

**Изучение поверхностей с помощью  
рентгеновской рефлектометрии и  
дифракции в скользящей геометрии**

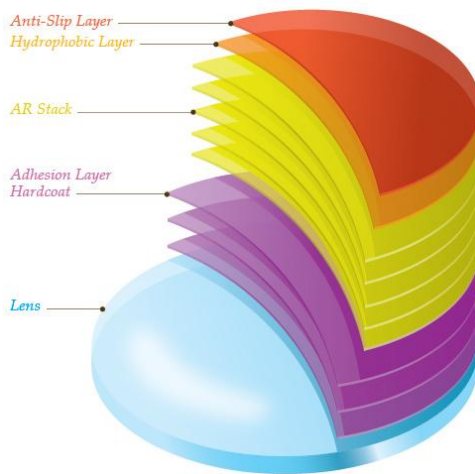
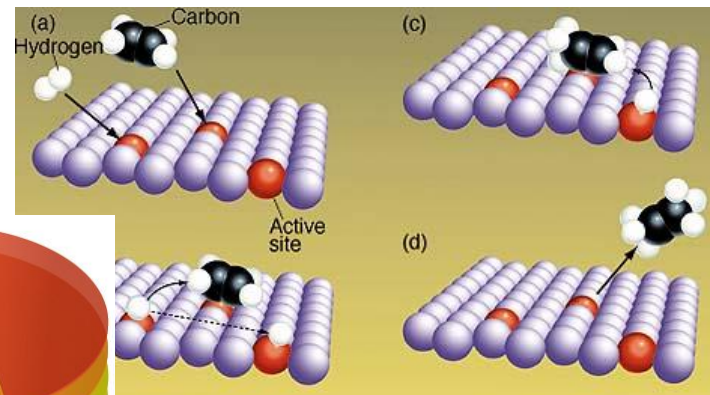
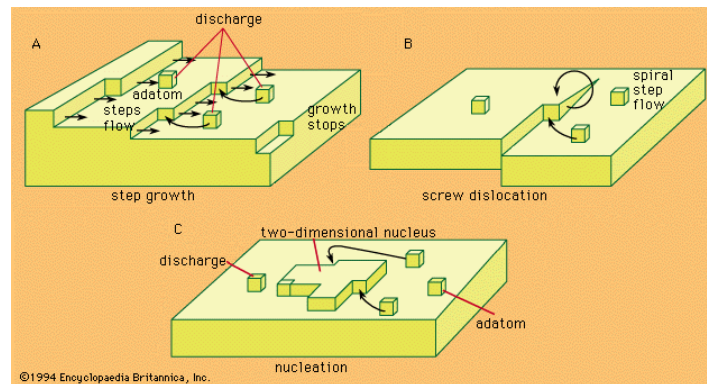
**Oleg Konovalov  
ESRF / ID10B**

# Outlook

- 1. Introduction**
- 2. Surface sensitivity**
- 3. Theory and Applications of**
  - X-ray reflectivity**
  - Diffuse scattering**
  - Grazing Incidence Diffraction**
  - Grazing Incidence Small Angle Scattering**
  - Total Reflection X-Ray Fluorescence**
- 4. Conclusions**

# Зачем изучать поверхности ?

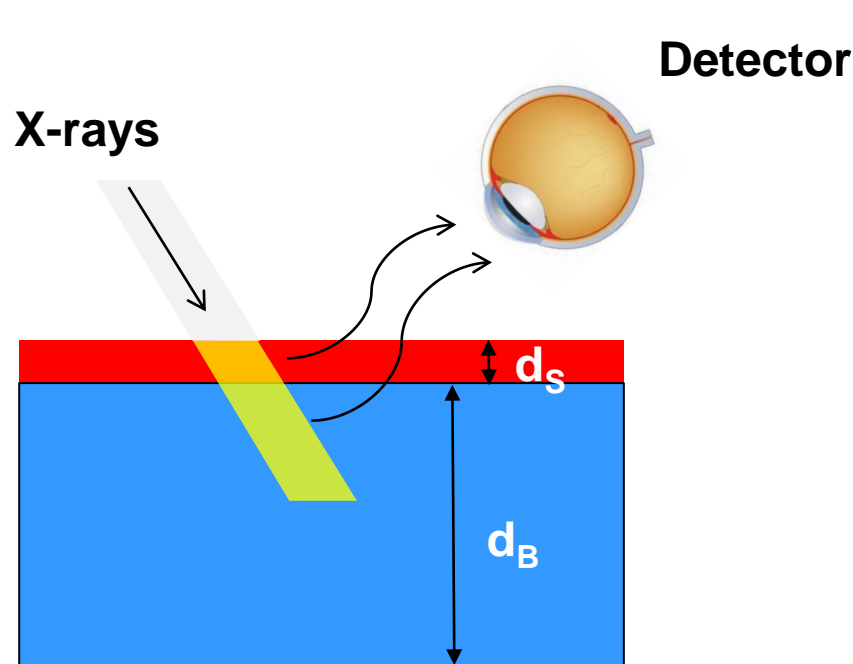
- ? фазовые границы раздела
- ? рост кристаллов
- ? химические реакции на поверхностях  
⇒ катализ
- ? физика двумерных систем
- ? тонкие пленки, мембраны
- ? ....



## Scientific Applications

- Surface structure of simple and complex fluids (colloid, gel, sol,...)
- Langmuir films, amphiphilic polymers and nano- particle at the air-water interface
- Capillary wave and surface roughness
- Structure and growth of two dimensional crystals of molecules, macromolecules and proteins
- Morphology and crystalline structure of thin organic and non-organic films on solid substrates
- Phenomena at liquid/liquid and solid/liquid interfaces
- Cell membranes
- Shape, strain, ordering and correlation of crystalline nanostructures, quantum dots and wires on substrates

## How to study surfaces and interfaces ?



$$I(\vec{q}) = \left| \sum_k^N f_k \exp(-i \cdot \vec{q} \cdot \vec{r}_k) \right|^2$$

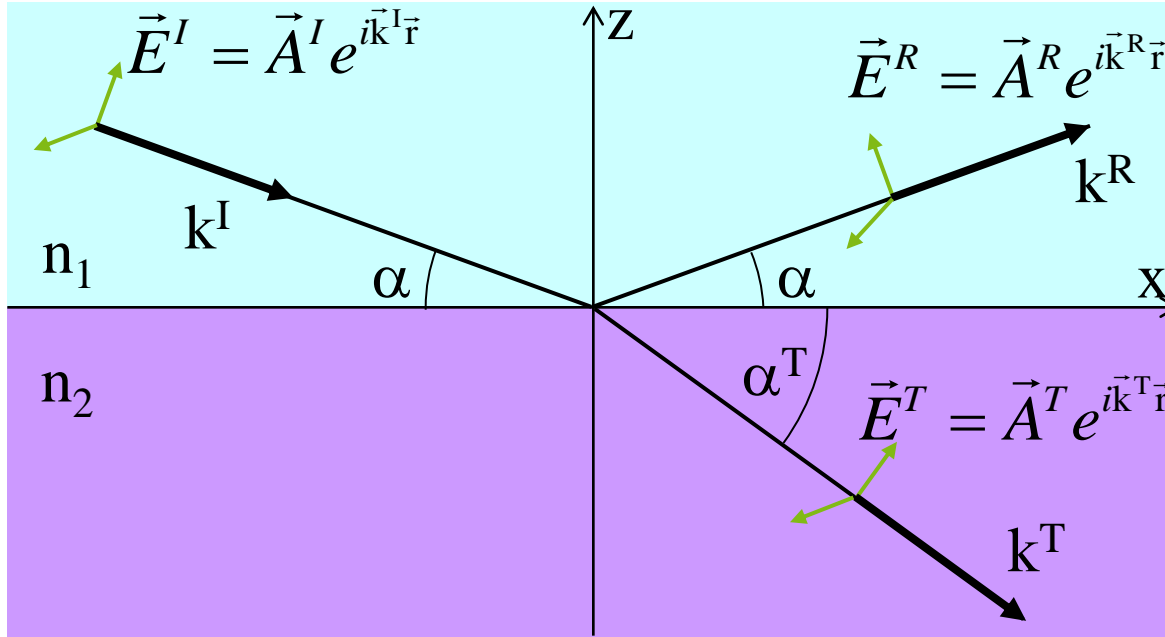
$$I \sim N \cdot f^2 = (N_S + N_B) \cdot f^2$$

$$\frac{I_S}{I_B} = \frac{N_S}{N_B} = \frac{d_S}{d_B}$$

$$\frac{I_S}{I_B} = \frac{100 \text{ nm}}{100 \mu\text{m}} = \frac{10^{-7}}{10^{-4}} = 10^{-3}$$



## Surface Sensitivity



Wave and its derivative are continuous at  $z=0$

$$A^I + A^R = A^T$$

$$A^I \vec{k}_I + A^R \vec{k}_R = A^T \vec{k}_T$$

$$k = |\vec{k}_I| = |\vec{k}_R| \quad nk = |\vec{k}_T|$$

$$\frac{\cos \alpha}{\cos \alpha^T} = \frac{n_2}{n_1} = n$$

For X-rays:  $n = 1 - \delta - i\beta$      $\delta = \frac{\lambda^2 r_e}{2\pi} \rho_{el}$      $\delta \sim 10^{-6}$      $|n| < 1$      $\alpha_c \sim \sqrt{2\delta}$

$$\alpha^T = \text{Re}(\alpha^T) + i \cdot \text{Im}(\alpha^T)$$

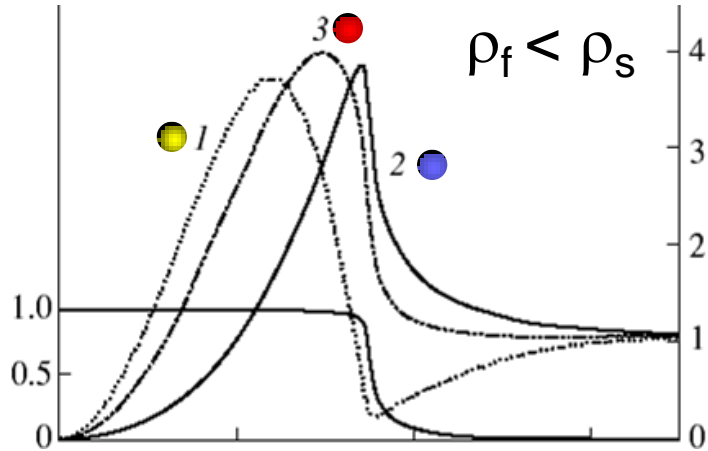
$$\beta = \frac{\mu\lambda}{4\pi}$$

Intensity falls off with 1/e penetration depth  $\Lambda$

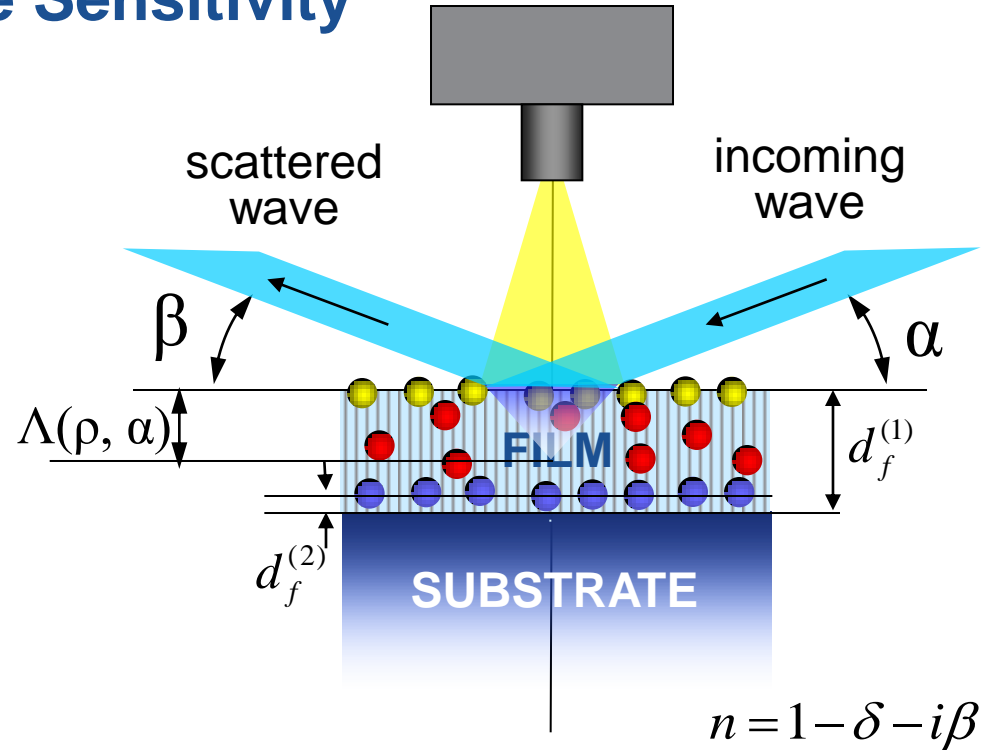
$\perp$  - component  $A^T e^{i(k\alpha^T)z} = A^T e^{ik\text{Re}(\alpha^T)z} e^{-k\text{Im}(\alpha^T)z}$

$$\Lambda = \frac{1}{2k \text{Im}(\alpha^T)}$$

# Surface Sensitivity



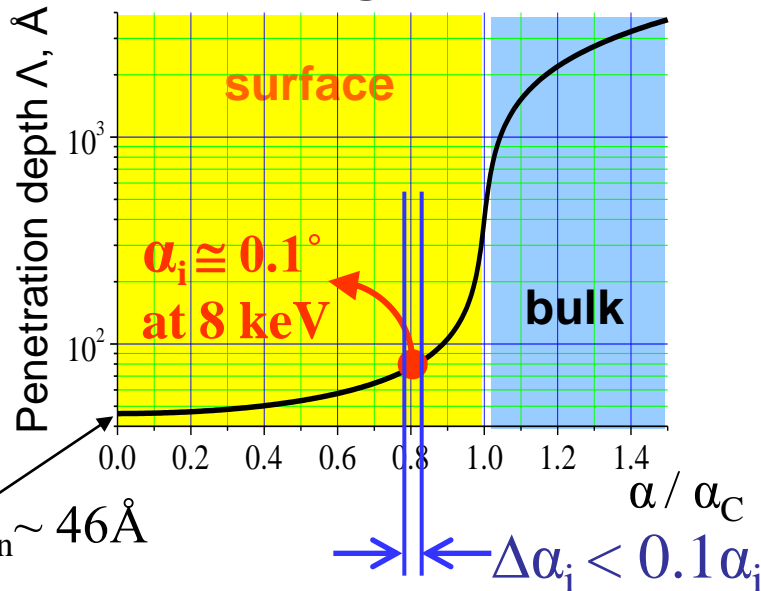
Water @  $\lambda=1.55 \text{ \AA}$



$$\delta = \frac{\lambda^2 \rho r_e}{2\pi} \quad \delta \approx 10^{-6} \quad \alpha_c = \sqrt{2\delta} \quad \alpha_c \sim \text{mrad}$$

$$\Lambda(\alpha) = \frac{\lambda}{2\sqrt{2\pi} \left( \sqrt{(\alpha^2 - \alpha_c^2) + 4\beta^2} - \sqrt{(\alpha^2 - \alpha_c^2)} \right)^{1/2}}$$

$$\text{if } \alpha < \alpha_c, \Lambda = \left( q_c \sqrt{1 - \left( \frac{q}{q_c} \right)^2} \right)^{-1}$$



# Surface Scattering Techniques

## XR

X-ray Reflectivity ( $\alpha = \beta, \gamma = 0$ )

In-depth electron density profile – thickness, density and roughness of films

## GISAXS

Grazing Incidence Small-Angle X-ray Scattering ( $\alpha < \alpha_c, \gamma \geq 0, \beta \geq 0$ )

Particle geometry, size distributions and spatial correlations on nanometer scale

## GID

Grazing Incidence Diffraction ( $\alpha < \alpha_c, \gamma \geq 0, \beta \geq 0$ )

Two dimensional crystals (lattice parameters, molecular structure, tilt angle of molecules, in-plane correlation lengths)

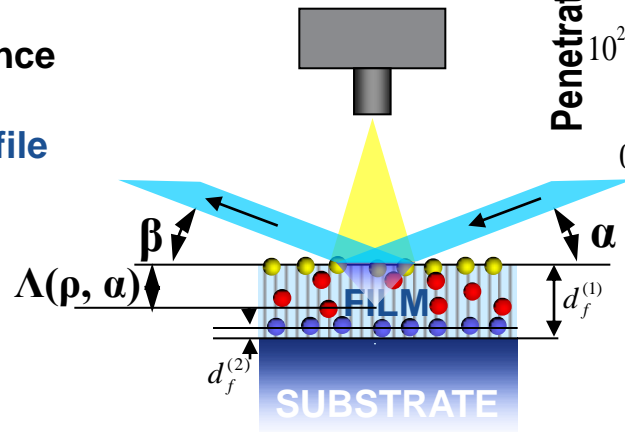
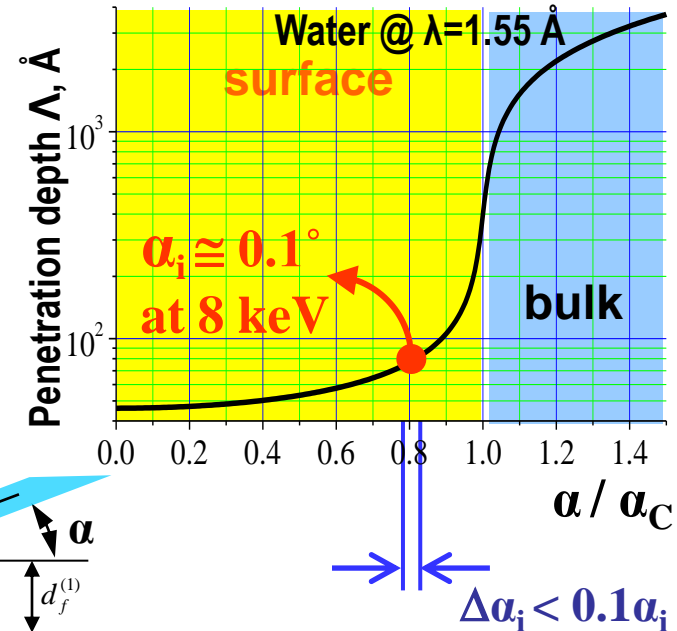
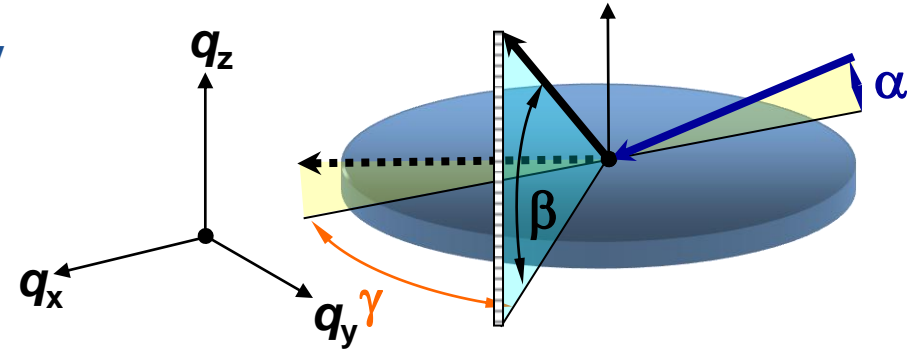
## GIXF

Grazing Incidence X-ray Fluorescence

( $\alpha < \alpha_c, \gamma = 90^\circ$ )

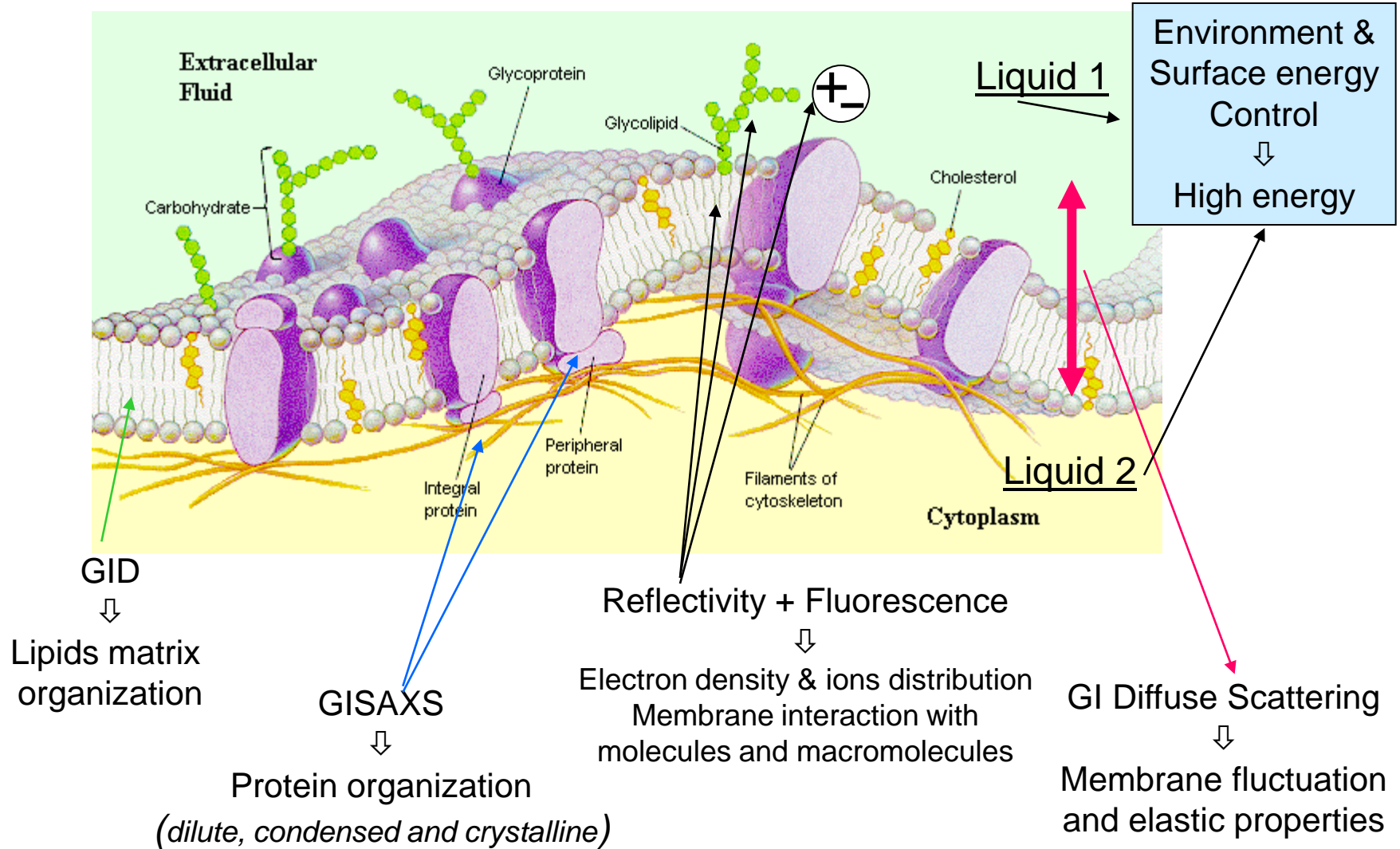
In-depth elemental distribution profile

$$q = \frac{2\pi}{\lambda} \begin{Bmatrix} \cos \beta \cos \gamma - \cos \alpha \\ \cos \beta \sin \gamma \\ \sin \beta + \sin \alpha \end{Bmatrix}$$

