

# Colloidal crystals studied with SAXS

## Condensed matter physics of elephants

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Universiteit Utrecht









# Schedule

## Part I

- Introduction to nanoelephants
- Instrumentation
- Example 1: Hard spheres

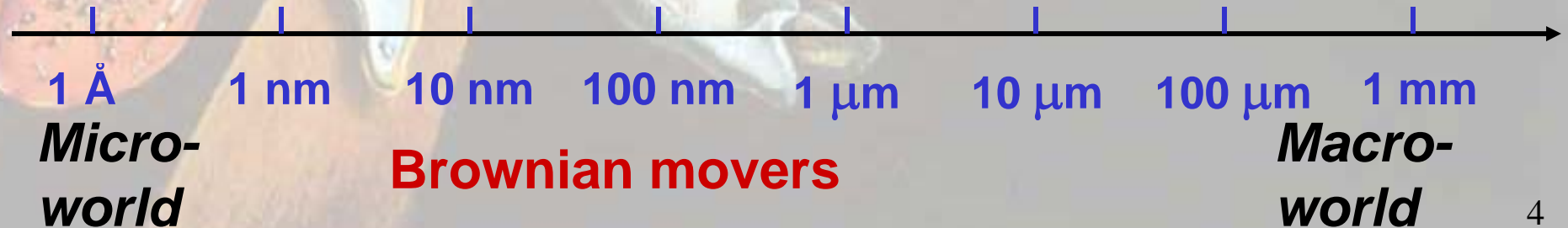
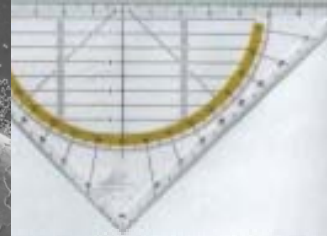
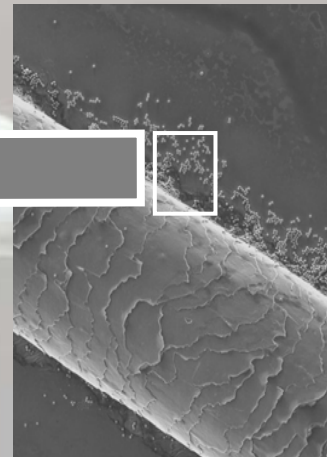
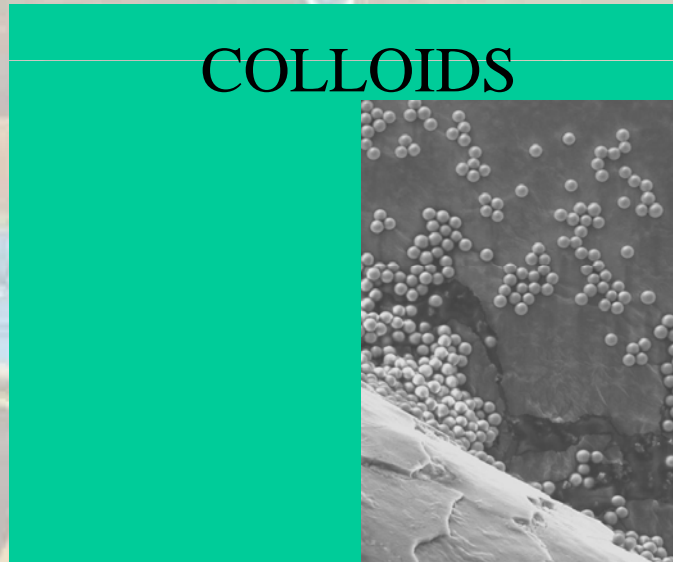
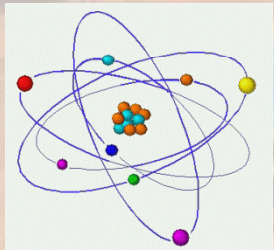
## Part II

- Example 2: Rusted nanonails
- Conclusion

# What is colloid?

International Union of Pure and Applied Chemistry

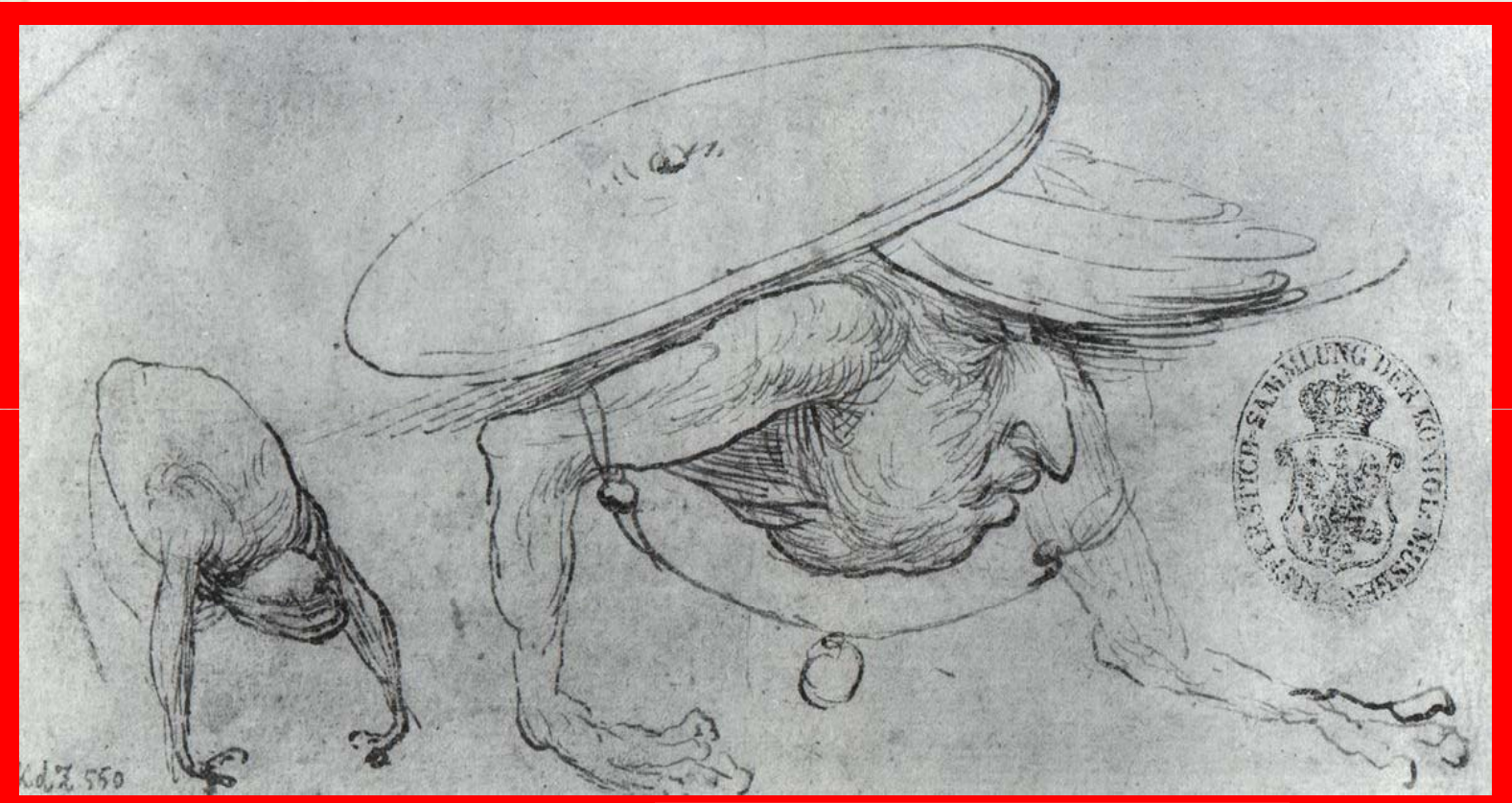
“The term **colloidal** refers to a state of subdivision, implying that the molecules or polymolecular particles dispersed in a medium have at least in one direction a **dimension roughly between 1 nm and 1  $\mu\text{m}$ .**”





# What is colloid?

“The mole least”



Hieronimus Bosch

1 Å

1 nm

10 nm

100 nm

1 μm

10 μm

100 μm

1 mm

**Micro-world**

**Brownian movers**

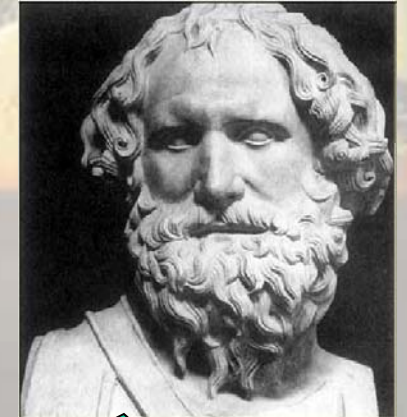
**Macro-world**

# Why $< 1 \mu\text{m}$ ?

Or Newton versus Boltzmann



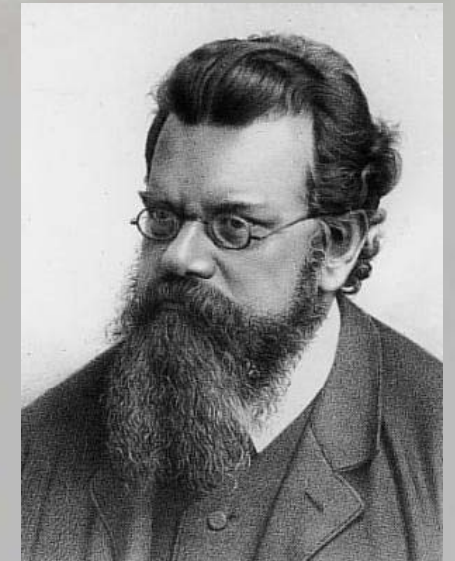
$$\begin{aligned}\Delta E &= m * g \Delta h \\ &= \Delta \rho V g \Delta h\end{aligned}$$



$\Delta h$



Thermal energy  $k_B T$   
 $\approx 4 \times 10^{-21} \text{ J @ } T = 300 \text{ K}$





# Let us see

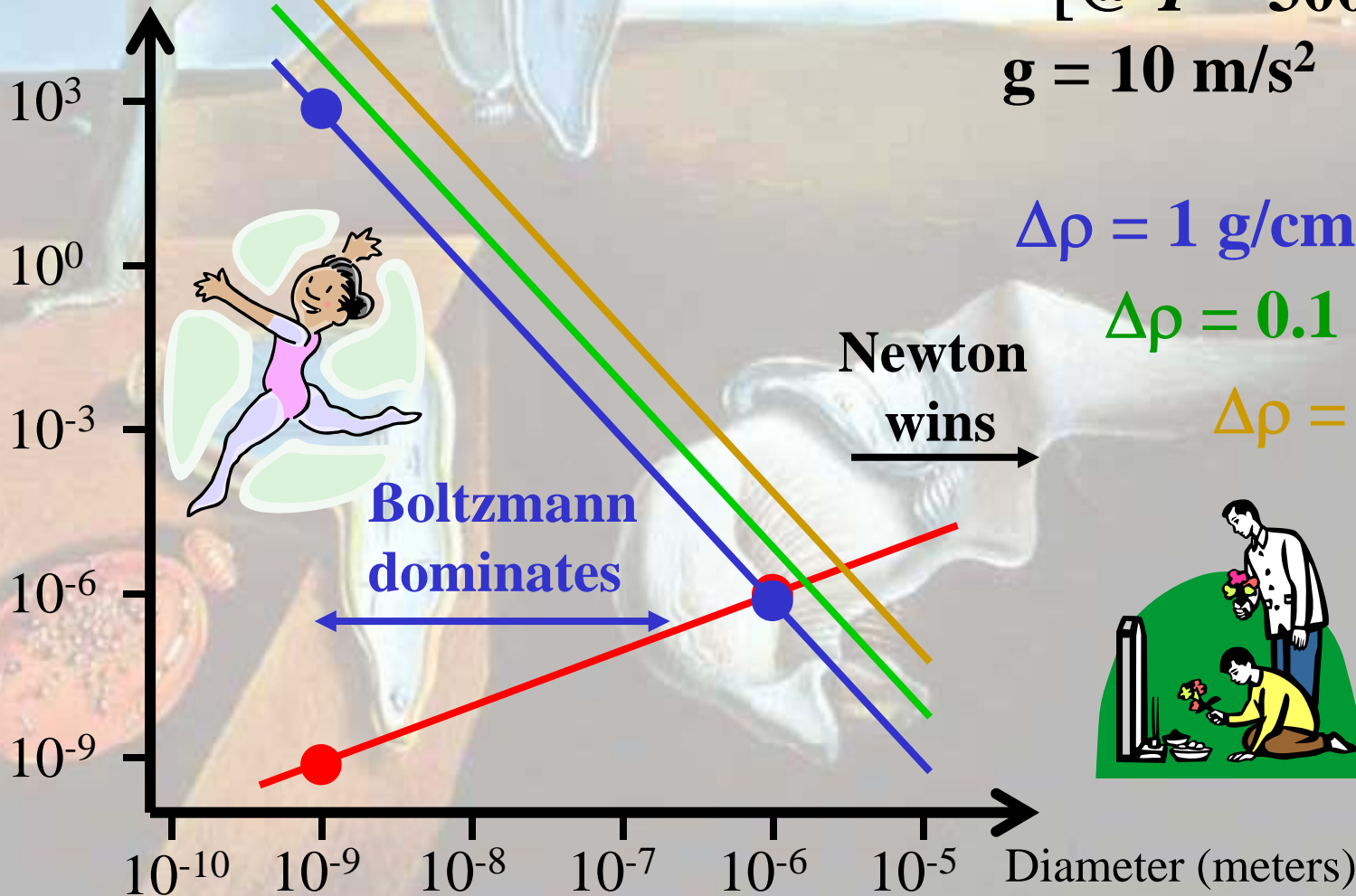


Gravitational length;  
diameter (meters)

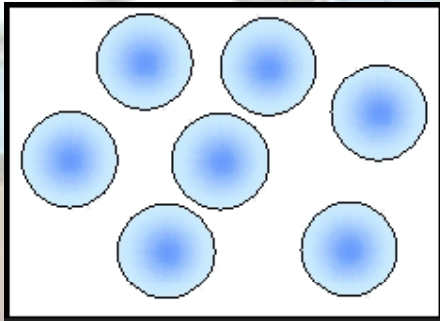
$$l_g = k_B T / m^* g \quad k_B T \approx 4 \times 10^{-21} \text{ J} \quad [\text{@ } T = 300 \text{ K}]$$

$$g = 10 \text{ m/s}^2$$

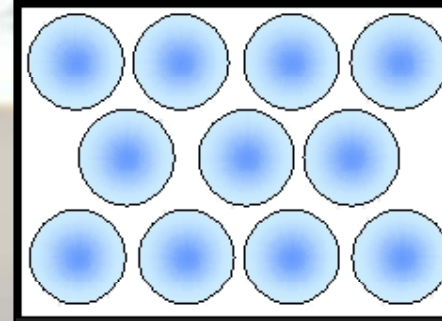
$\Delta\rho = 1 \text{ g/cm}^3$   
 $\Delta\rho = 0.1 \text{ g/cm}^3$   
 $\Delta\rho = 0.01 \text{ g/cm}^3$



# Colloid self-assembly: Entropy-induced order



**fluid**



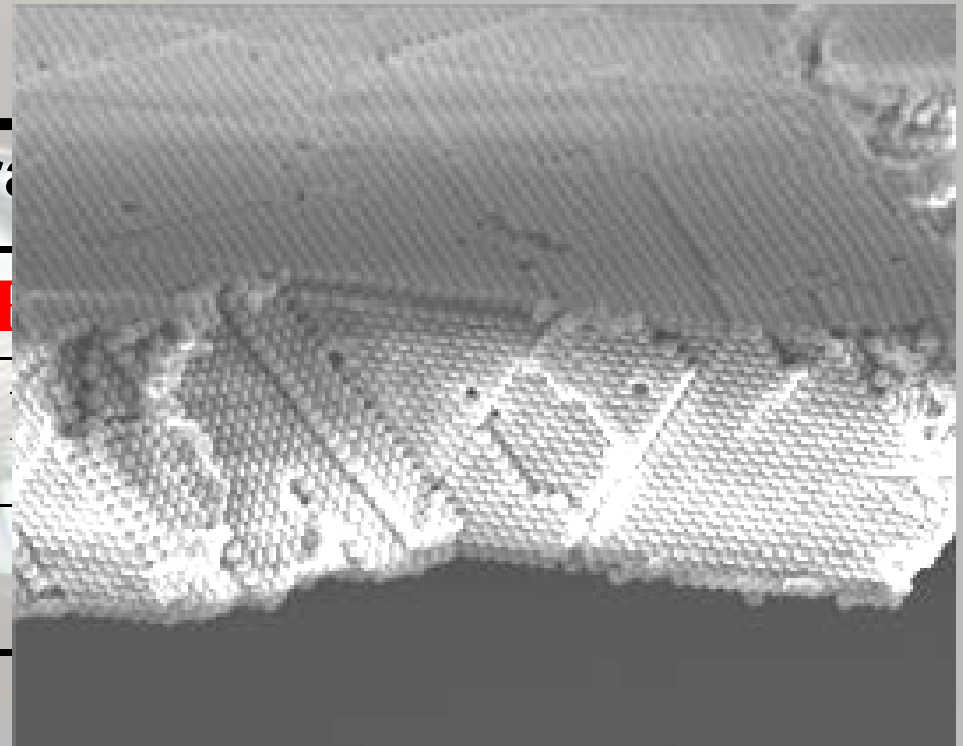
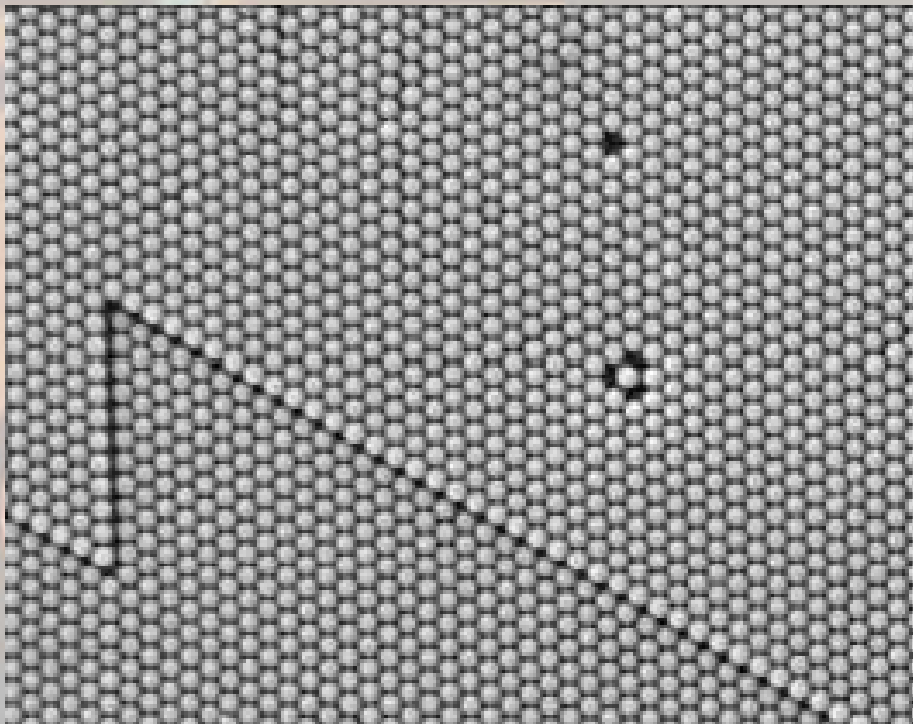
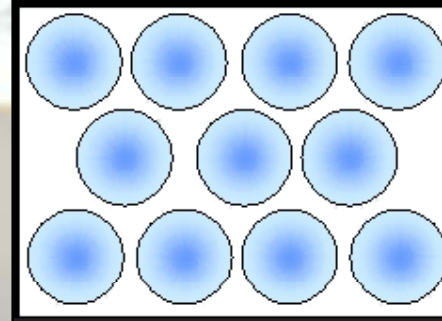
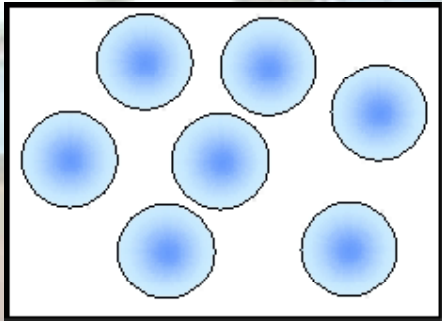
**crystal**

**concentration** →

Entropy	<b>Fluid</b>	<b>Crystal</b>
Configurational (macroscopic)	high	low
Excluded volume (microscopic)	low	high

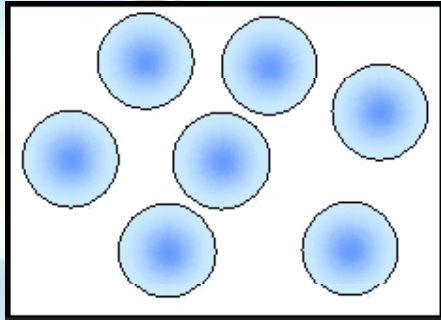


# Colloid self-assembly: Entropy-induced order

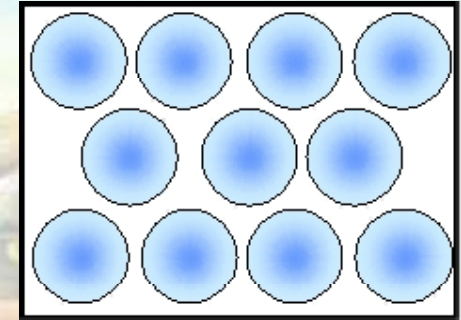


concentration →

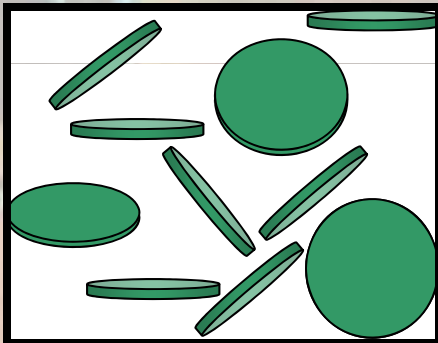
Shape matters!



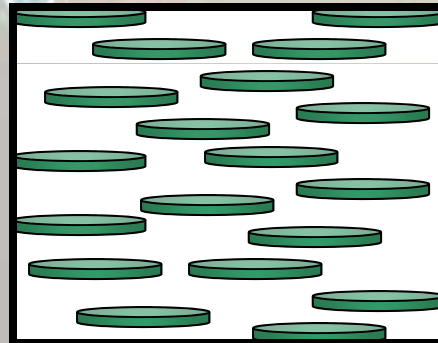
fluid



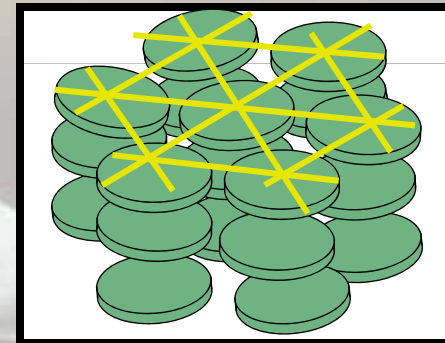
crystal



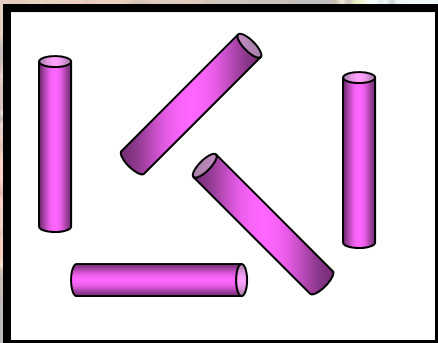
isotropic



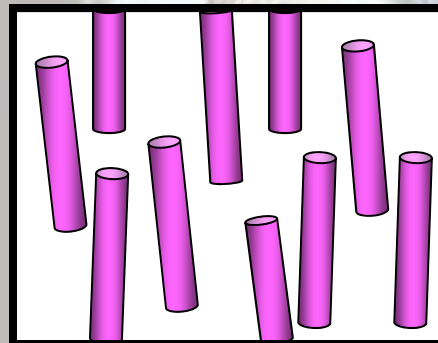
nematic



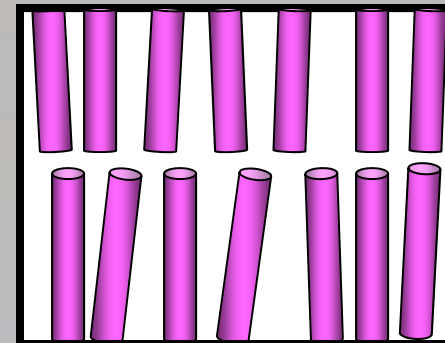
columnar



isotropic



nematic

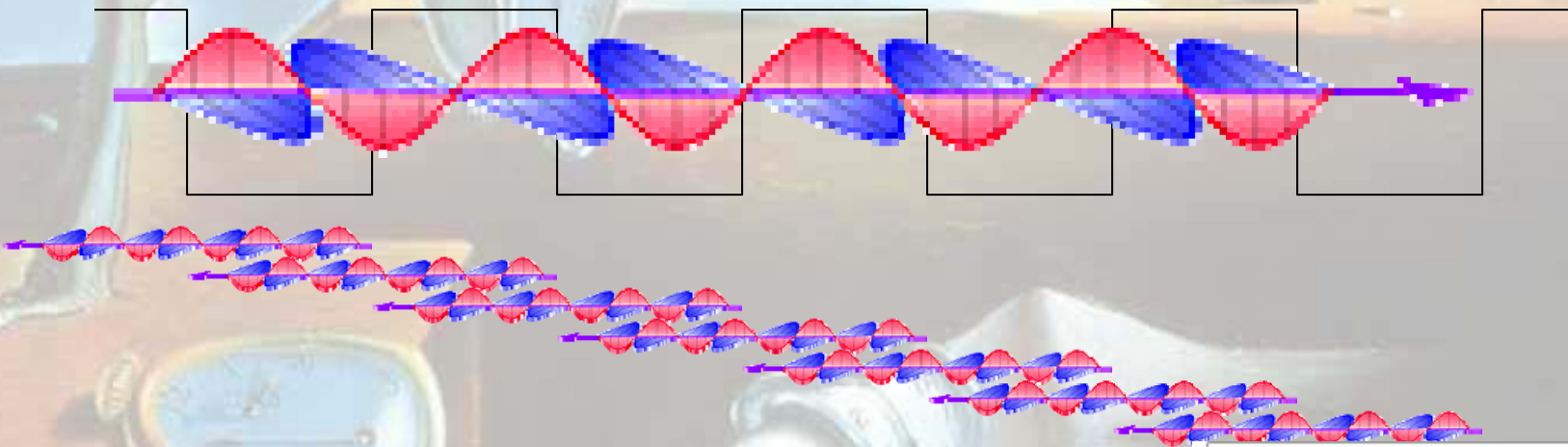


smectic



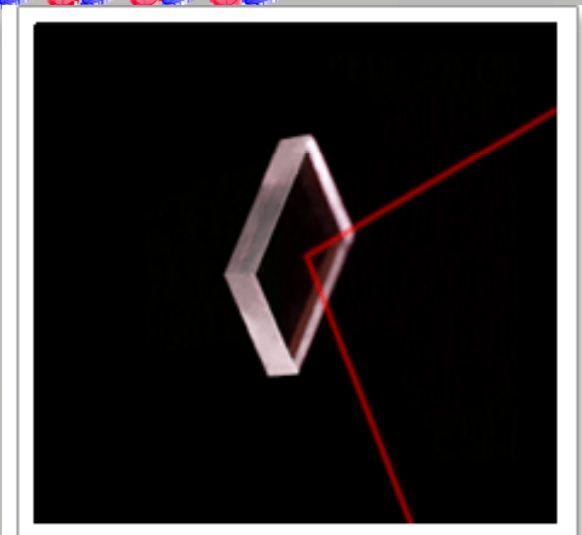
# Why is it useful: Photonics

Material with periodic modulation of optical properties on the scale comparable to the wavelength of light (hundreds of nm).



