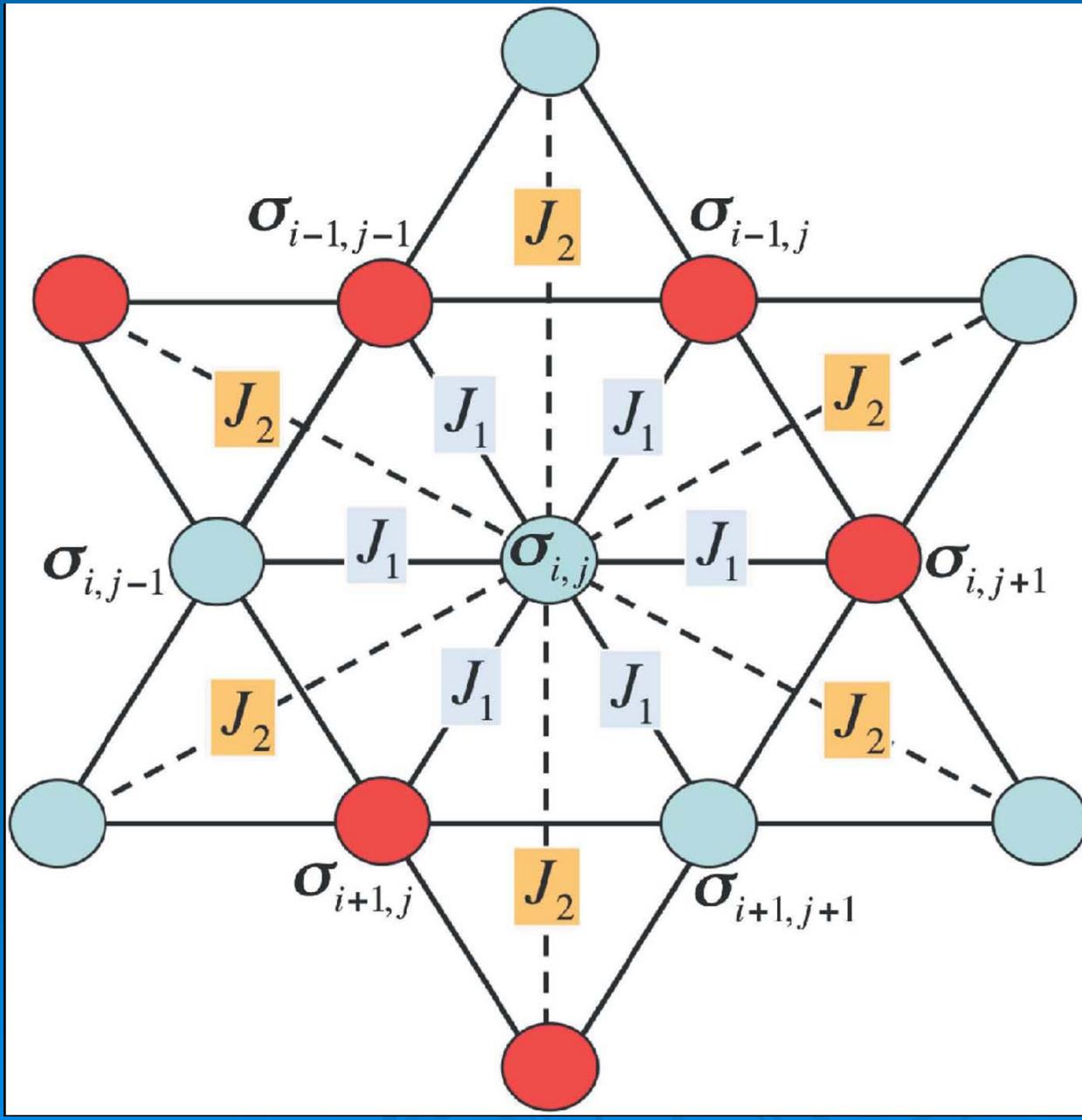
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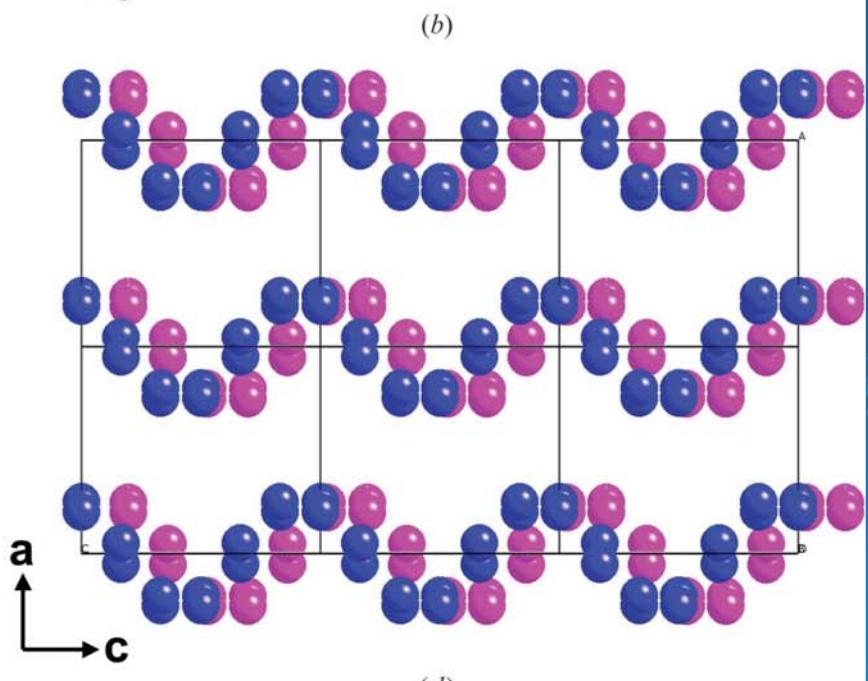