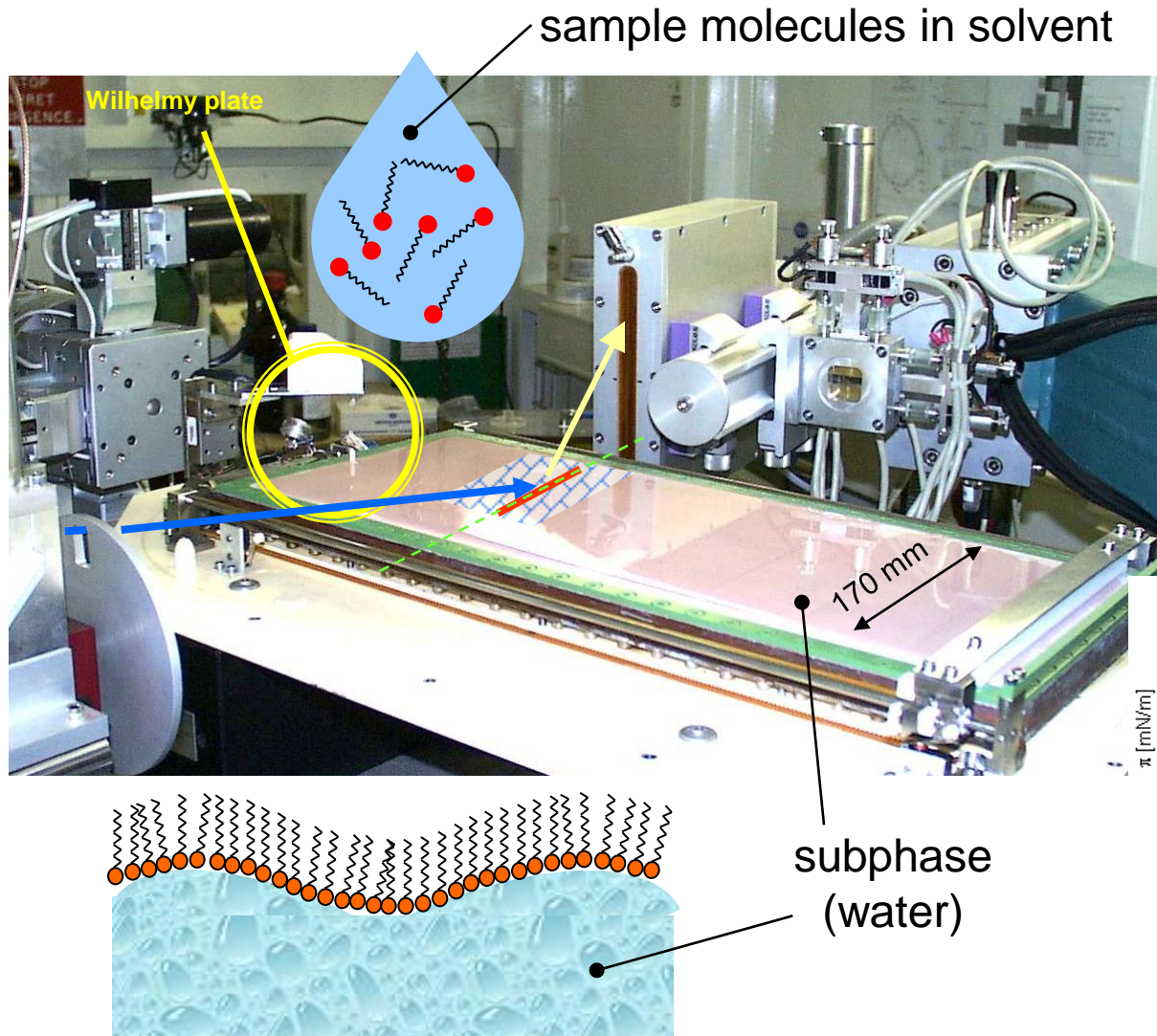




# Cell Membrane ↔ Surface Scattering Methods



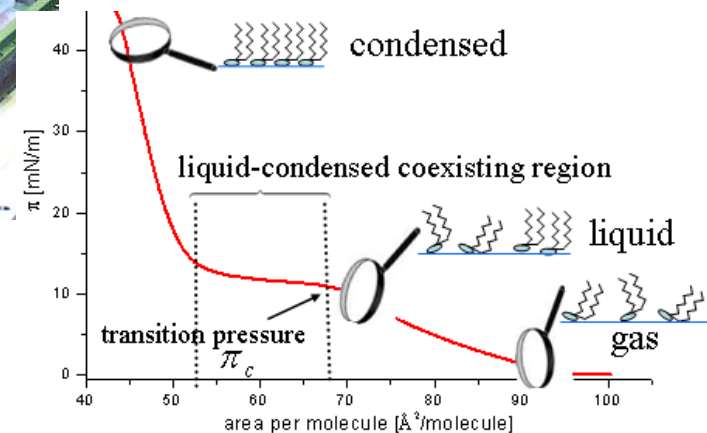
# Surface scattering on membranes mimicked with Langmuir method



Control  
area per molecule  
(i.e. surface pressure)  
temperature

phase transition:  
gas – liquid – crystal

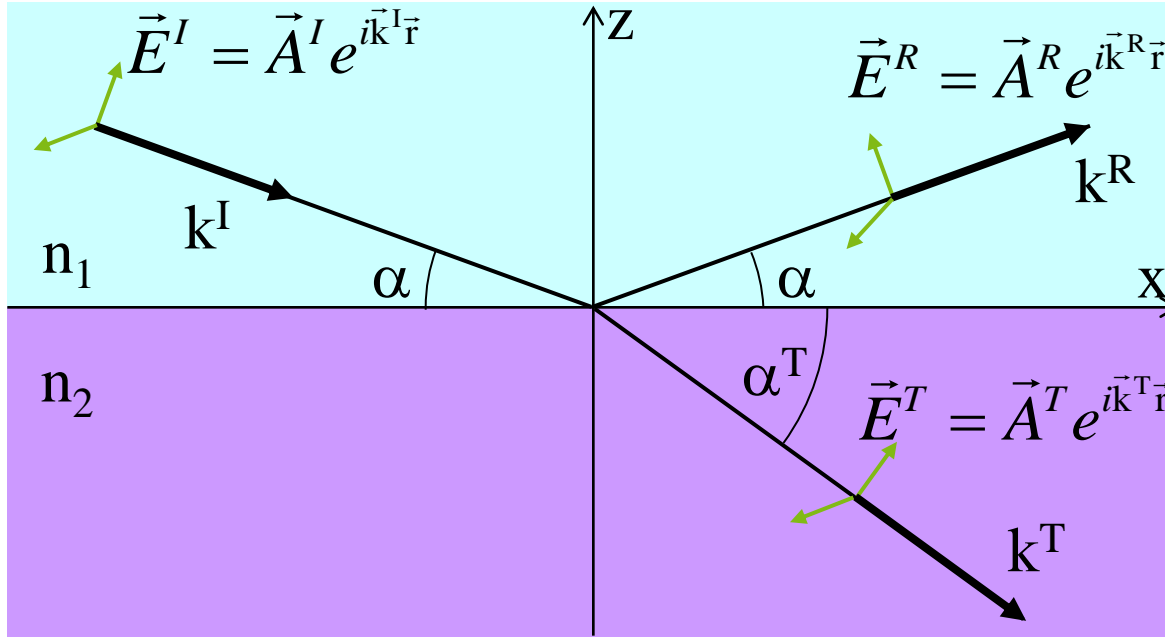
$\alpha_i = 2$  mrad  
foot print at 100  $\mu\text{m}$  beam is 50 mm



# Рентгеновская Рефлектометрия

## X-Ray Reflectivity

## Fresnel Formulas



Wave and its derivative are continuous at  $z=0$

$$A^I + A^R = A^T$$

$$A^I \vec{k}_I + A^R \vec{k}_R = A^T \vec{k}_T$$

$$k = |\vec{k}_I| = |\vec{k}_R| \quad nk = |\vec{k}_T|$$

$$\frac{\cos \alpha}{\cos \alpha^T} = \frac{n_2}{n_1} = n = 1 - \delta - i \cdot \beta$$

$$r_{\perp} = \frac{A_{\perp}^R}{A_{\perp}^I} = \frac{n_1 \sin \alpha - n_2 \sin \alpha^T}{n_1 \sin \alpha + n_2 \sin \alpha^T} = \frac{\sin \alpha - \sqrt{n^2 - \cos^2 \alpha}}{\sin \alpha + \sqrt{n^2 - \cos^2 \alpha}} \approx \frac{\sin \alpha - \sqrt{\sin^2 \alpha - 2\delta}}{\sin \alpha + \sqrt{\sin^2 \alpha - 2\delta}}$$

$$t_{\perp} = \frac{A_{\perp}^T}{A_{\perp}^I} = \frac{2n_1 \sin \alpha}{n_1 \sin \alpha + n_2 \sin \alpha^T}$$

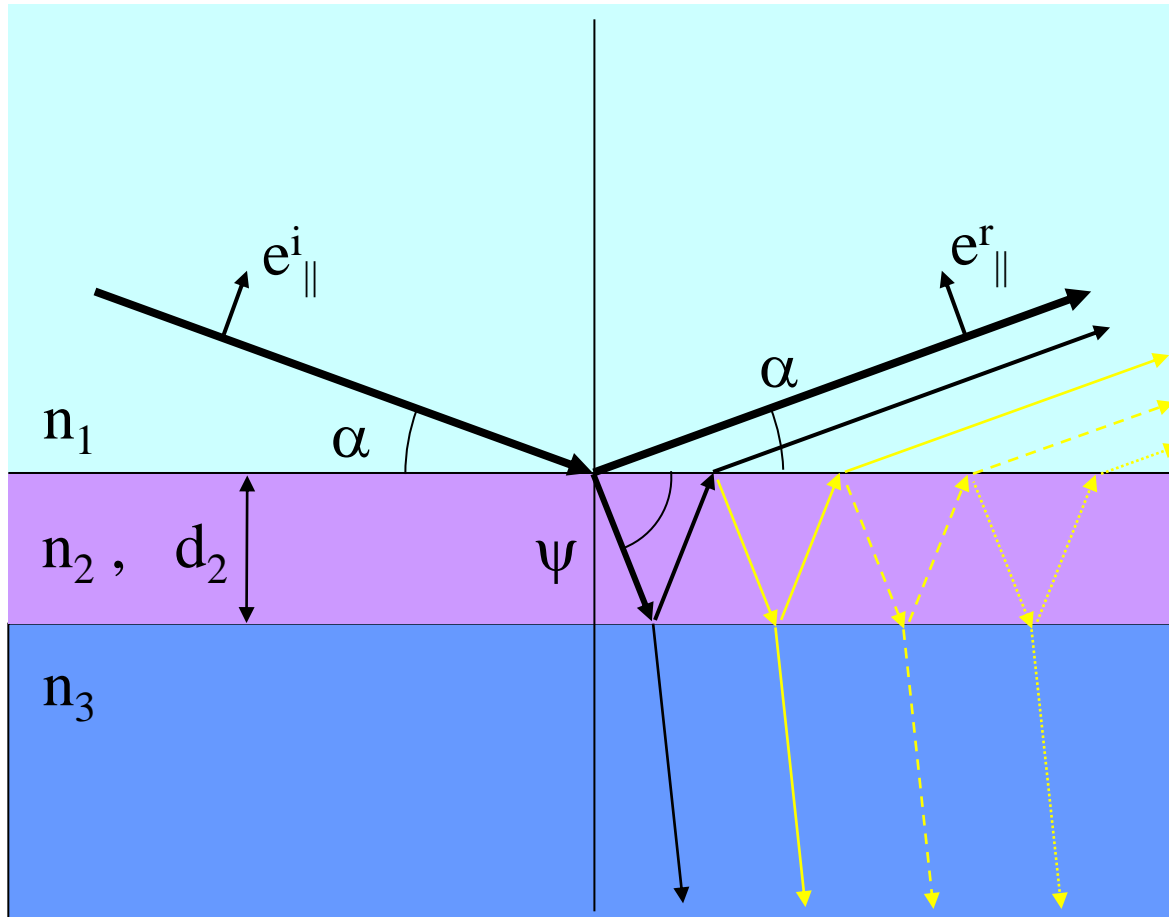
$$r_{\parallel} = \frac{A_{\parallel}^R}{A_{\parallel}^I} = \frac{n_2 \sin \alpha - n_1 \sin \alpha^T}{n_2 \sin \alpha + n_1 \sin \alpha^T}$$

$$t_{\parallel} = \frac{A_{\parallel}^T}{A_{\parallel}^I} = \frac{2n_1 \sin \alpha}{n_2 \sin \alpha + n_1 \sin \alpha^T}$$

$$2\delta = \sin^2 \alpha_c$$

$$\alpha_c \approx \sqrt{2\delta} = \sqrt{\pi^{-1} \lambda^2 r_e \rho_{el}}$$

## Reflectivity from homogeneous layer



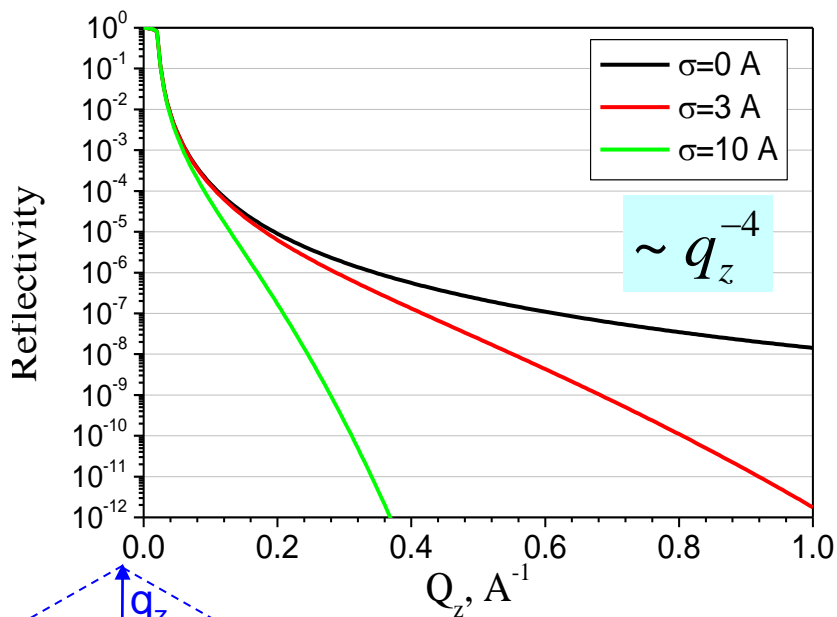
$$r_{\perp}^{1,2} = \frac{n_1 \sin \alpha - n_2 \sin \psi}{n_1 \sin \alpha + n_2 \sin \psi}$$

$$r_{\perp}^{eff} = \frac{r_{\perp}^{1,2} + r_{\perp}^{2,3} X}{1 + r_{\perp}^{1,2} r_{\perp}^{2,3} X}$$

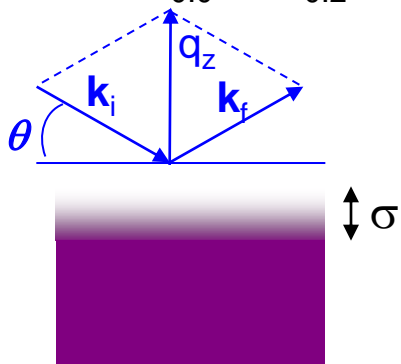
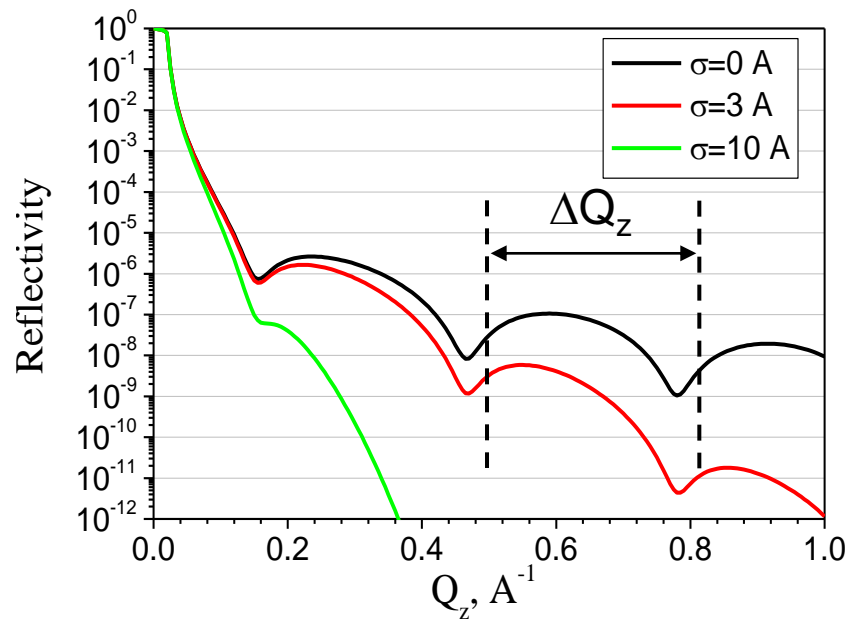
$$X = e^{-\frac{i4\pi d_2 n_2 \sin \psi}{\lambda}}$$

# Typical Examples of Reflectivity Curves

air/water interface



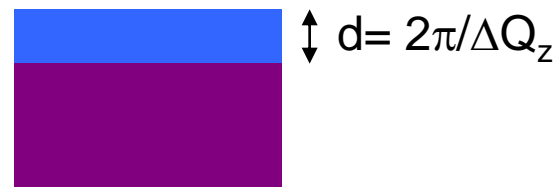
film on water (thickness  $d=20\text{\AA}$ )



$$q_z = \frac{4\pi}{\lambda} \sin \theta$$

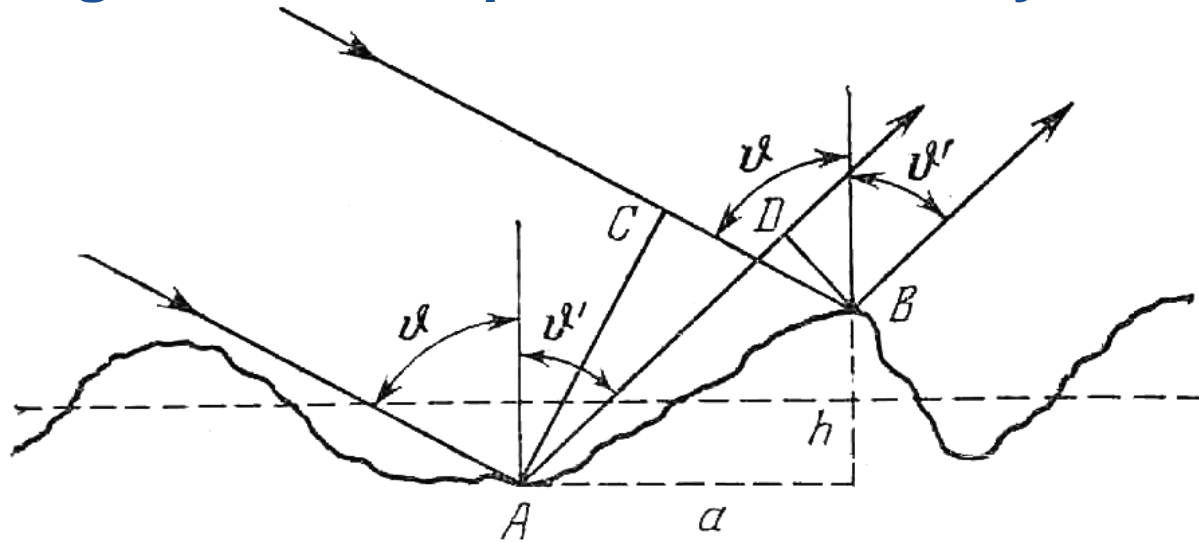
$$F_{1,2} = \frac{\eta_1 - \eta_2}{\eta_1 + \eta_2}$$

$$\eta_j = \sqrt{\sin^2 \theta - 2(\delta_j + i\beta_j)}$$





## Roughness and specular reflectivity limitation



$$\Delta = AD - BC = a(\sin \vartheta' - \sin \vartheta) + h(\cos \vartheta' + \cos \vartheta)$$

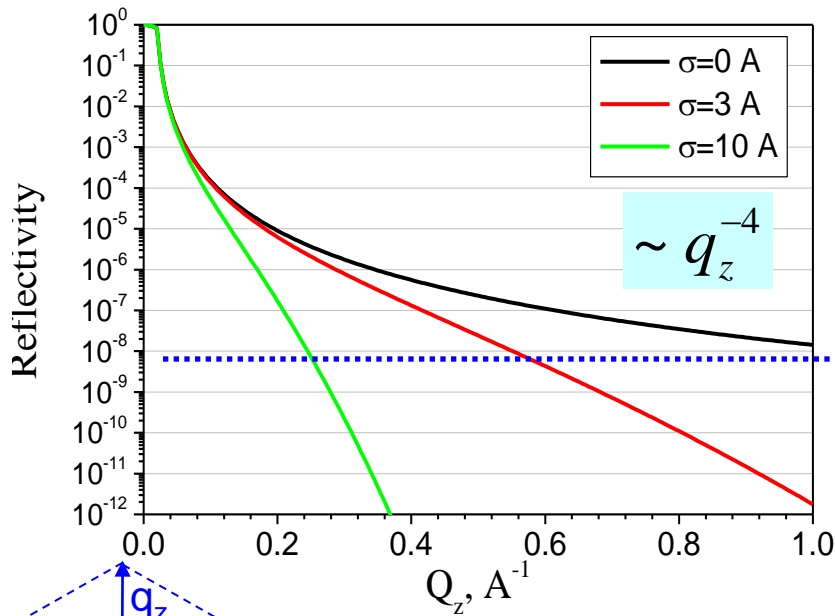
$$\vartheta' = \vartheta \quad \Delta = 2h \cos \vartheta \quad \theta = \pi/2 - \vartheta$$

$$\Delta = 2h \sin \theta \quad \langle \langle \lambda \leq \lambda/n \rightarrow \sin \theta = \frac{\lambda}{2nh}$$

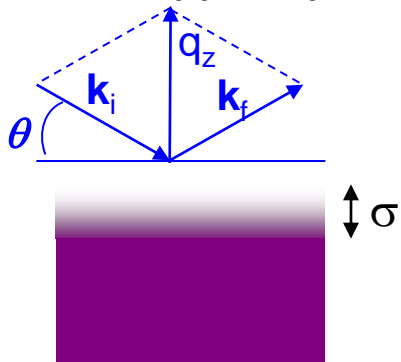
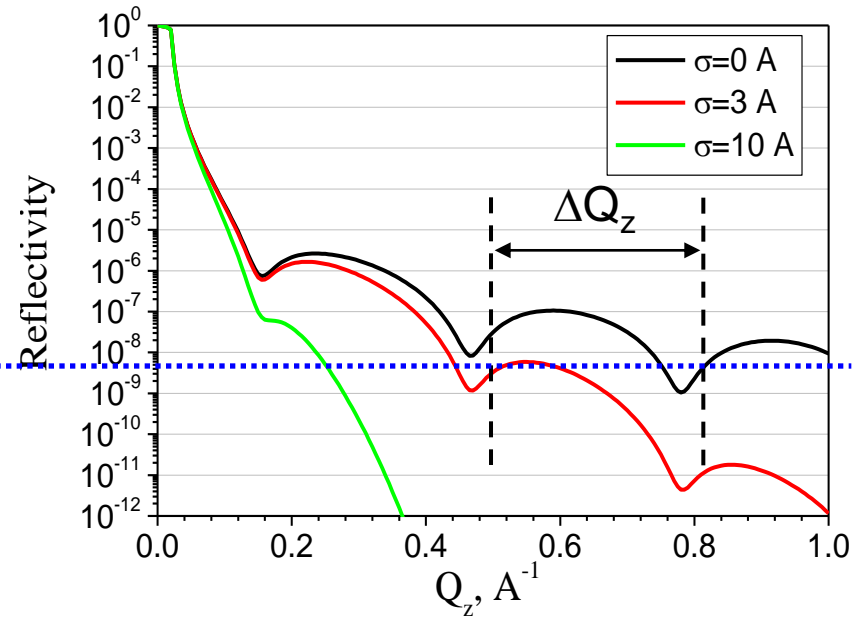
$$q_z^{\max} = \frac{4\pi}{\lambda} \sin \theta_{\max} = \frac{2\pi}{nh} \approx 0.52 \text{ \AA}^{-1} \quad / \text{ at } n = 4 \text{ \& } h = 3\text{\AA}$$