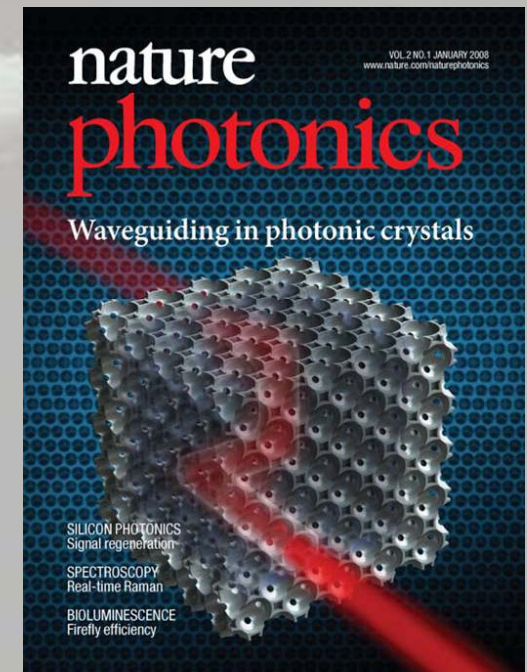
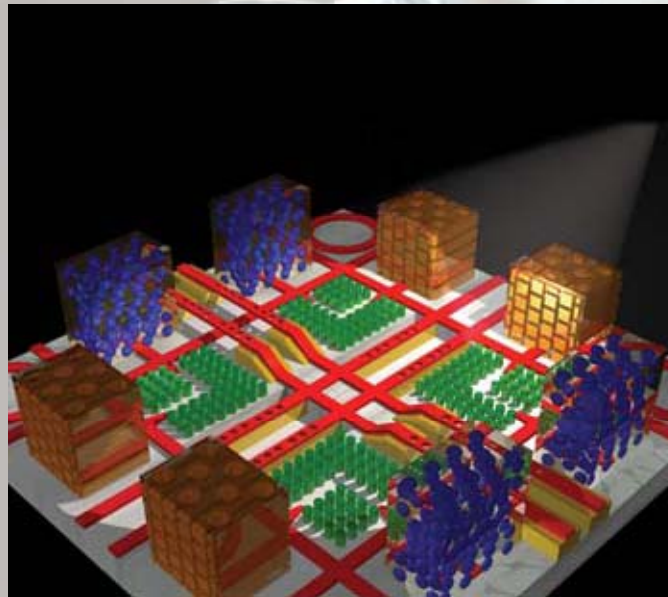
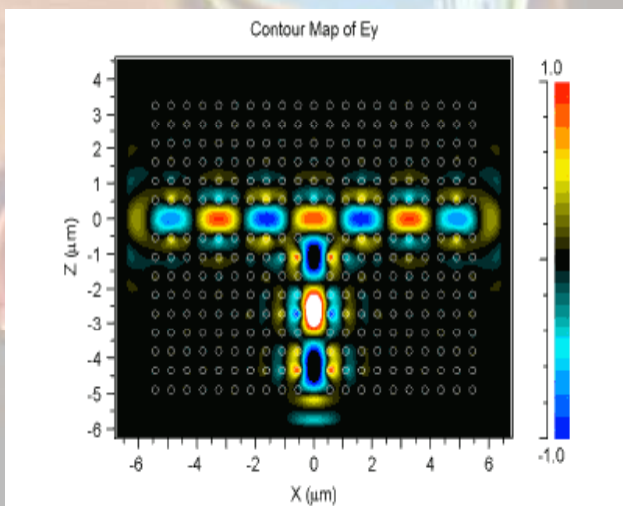
Resonant light scattering will cause photonic band gaps: light with certain wavelength will not be able to propagate through.

Example of 1D photonic nanomaterial:  
Dielectric multilayer laser mirrors



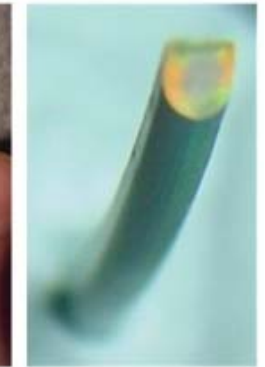
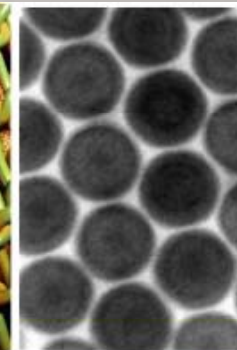
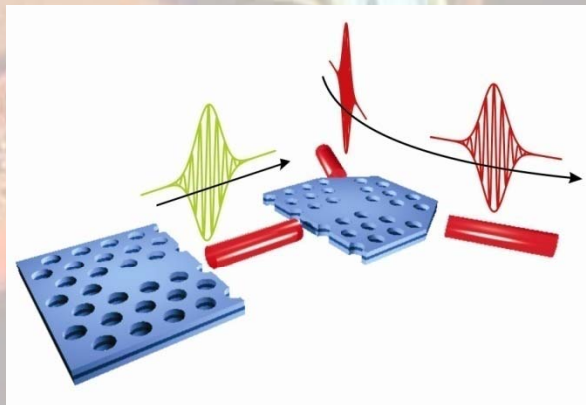
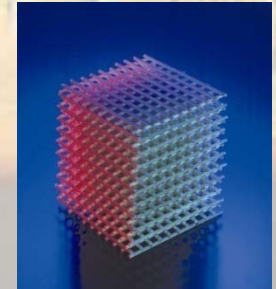
# Going from 1D to 3D:

- Creating full band gap  
Photonic crystal = Semiconductor for light
- Fine control of light propagation  
& emission
- Optical circuits



# Applications

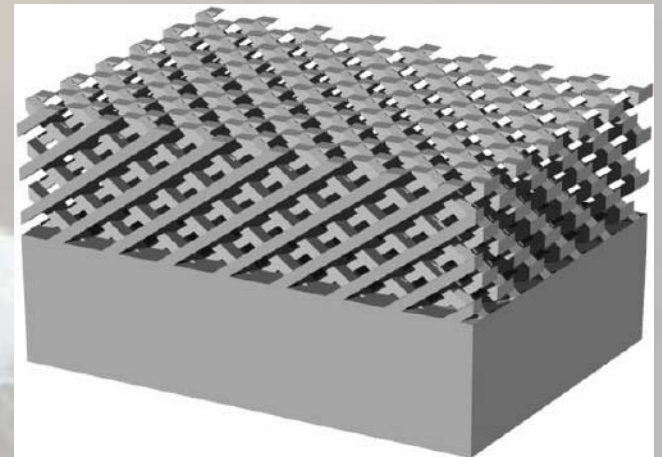
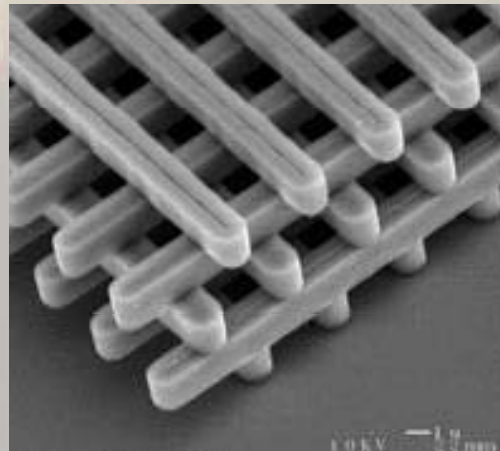
- Optical communications
- Optical computing
- Visualisation/display technology
- Light Harvesting (solar cells)
- Sensors
- Microlasers, ...





# How can one synthesize photonic nanomaterials: Lythography techniques

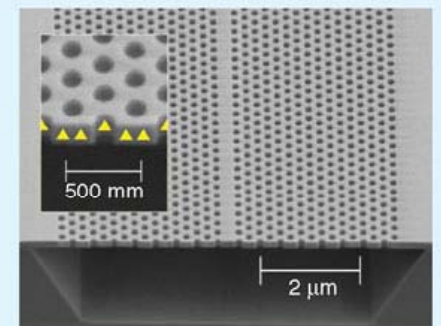
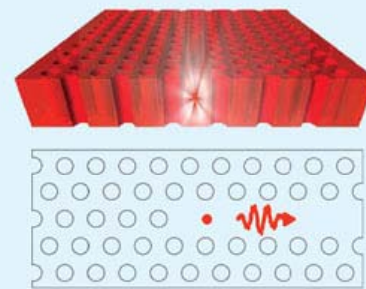
- Electron Lythography
- Focused Ion Beam
- Optical Lythography
- ...



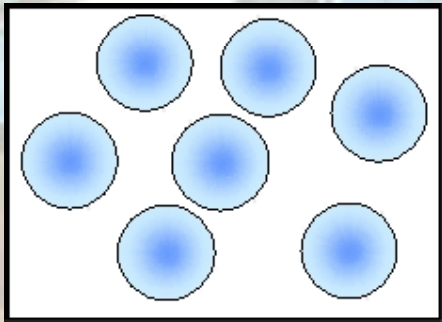
Beautiful design possibilities

**BUT**

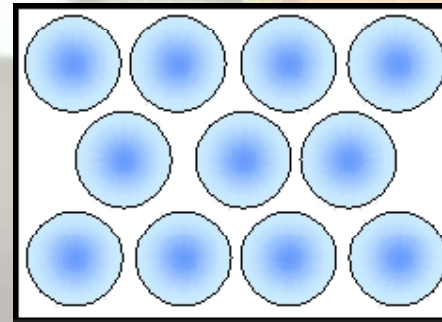
- difficult in 3D
- Scale-up problems
- Too involved and too expensive



# Alternative approach: use colloidal self-assembly

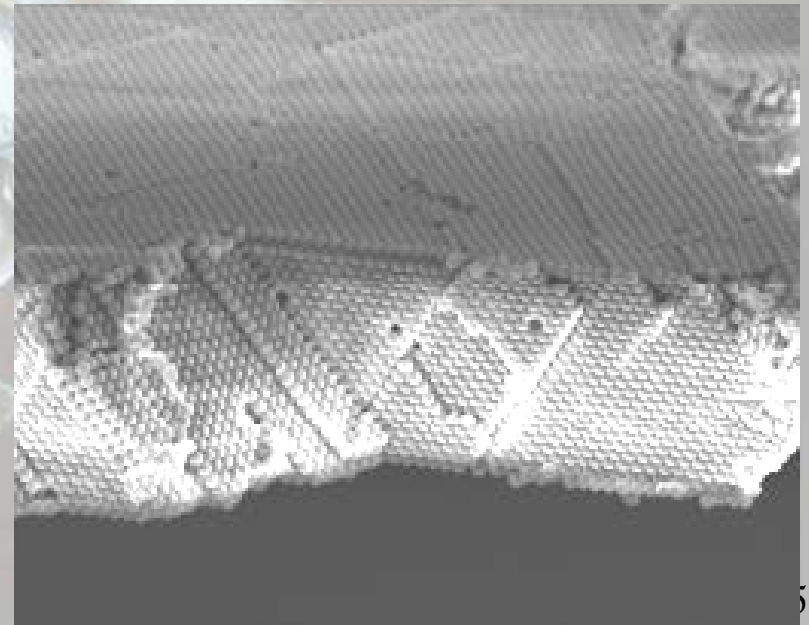


**fluid**

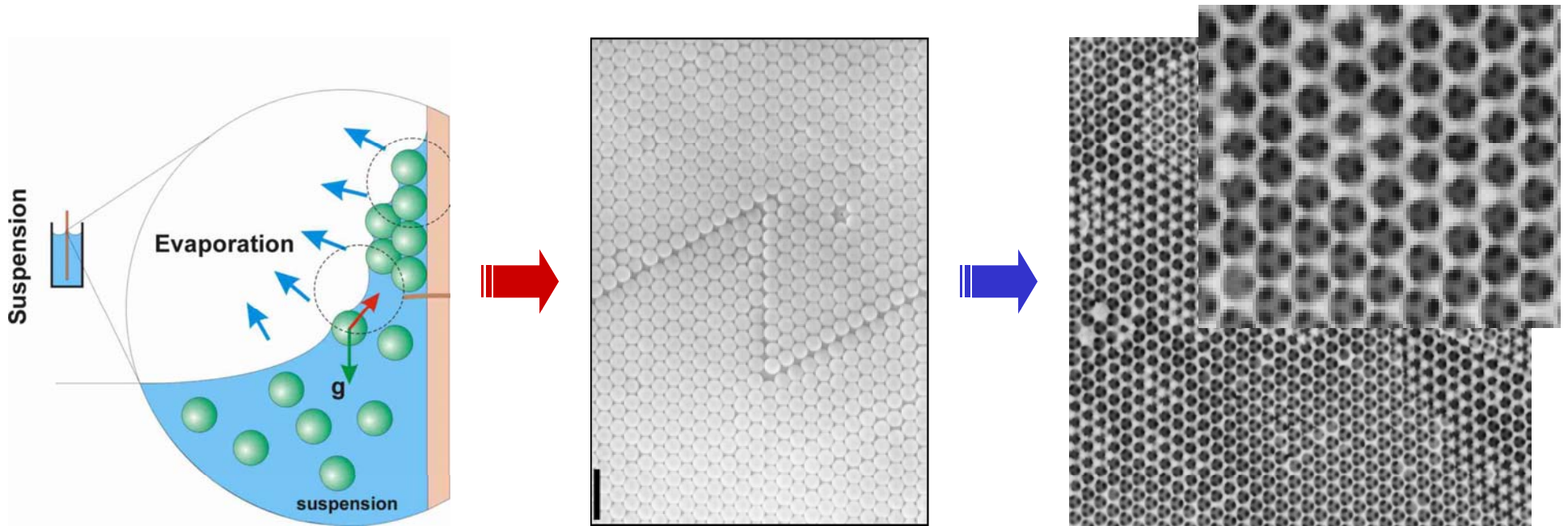


**crystal**

- Three-dimensional
- Easy tuneable
- Can be scaled up
- Inexpensive



# photonic materials



**Colloid self-assembly by  
convective & capillary forces**

**Filling the voids with another  
material and removing the spheres**

**high contrast (no optical techniques applicable)**



# Schedule

- Introduction to nanoelephants
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- Example 1: Hard spheres
- Example 2: Rusted nanonails
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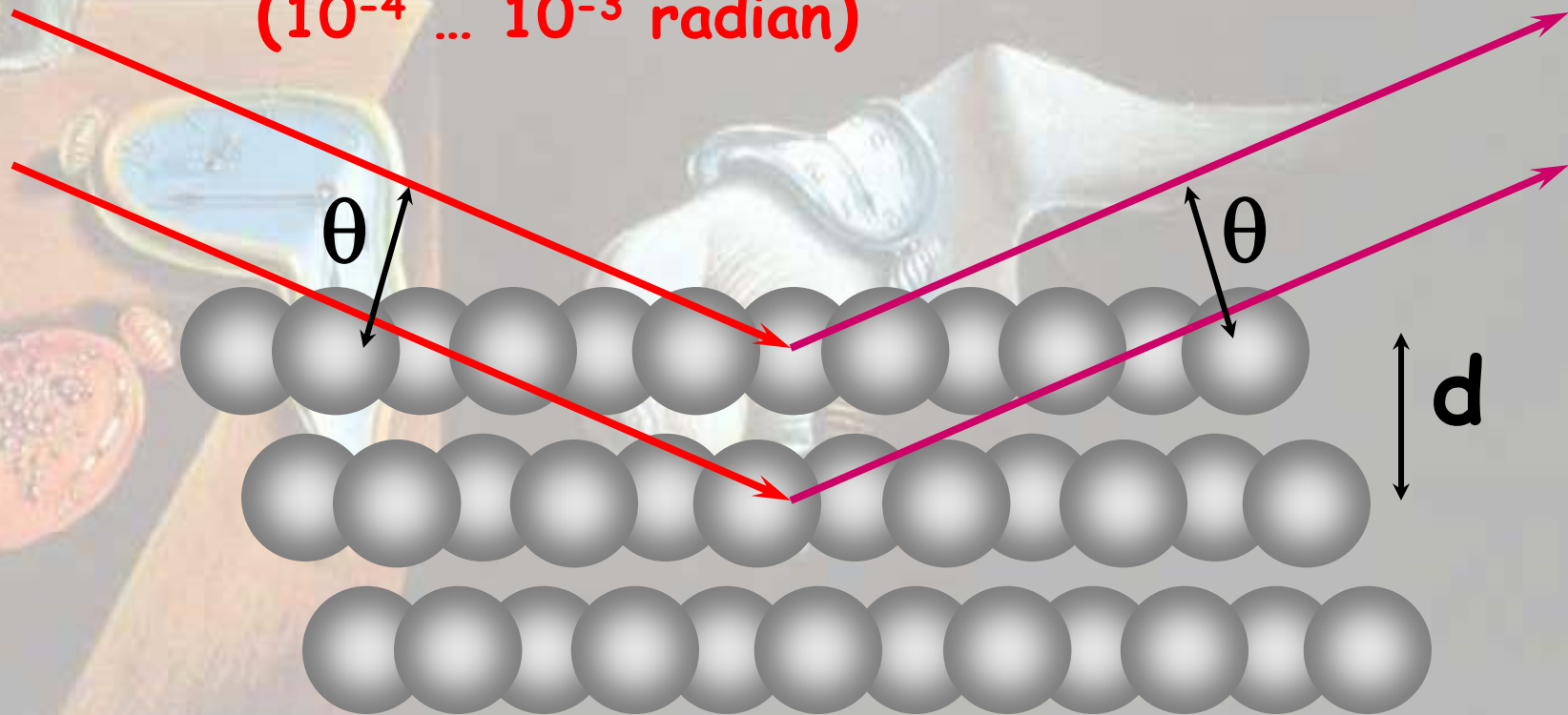
# Theory: Bragg's law

Ordinary (atomic) crystals:  $d \sim \lambda$   
=> large diffraction angle  $2\theta$

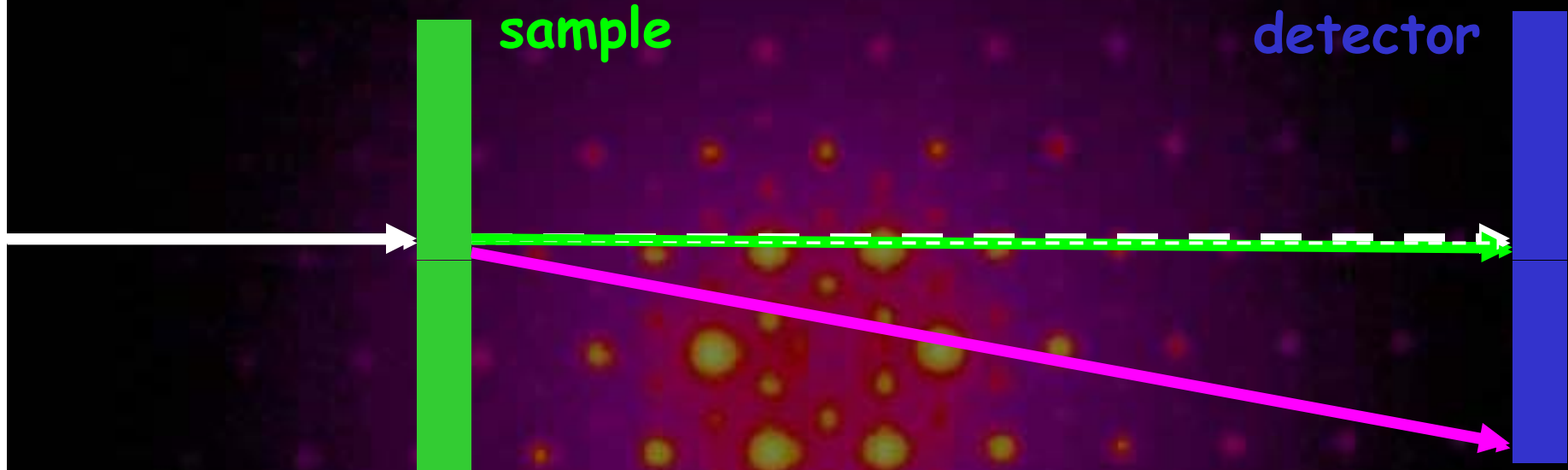
X-rays:  $\lambda \sim 1 \text{ \AA}$

Colloidal crystals:  $d \gg \lambda$   
=> small diffraction angle  $2\theta$   
( $10^{-4} \dots 10^{-3}$  radian)

$$\sin\theta = n\lambda/2d;$$
$$n=1,2,\dots$$



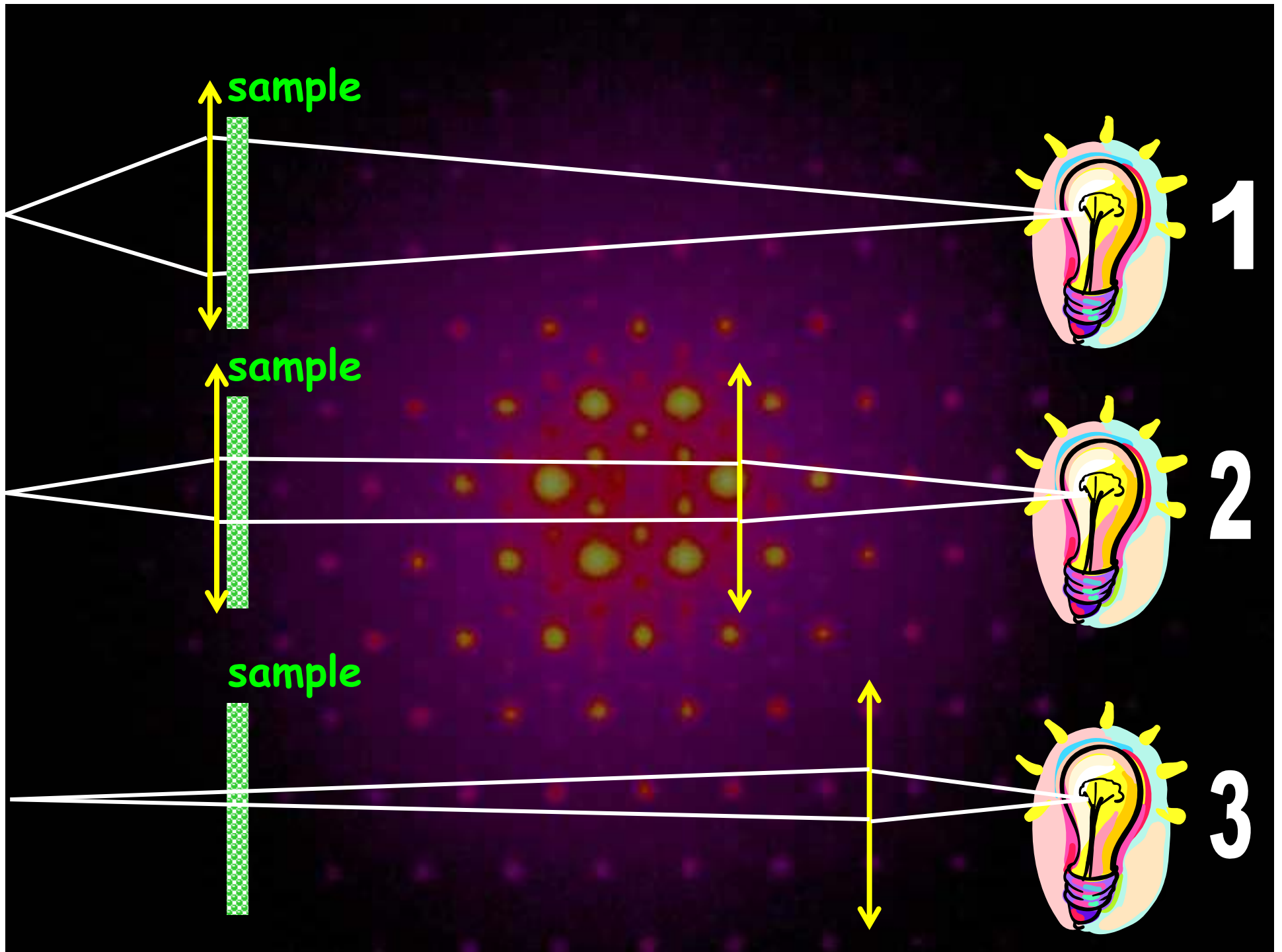
# Scattering experiment



Extreme angular resolution is needed  
How do we get it?