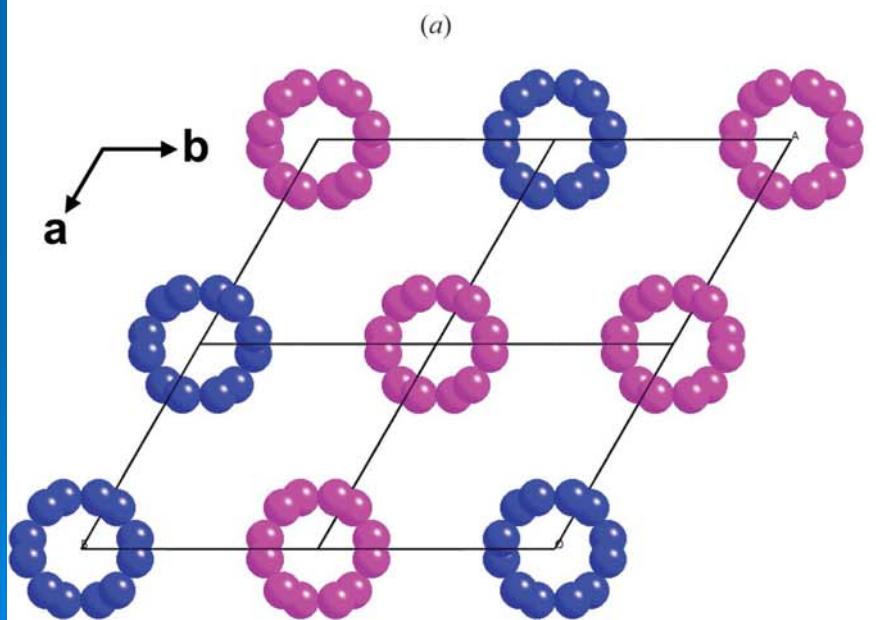
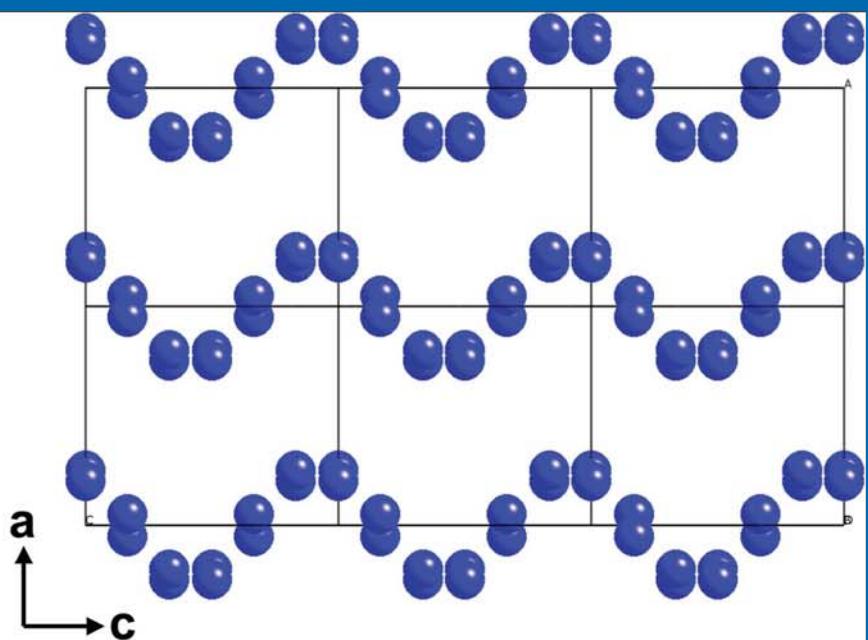
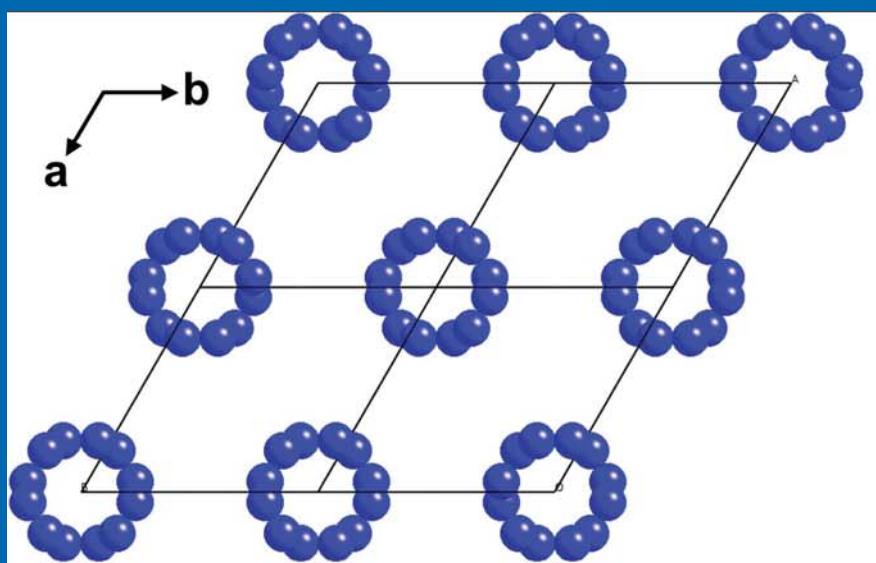