# Roughness and specular reflectivity limitation

air/water interface



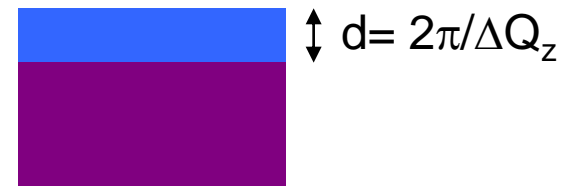
film on water (thickness d=20A)



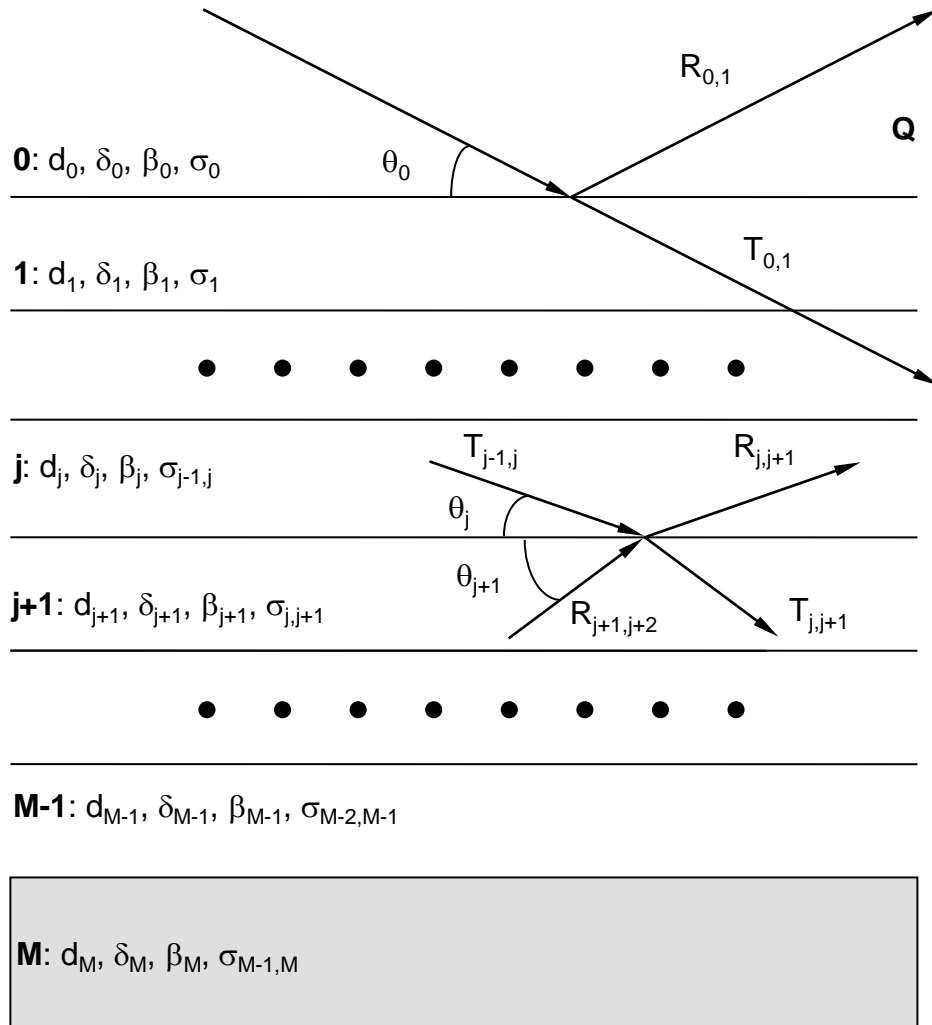
$$q_z = \frac{4\pi}{\lambda} \sin \theta$$

$$F_{1,2} = \frac{\eta_1 - \eta_2}{\eta_1 + \eta_2}$$

$$\eta_j = \sqrt{\sin^2 \theta - 2(\delta_j + i\beta_j)}$$



## Reflectivity calculation (*Parratt version*)



Reflectivity is  $I(q) = |R_{0,1}(q)|^2$ ,  
where  $R_{0,1}(q)$  is calculated from  
recursive formula

$$R_{n-1,n} = a_{n-1}^4 \cdot \left| \frac{R_{n,n+1} + F_{n,n-1}}{1 + R_{n,n+1}F_{n-1,n}} \right|$$

$$R_{n,n+1} = a_n^2 \times E_n^R / E_n,$$

$$F_{n-1,n} = (\eta_{n-1} - \eta_n) / (\eta_{n-1} + \eta_n),$$

$$\eta_n = (N_n^2 + \cos^2(\theta)) / 2,$$

$$a_n = \exp(-ik\eta_n d_n / 2),$$

$$n = 0, 1, 2, \dots, M; k = 2\pi/\lambda,$$

$\lambda$  - wave length,

$E_n, E_n^R$  - amplitudes of transmitted and  
reflected fields in the layer  $n$ ,

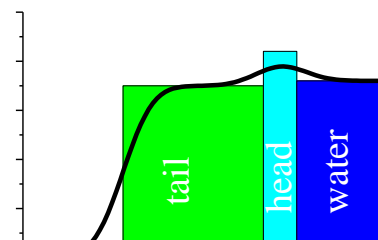
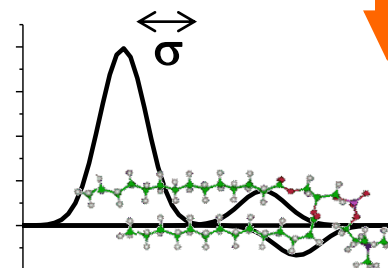
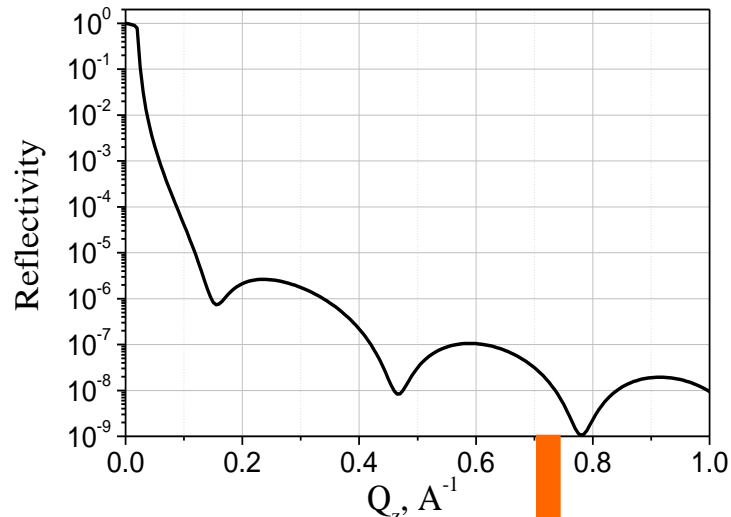
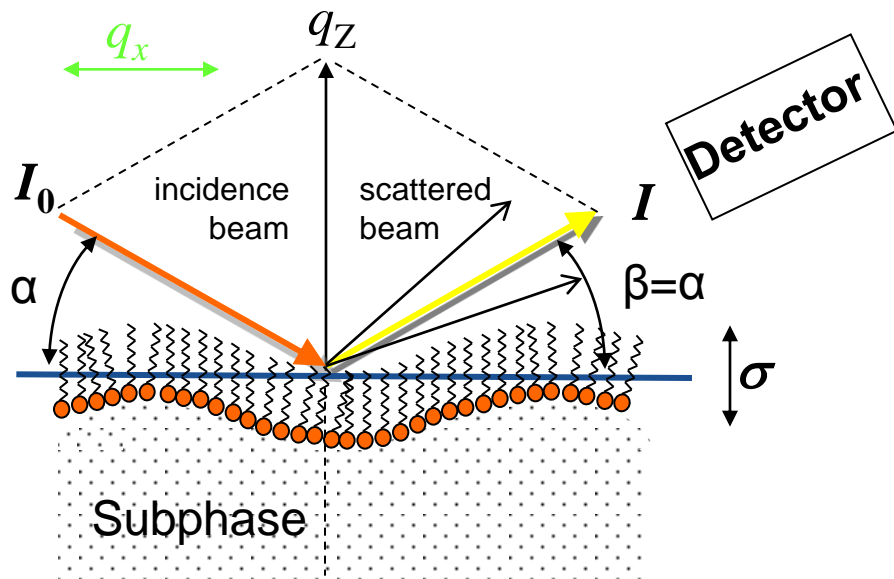
$d_n$  - thickness of layer  $n$ , material index

$$N_n = 1 - \delta_n - i \times \beta_n;$$

$n = M$  for substrate,

$$R_{M,M+1} = 0.$$

# X-ray Reflectivity Principle



$$I/I_0 = R_F(q_z) |F(q_z)|^2 \exp(-(q_z \sigma)^2)$$

where

$$q_z = 4\pi \sin(\alpha)/\lambda$$

$|F(q_z)|$  = Fourier transform of  $\partial\rho(z)/\partial z$

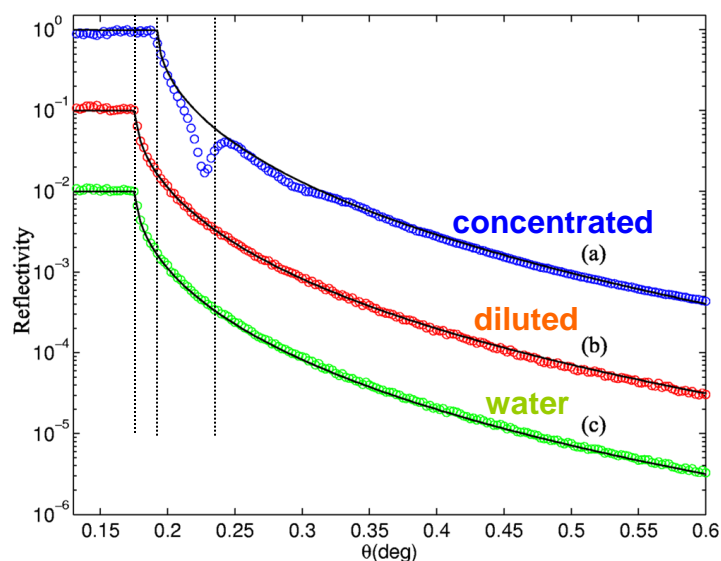
$$R_F(q_z) = \left(\frac{2\pi}{\lambda}\right)^2 \left| \frac{\sin \alpha - \sqrt{\sin^2 \alpha - \sin^2 \alpha_c}}{\sin \alpha + \sqrt{\sin^2 \alpha - \sin^2 \alpha_c}} \right|^2$$

# Layering of Nano-Particles at the Air/Water Interface

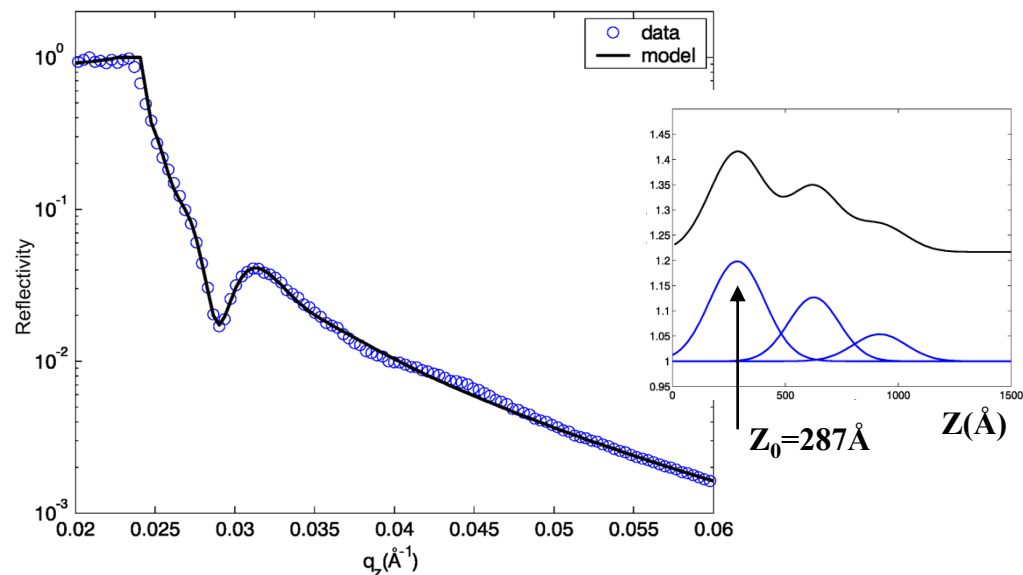
**Sample:** Colloidal suspension of spherical Silica particles (diameter  $\sim 320\text{\AA}$ ) in water a suspension. (Concentrated 40% and dilute 1.8% of weight)

**Aim :** Study of structure organization of nano-particles near air/water interface.

**X-ray reflectivity profiles from the concentrated (a) and dilute sample (b) and from the solvent (c).**



The (b) and (c) curves have been offset by one and two decades respectively. The solid lines are fits of Fresnel's law to the data.



Detailed view of the profile from the concentrated sample and a model fit (solid line) with the SLD profile yielding the best fit shown in the insert)

# Lipid monolayers on water, sol and gel surface

## I) Gelation of clays

### Montmorillonite

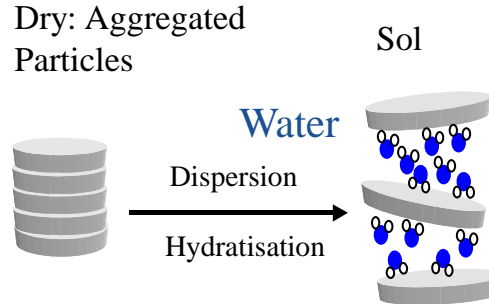
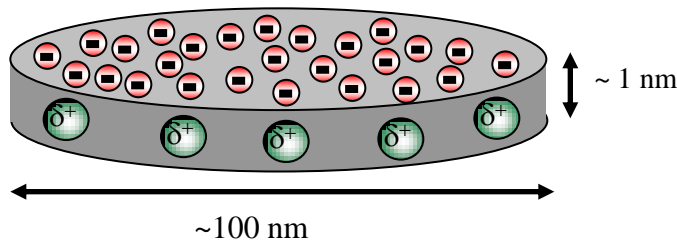
Used as additive in many industrial processes

#### The Mineral

- Phyllosilicate
- Disc shaped nano particles
- Surface area  $\sim 400 \text{ m}^2/\text{g}$
- Charge deficiency of 0.7 / unit cell
- Charging: surface  $\ominus$ , edges  $\bullet$
- With water: gives clear and colourless dispersions and gels

#### The Gel

- Thixotropic, highly viscous
- Ionic bonds, not affected by temperature
- Gel Formation at concentrations  $< 1\%$  in water

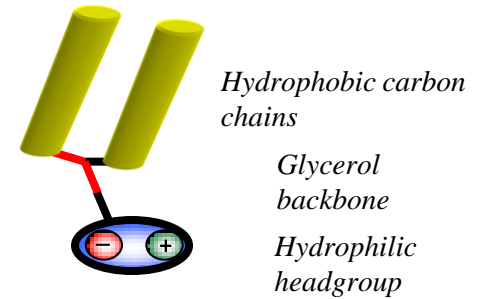


After some hours:  
Gel formation – House of cards

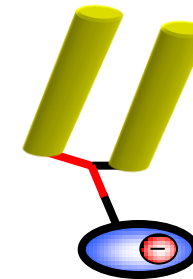


## II) Phospholipids

### DSPC



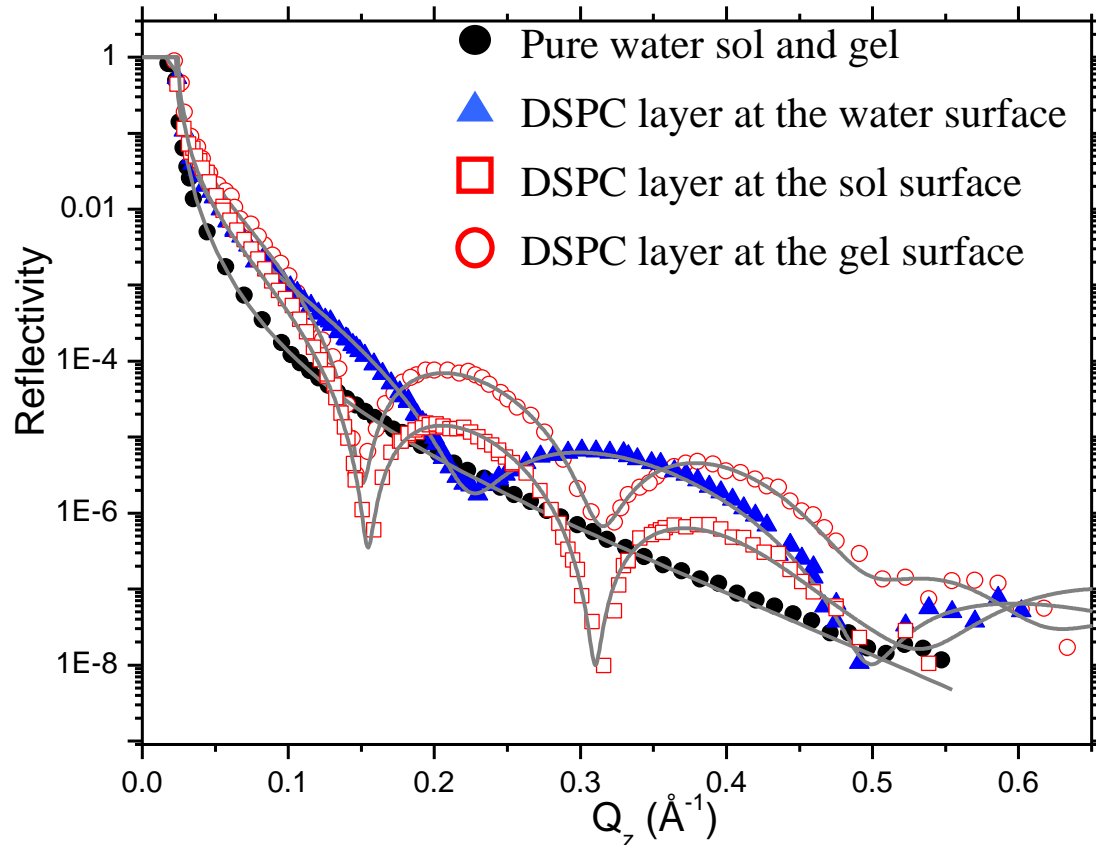
### DPPA



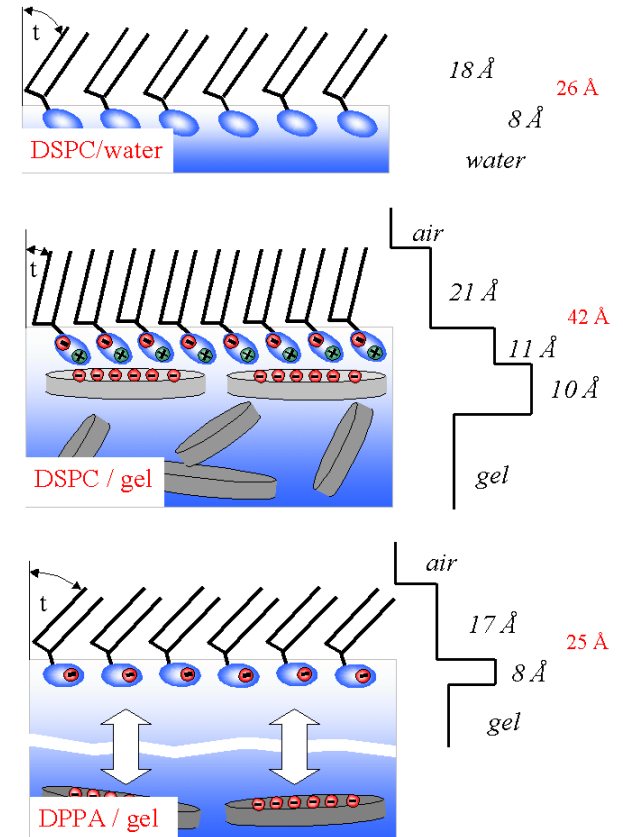
Struth B., et.al. Phys. Rev. Let., 88, 25502, (2002)



# Lipid monolayers on water, sol and gel surface

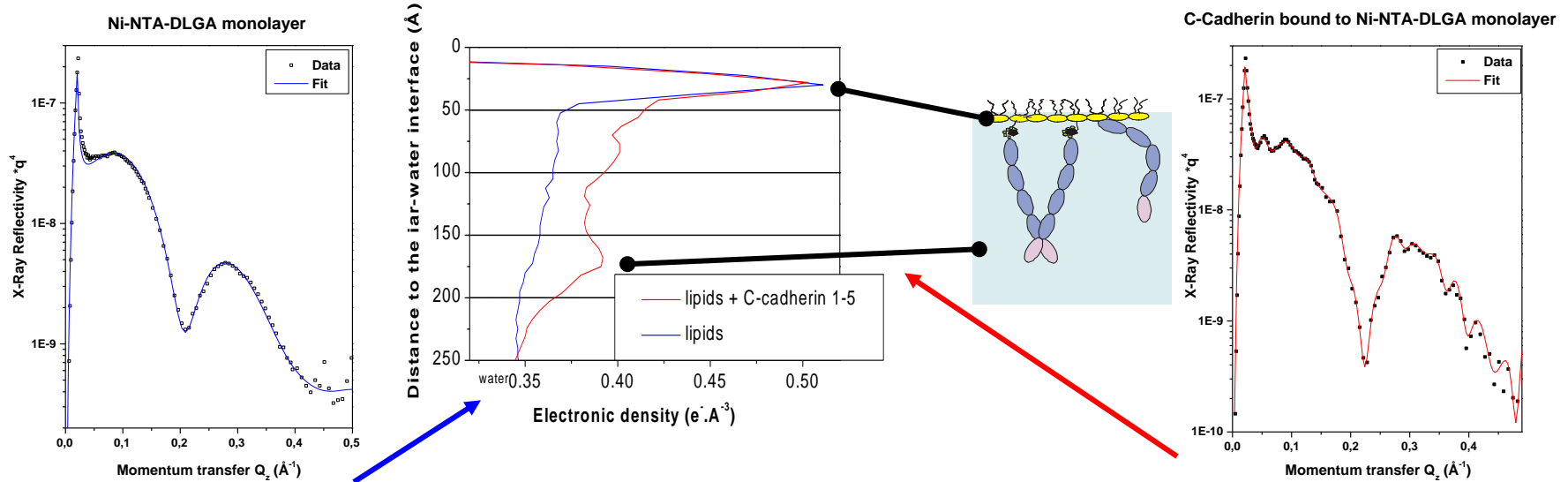


- Identical roughness of free water, sol and gel surfaces
- Lipids form stable monolayers on water, sol and gel
- Attractive electrostatic interactions between the anionic mineral particles and the zwitterionic lipid headgroup
- These interactions influence the lateral lattice of the monolayer



Struth B., et.al. Phys. Rev. Let., 88, 25502, (2002)

# Reflectivity measured and model of electron density profile before and after injection of C-cadherin in the subphase

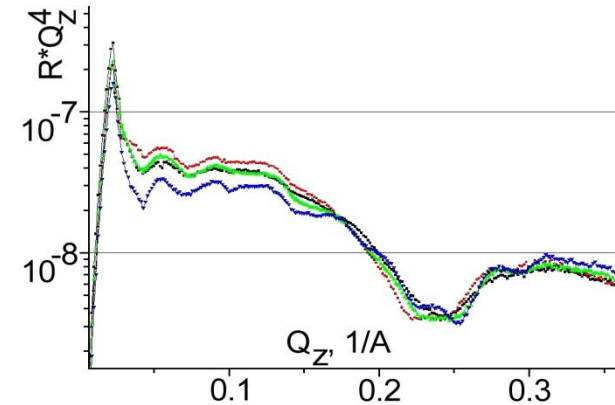


- Cadherins extend over 230Å. That is shorter than cadherin length : cadherin may **be curved**
- High density at large distance : **parallel interactions ?**

Initial state    After EGTA    After Ca<sup>2+</sup>

- 1) After injecting proteins in the subphase, a homogenous layer is obtained in 4 hours
- 2) The decrease of bound proteins after adding chelates divalent ions EGTA is interpreted as a partial dissociation of adhesive dimers
- 3) Subsequent addition of calcium restores the dimers