- parallel beam?
- pencil beam?





$$l_{tr} = \frac{\lambda L}{d}$$

A coherent patch

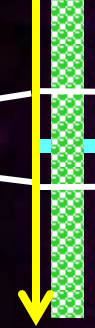
Up to a mega-Ångstrom!

sample



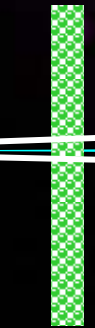
1

sample

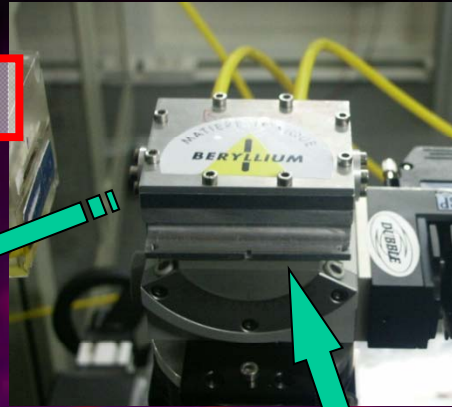
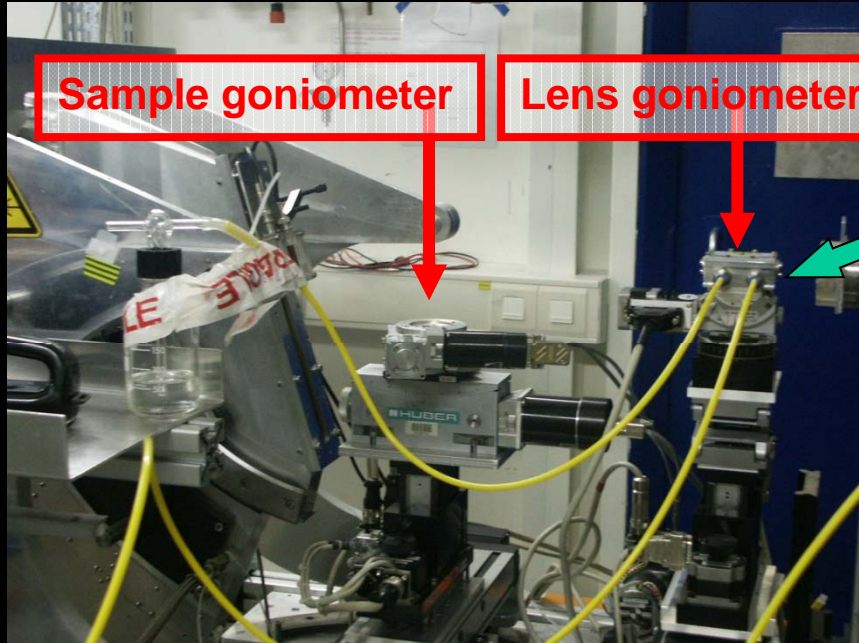


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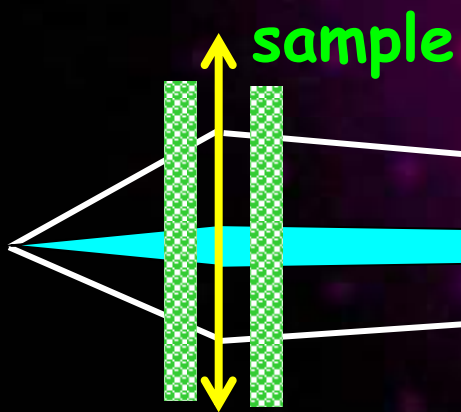
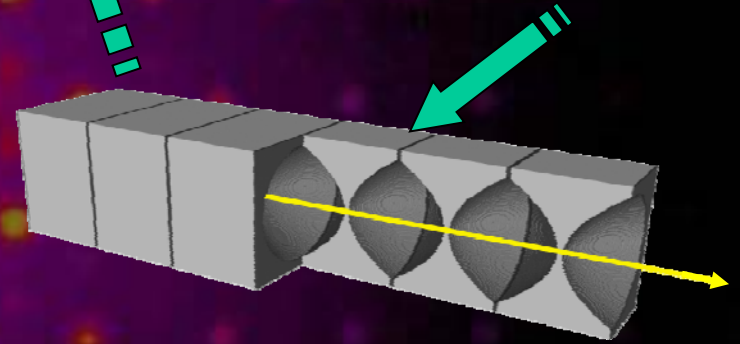
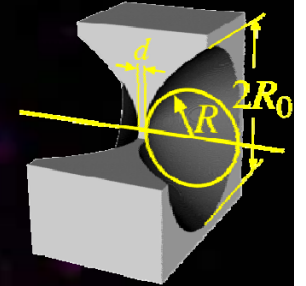
sample



3

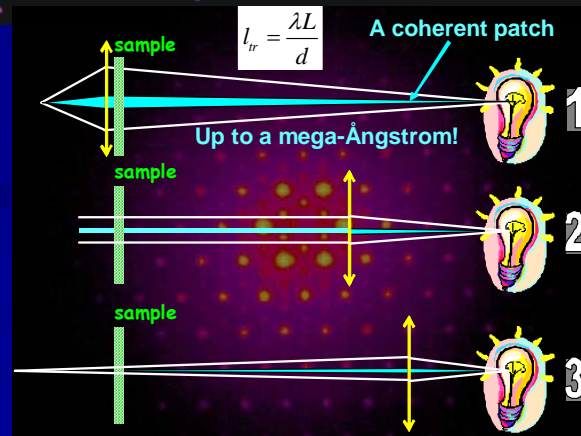
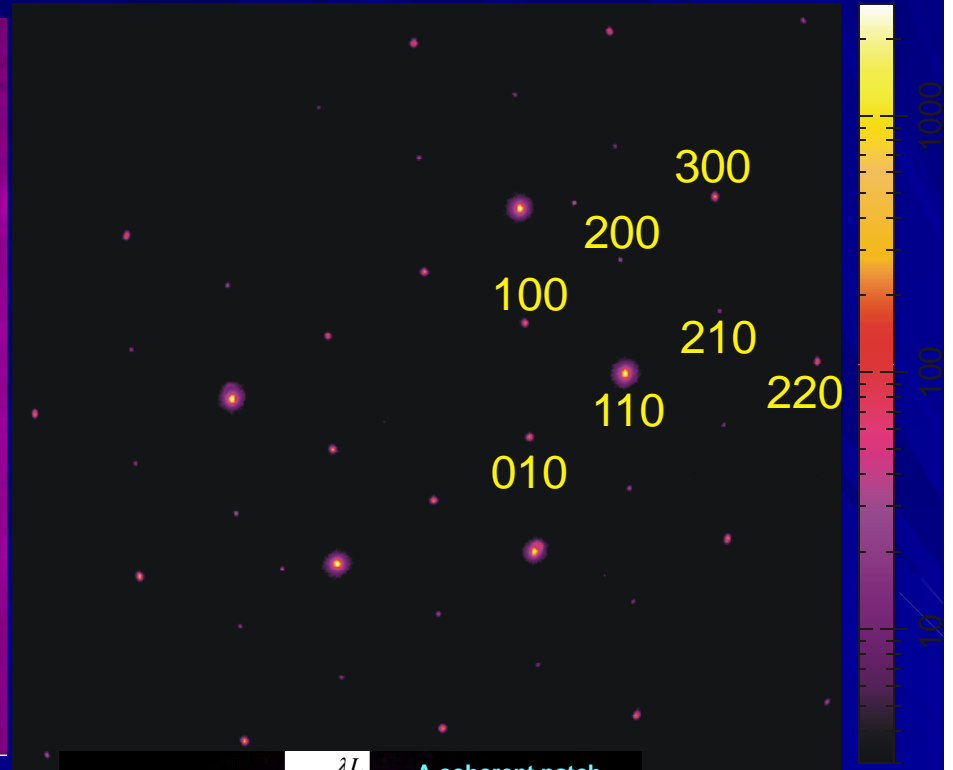
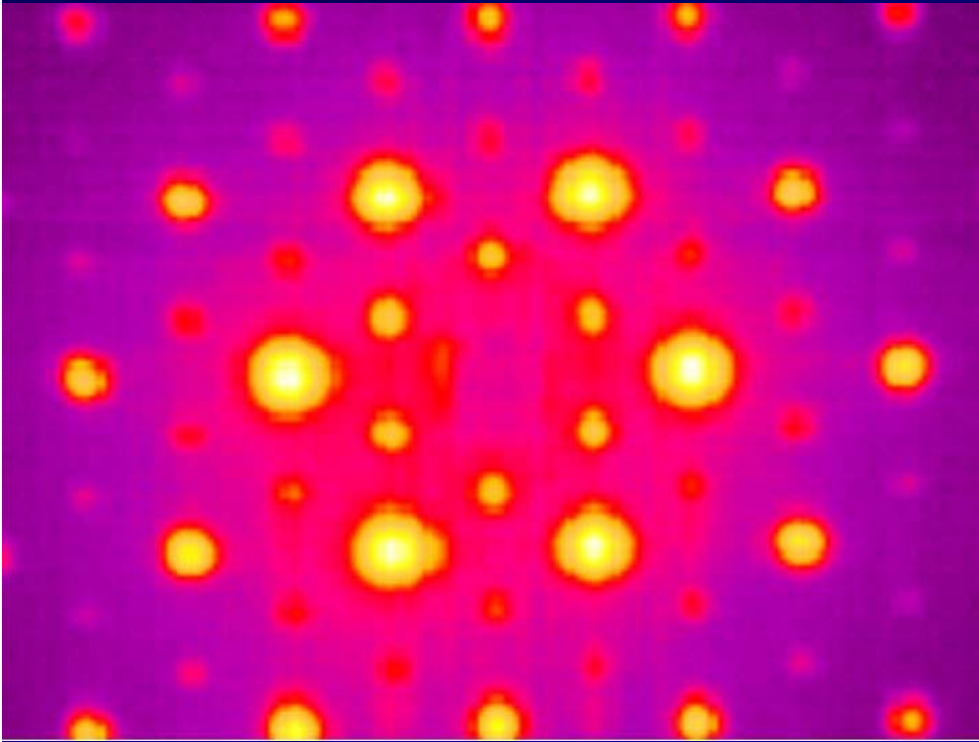


Be lens



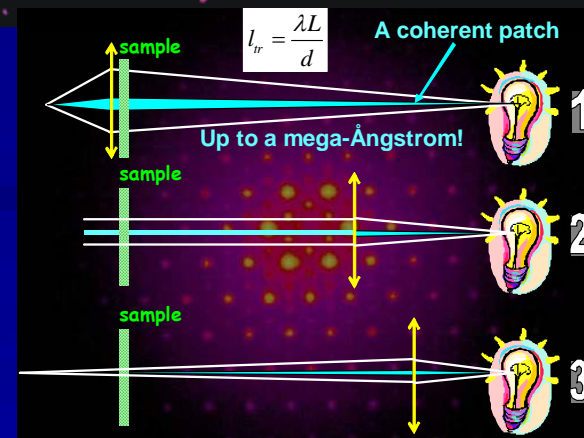
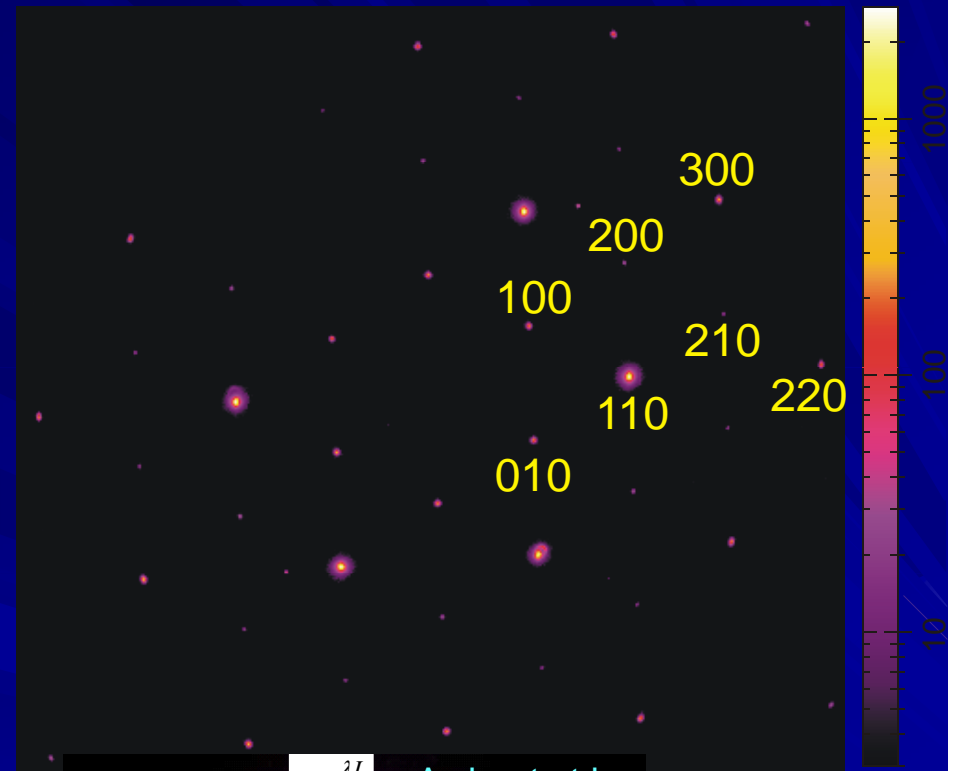


# Microradian diffraction



# Microradian diffraction

- Colloids = elephants => microradian XRD
- Peak positions: Crystal structure
- Peak width: Long-range order
- Peak tails: fluctuations



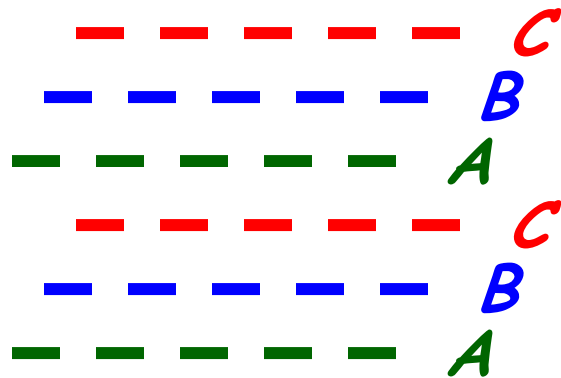
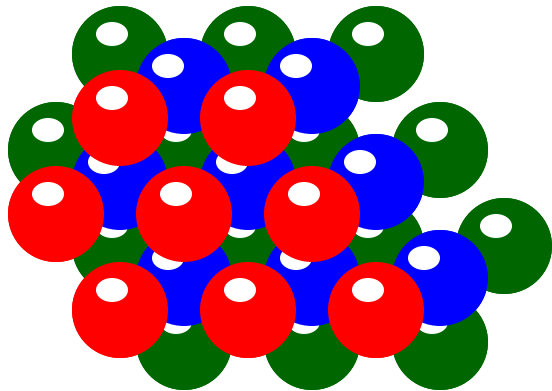
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- **Example 1: Hard spheres**
- Example 2: Rusted nanonails
- Conclusion

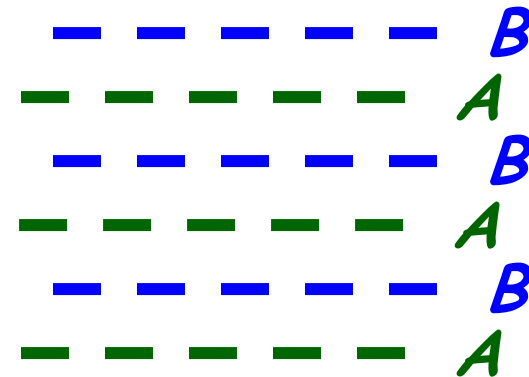
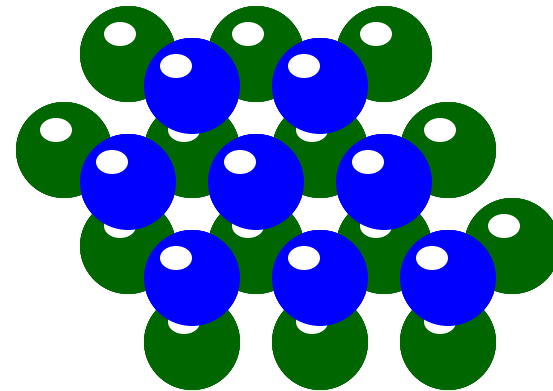


# Example 1: Hard balls

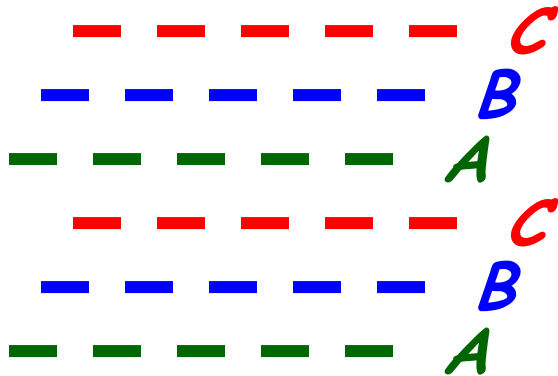




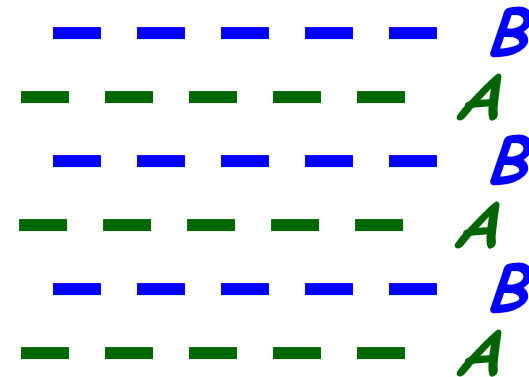
Face-centred  
cubic (fcc)



Hexagonal close  
packed (hcp)

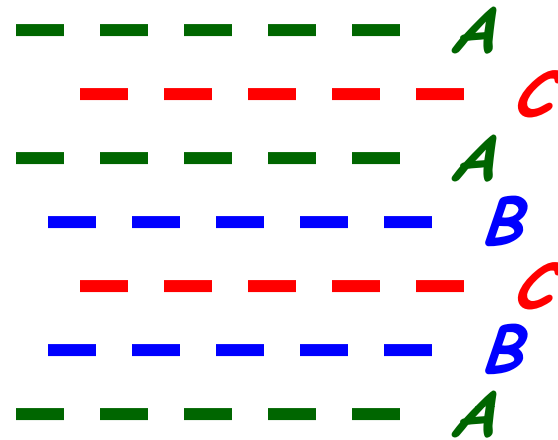
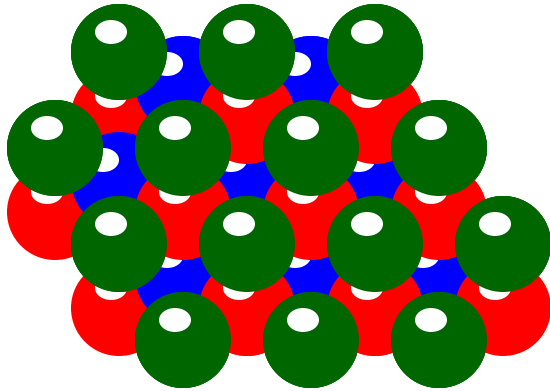


Face-centred  
cubic (fcc)



Hexagonal close  
packed (hcp)





Random hexagonal  
close packed (rhcp)

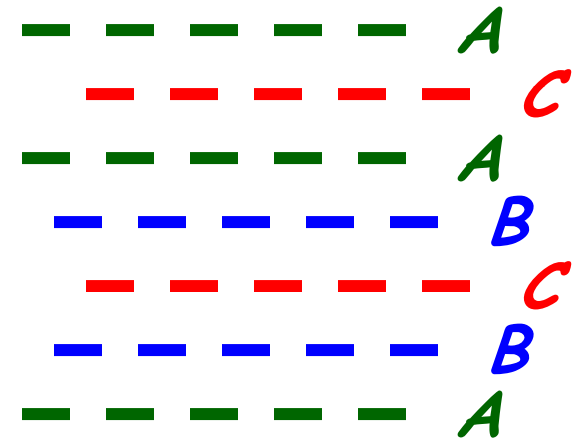
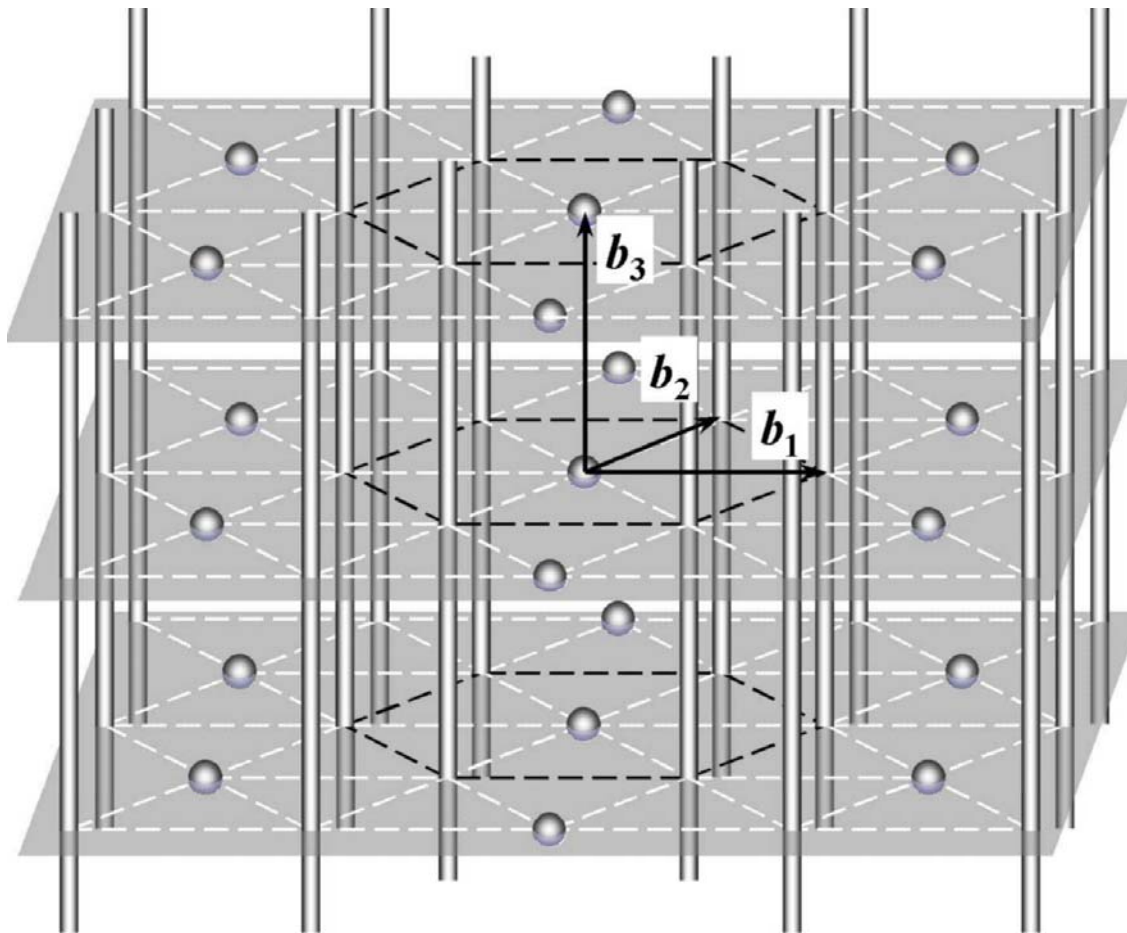
All three (fcc, hcp & rhcp)  
have the same packing ratio