(e)



(f)



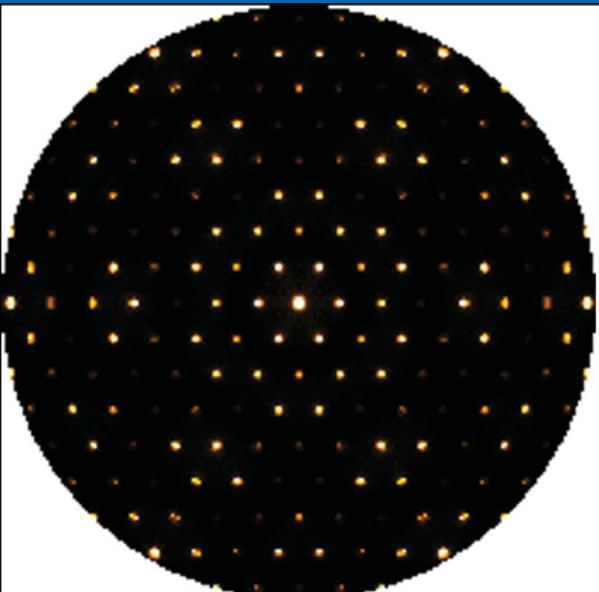


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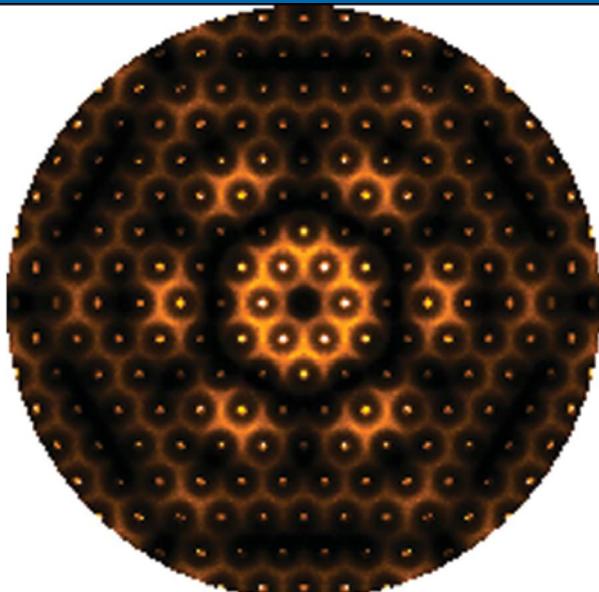
(b)

(c)