## Ca influence



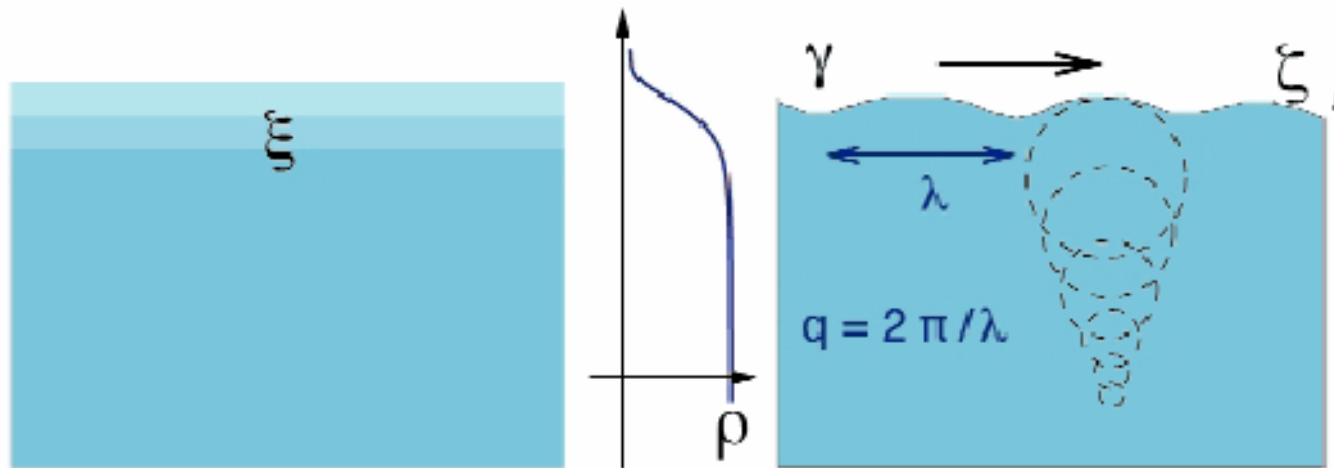
L. Martel, et. al., J. Phys. IV France, v.12, 365 (2002)

# Grazing Incidence Diffuse Scattering

# Liquid-Vapour Interfaces at Short Length Scales

Liquid-vapour interfaces, are common in both natural and artificial environments

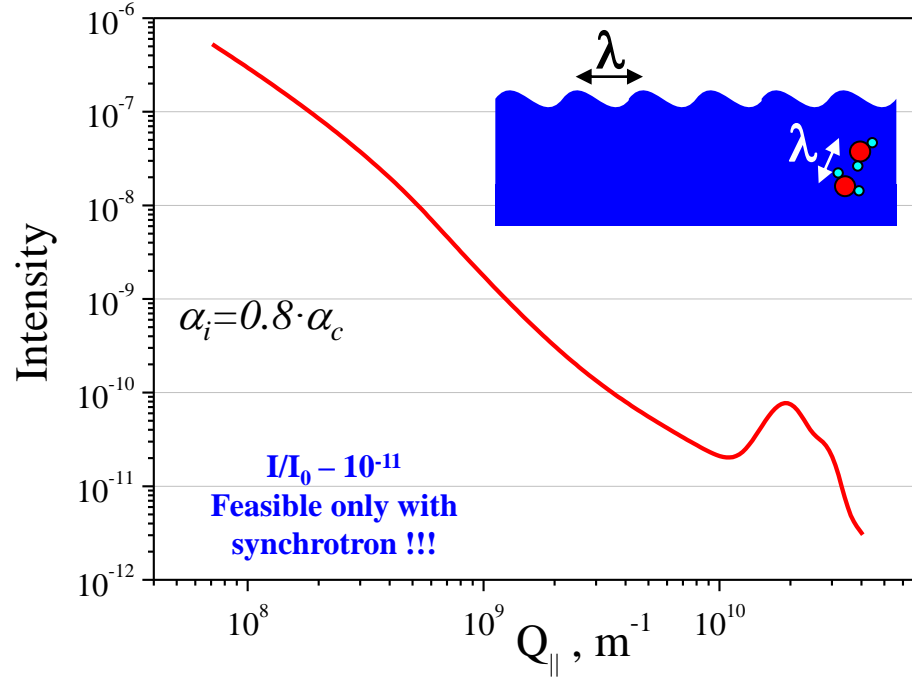
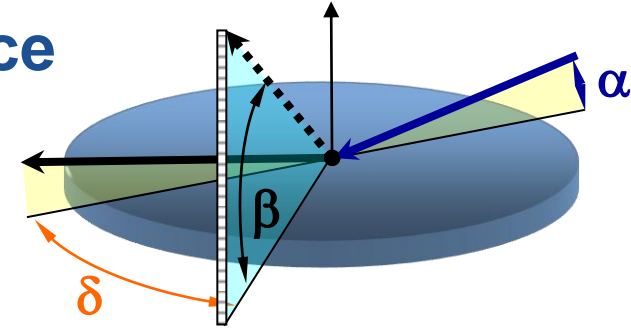
Liquid-vapour interfaces were first described, in 1893 by van der Waals, as regions of continuous variation of density caused by density fluctuations within the bulk phases. In contrast, the more recent capillary-wave model (1965, F.P.Buff, R.A.Lovett, R.H.Stillingir)) assumes a step-like density profile across the liquid-vapour interface, whose width is the result of the propagation of thermally excited capillary waves.



The model has been validated for length scales of tens of micrometres and larger, but the structure of liquid surfaces on submicrometre length scales, where the capillary theory is expected to break down, remains poorly understood. One reason is that, in contrast to solid surfaces, the absence of relevant experimental information even for the simplest liquid-vapour interfaces precludes the assessment of any of the existing theories which considerably diverge in their conclusions

*C. Fradin et al., Nature, 403, 871-874, (2000)*

# Diffuse scattering on liquid surface



Capillary waves -> height correlation spectrum determined by the **surface energy** ( $\gamma$ ) associated with the **deformation modes** ( $\kappa$ ) [Helfrich, *Z. Naturforsch.*, 28c, 693, (1973)]

$$\langle z(q_{\parallel})z(-q_{\parallel}) \rangle = \frac{1}{A} \frac{k_B T}{\Delta \rho g + \gamma q_{\parallel}^2 + \kappa q_{\parallel}^4}$$

$$\left( \frac{d\sigma}{d\Omega} \right) \approx A \frac{k_0^4 \theta_c^4}{16\pi^2} |t_{0,1}^{in}|^2 |t_{0,1}^{sc}|^2 \left[ \frac{k_B T}{\gamma q_{\parallel}^2} \left( \frac{q_{\parallel}}{q_{\max}} \right)^\eta + \frac{k_B T \kappa_T}{2 \text{Im}(q_z^t)} \right]$$

C. Fradin et al., *Nature*, **403**, 871-874, (2000)

conformal roughness

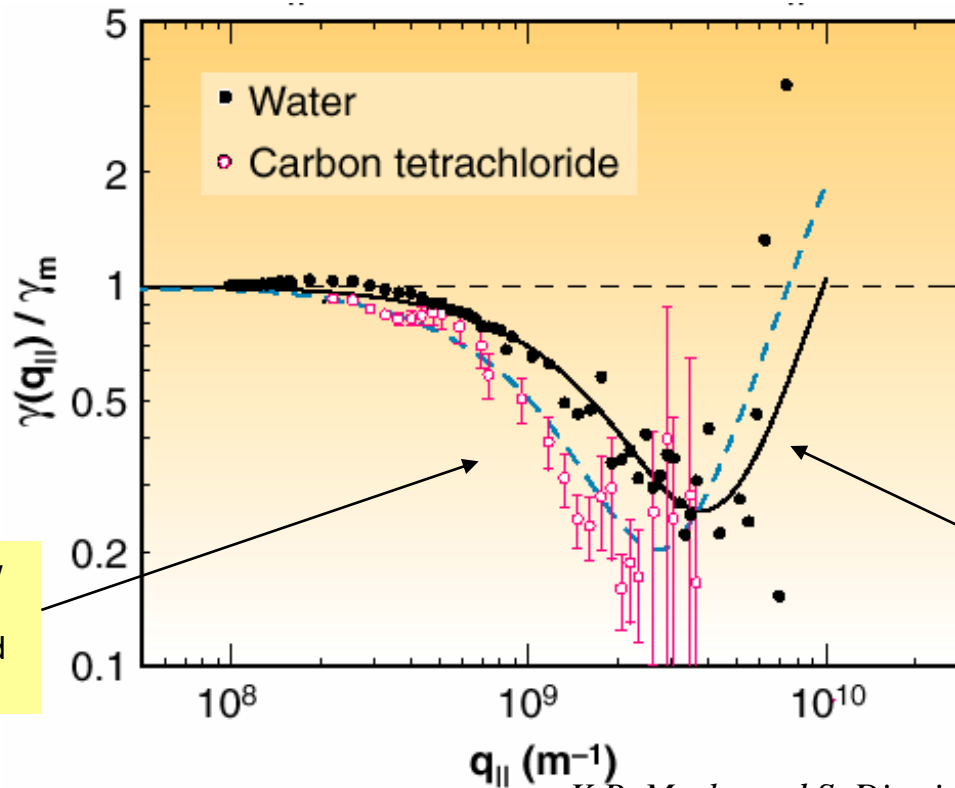


$$\frac{d\sigma}{d\Omega} \approx A r_e^2 |t_{0,1}^{in}|^2 |t_{0,1}^{sc}|^2 |\tilde{\rho}(q_z)| e^{-q_z^2 \langle z^2 \rangle} \int d\mathbf{r}_{\parallel} \left( e^{q_z^2 \langle z(0)z(\mathbf{r}_{\parallel}) \rangle} - 1 \right) e^{i\mathbf{q}_{\parallel} \cdot \mathbf{r}_{\parallel}}$$

# Scale-dependent surface tension

Using grazing-incidence X-ray scattering, the first complete determination of the free surface structure and of the wavevector-dependent surface energy for water and organic liquids was obtained.

**Observed**  $\Rightarrow$  A large decrease of the surface energy of sub-micrometer waves, which cannot be explained by the phenomenological capillary theories, and which is decisive in the long-standing dispute on structure of liquid interfaces.



Long-ranged power-law decay of the dispersion forces between the fluid particles

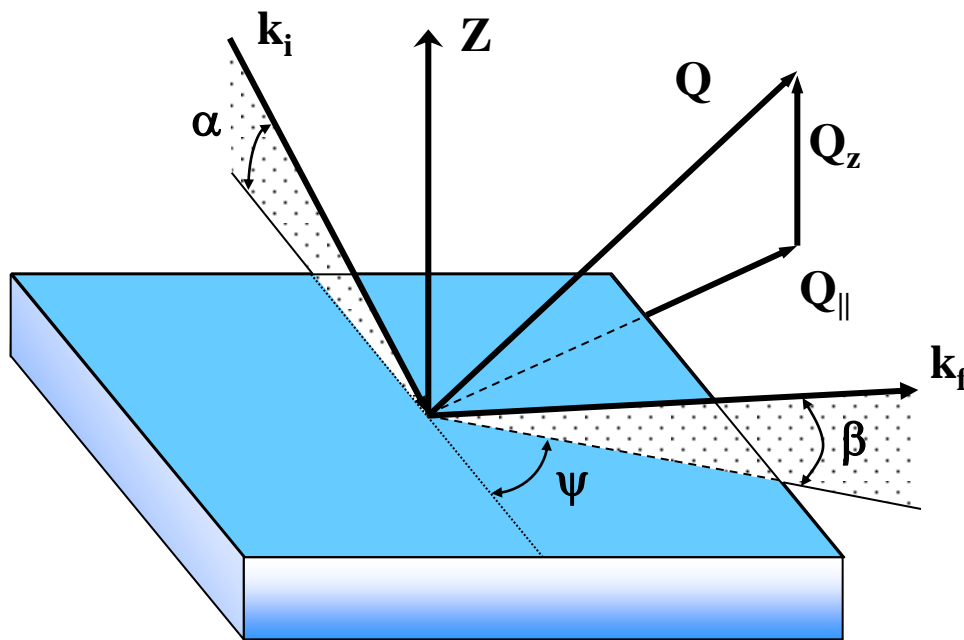
Distortion of density profile when surface is bent

*K.R. Mecke and S. Dietrich, Phys. Rev. E., v.59, 6766 (1999)*



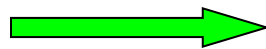
# Grazing Incidence Diffraction

*(Two dimensional crystals)*



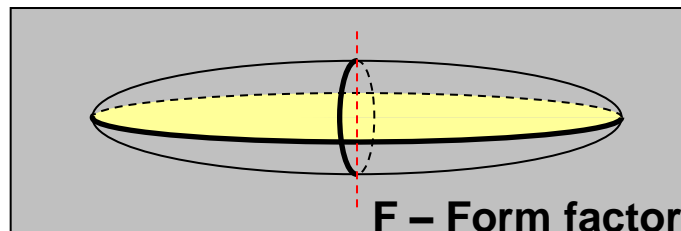
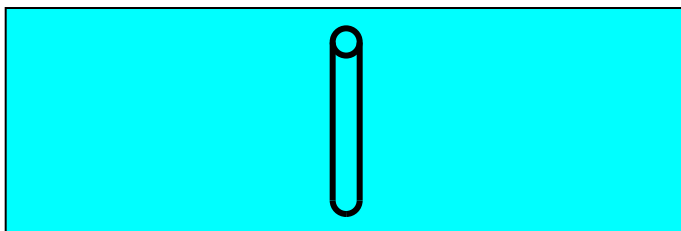
# Diffraction from 2D array of rodlike molecules

Real space

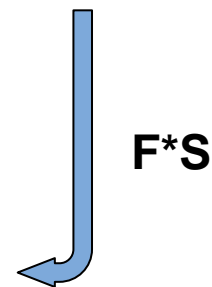
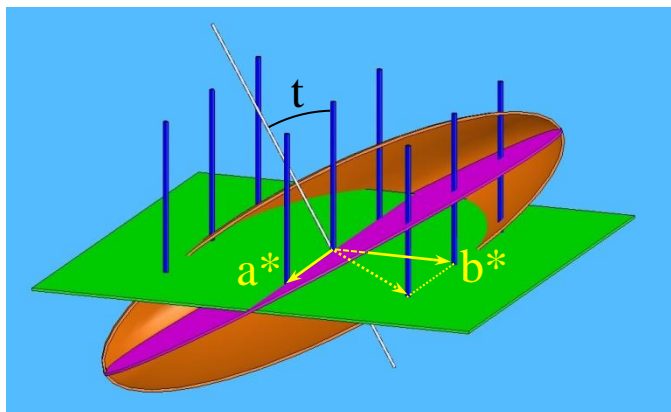
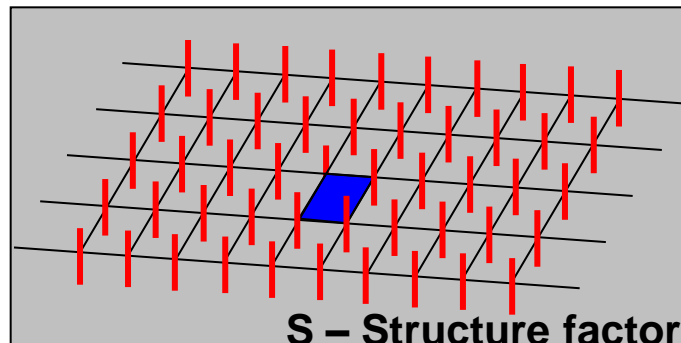
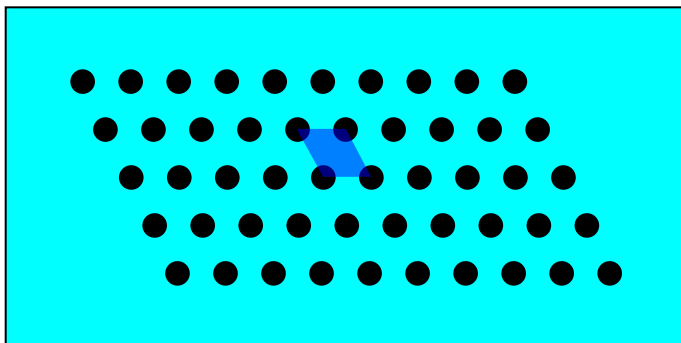


Reciprocal space

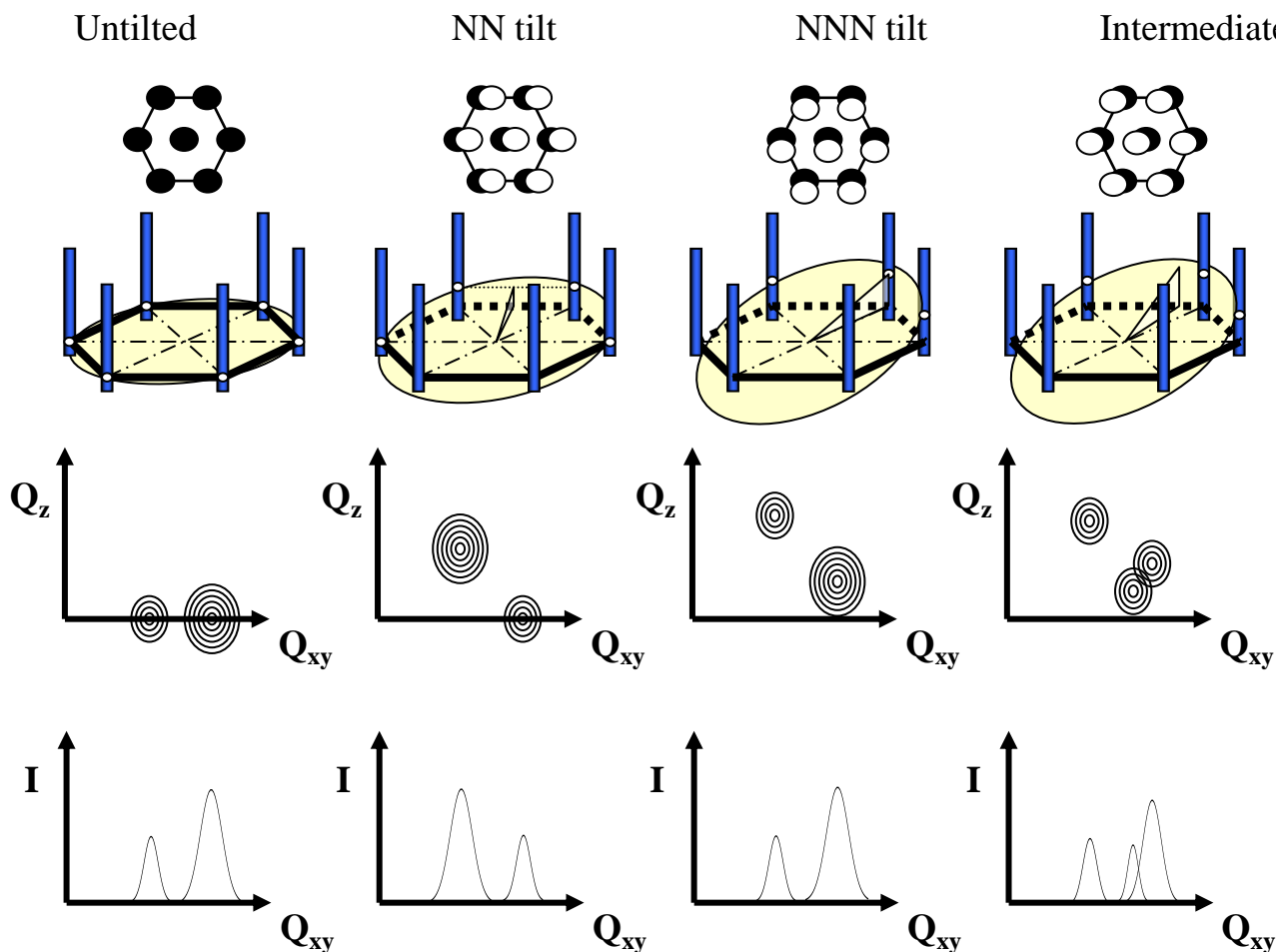
Rod like molecule



2D lattice



# GI Diffraction from 2D array of rodlike molecules

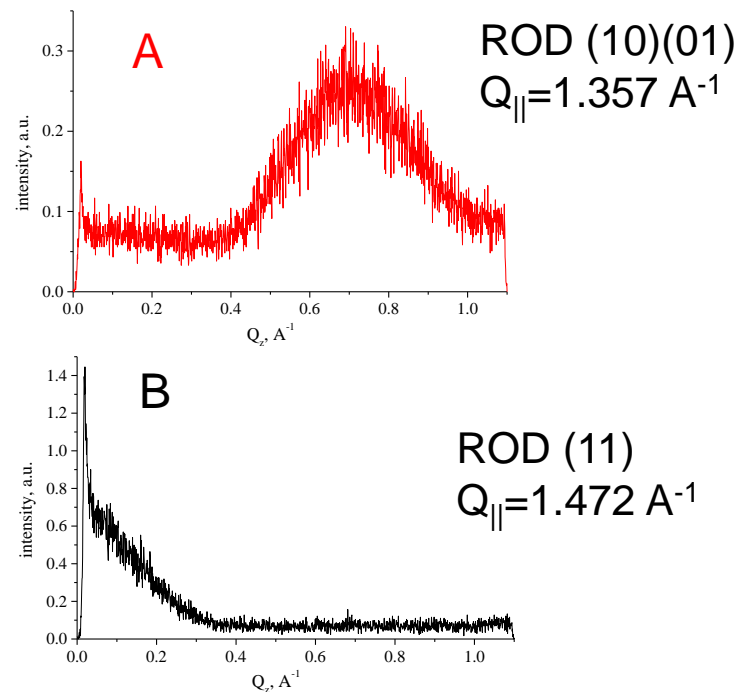
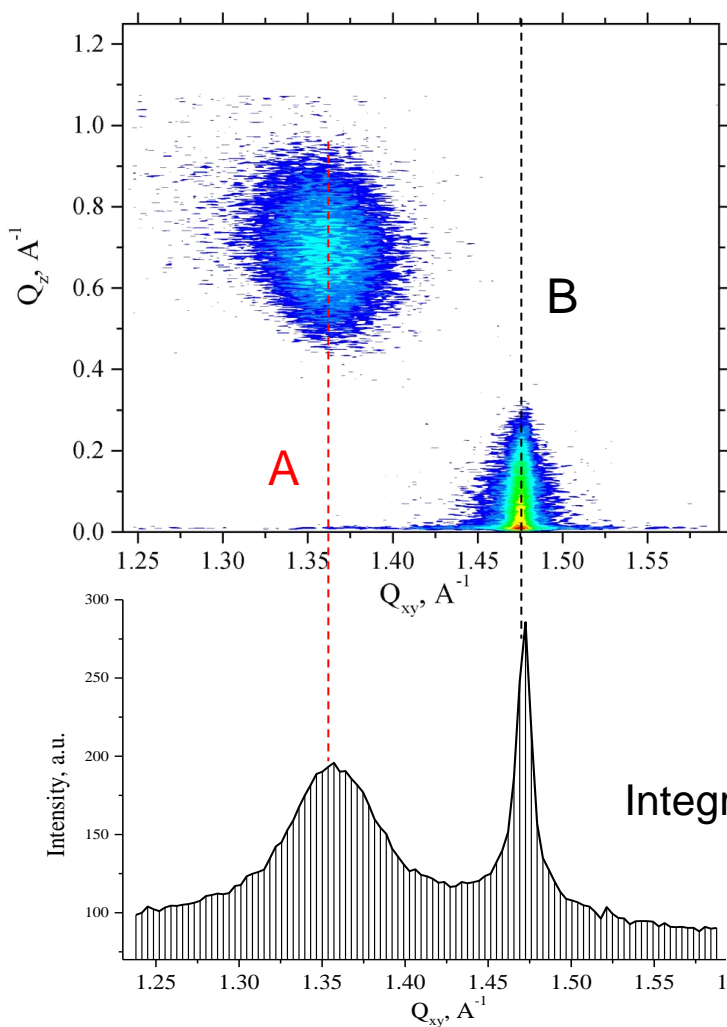


**Output:**

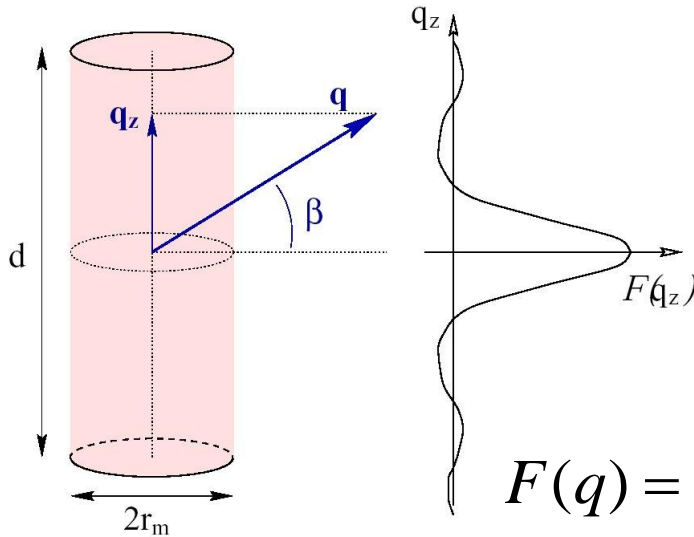
Lattice parameters, tilt angle & azimuth, correlation length, molecular length and structure.