# rhcp seen in the reciprocal space

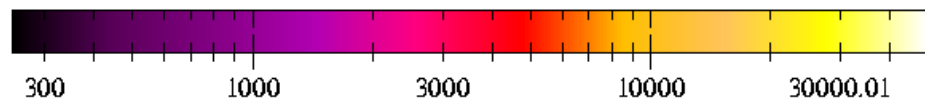
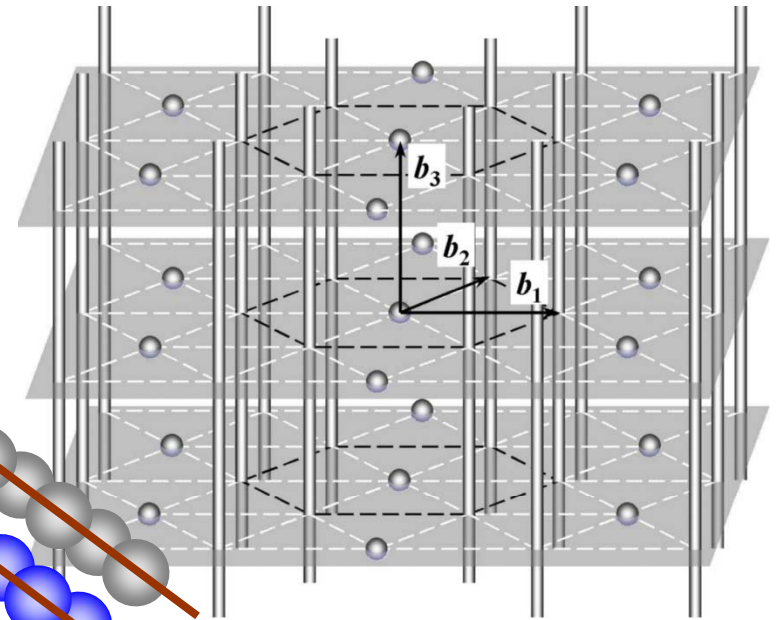
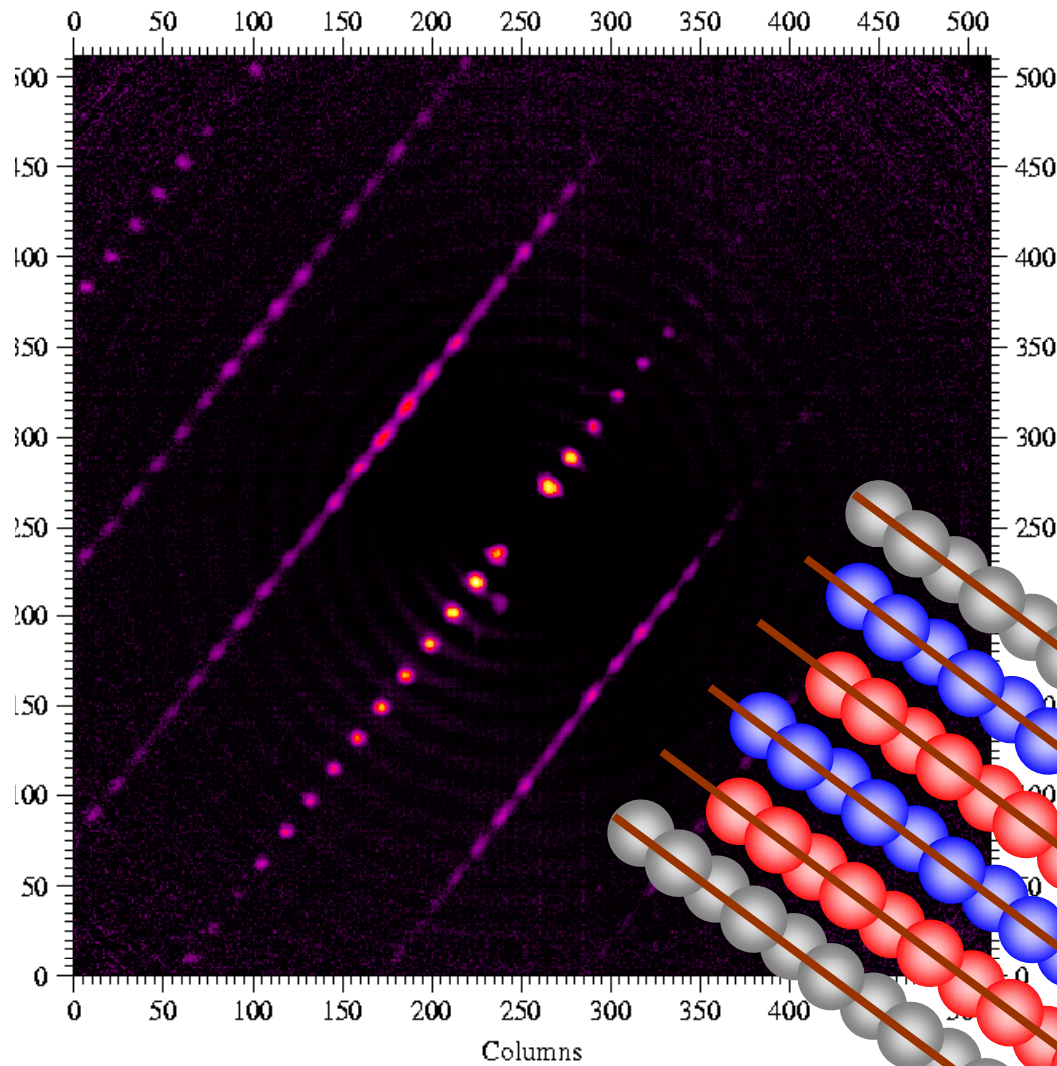
Truly periodic crystal – sharp Bragg spots

No interlayer periodicity  $\Rightarrow$  Bragg rods

Yet, some reflections stay sharp (only 3 lateral positions)



# Bragg rods are real! (our earlier result)



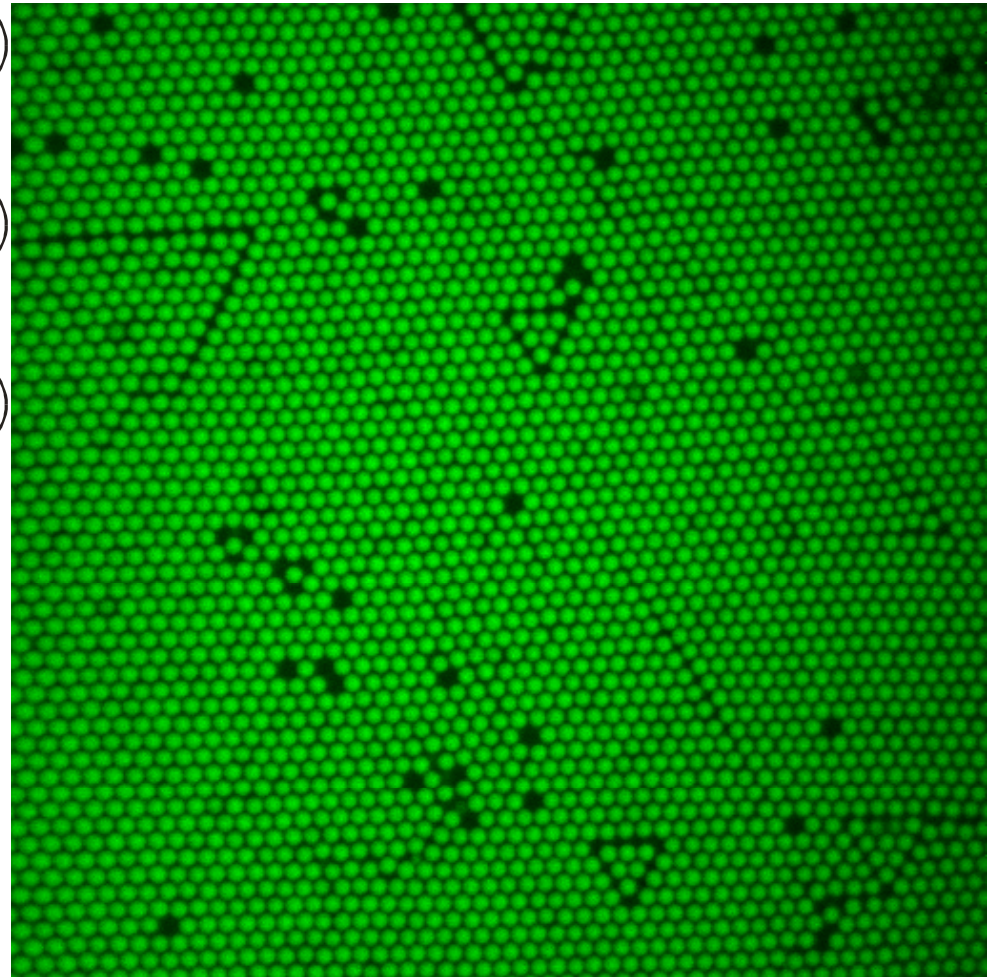
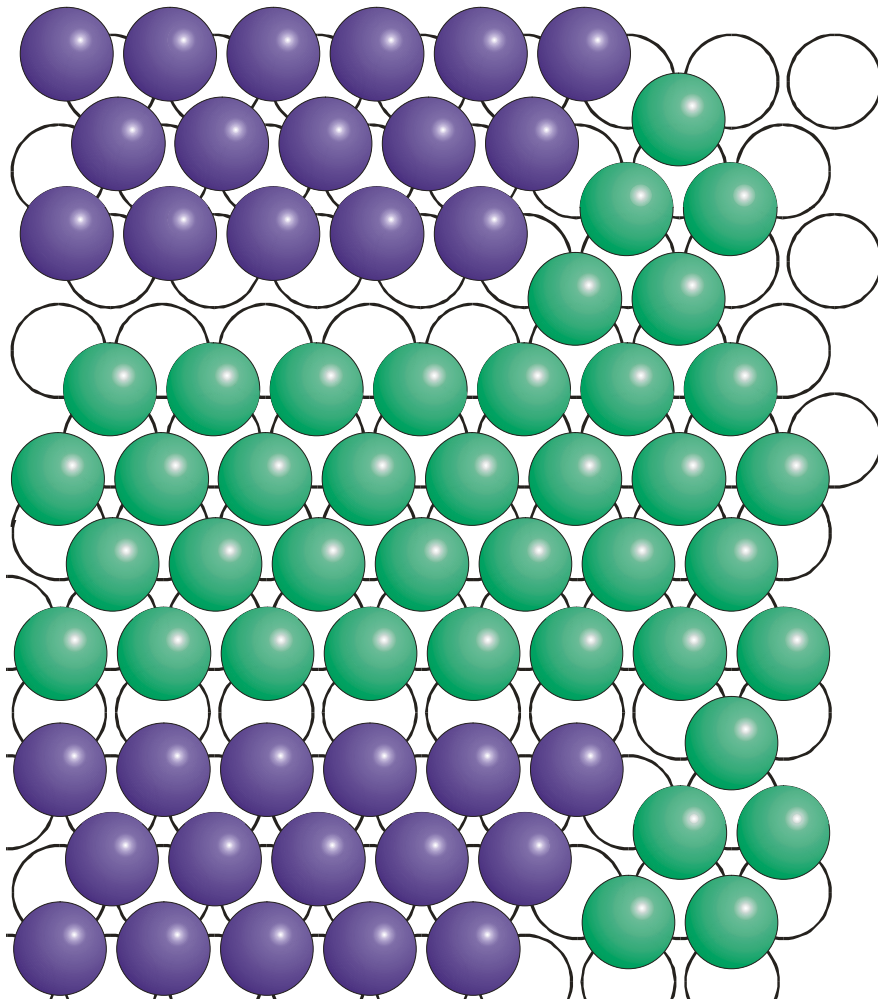
Structure factor

*AVP, Dolbnya, Aarts,  
Vroege, Lekkerkerker,  
Phys.Rev.Lett., 90,  
028304 (2003).*



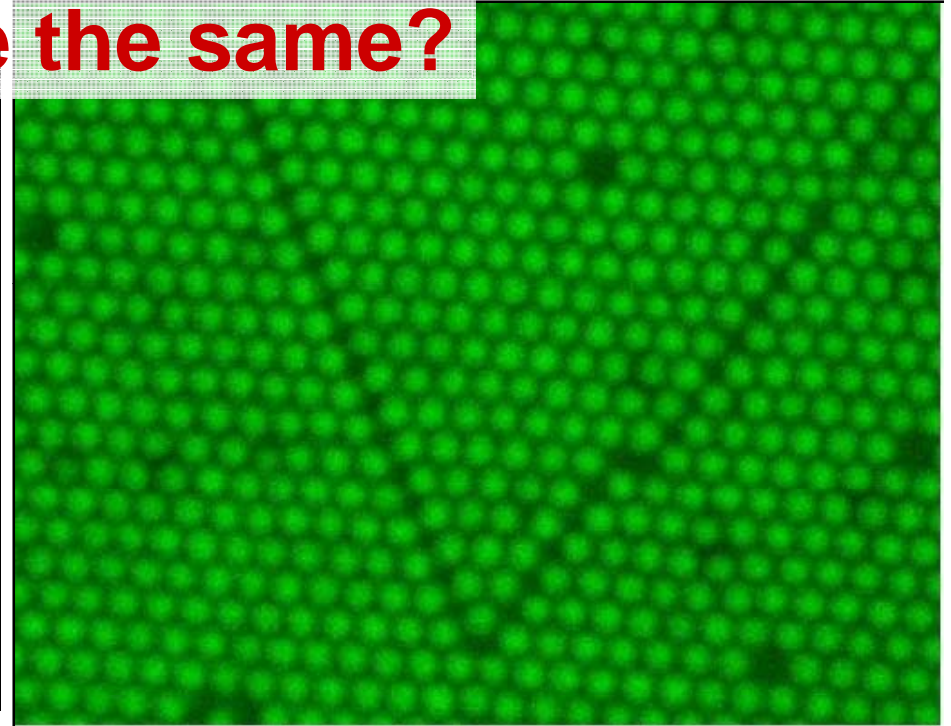
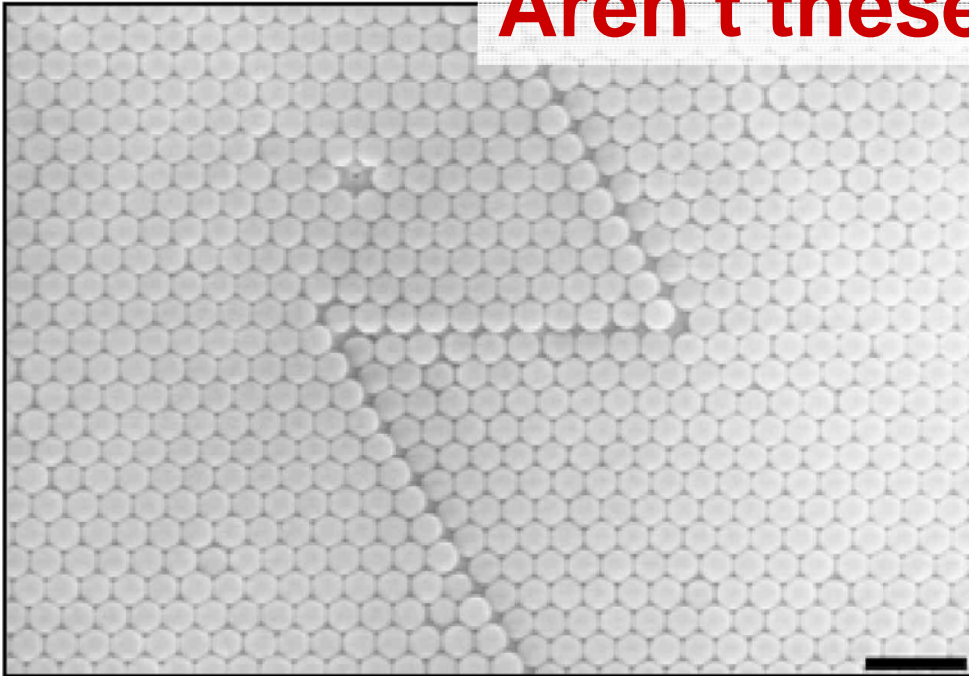
# Earlier: in-plane stacking disorder

- J.M. Meijer, V.W.A. de Villeneuve, AVP, Langmuir, 23, 3554 (2007)
- V.W.A. de Villeneuve, P.S. Miedema, J.M. Meijer, AVP, EPL, 79, 56001 (2007)
- P.S. Miedema, V.W.A. de Villeneuve, AVP, PRE, 77, 010401 (2008)



# The idea of the experiment

**Aren't these the same?**

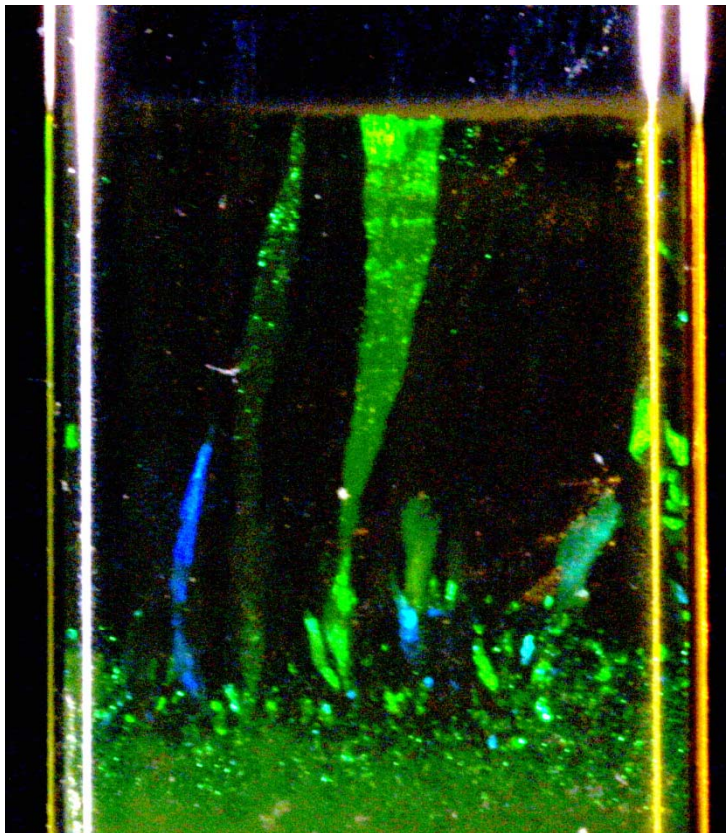
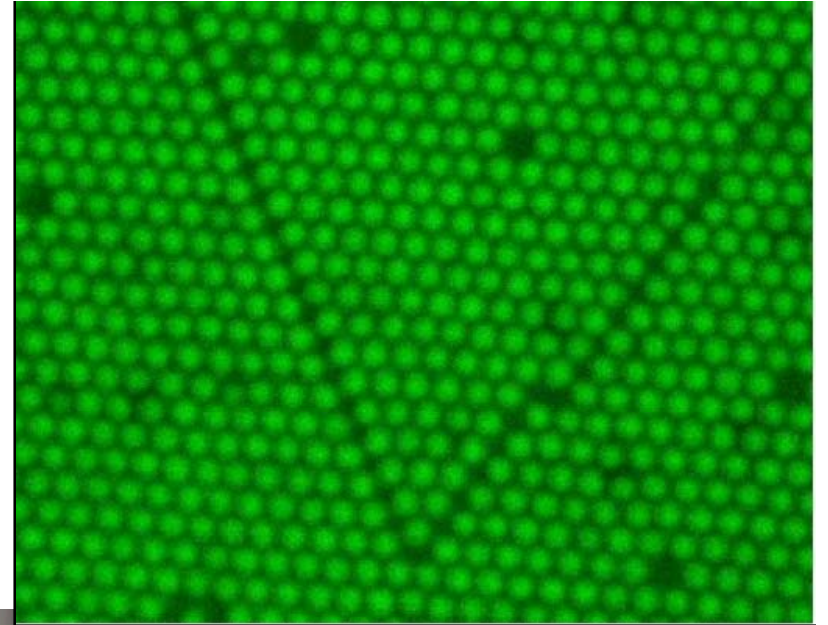


**Alexander Sinitskii et al.**  
SEM of vertical  
deposition crystals  
*Mendeleev Comm., 2007*

**Volkert de Villeneuve et al.**  
Confocal microscopy of  
sedimentary crystals,  
*Langmuir & EPL, 2007*



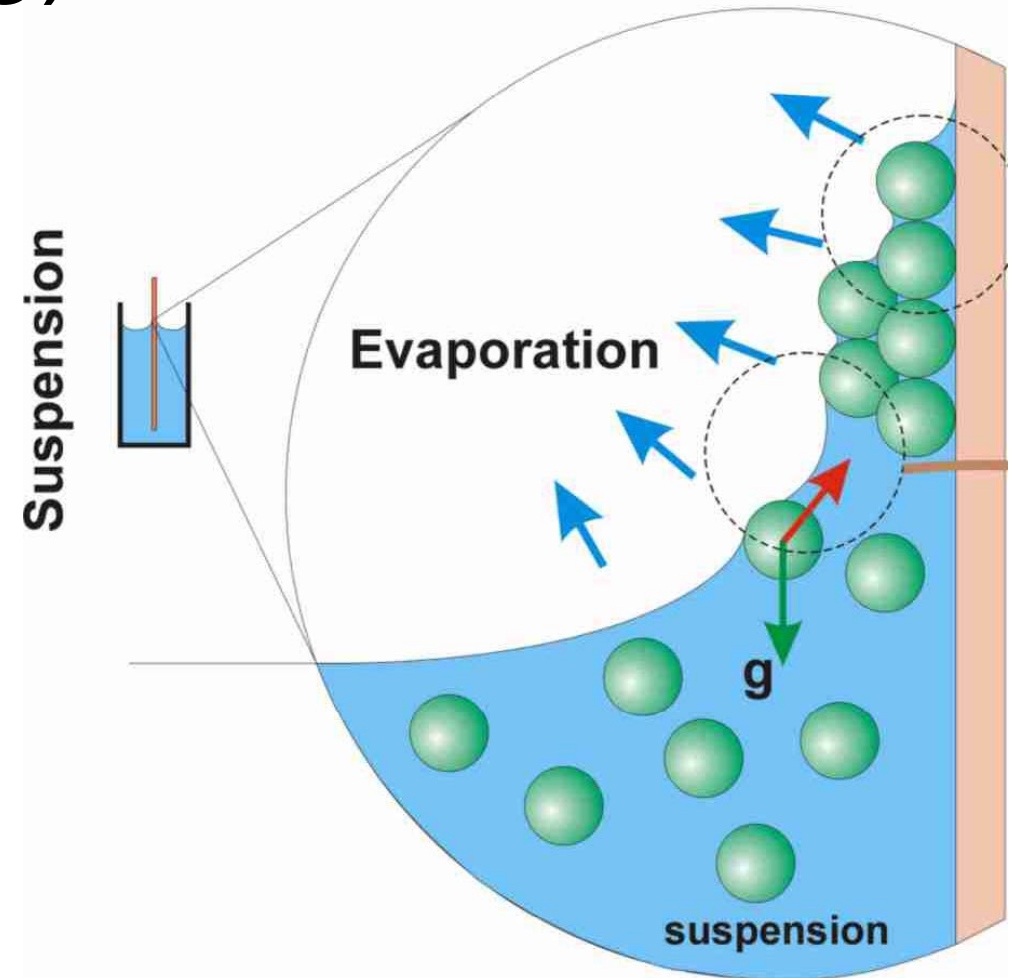
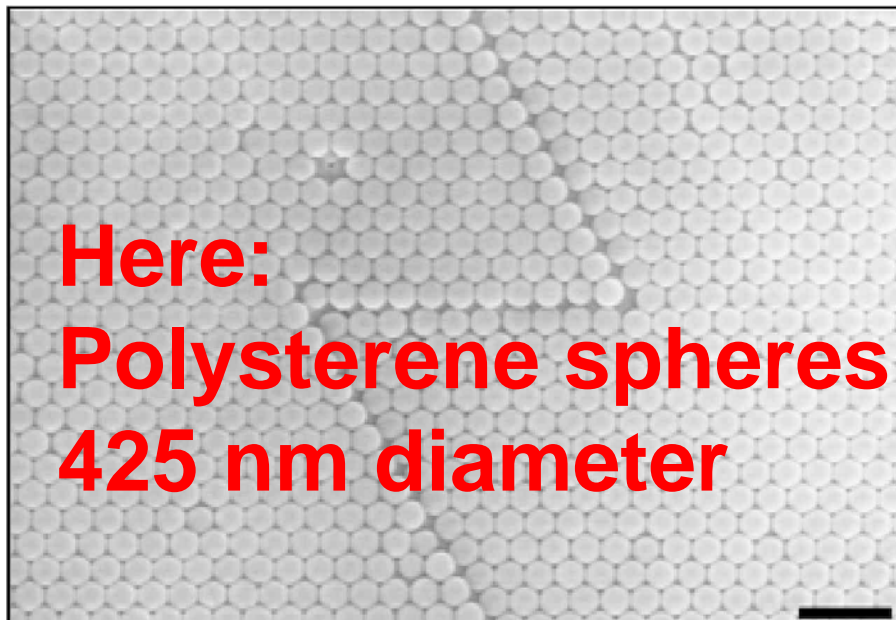
# Sedimentary crystals