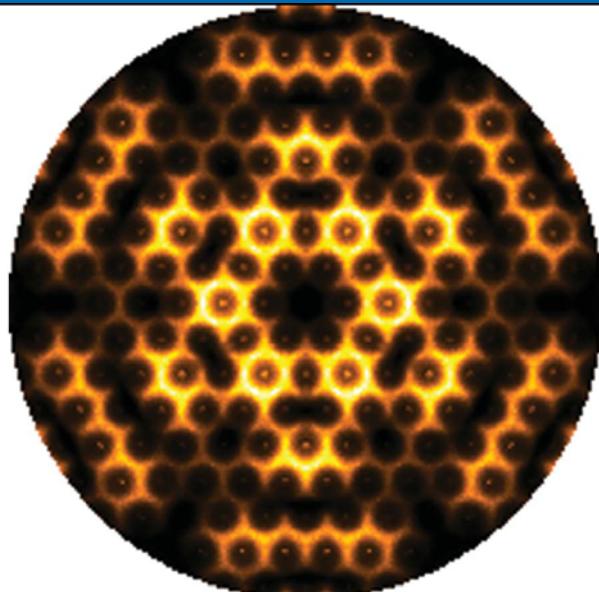
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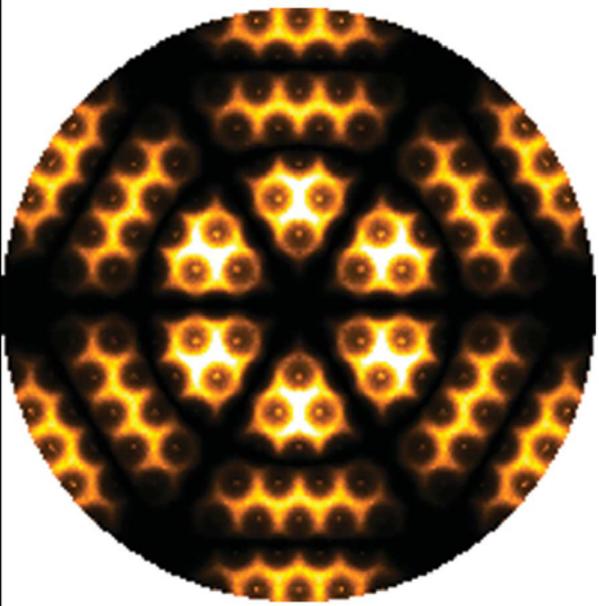
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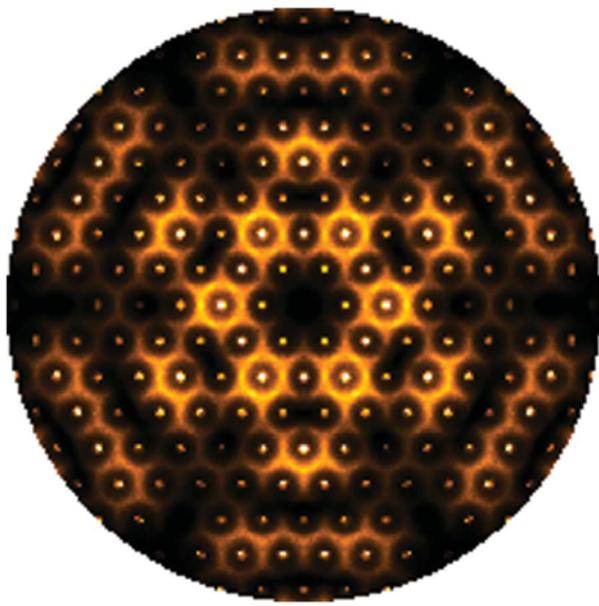
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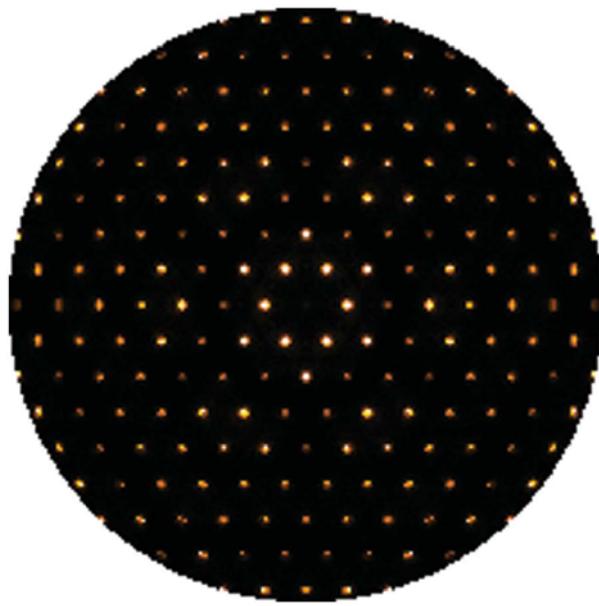
(c)



(d)



(e)



(f)