*Kaganer et al., Reviews of Modern Physics, 71 (1999) 779*

# Typical GID map obtained on monomolecular film of lipids DPPC at 30 mN/m on the air/water interface



## Molecular form factor



$$F(q) = \int_0^{r_m} \int_{-\pi}^{\pi} \int_{-d/2}^{d/2} \rho_e e^{iqr} r dr d\alpha dz$$

$$F(q) = 2\pi d \rho_e \frac{\sin(qd \sin(\beta) / 2)}{qd \sin(\beta) / 2} \int_0^{r_m} r J_0(qr \cos \beta) dr$$

if  $J_0(qr \cos \beta) \approx 1$  (@  $qr_m \cos(\beta) \ll 1$ ) and  $Z_m = \pi r_m^2 d \rho_e$

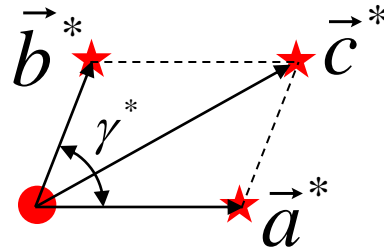
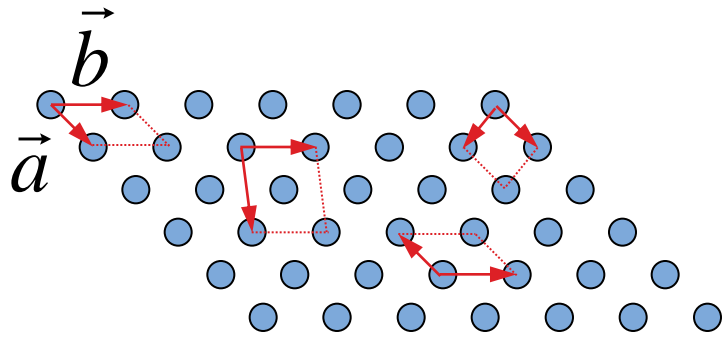
$$F(q) = Z_m \frac{\sin(qd \sin(\beta) / 2)}{qd \sin(\beta) / 2}$$

$$I(q_z) \approx \left( \frac{\sin((q_z - q_{zM})t / 2)}{q_z t / 2} \right)^2$$

t – film thickness

# What to do with measured Bragg rods $Q_1(\parallel, \perp)$ $Q_2(\parallel, \perp)$ $Q_3(\parallel, \perp)$ ?

(simple way to solve 2D structure)



$$\vec{c} = \vec{a} + \vec{b}$$

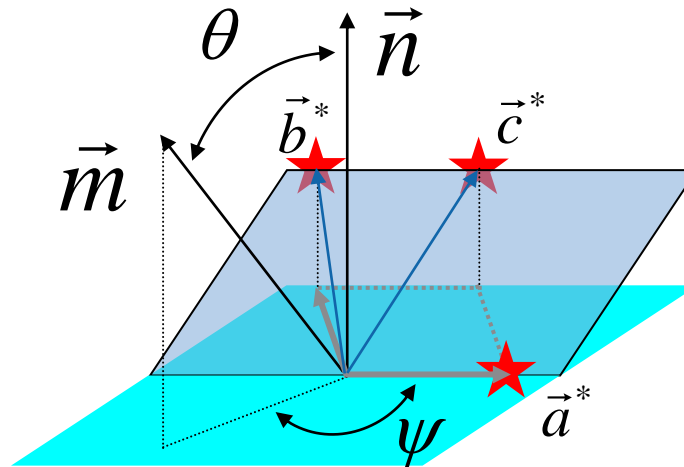
$$\gamma^* = \pi - \gamma$$

$$c_{\parallel}^{*2} = a_{\parallel}^{*2} + b_{\parallel}^{*2} - 2a_{\parallel}^* b_{\parallel}^* \cos \gamma$$

$$\vec{m} = (\vec{a}^* - \vec{b}^*) \times (\vec{c}^* - \vec{b}^*)$$

$$\vec{m} \cdot \vec{n} = |\vec{m}| \cdot |\vec{n}| \cos \theta$$

$$\vec{m}_{\parallel} \cdot \vec{a} = |\vec{m}_{\parallel}| \cdot |\vec{a}| \cos \psi$$

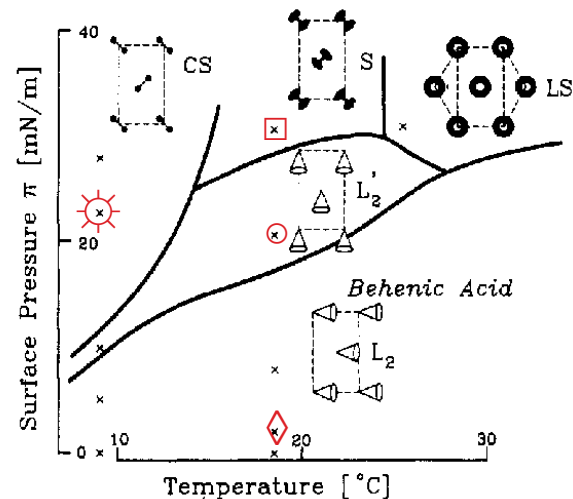
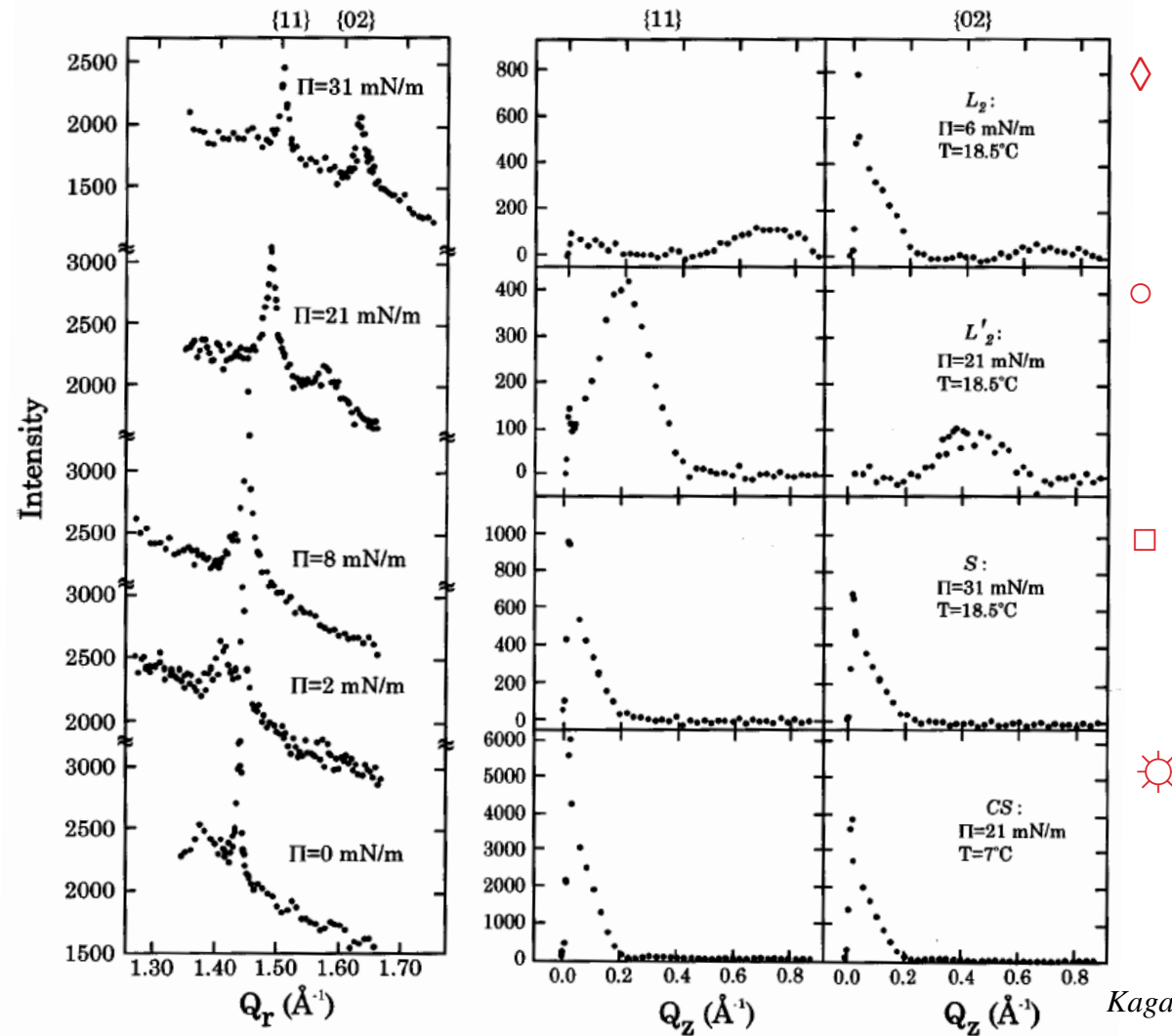


$$a = \frac{2\pi}{a_{\parallel}^* \sin \gamma}$$

$$b = \frac{2\pi}{b_{\parallel}^* \sin \gamma}$$



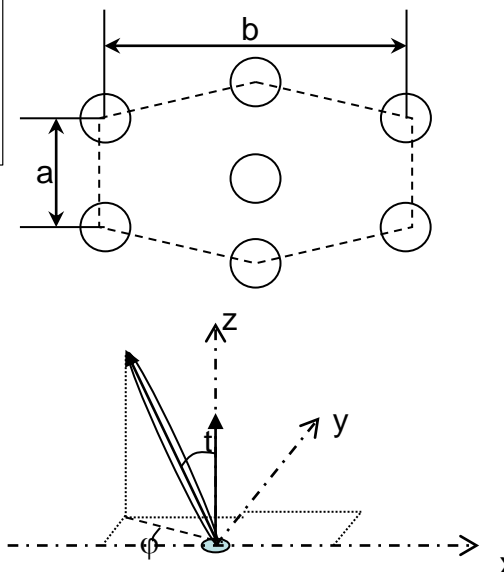
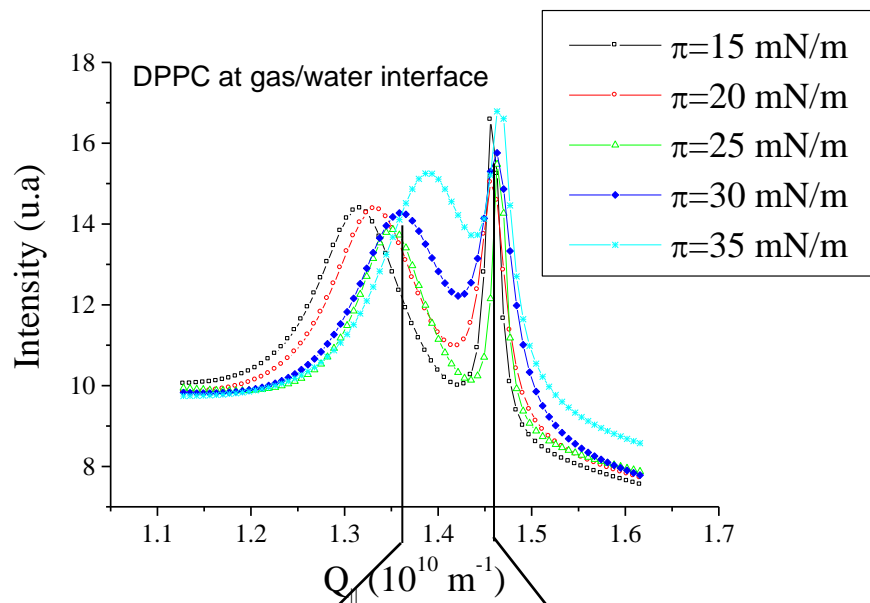
# Behenic acid ( $C_{22}$ ) phase diagram



Kaganer et al., *Reviews of Modern Physics*, 71 (1999) 779

Kenn, et al., *The Journal of Physical Chemistry*, Vol. 95, No. 5, 1991

# GID: 2D Lattice Compressibility



Isothermal compressibility  $\chi$

$$\chi = -\frac{1}{A} \times \left( \frac{\partial A}{\partial \pi} \right)_T$$

Landau theory

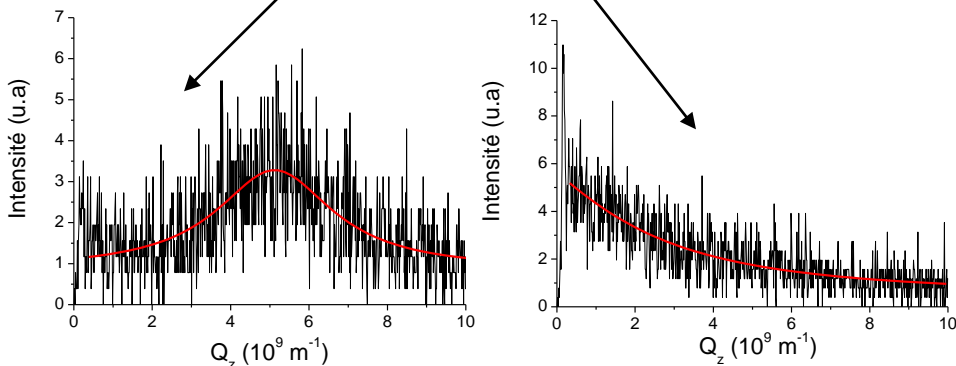


Bending rigidity  $\kappa$



$$K = \frac{h^2}{12 \times k_b T \times \chi}$$

$h$  – film thickness



	Rigidity $\kappa$ ( $k_B T$ ) $\pi < \pi_{cp}$ of PGLa	Rigidity $\kappa$ ( $k_B T$ ) $\pi > \pi_{cp}$ of PGLa
DPPC	15	17
DPPG	30	45

# Two dimensional protein crystallography

Soluble and membrane proteins do not form 3D crystals  
But can be assembled in 2D crystals using surface-bound affinity ligands or surface-bound charged lipids

## *Electrostatic interaction*

**Annexin V + DOPC**

DOPC:DOPS (4:1)

## *Molecular recognition*

**Streptavidin + biotine-LC-DPPE**

DPPE: biotine-LC-DPPE (4:1)

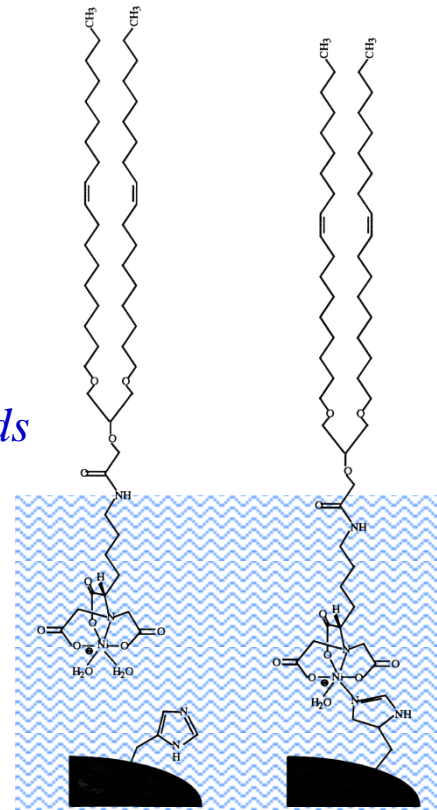
## *Binding of histidin-tag with Ni chelated lipids*

**HupR + Ni-NTA-DOGA**

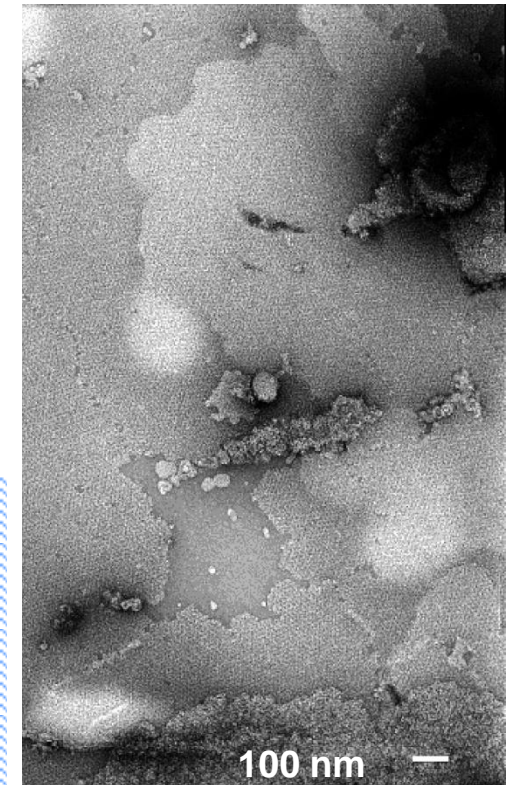
DOPC : Ni-NTA-DOGA 3:1

## Three steps of 2D crystal formation

1. Molecular recognition
2. Diffusion and concentration
3. Self assemble of the protein



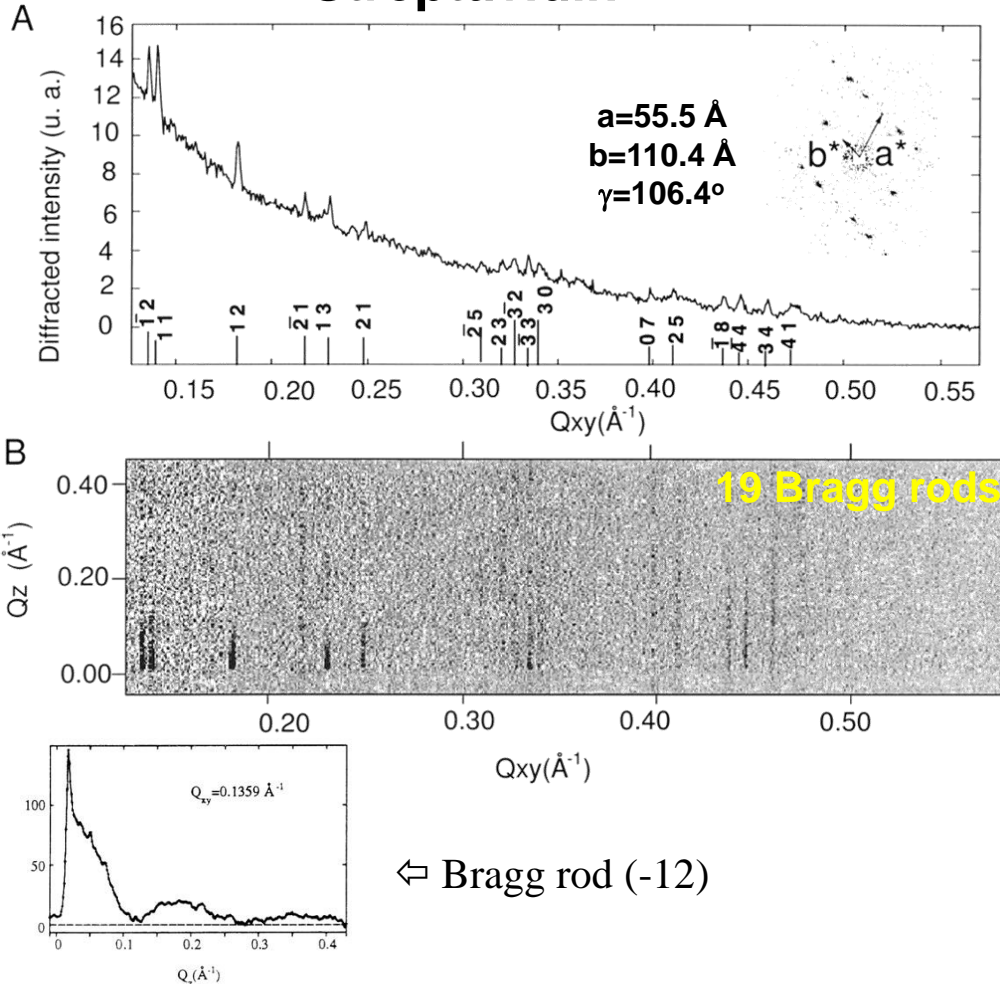
Electron micrograph of HupR crystals



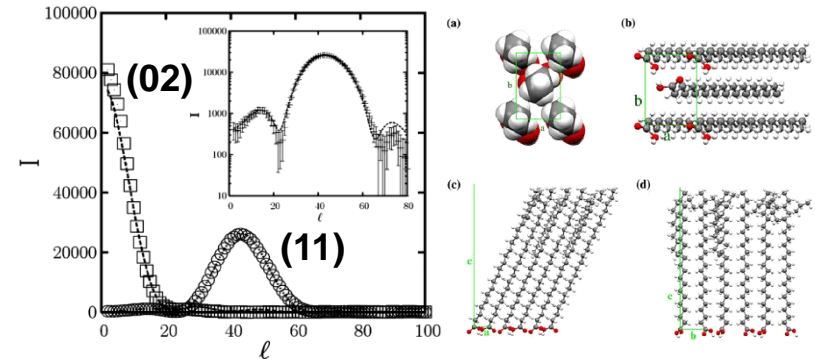
S. Courty et al., *Langmuir*, v. 18, 9502 (2002)