# Vertical deposition crystals (controlled drying)

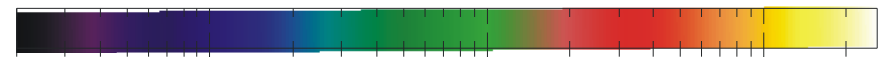
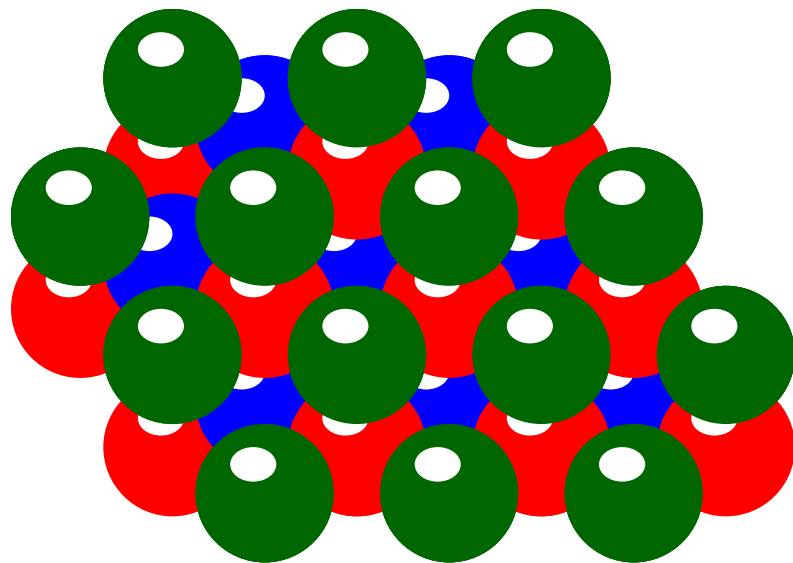
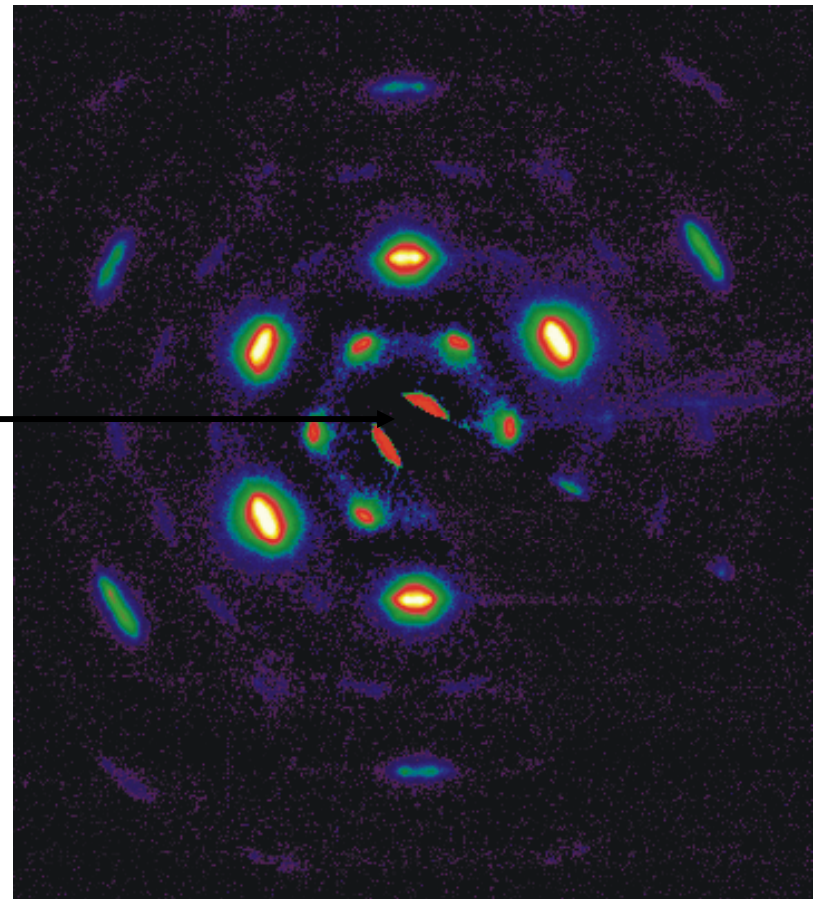
Popular technique to  
fabricate inverted  
photonic crystals



Picture courtesy K. Velikov

# Pattern #1

sample



10

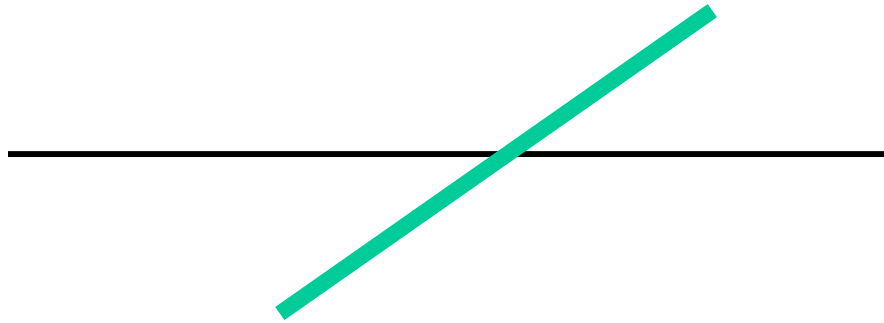
100

1000

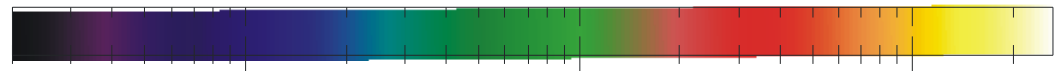
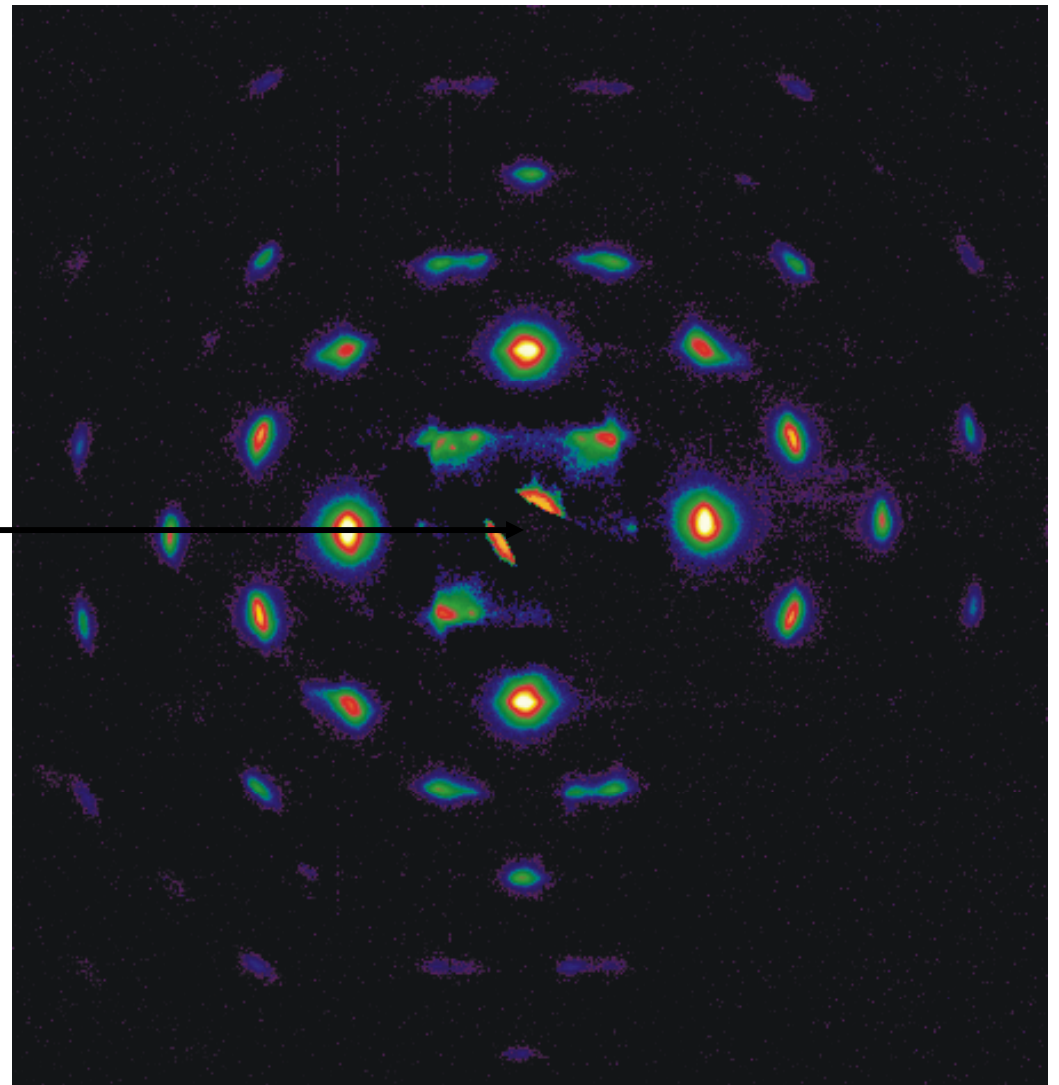
Intensity

# Pattern #2

sample



Sample turned  
by 55 degrees

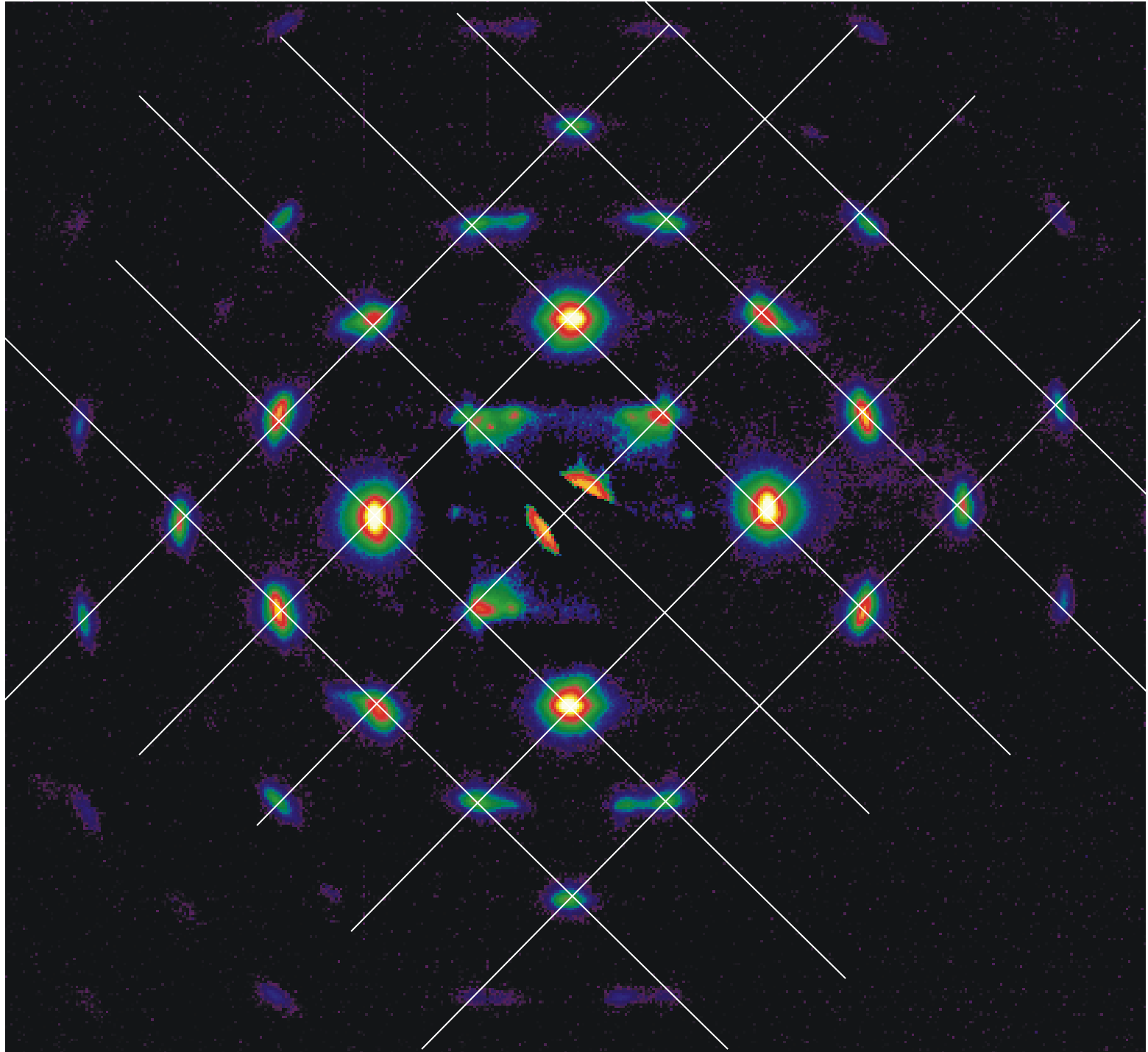


10

100

1000

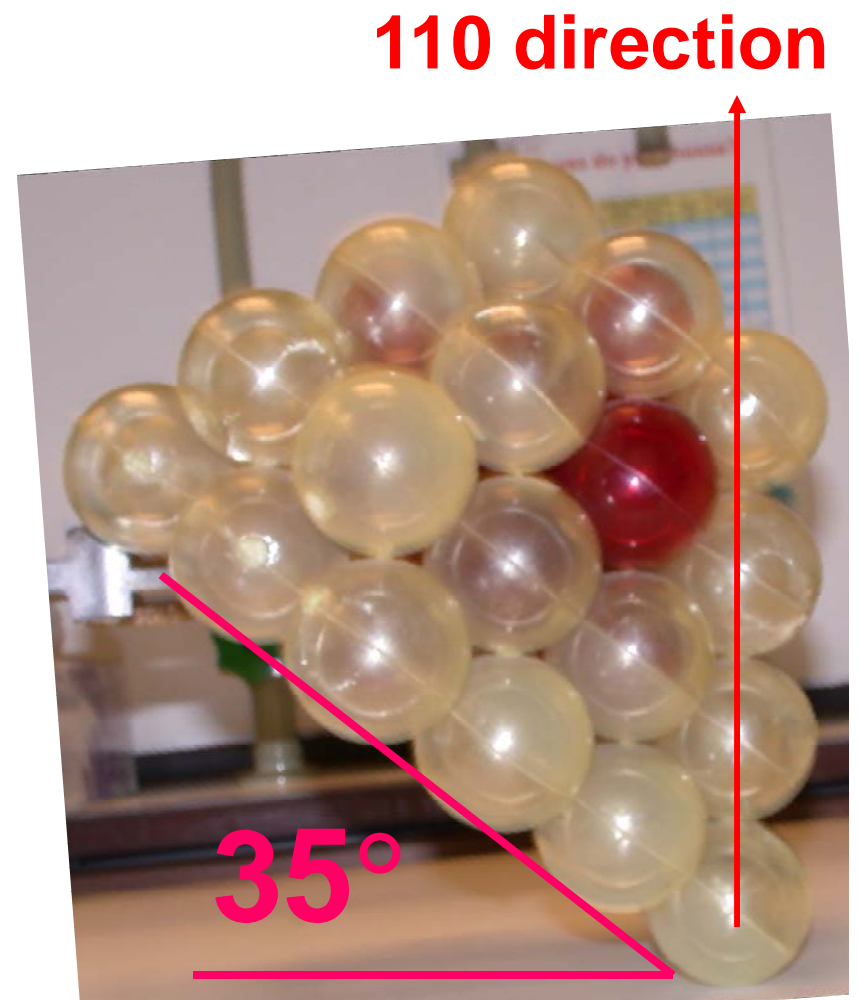
Intensity





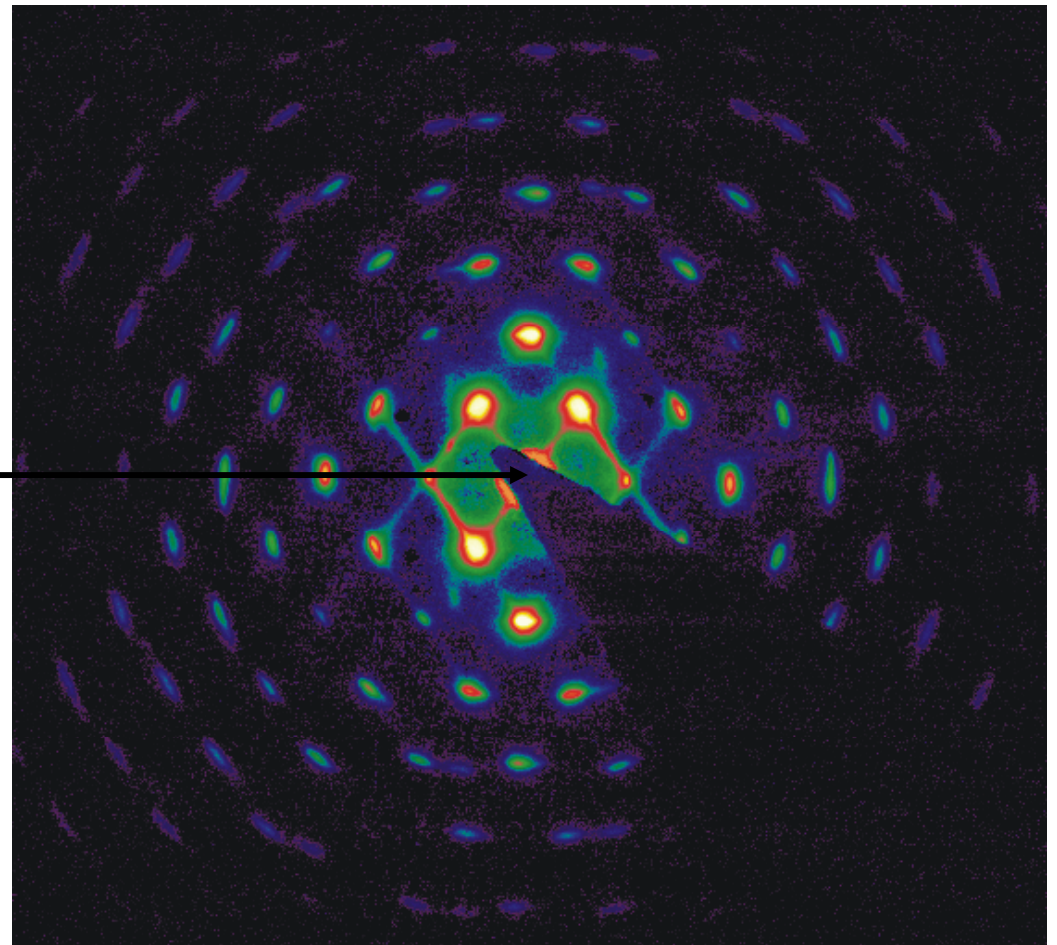
# Can we look along the 110 direction?

Sample is to be turned by 35 degrees

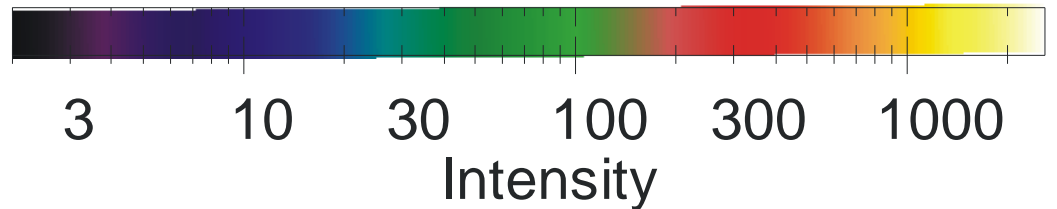


# Pattern #3

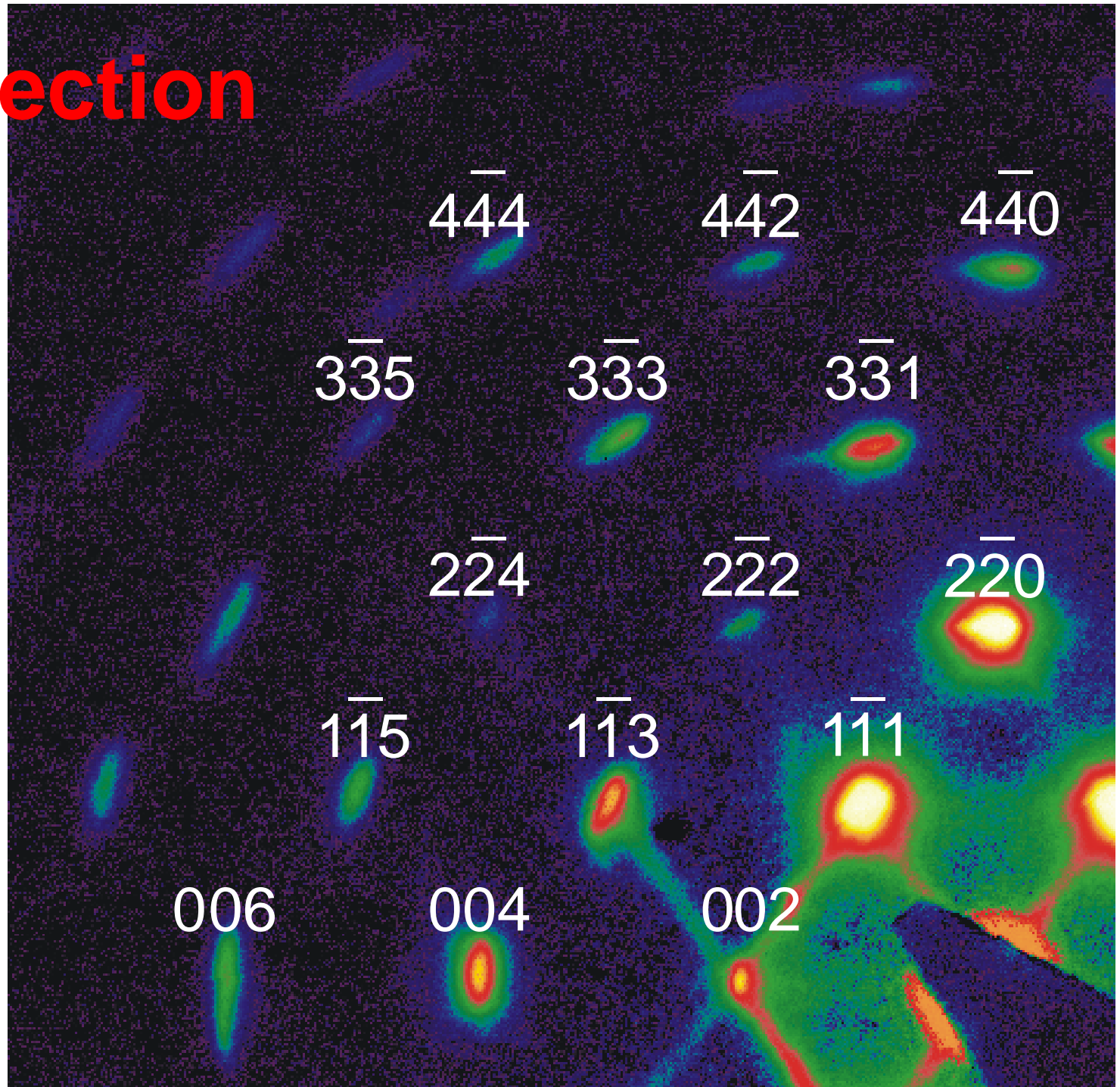
sample



Sample is turned  
by 35 degrees

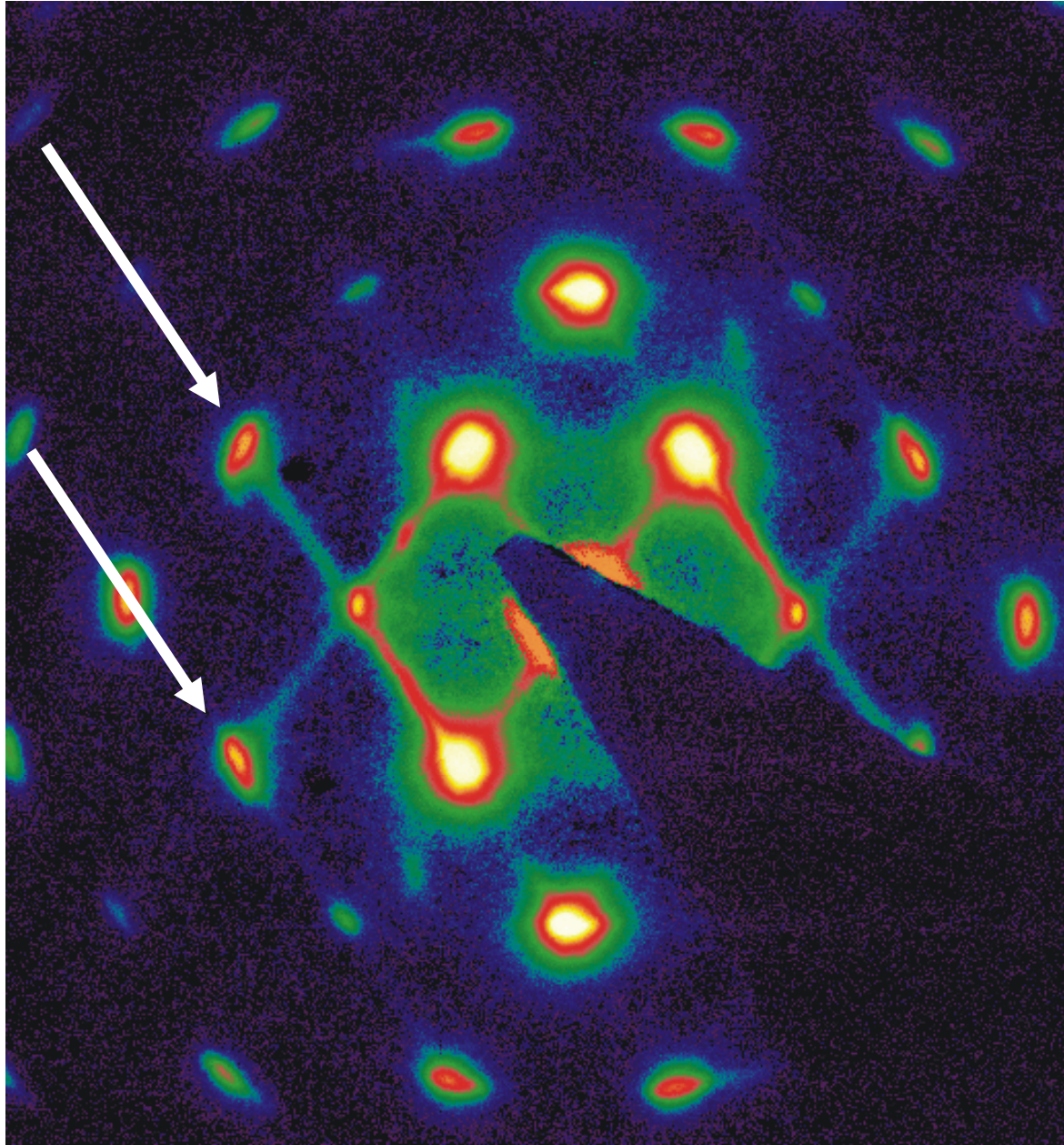


**110 direction**





# What are the lines?

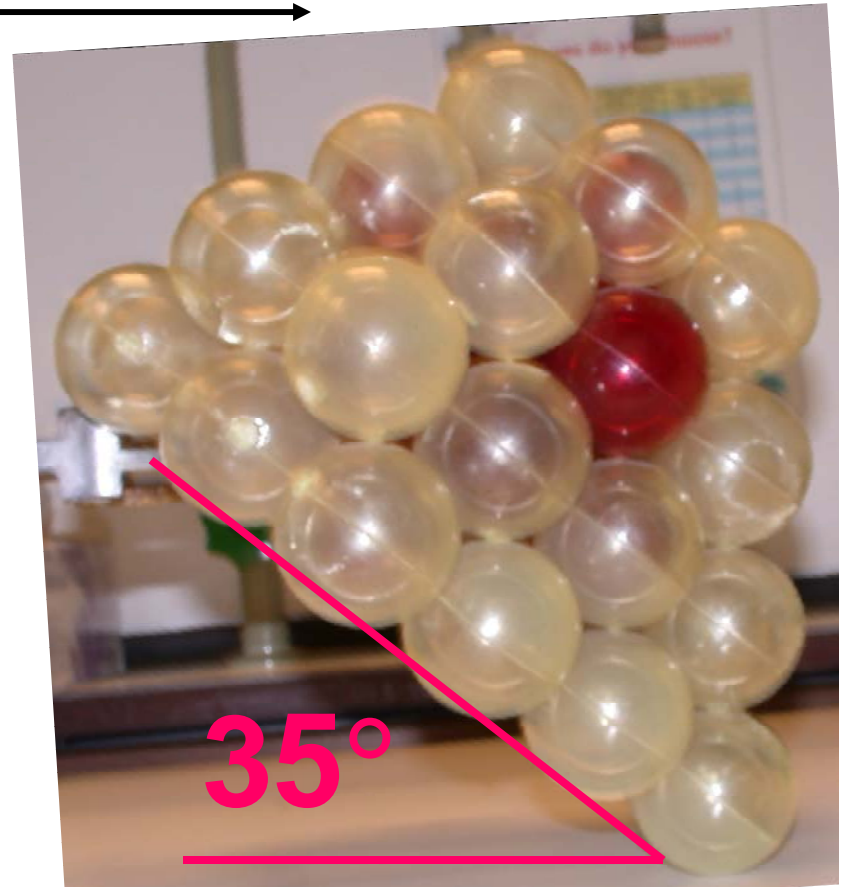
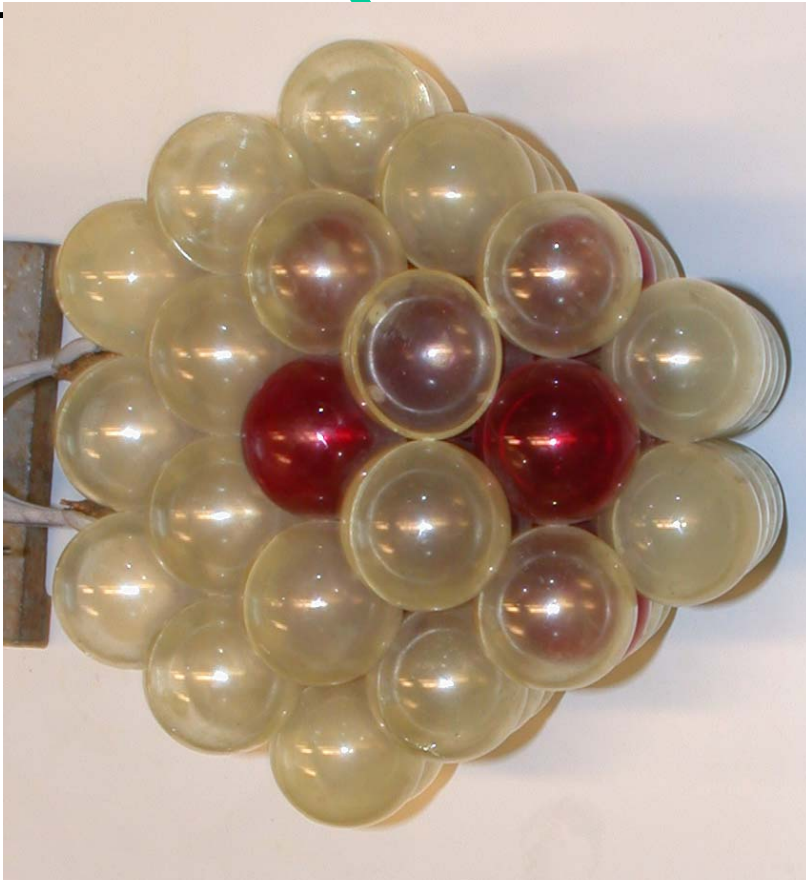


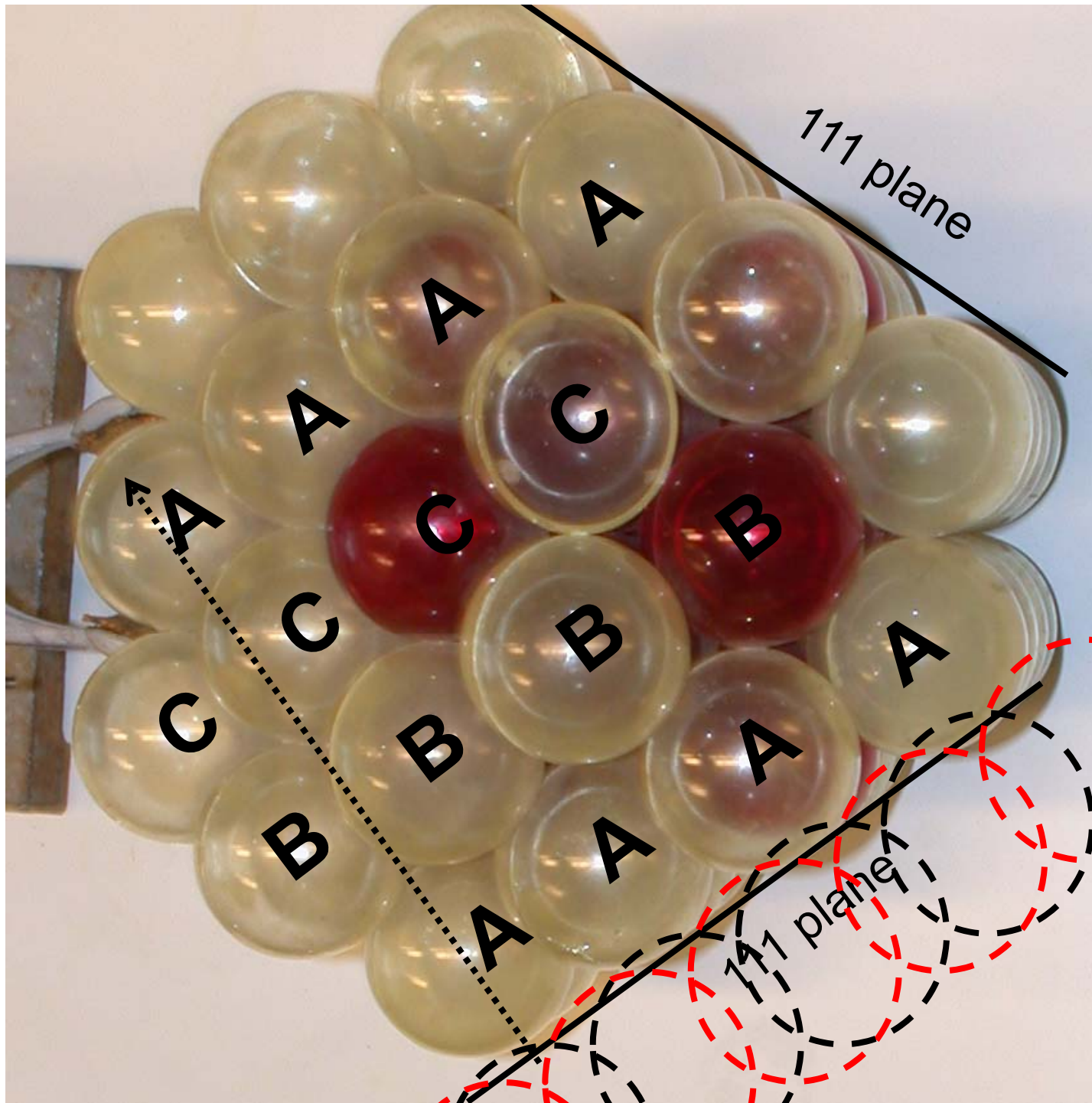


# Pattern #3

sample

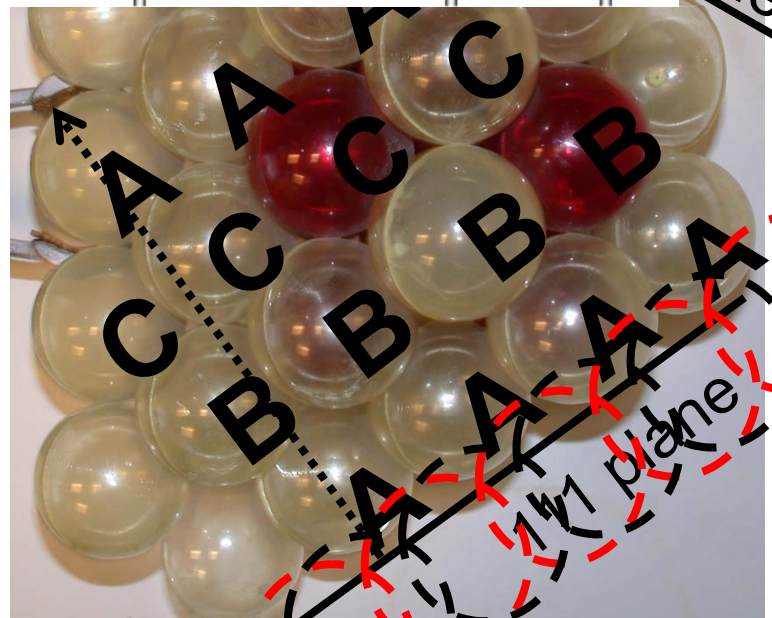
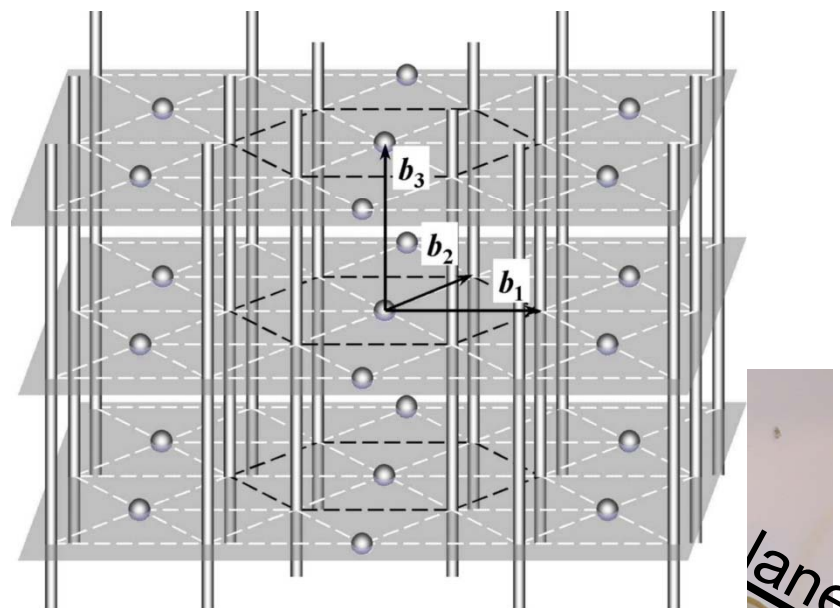
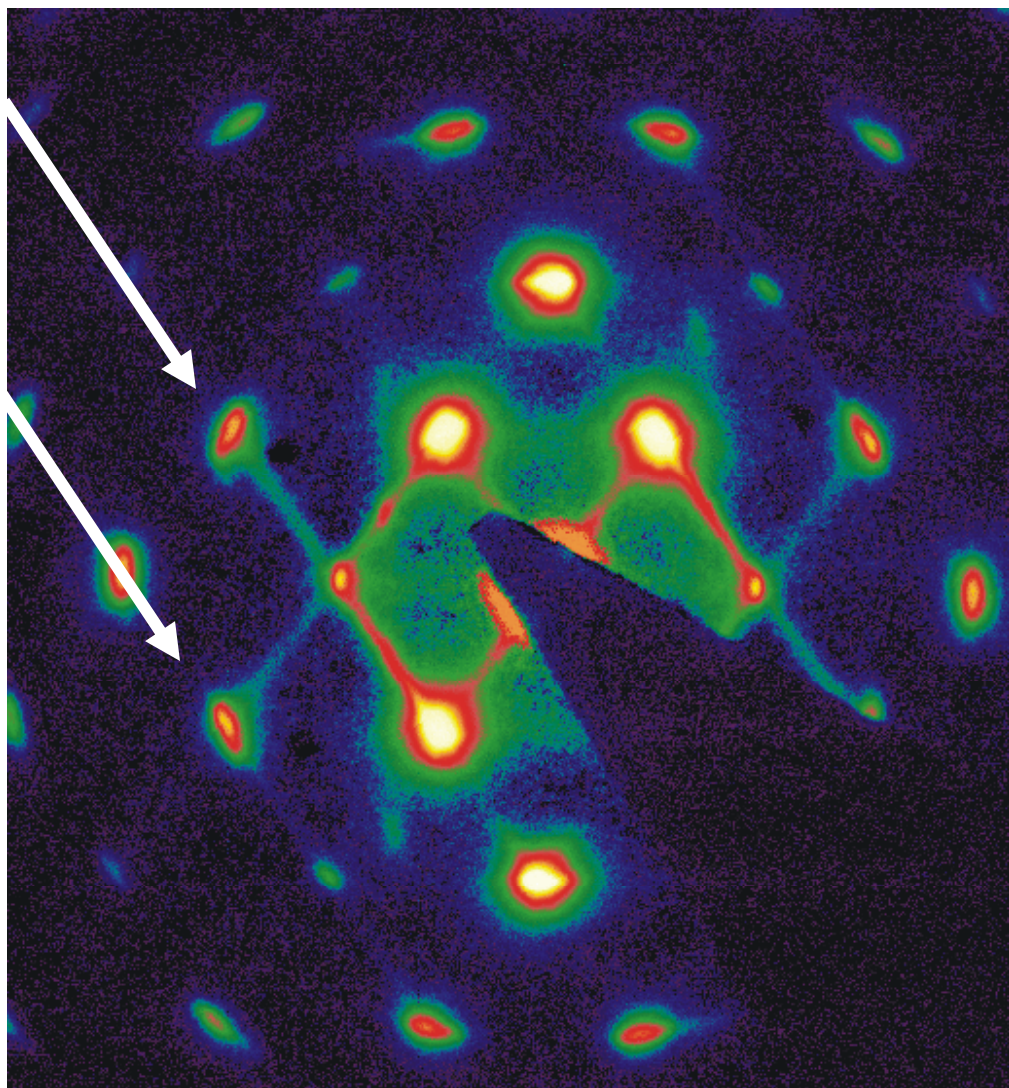
Sample is turned  
by 35 degrees



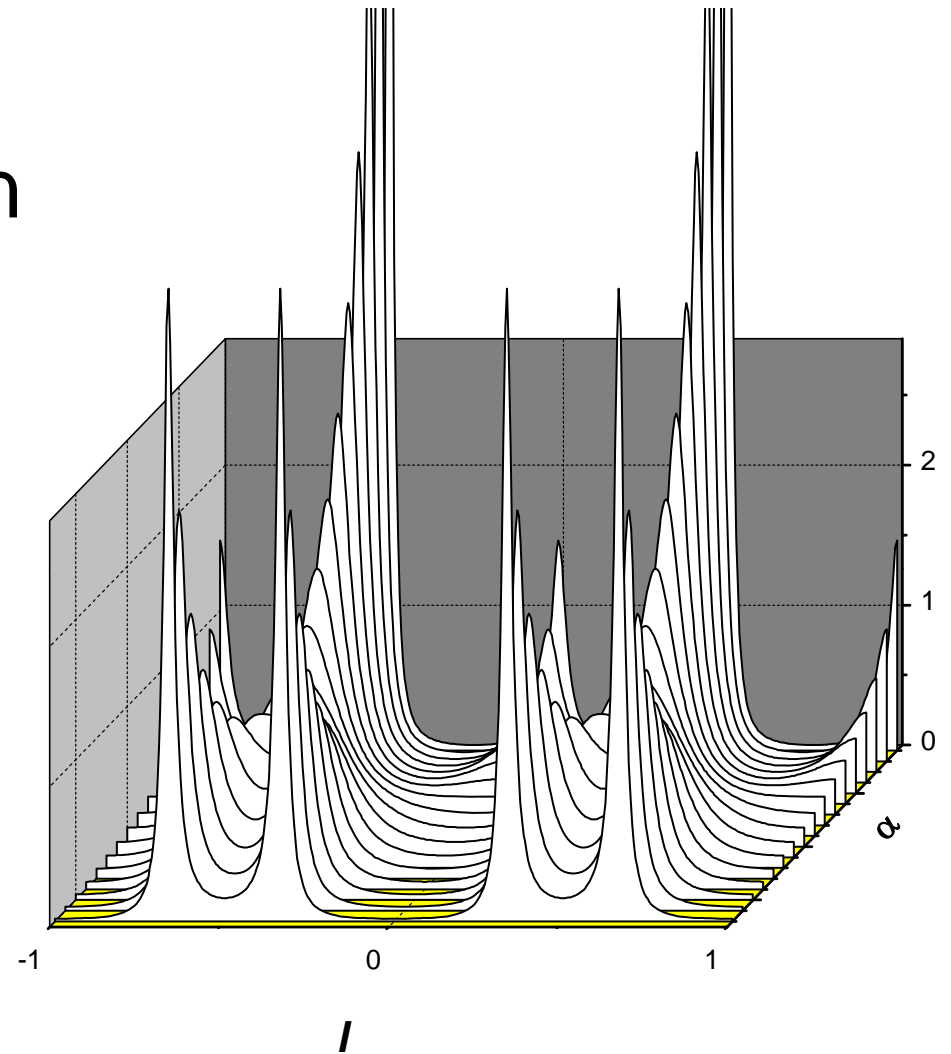
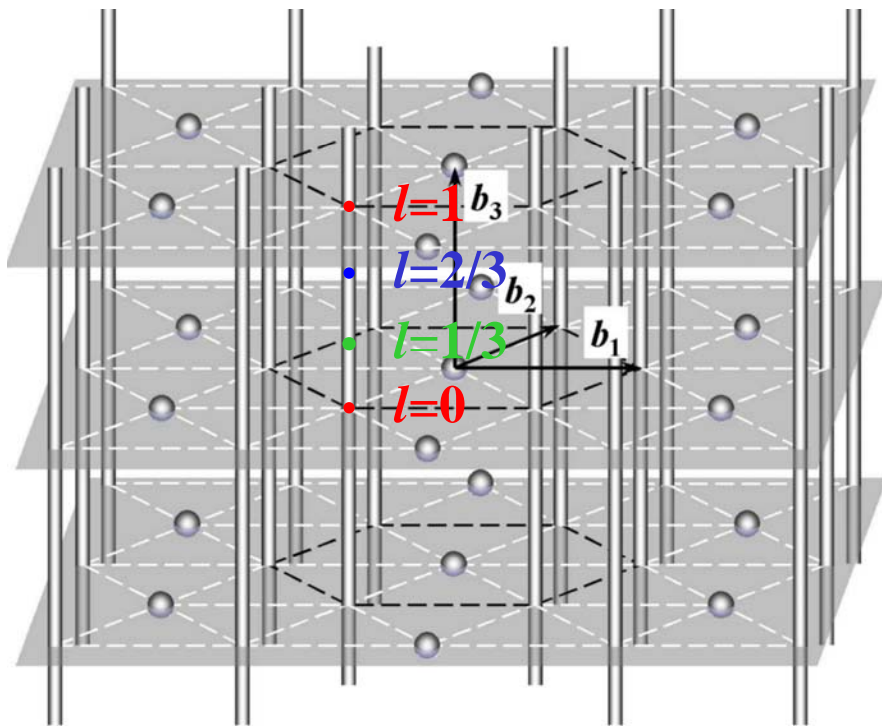




- Stacking disorder can be clearly seen in this projection!
- These are the Bragg rods!



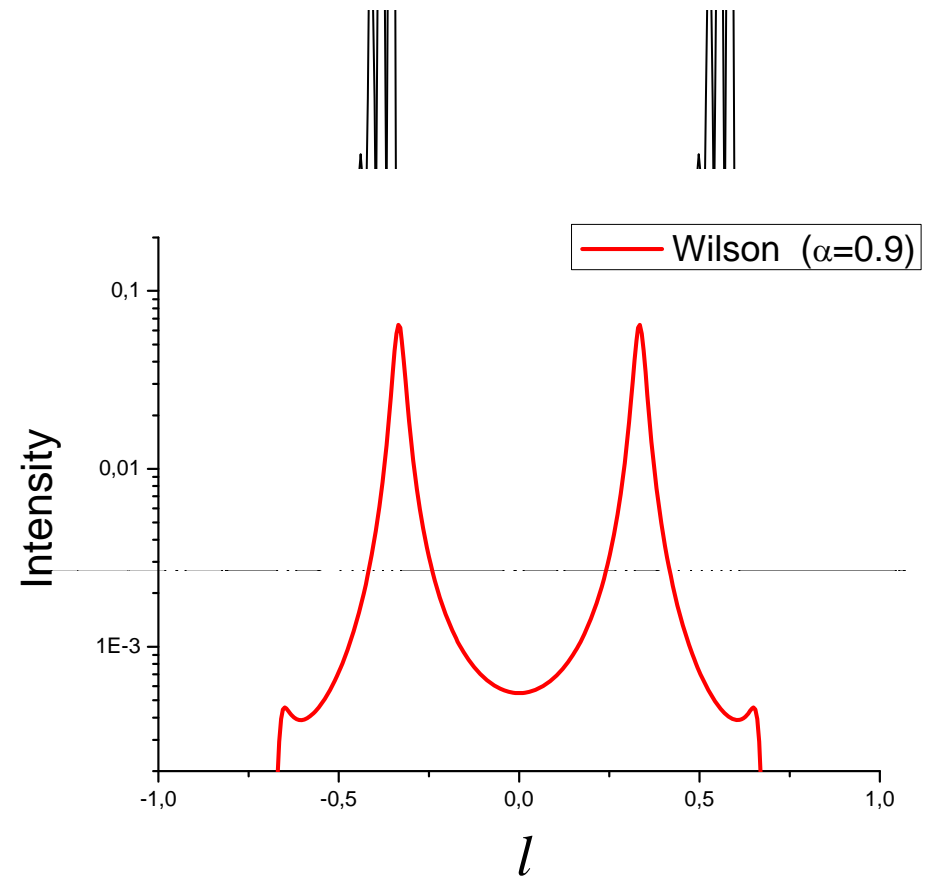
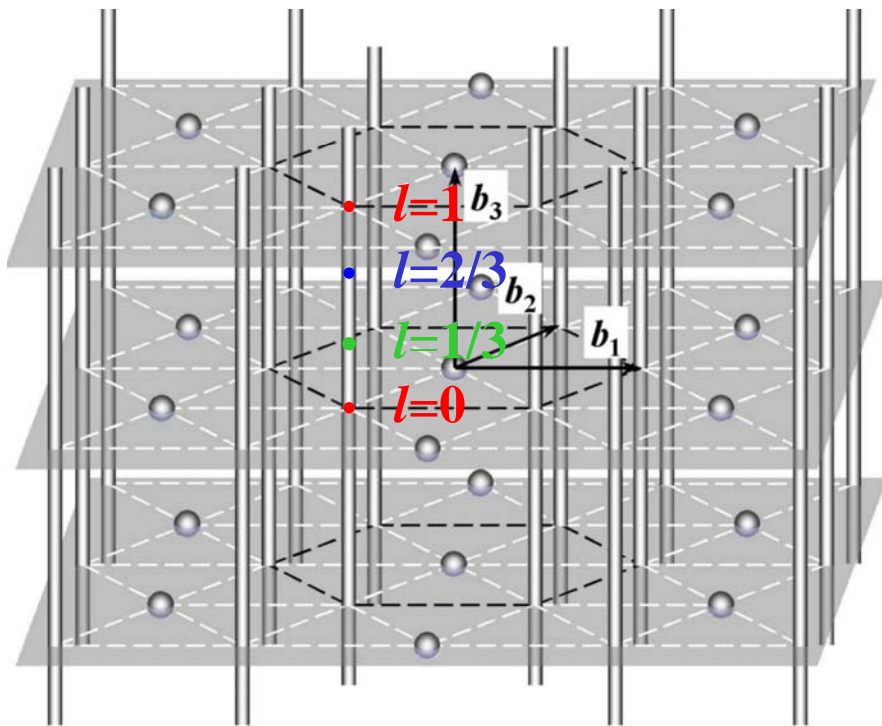
# Wilson's theory: Structure factor variation along Bragg rods