# 2D protein crystals: Towards atomic resolution

## Streptavidin



## Behenic acid



Reflections intensity ratio

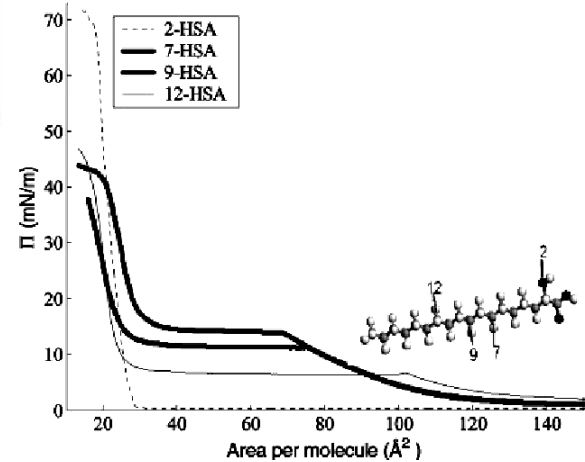
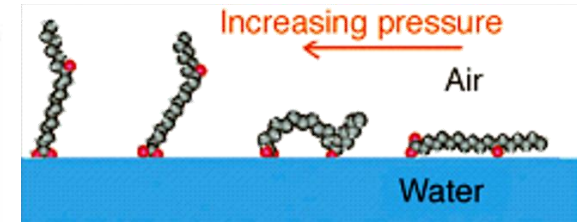
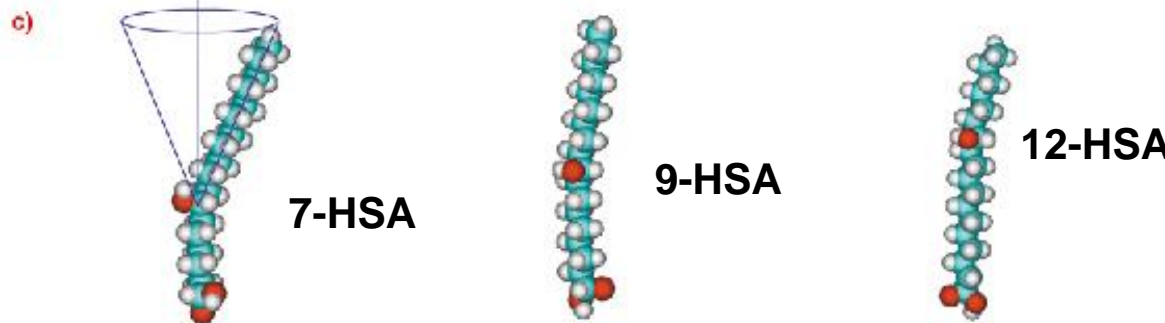
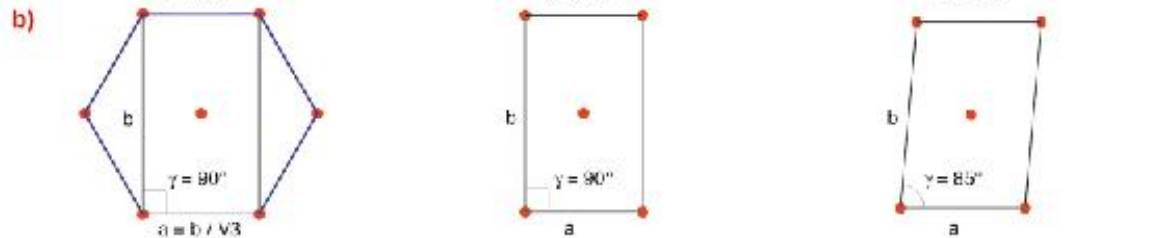
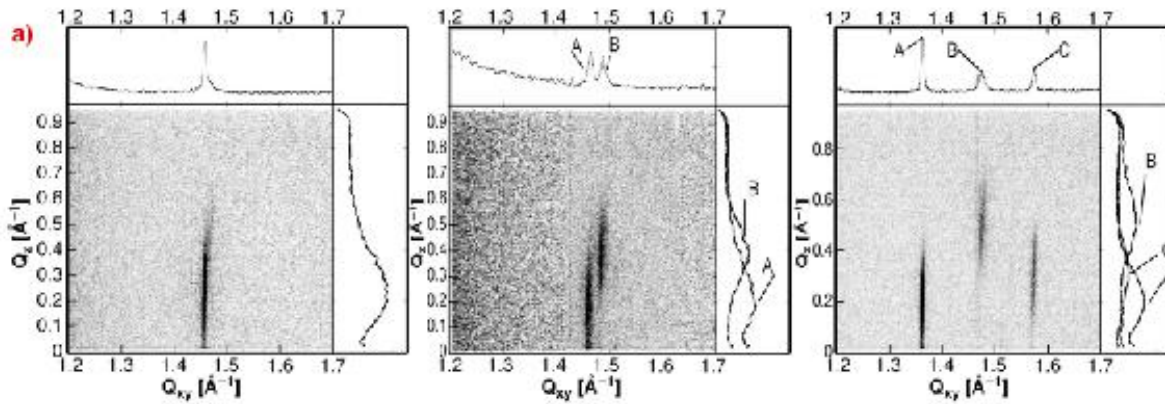
orientation of the backbone planes

Bragg rod profiles

conformation defects in the hydrocarbon chain



# Effect of OH group position on the 2D structure of Langmuir monolayers of hydroxystearic acids

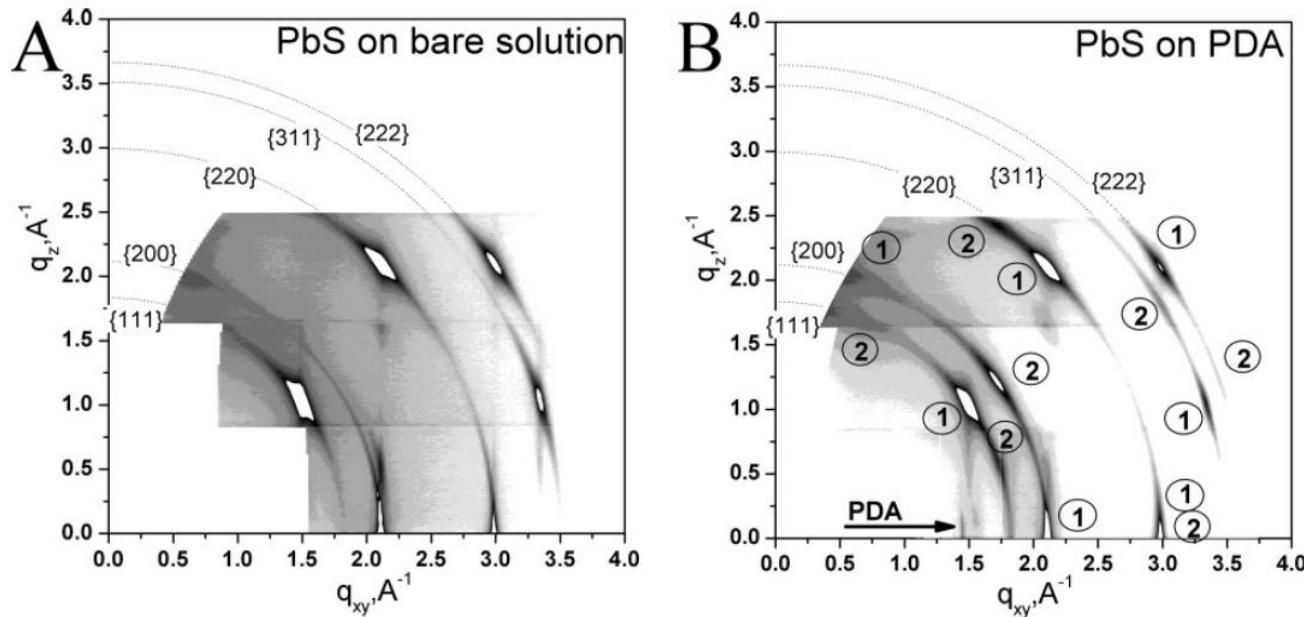


GID patterns for molecules:  
 7HSA (@16 mN/m)  
 9HSA (@12 mN/m)  
 12HSA (@7 mN/m)  
 T=20°C.

Rotor phase is proposed for molecular conformation of 7HSA,

*L. Cristofolini et al., Langmuir, v. 21, 11213 (2005)*

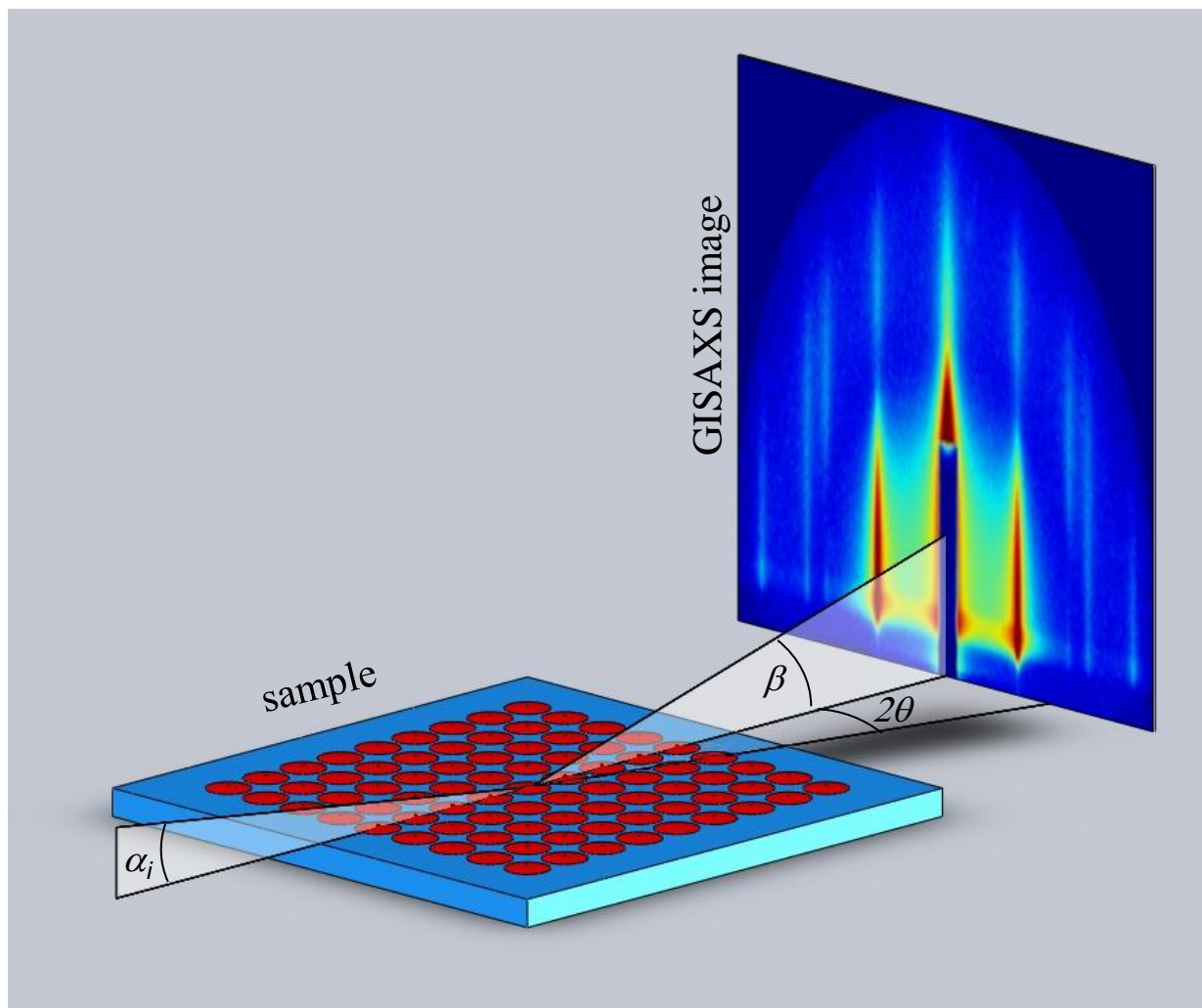
# Template growth of nanocrystalline PbS, CdS and ZnS on a polydiacetylene (PDA) Langmuir film



GID reciprocal maps of PbS nanocrystals at the air/solution interface. (A) in the absence of PDA and (B) in the presence of a PDA film. In (A) a single (100) orientation is observed. The notations (1) and (2) in (B) denote reflections corresponding to the (100) and (111) orientations, respectively. The reflection marked with an arrow in (B) corresponds to the PDA template

*Y. Lifshitz et al., Adv. Funct. Mater., v.16, 2398–2404, (2006)*

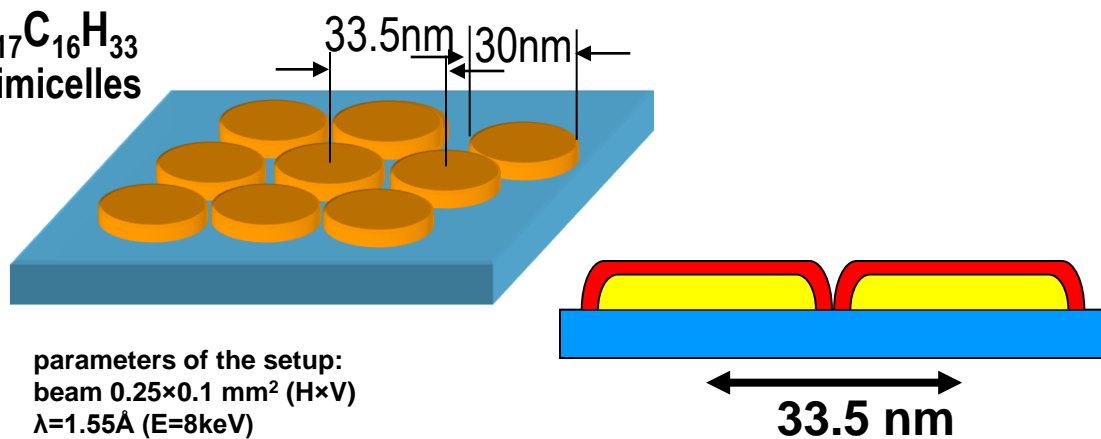
## Grazing Incidence Small Angle Scattering



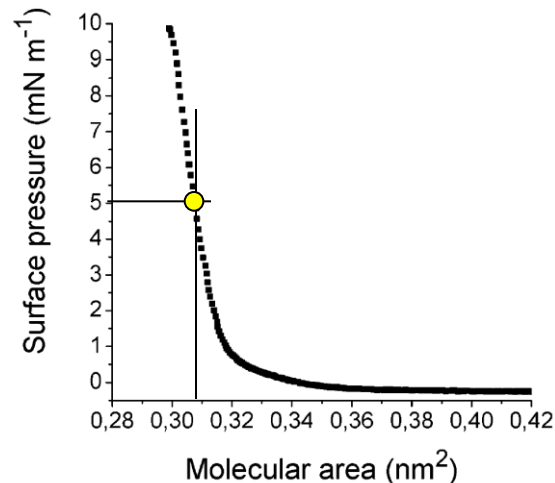
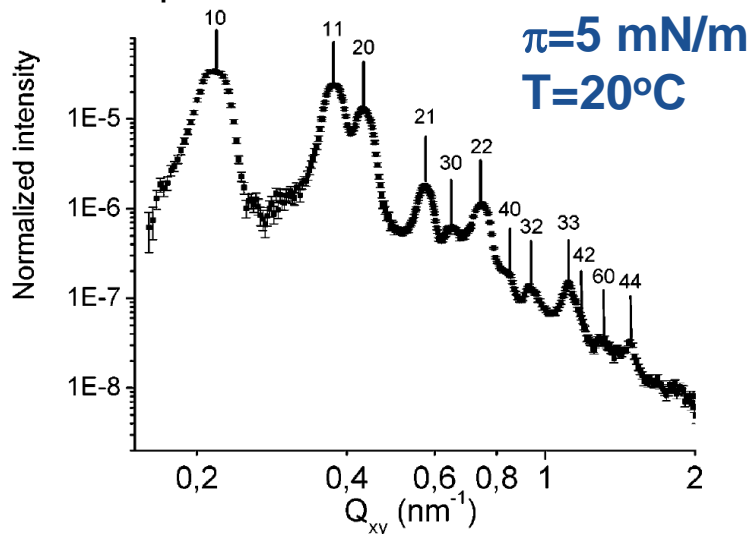


## Direct Evidence for Highly Organized Networks of Circular Surface Micelles of Surfactant at the Air-Water Interface

$C_8F_{17}C_{16}H_{33}$   
hemimicelles



parameters of the setup:  
beam  $0.25 \times 0.1 \text{ mm}^2$  (H×V)  
 $\lambda = 1.55 \text{ \AA}$  (E=8keV)  
 $\alpha = 2 \text{ mrad}$  ( $\alpha_c = 2.5 \text{ mrad}$ )  
linear PSD (vertical)  $Q_z^{\text{max}} = 5 \text{ nm}^{-1}$   
in-plane resolution 1 mrad



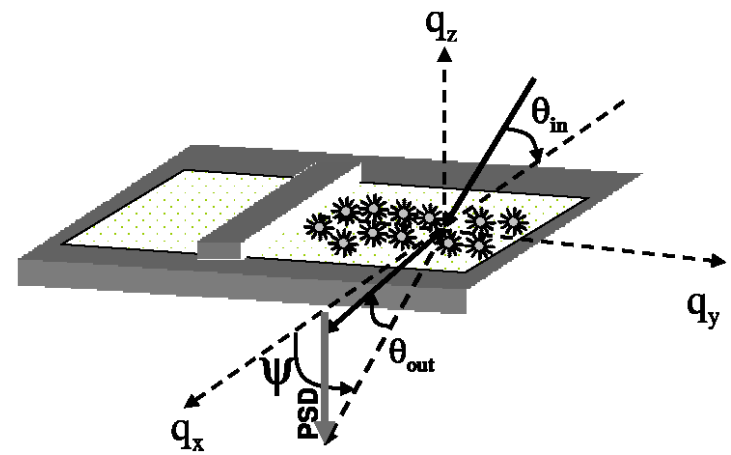
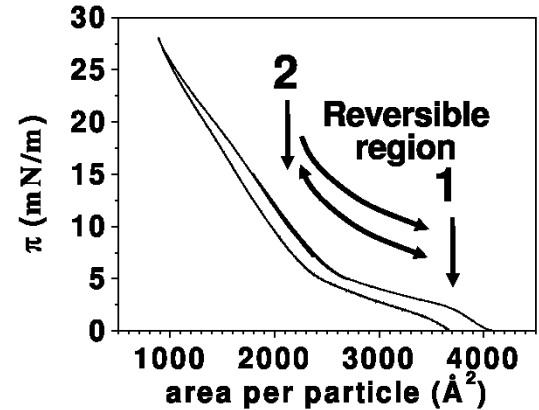
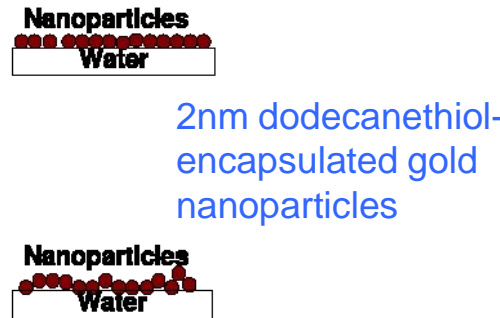
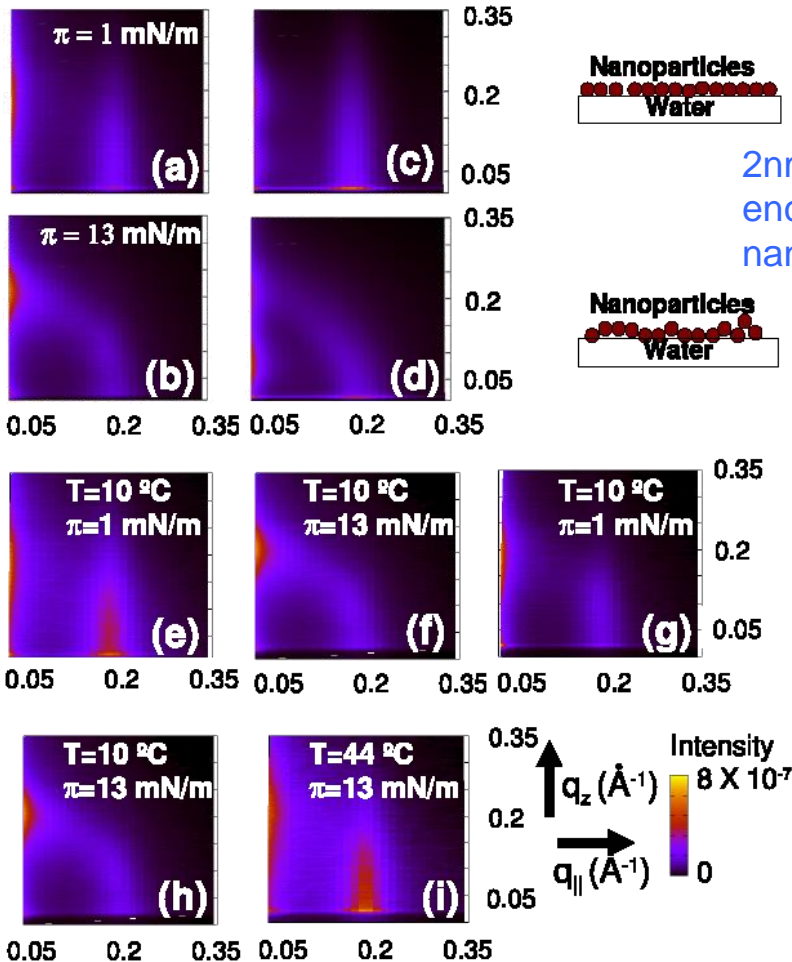
**Table 1.** Peak Positions ( $Q_{xy}$ ) and Widths ( $W$ ) Deduced from a Lorentzian Fit of the Diffraction Peaks<sup>a</sup>

$Q$ ( $\text{nm}^{-1}$ )	$W$ ( $\text{nm}^{-1}$ )	indexation (hexagonal lattice)
0.2159	0.0249	(1 0)
0.3772	0.0303	(1 1)
0.4333	0.0307	(2 0)
0.575	0.033	(2 1)
0.6509	0.0299	(3 0)
0.747	0.0467	(2 2)
0.8478	0.0222	(4 0)
0.939	0.044	(3 2)
1.113	0.0524	(3 3)
1.172	0.0362	(4 2)
1.293	0.068	(6 0)
1.482	0.0438	(4 4)

<sup>a</sup> Last column is the indexation of the peaks in a hexagonal lattice with a parameter of 33.5 nm.

Fontaine et al., *J. Am. Chem. Soc.* **127**, p.512 (2005)

## Reversible buckling in monolayer of gold nanoparticles on water surface



*M. K. Bera et al., EPL, v. 78, 56003, (2007)*

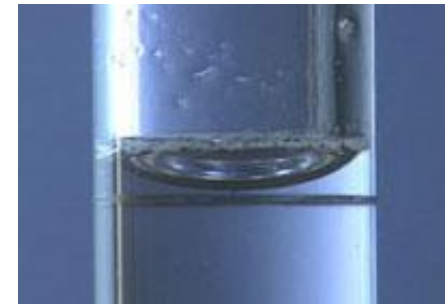
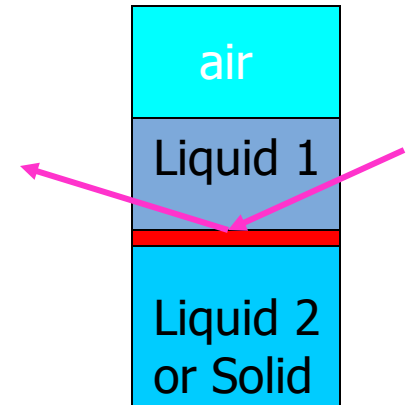
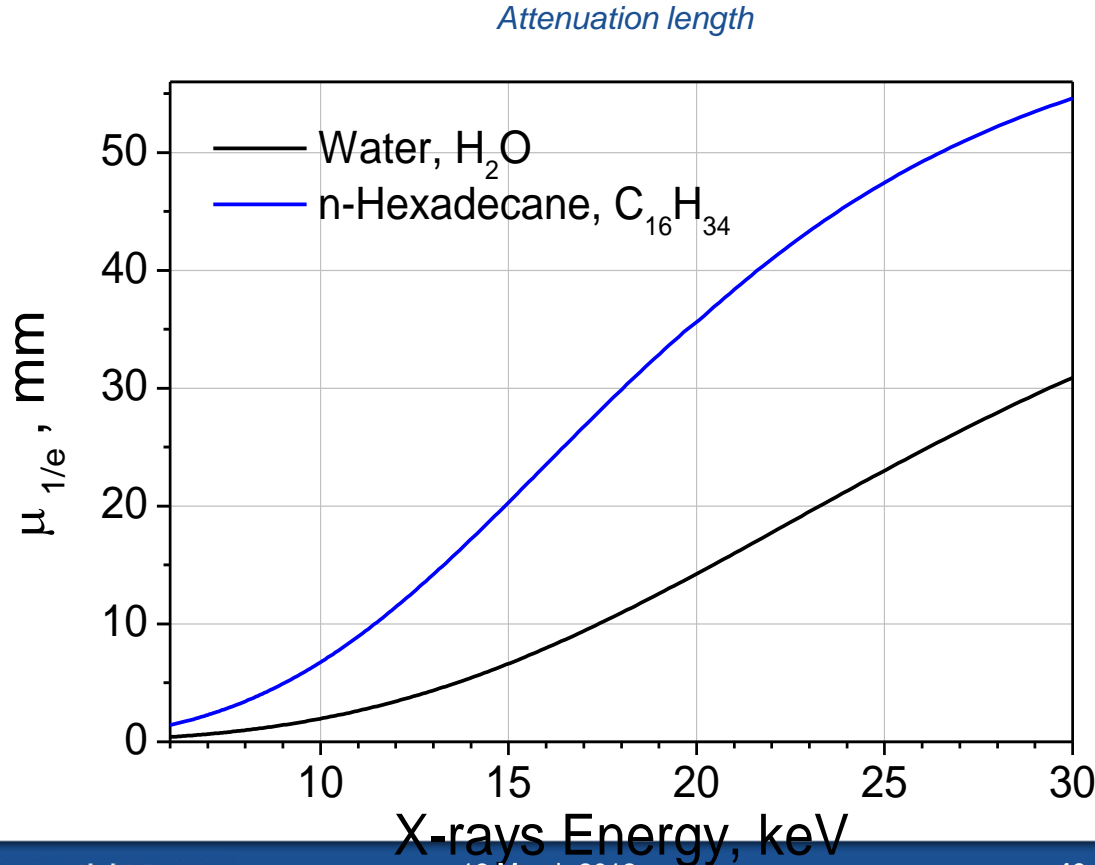
## Buried Interfaces

The liquid-liquid and liquid-solid interfaces play an important role in many physical, chemical and biological processes of everyday life. Its characterization would enhance our understanding of fundamental processes occurring in nature.