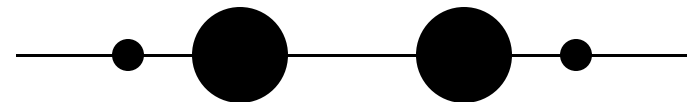
**Is this what we see?**



# Wilson's theory: Structure factor variatic along Bragg rods



<sup>-1</sup> Times the form factor:



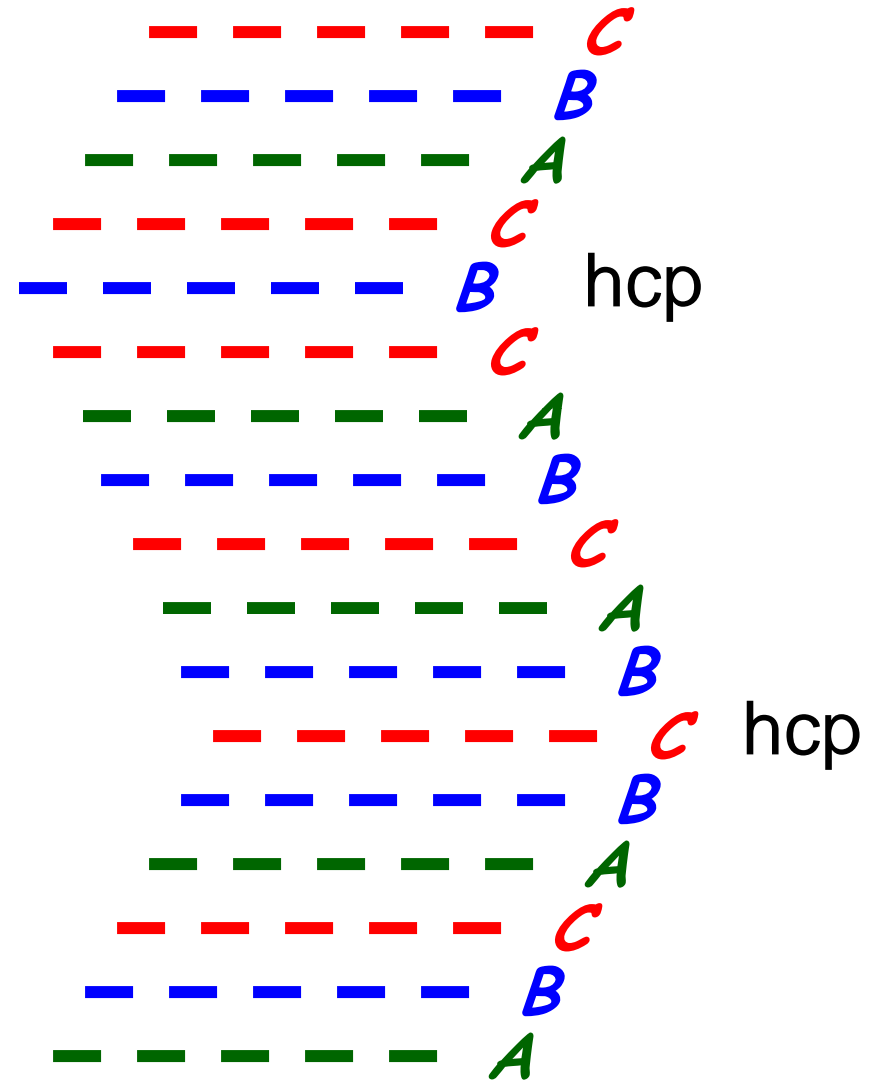
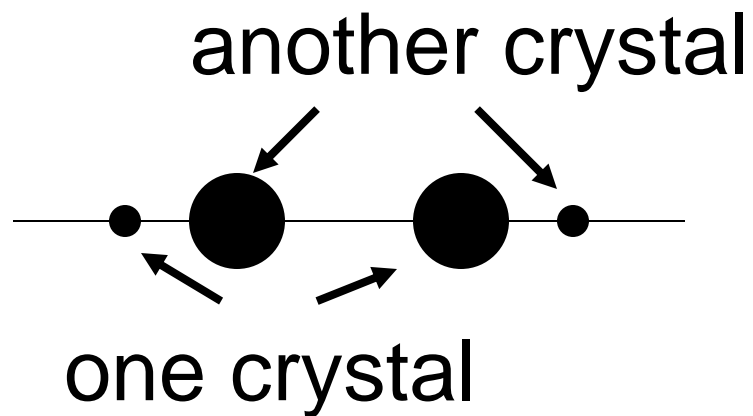
Is this what we see?

Wilson's theory does not work!  
Why?



# Wilson's theory:

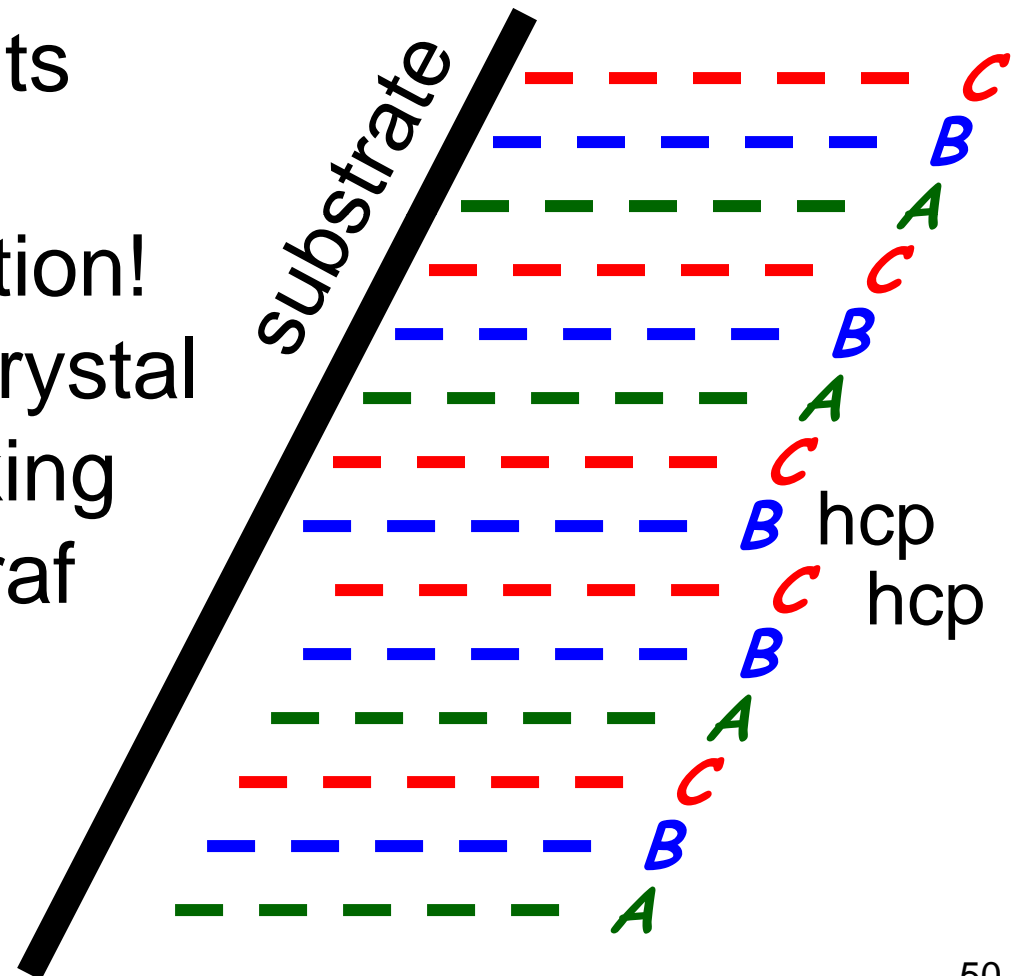
- Stacking fault changes stacking direction
- One gets not one but two (twin) crystals with ...ABCABC... and ...ACBACB... stacking

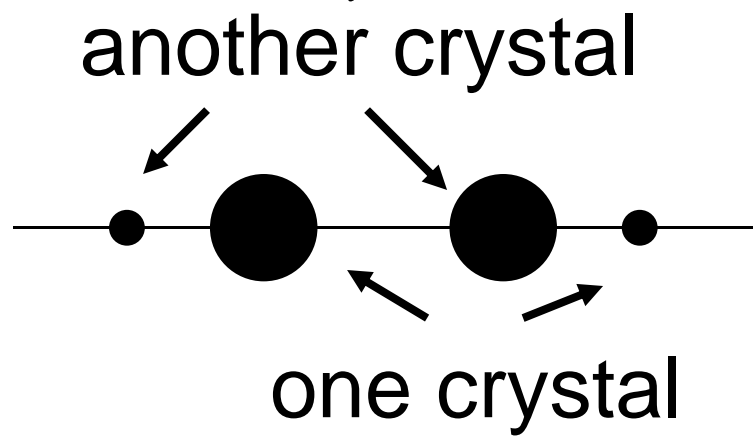
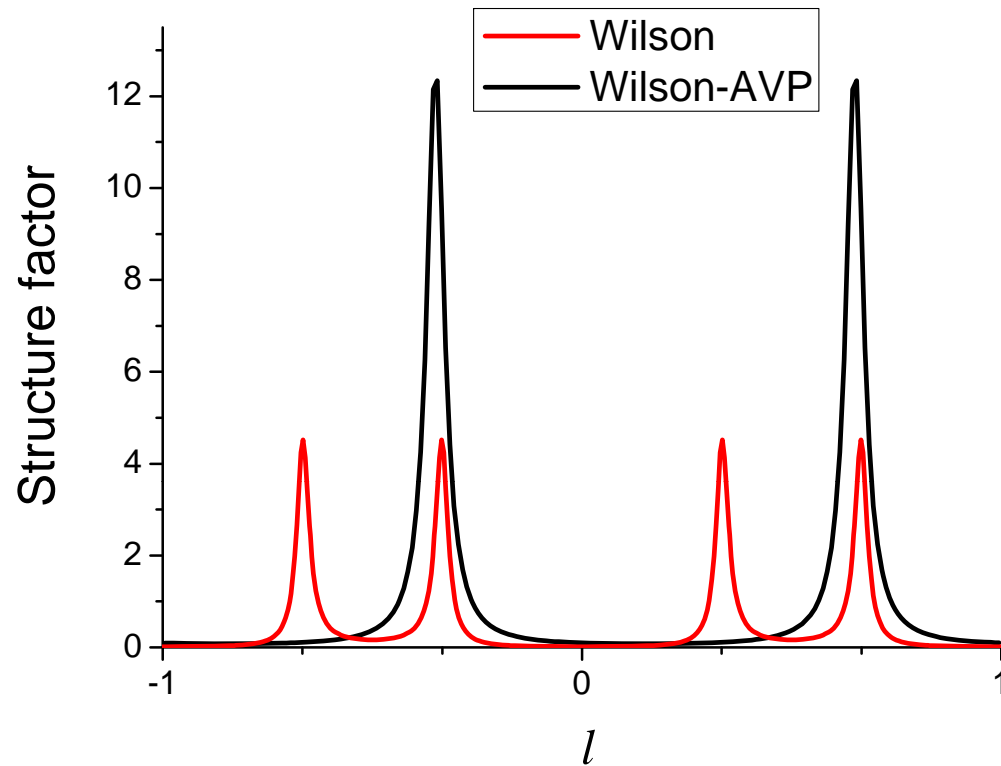


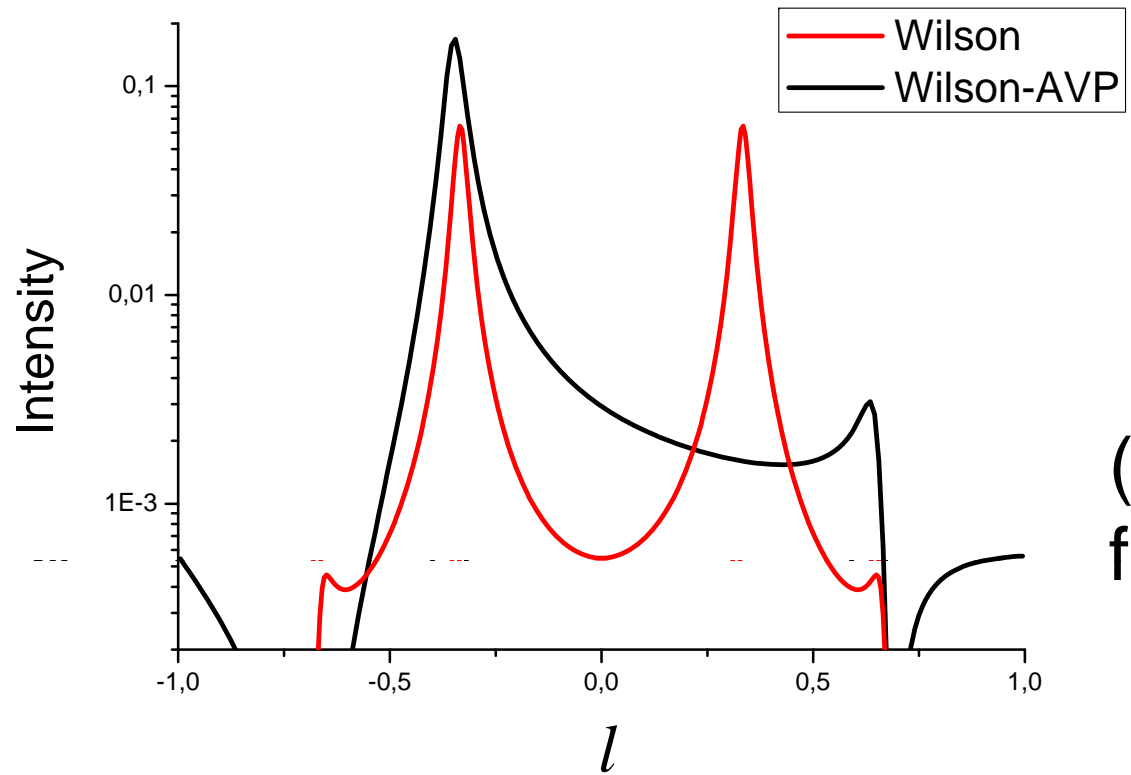


# How should we modify Wilson's theory?

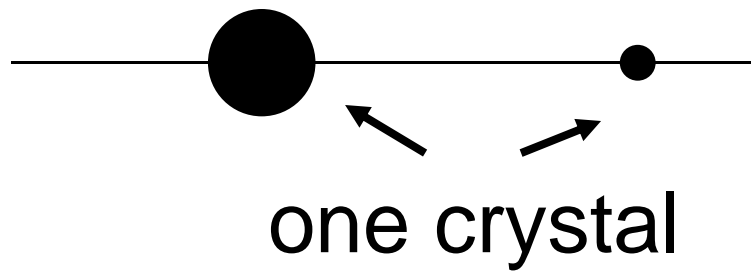
- Double stacking faults do not change the stacking direction!
- One gets only one crystal with a unique stacking
- Het is logisch achteraf te zien (Dirk Aarts)





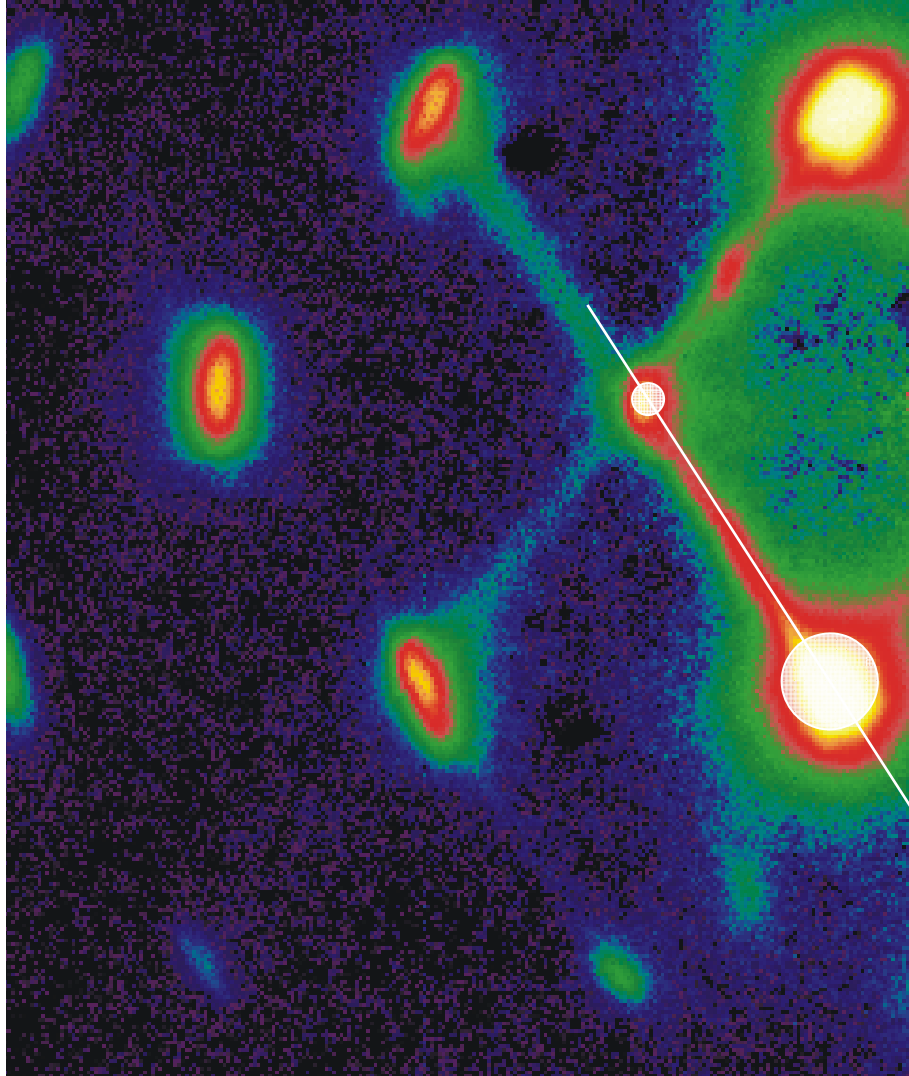
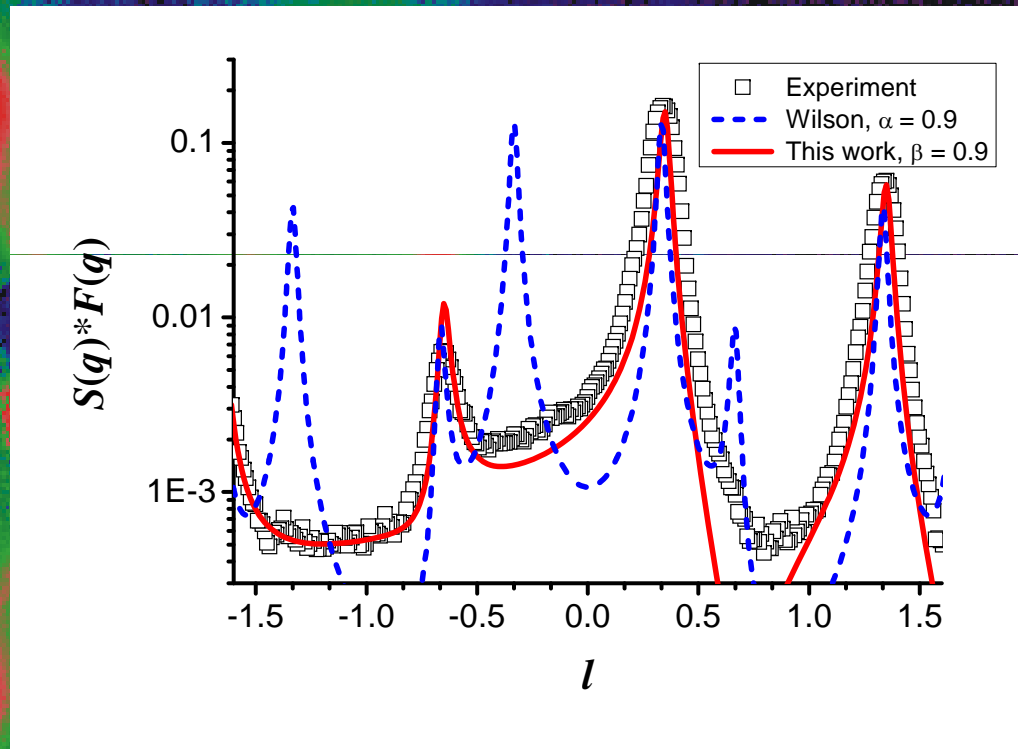


(times the  
form factor)

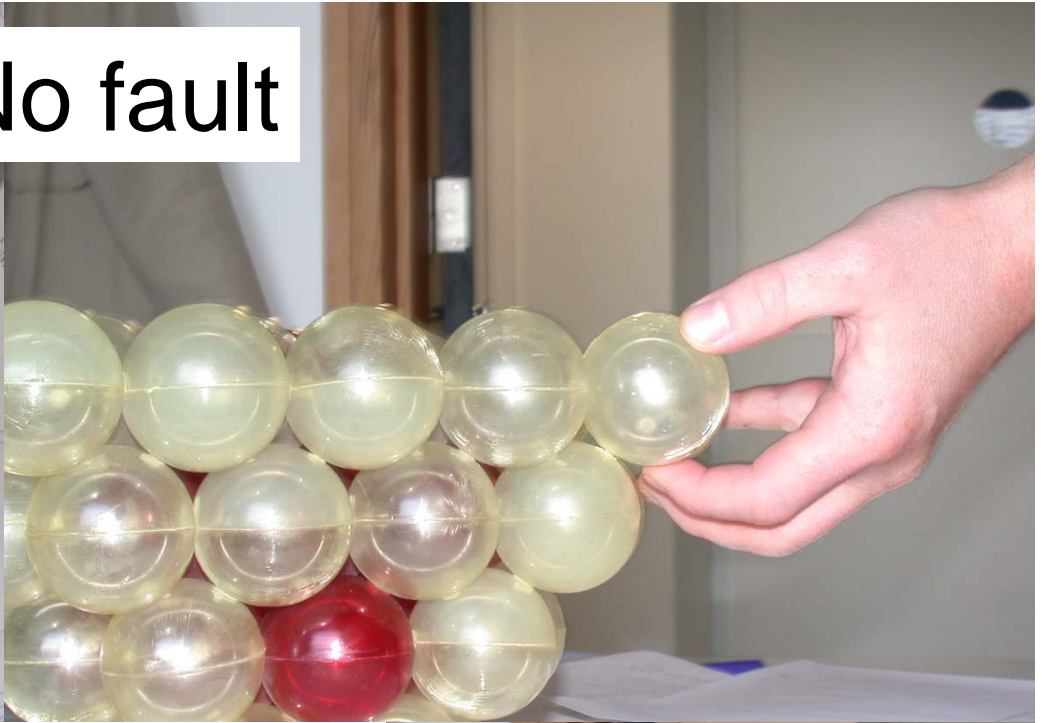




# Modified Wilson's theory does work!



No fault



With fault



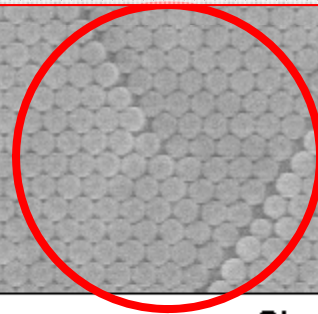


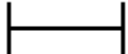
# 'Slanted' double stacking faults

higher

lower

**There is more in the picture: e.g., 'dissolving' stacking fault (partial dislocation + strain)**



Mag = 10.00 K X  2 $\mu$ m

EHT = 14.00 kV  
WD = 15 mm

Signal A = VPSE  
Photo No. = 1233

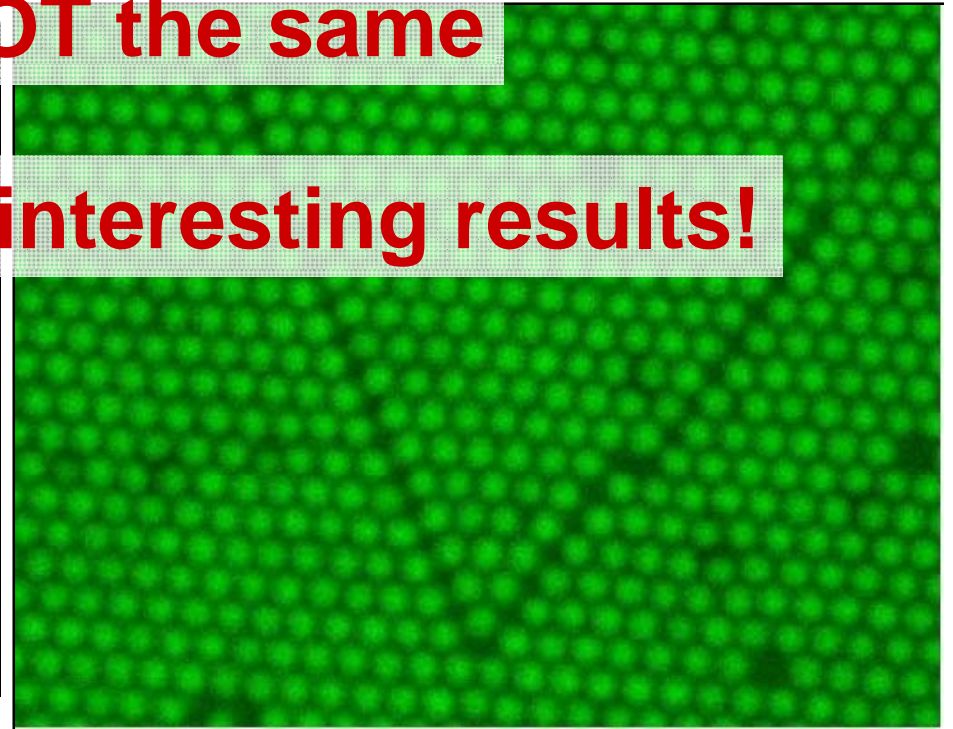
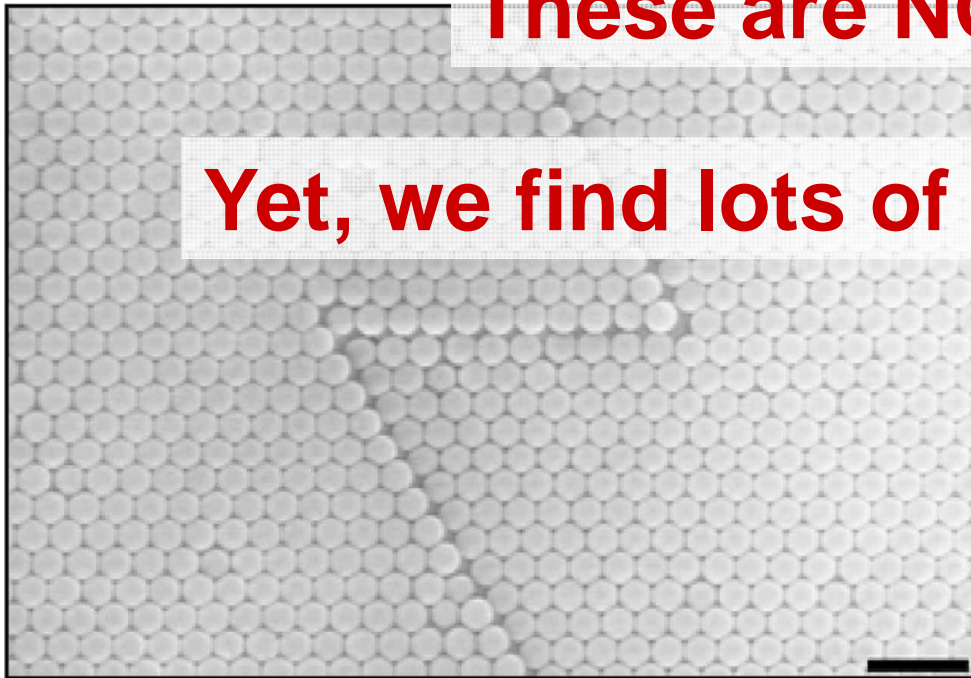
MSU HSMS  
Date :10 Oct 2005