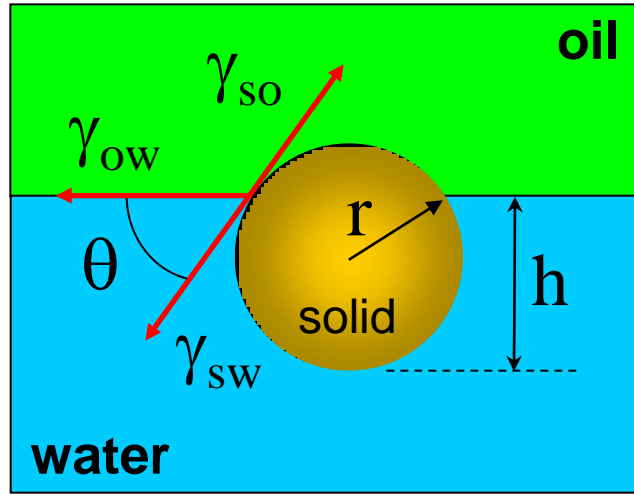
- Molecular ordering of the liquids near and within LL interfaces
- Surfactants and ions ordering at the LL interface
- Bio-mimetic systems (model membranes at LL and LS interfaces)
- Bio-mineralization
- Emulsion (fundamental aspects and applications: food industry, paints, hydrometallurgy ...)
- Studies of reactions, interfacial synthesis
- Growth and ordering of nano particles
- Electrochemical processes
- Photochemistry at LL Interfaces
- ....

# X-ray scattering at Liquid/Liquid Interfaces: Attenuation length

- Penetration
- Background
- Meniscus



# Nanoparticles as surfactants: contact angle & binding energy



**Particle immersion:**  $h = r(1 + \cos \theta)$

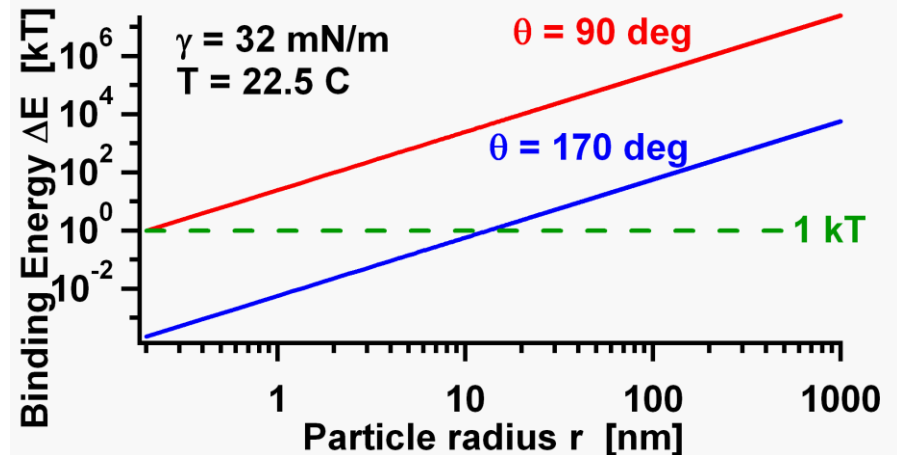
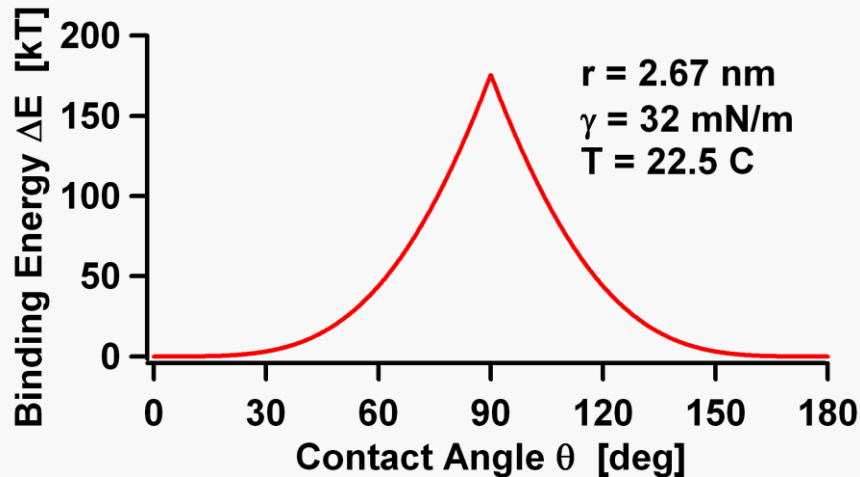
**Young's equation:**  $\gamma_{so} - \gamma_{sw} = \gamma_{ow} \cos \theta$

**Solid-water contact area:**  $A_1 = 2\pi r h$

**Missing oil-water area:**  $A_2 = \pi r^2 \sin^2 \theta$

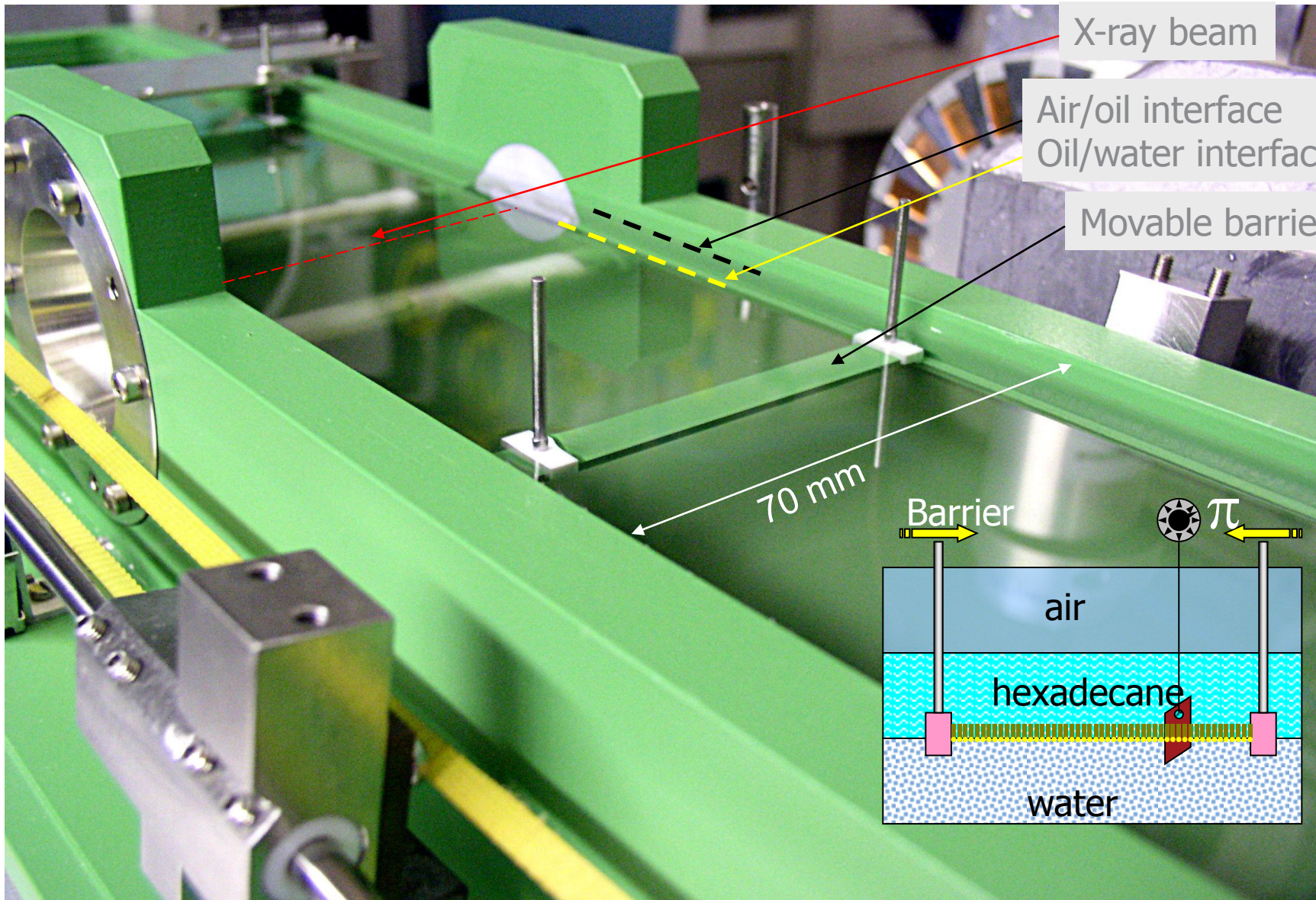
**Binding energy:**  $\Delta E = A_1(\gamma_{so} - \gamma_{sw}) + A_2\gamma_{ow}$

$$\Delta E = \pi r^2 [1 - |(\gamma_{sw} - \gamma_{so}) / \gamma_{ow}|]^2 = \pi r^2 \gamma_{ow} [1 - |\cos \theta|]^2 = \pi \gamma_{ow} h^2$$

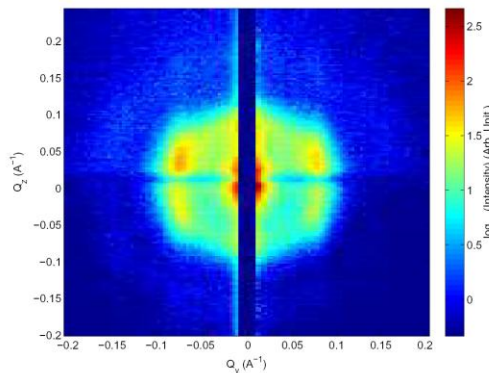
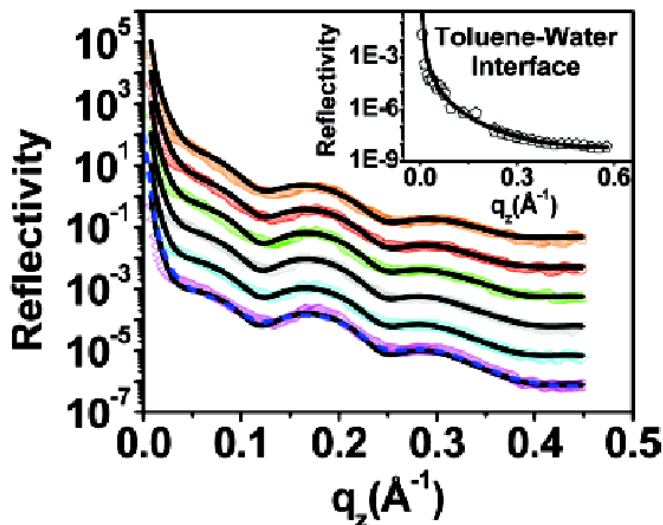




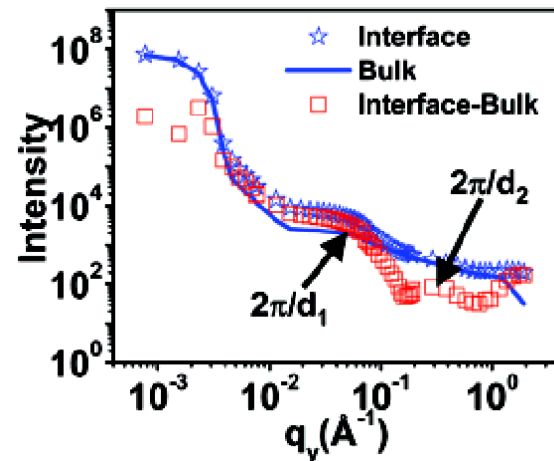
# Langmuir Trough for Liquid-Liquid interface



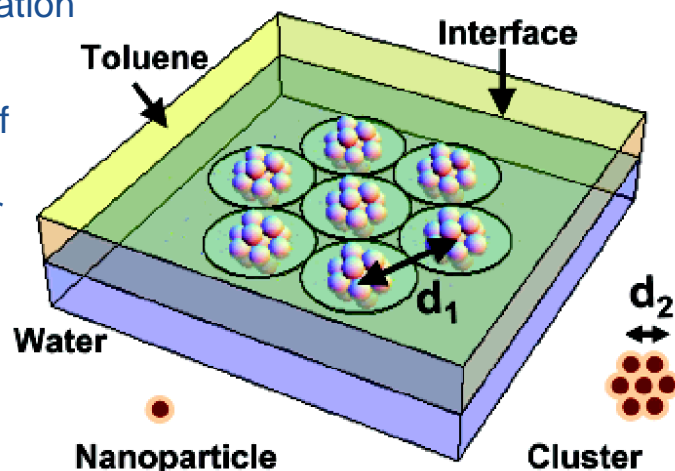
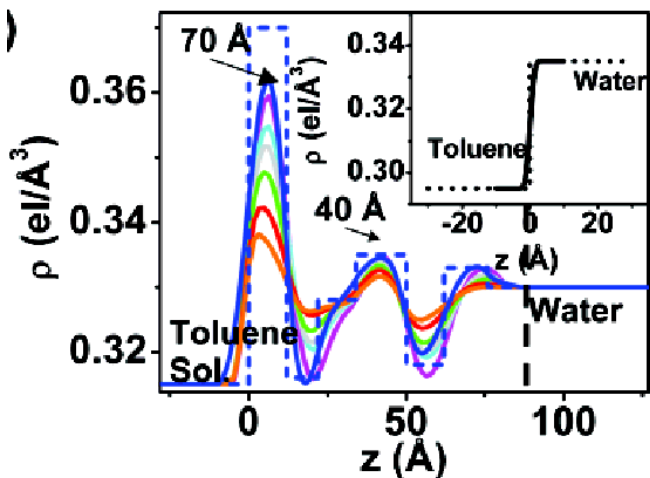
# Formation and Ordering of Gold Nanoparticles at the Toluene-Water Interface



cluster-cluster separation  $d_1 = 180 \text{ \AA}$   
particle-particle separation  $d_2 = 34 \text{ \AA}$



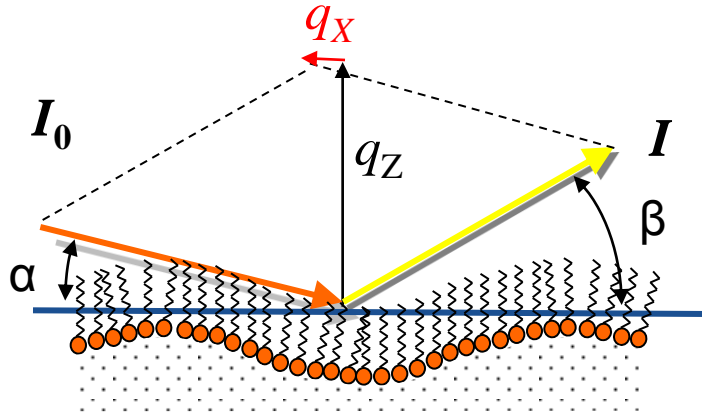
Each cluster consists of 13NPs with  $\text{\AA} 12 \text{ \AA}$  &  $11 \text{ \AA}$  thick organic layer



*M.K. Sanyal et al., J. Phys. Chem. C, v. 112, 1739 (2008)*



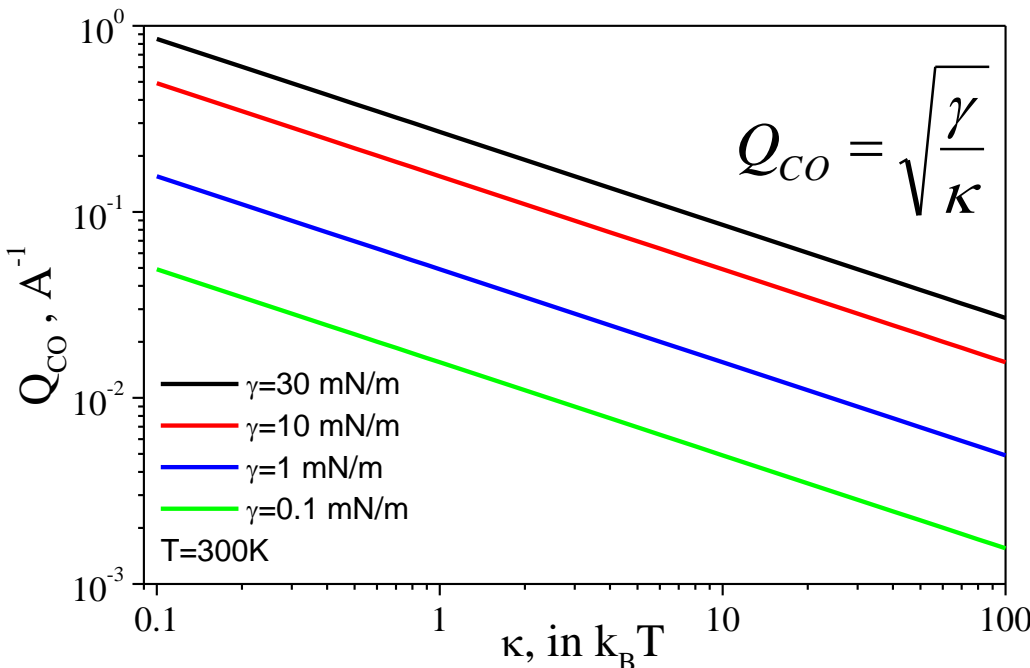
# Bending Rigidity ( $\kappa$ ) From GI Diffuse Scattering



Capillary waves  $\rightarrow$  height fluctuation spectrum determined by the **surface energy** ( $\gamma$ ) associated with the **deformation modes** ( $\kappa$ )  
[Helfrich, *Z. Naturforsch.*, 28c, 693, (1973)]

$$\langle z(q_{\parallel})z(-q_{\parallel}) \rangle = \frac{1}{A} \frac{k_B T}{\Delta \rho g + \gamma q_{\parallel}^2 + \kappa q_{\parallel}^4}$$

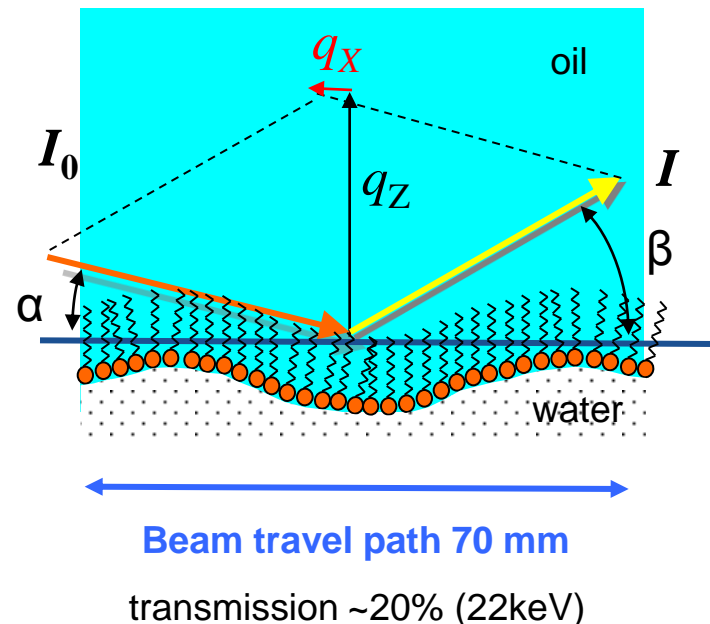
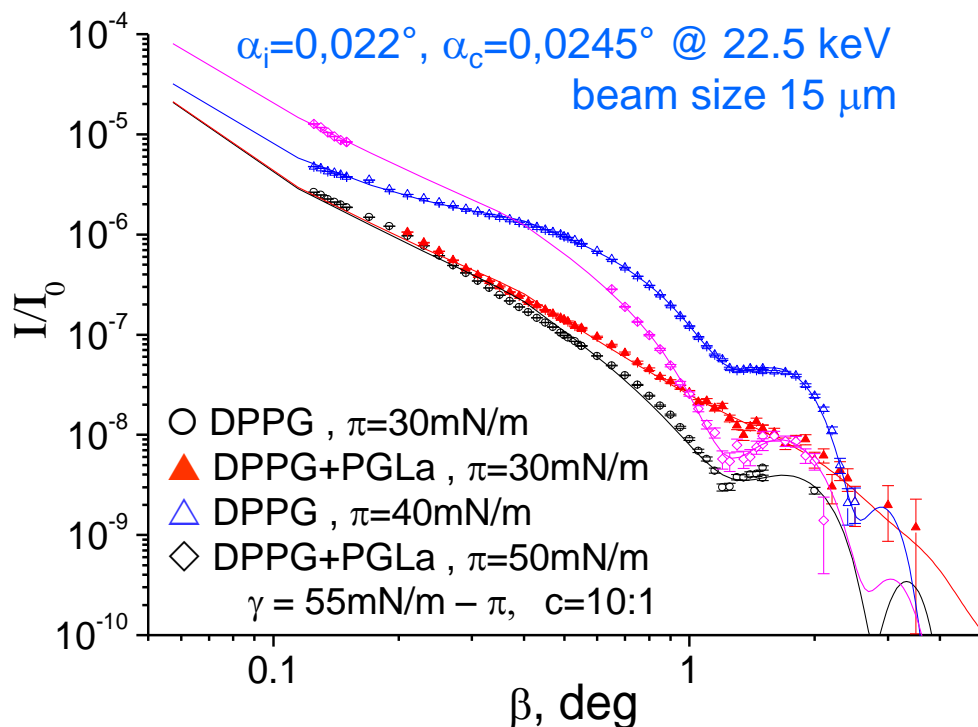
$$\frac{d\sigma}{d\Omega} \propto |t_{0,1}^{in}|^2 |t_{0,1}^{sc}|^2 |\tilde{\rho}(q_z)| e^{-q_z^2 \langle z^2 \rangle} \times \int d\mathbf{r}_{\parallel} \left( e^{q_z^2 \langle z(0)z(\mathbf{r}_{\parallel}) \rangle} - 1 \right) e^{i\mathbf{q}_{\parallel} \mathbf{r}_{\parallel}}$$



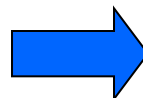
S. Mora et al., *Europhys. Lett.*, v. 66, p. 694 (2004)

# Phospholipid monolayer at hexadecane water interface

## Bending Rigidity ( $\kappa$ )



Bending rigidity of the DPPG membrane decreases upon insertion of the antimicrobial peptide PGLa



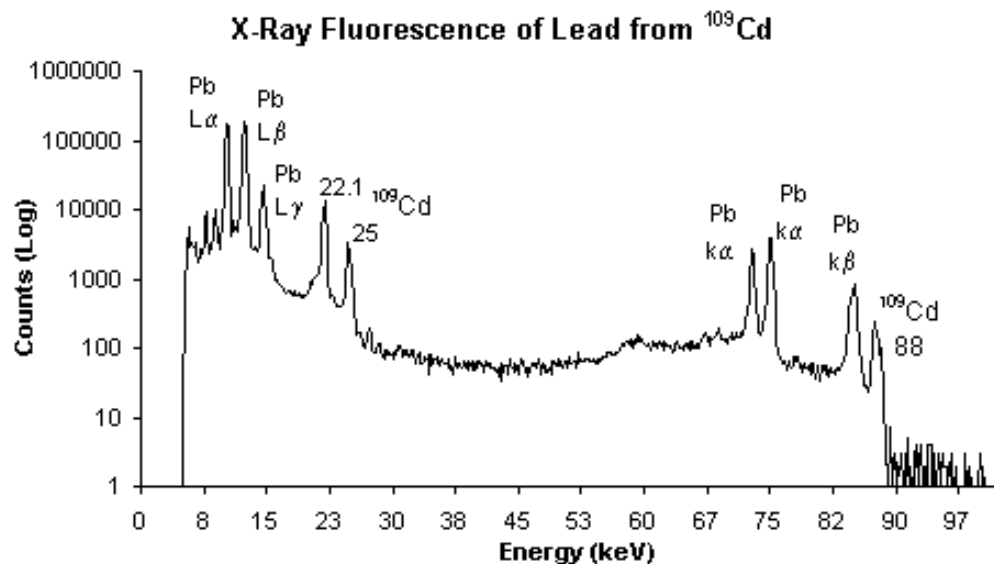
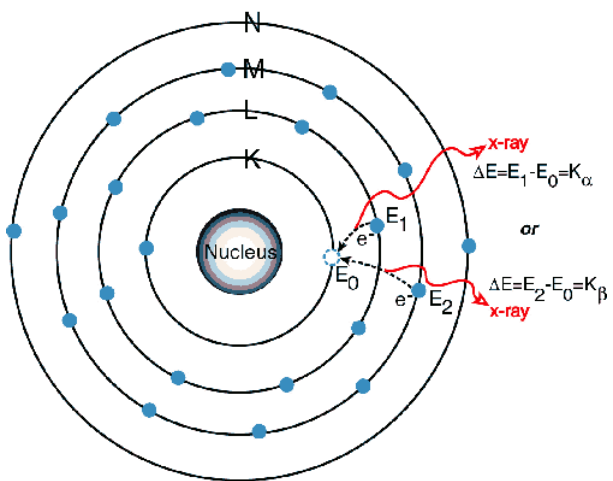
*E. Saint Martin et al., Thin Solid Films, v.515, p.5678, (2007)*

	Rigidity $\kappa$ ( $k_b T$ ) @ $\pi = 30 \text{ mN/m}$ $\pi < \pi_c$	Rigidity $\kappa$ ( $k_b T$ ) @ $\pi > 40 \text{ mN/m}$ $\pi > \pi_c$
DPPG	$55 \pm 5$	$145 \pm 5$
DPPG+PGLa	$27 \pm 5$	$20 \pm 5$

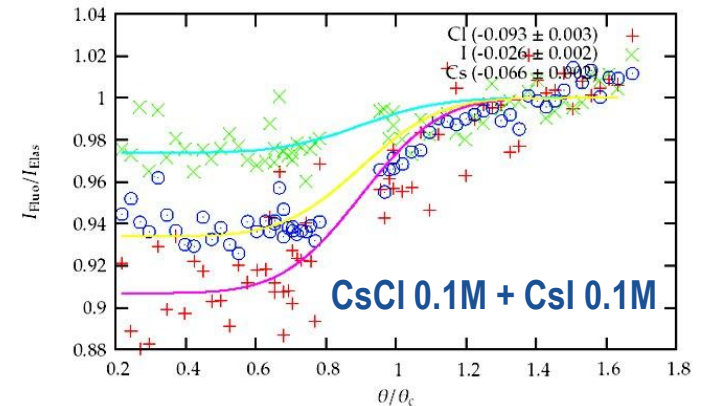
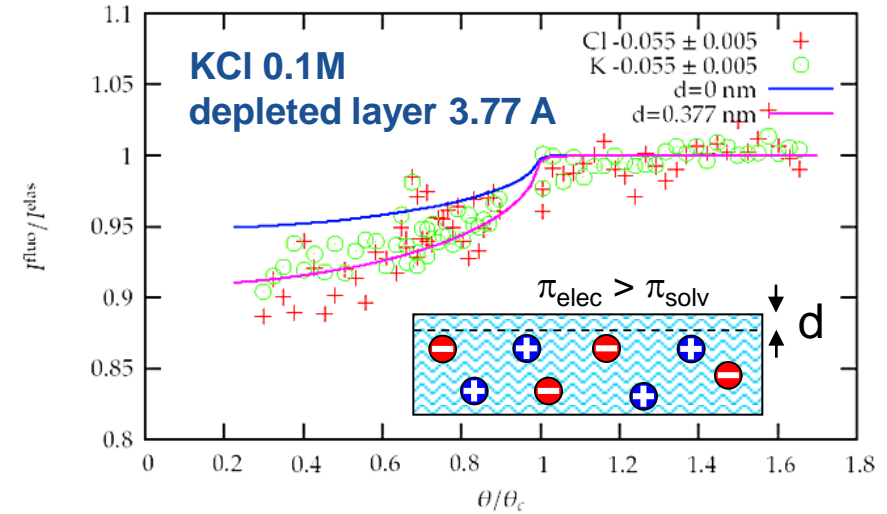
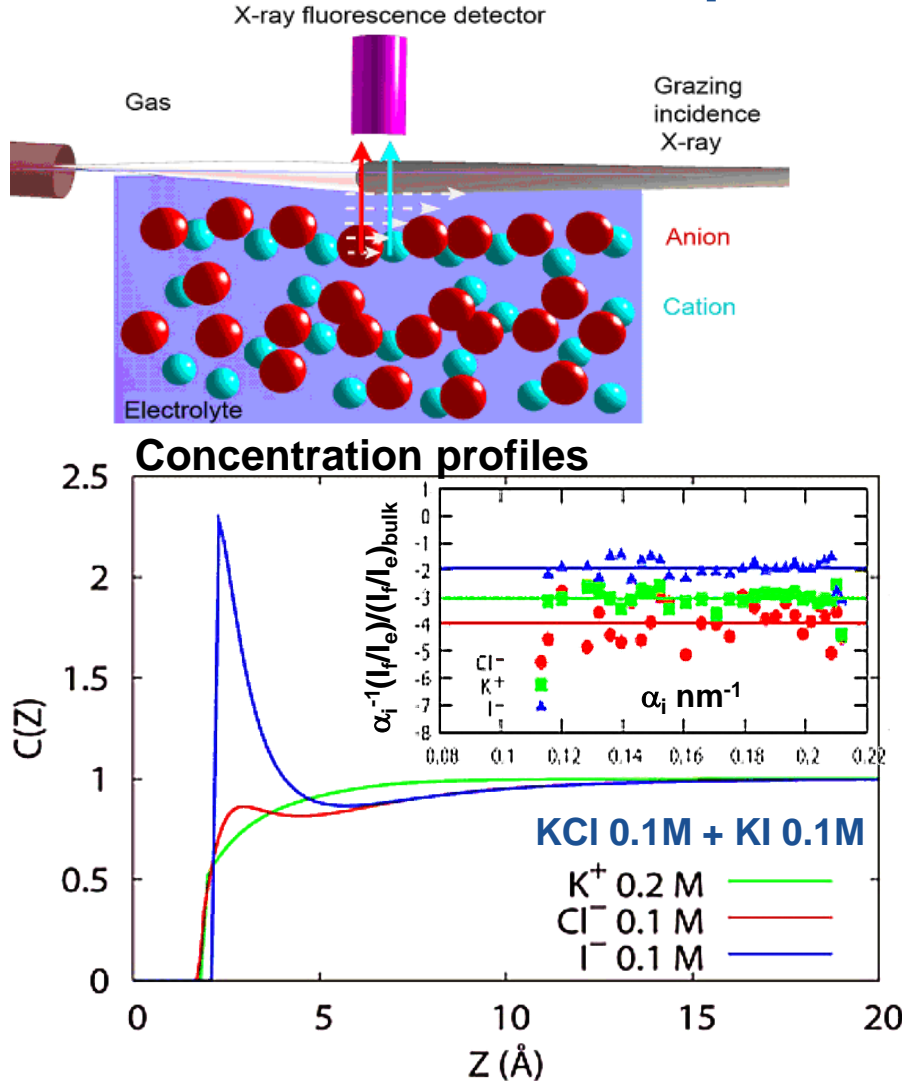
# X-ray Reflectivity + Fluorescence



## Total Reflection X-Ray Fluorescence (TXRF)



# Specific ion adsorption and short-range interactions at the air aqueous solution interface



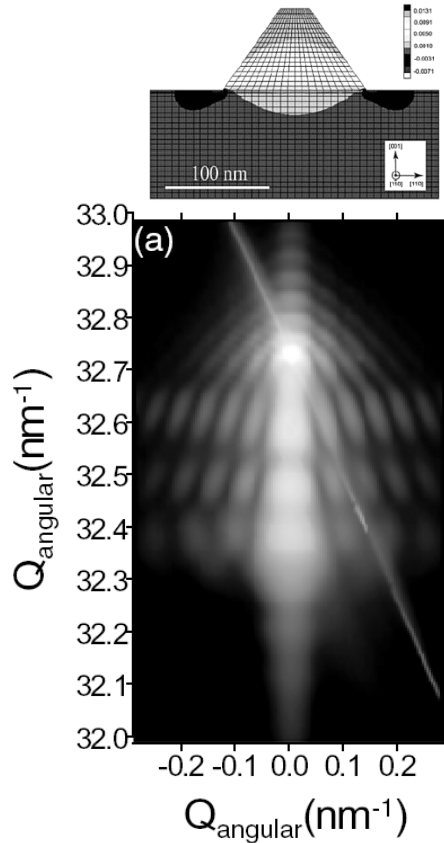
V. Padmanabhan et al., *Phys. Rev. Lett.* 99, 086105 (2007)

# Semiconductor nano-structures.

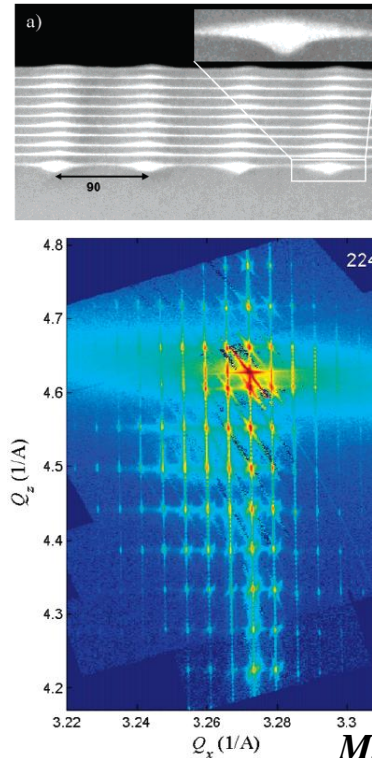
## Quantum: dots, wires, crystals and molecules

size, shape, strain, chemical composition & spatial ordering

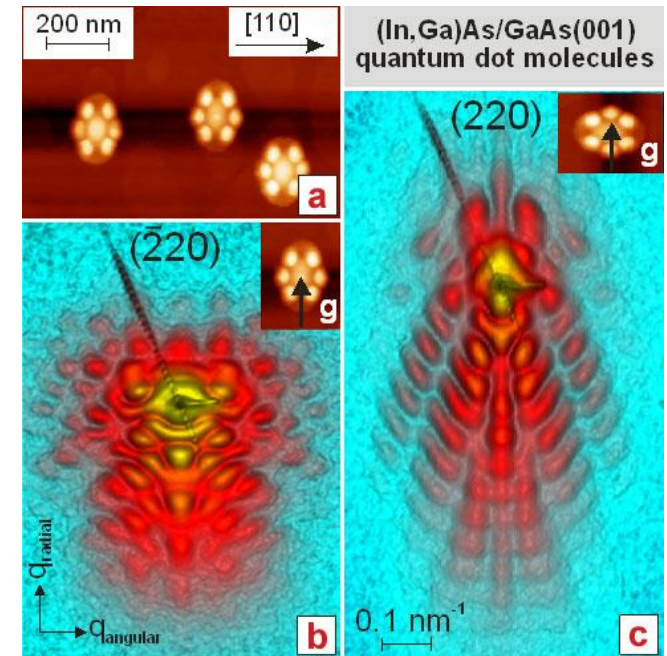
Free-standing  $\text{Si}_{1-x}\text{Ge}_x$  nanoscale islands on Si(100)



Three-Dimensional Si/Ge Quantum Dot Crystals



Hexapod-like (In,Ga)As/GaAs(001) quantum dot molecules



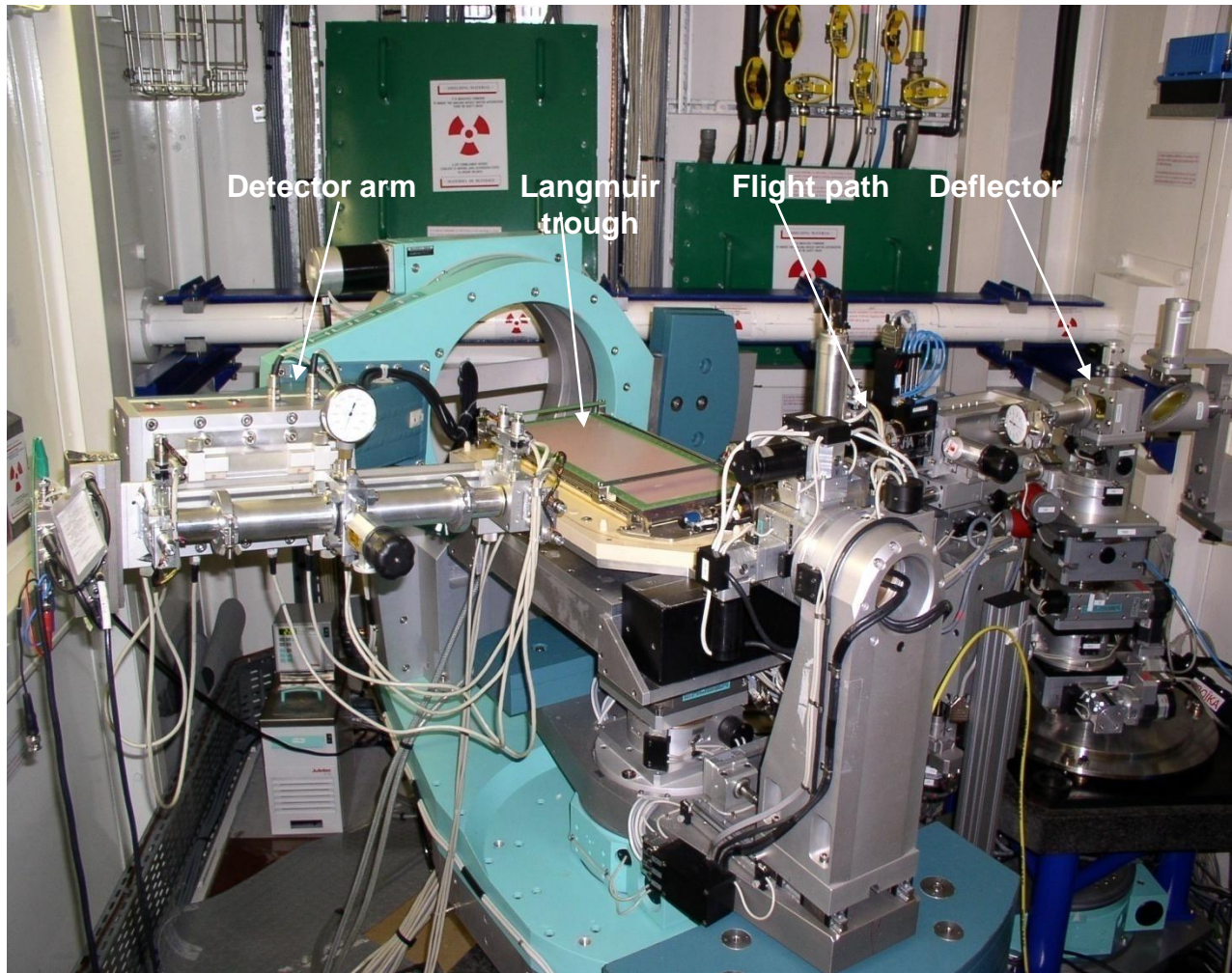
*M. Hanke et al. Appl. Phys. Lett., v. 95, 023103, (2009)*

*D. Grützmacher et al., Nano Lett., Vol. 7, 3150, (2007)*

*D. Grigoriev et al., J. Phys. D: Appl. Phys., v. 36, A225-A230, (2003)*



## GENERAL VIEW OF EXPERIMENTAL HUTCH OF THE ID10B BEAMLINE AT ESRF



The ID10B beamline is a multi-purpose, high-brilliance undulator beamline for **high resolution** X-ray scattering and surface diffraction on **liquid** and **solid** interfaces, combining **grazing-incidence diffraction (GID)**, **X-ray reflectivity (XRR)**, and **grazing-incidence small-angle scattering (GISAXS)** techniques in a **single instrument**. Scattering experiments can be performed in both **horizontal** and in **vertical** scattering geometry.

*The beamline is optimized for experiments on liquid and fluid surfaces which are a particular specialty of the ID10B.*

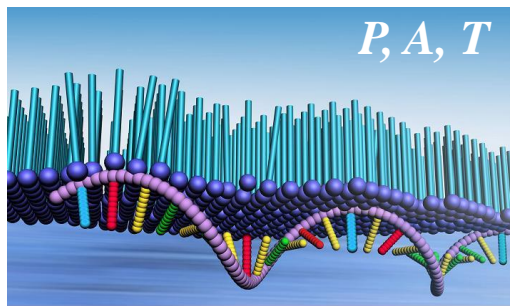
max beam size at sample  $1 \times 0.5 \text{ mm}^2$  (H×V) 44 m from the source  
photon energy  $7 \text{ keV} < E < 30 \text{ keV}$  ( $1.77 < \lambda < 0.41$ )  
flux at sample:  $10^{13} \text{ ph/s/mm}^2$  (at  $I=100 \text{ mA}$ ,  $E=9 \text{ keV}$ )

Scientific applications cover studies of the structural properties of soft and hard condensed matter materials.

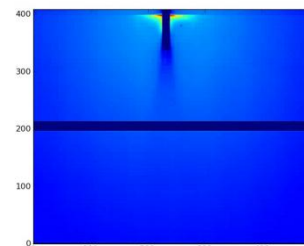
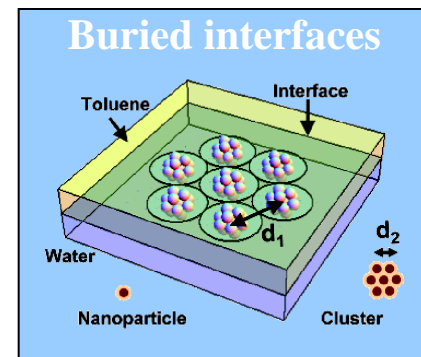
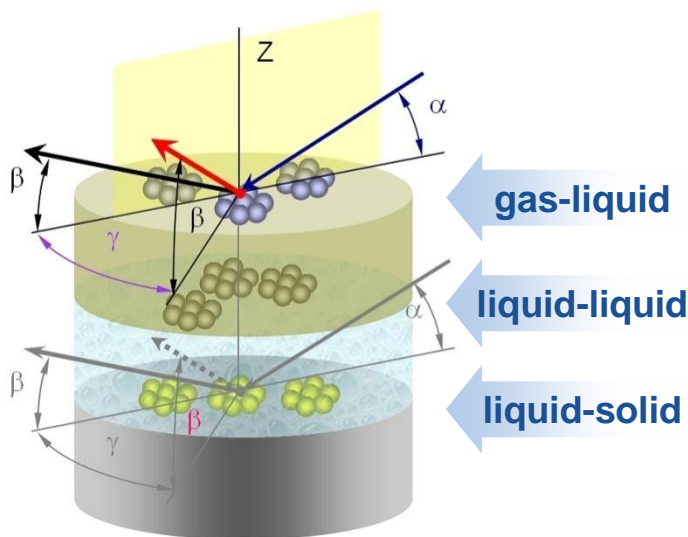
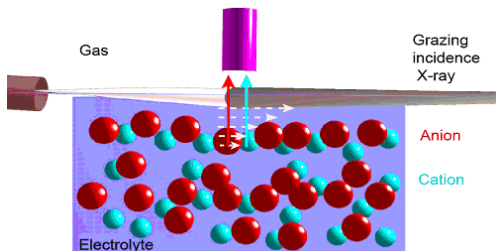
# Conclusion

**X-ray surface sensitive technique is a powerful tool to study broad spectrum of science at surfaces and interfaces**

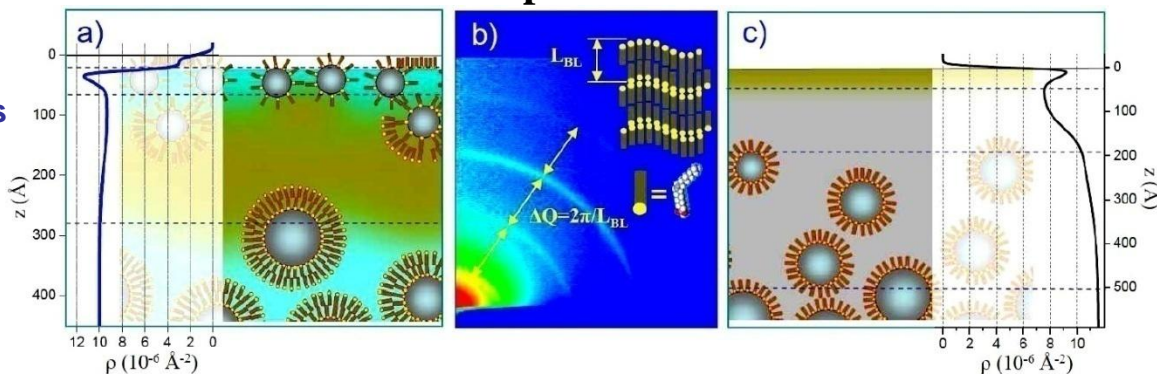
## Langmuir films



## Elements distribution



## Complex fluids



- Surface structure of simple and complex fluids
- Morphology and crystalline structure of thin organic and inorganic films
- 2D organization of molecules, macromolecules and nano particles
- Bio-mimetic systems & Bio-mineralization
- Chemistry & Electrochemistry
- Surfactants & ions ordering



## Acknowledgments

**ID10B & ESRF staff**  
**A. Vorobiev**

**Numerous ID10B users**

***Thank you !***

## Further reading

**J. Daillant & A. Gibaud, “X-Ray and Neutron Reflectivity: Principles and Applications”, Springer, 1999**

**M. Tolan “X-Ray Scattering from Soft-Matter Thin Films” Springer, 1999**

**J. Als-Nielsen & D. McMorrow “Element of Modern X-ray Physics”, John Wiley, 2001**

**I. K. Robinson and D. J. Tweet, Rept. Prog. Phys. 55, p.599 (1992)**

**J. Daillant, M. Alba, Rep. Prog. Phys. 63 (2000) 1725–1777**

# Grazing Incidence Scattering : Flux Requirements

$$I = \frac{I_0}{w_i h_i} \frac{d\sigma}{d\Omega}(q) \frac{w_d h_d}{L_d^2}$$

$$\frac{d\sigma}{d\Omega}(q) \sim r_e^2 \cos^2 \psi |t_\alpha|^2 |t_\beta|^2 \Delta \rho_e^2 A_\parallel \frac{k_B T}{\gamma q_\parallel^2}$$

$$\gamma = 72 \cdot 10^{-3} \text{ N/m} \quad w_i = w_c = w_d = h_d = 3 \cdot 10^{-4} \text{ m}$$

$$r_e = 2.8 \cdot 10^{-15} \text{ m} \quad h_i = 10^{-4} \text{ m} \quad L_d = 0.5 \text{ m}$$

$$\rho_{H_2O} = 3.3 \cdot 10^{29} \text{ el/m}^3 \quad q_\parallel = 10^9 \text{ m}^{-1}$$

$$\cos^2 \psi |t_\alpha|^2 |t_\beta|^2 \sim 1 \quad A_\parallel \sim \frac{w_i w_c}{\sin \psi} = 3.6 \cdot 10^{-6} \text{ m}^2$$

$$\frac{d\sigma}{d\Omega}(q) \sim A_\parallel \times 5 \cdot 10^{-8}$$

$$\frac{d\sigma}{d\Omega}(q) \sim 2 \cdot 10^{-13}$$

$$I \sim I_0 \cdot 2 \cdot 10^{-12}$$

$$I_{\text{Sollers}} \sim I_0 \cdot 4 \cdot 10^{-11}$$

for 3% error bar  $N \sim 10^3$   
& 60sec counting time

$$I_0 \sim 4 \cdot 10^{11} \text{ ph/s}$$