# The wrong idea of the experiment

**These are NOT the same**

**Yet, we find lots of interesting results!**



**Alexander Sinitskii et al.**  
SEM of vertical  
deposition crystals  
*Mendelev Comm., 2007*

**Volkert de Villeneuve et al.**  
Confocal microscopy of  
sedimentary crystals,  
*Langmuir & EPL, 2007*

# Conclusions

- X-ray diffraction from 'nano-elephants' is doable
  - period:  $> 1$  micron
  - long-range order:  $> 10$  micron
- New type of defects in colloidal crystals are found and characterized

# Schedule

- Introduction to nanoelephants
- Instrumentation
- Example 1: Hard spheres
- Example 2: Rusted nanonails
- Conclusion

# Самоорганизация ржавых напогвоздиков

(жидко-кристаллические фазы  
коллоидных частиц гётита)

Andrei Petukhov

Van 't Hoff laboratory for physical and colloid chemistry  
Utrecht University, The Netherlands



Universiteit Utrecht



Universiteit Utrecht





# Colloidal Goethite

Горные вершины  
Спят во тьме ночной;  
Тихие долины  
Полны свежей мглой;  
Не пылит дорога,  
Не дрожат листы...  
Подожди немного,  
Отдохнешь и ты.

**Лермонтов**

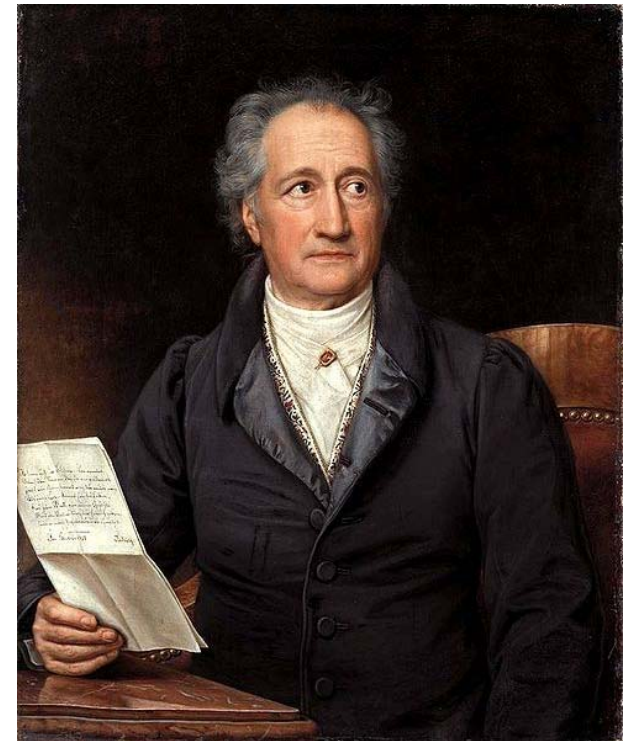


Über allen Gipfeln  
ist Ruh',  
in allen Wipfeln  
spurest du  
kaum einen Hauch.  
Die Vögelein schweigen im Walde.  
Warte nur, bald  
ruhest du auch.

**Johann Wolfgang von Goethe**

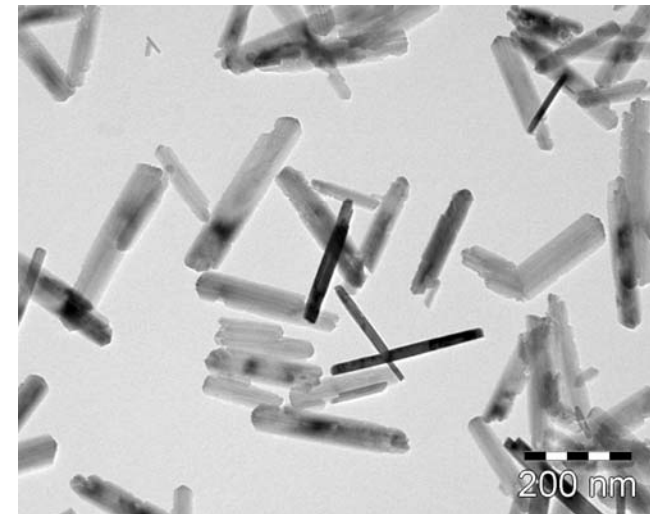
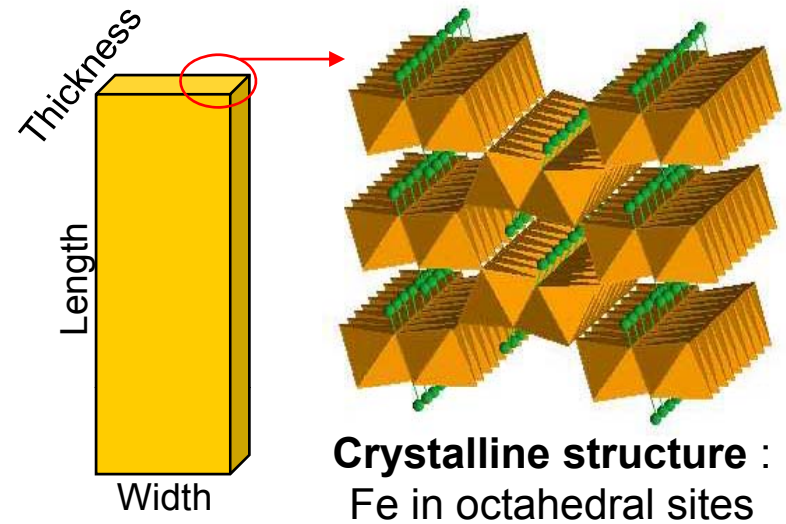
Мирно высятся горы.  
В полусон  
Каждый листик средь бора  
На краю косогора  
Погружен.  
Птичек замерли хоры.  
Погоди: будет скоро  
И тебе угомон.

**Пастернак**

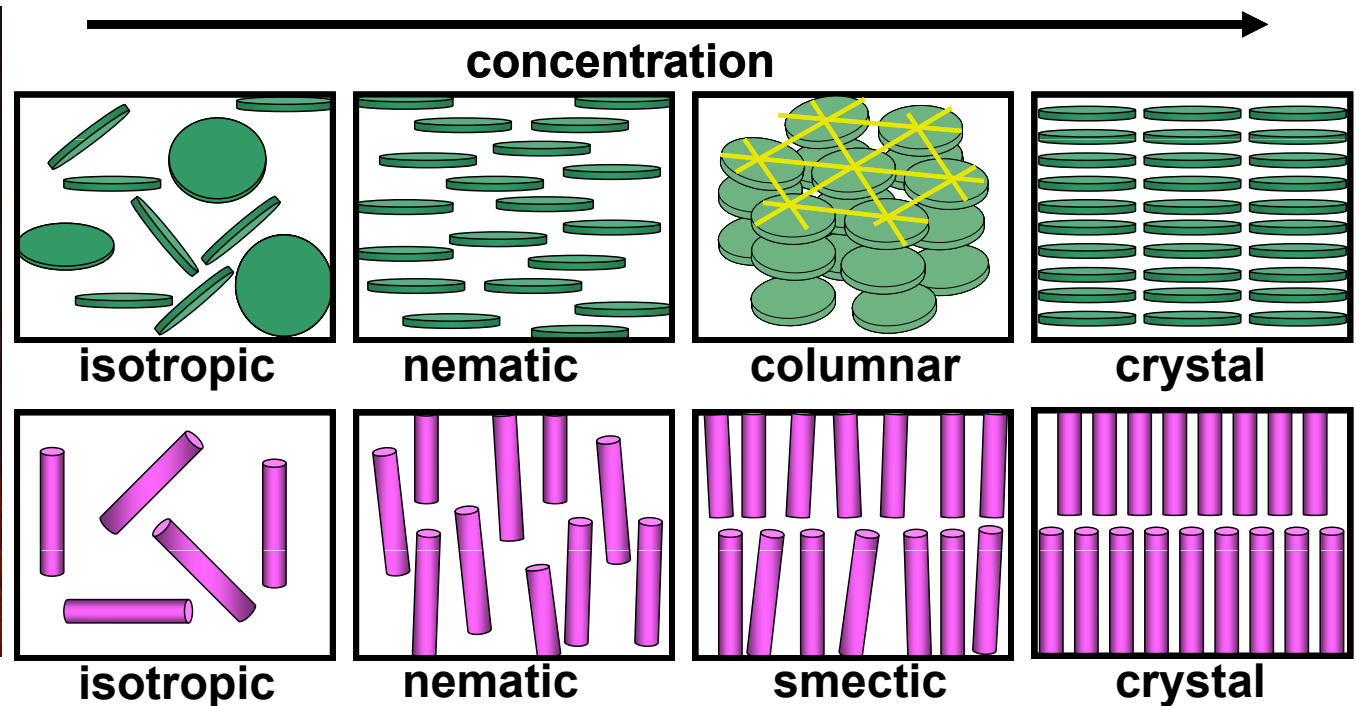
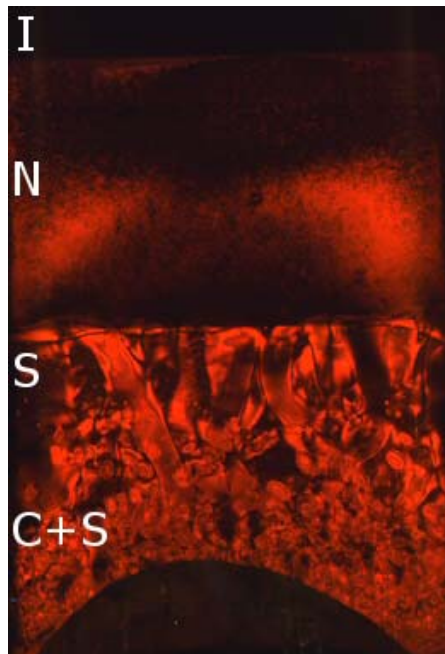
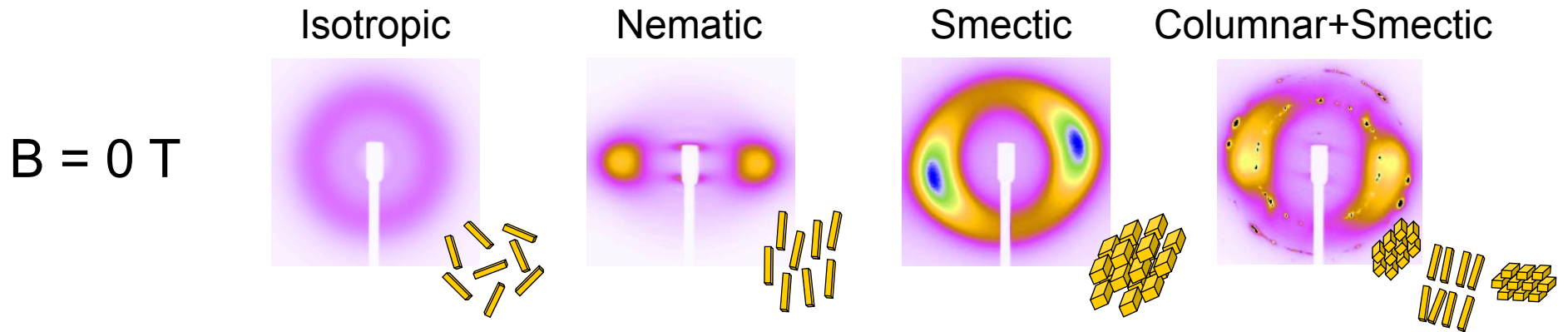


# Goethite

- $\alpha$ -FeOOH
- Preferred direction of crystal growth  $\rightarrow$  boardlike particles
- Majorana 1902 / Cotton, Mouton 1907
- B.J. Lemaire / P. Davidson 2002-2005

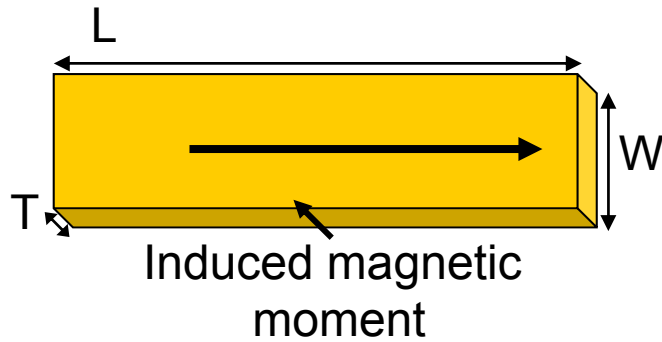


# Self-organisation of colloidal goethite



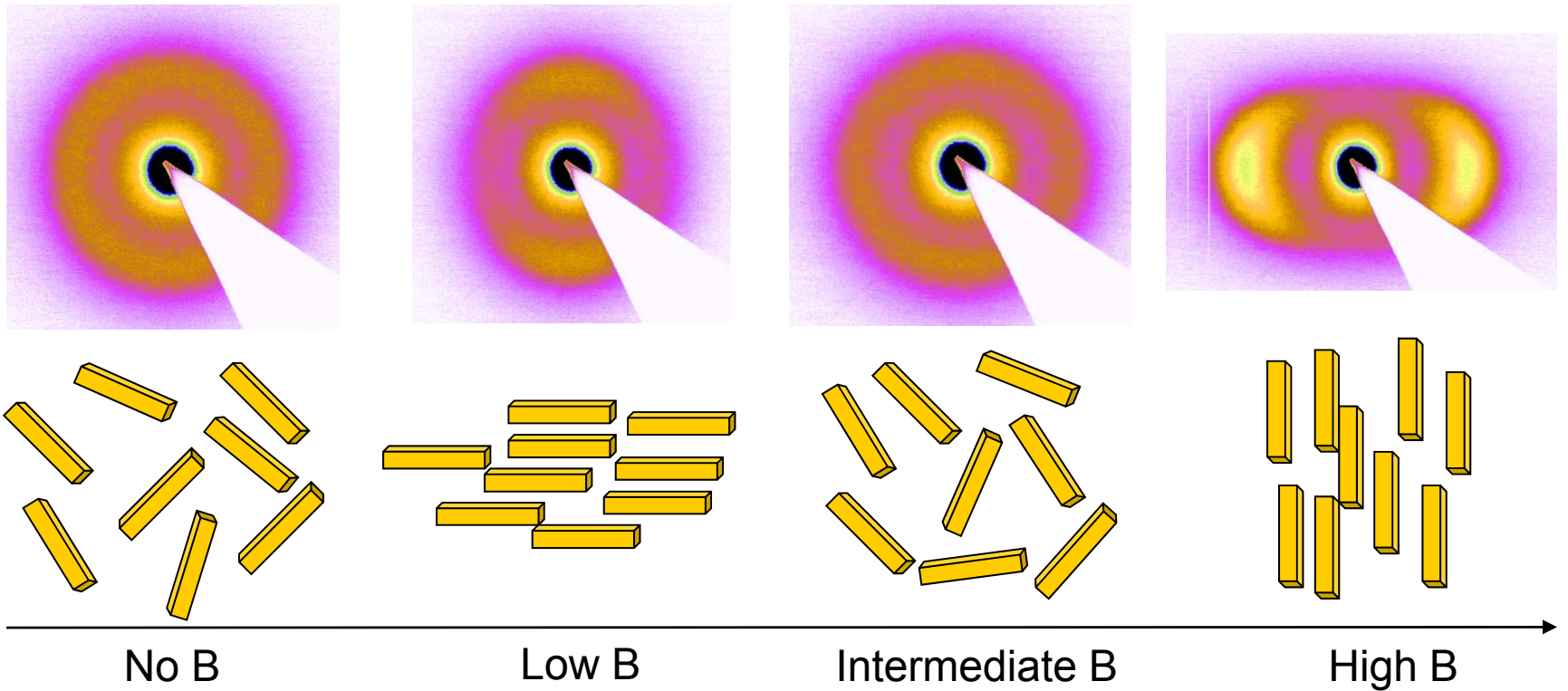


# Magnetic properties

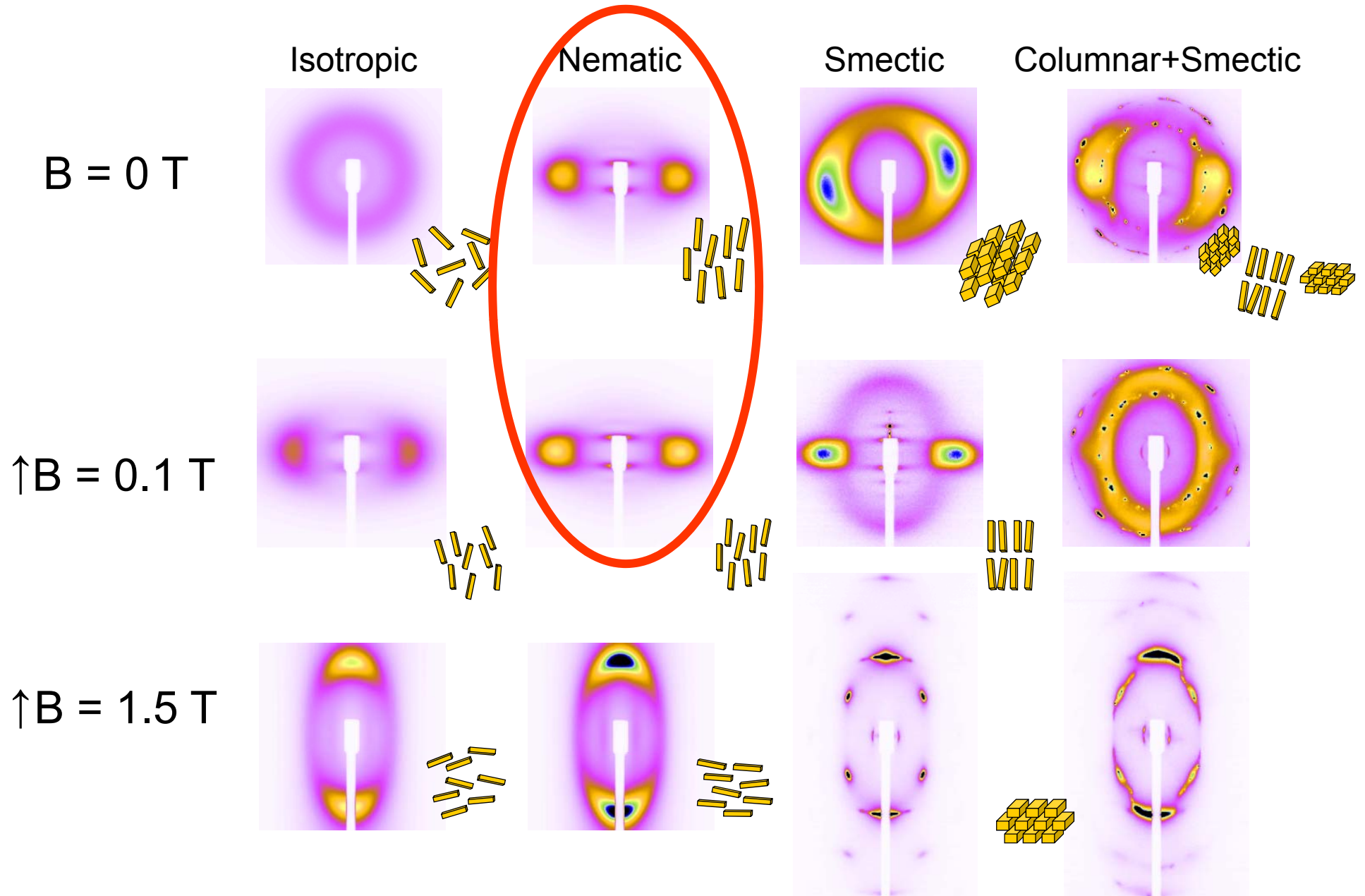


Permanent magnetic moment

SAXS



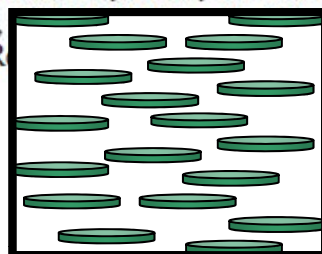
# Influence of an external magnetic field



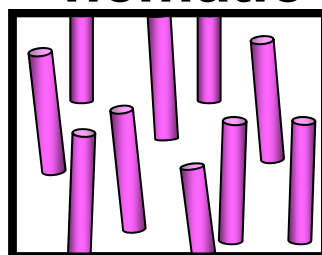
# Experimental Realization of Biaxial Liquid Crystal Phases in Colloidal Dispersions of Boardlike Particles

E. van den Pol, A. V. Petukhov, D. M. E. Thies-Weesie, D. V. Byelov, and G. J. Vroege\*

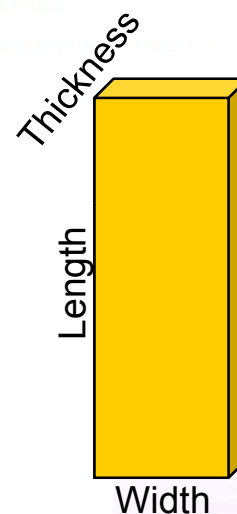
*Van 't Hoff Laboratory for Physical and Colloid Chemistry, Debye Institute for Nanomaterials Science, Utrecht University, Padualaan 8, (R) Netherlands*



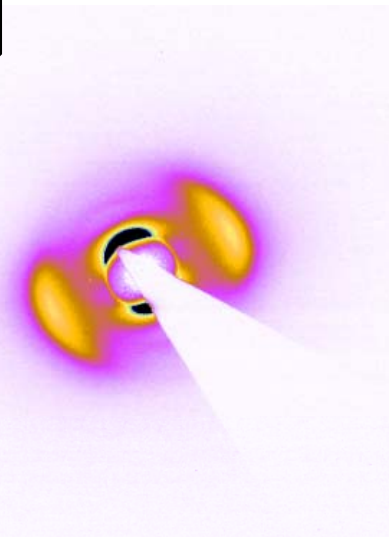
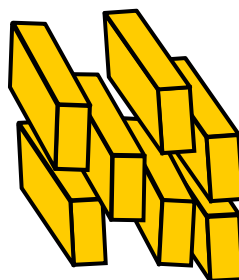
nematic



nematic



$$L/W \approx W/T$$



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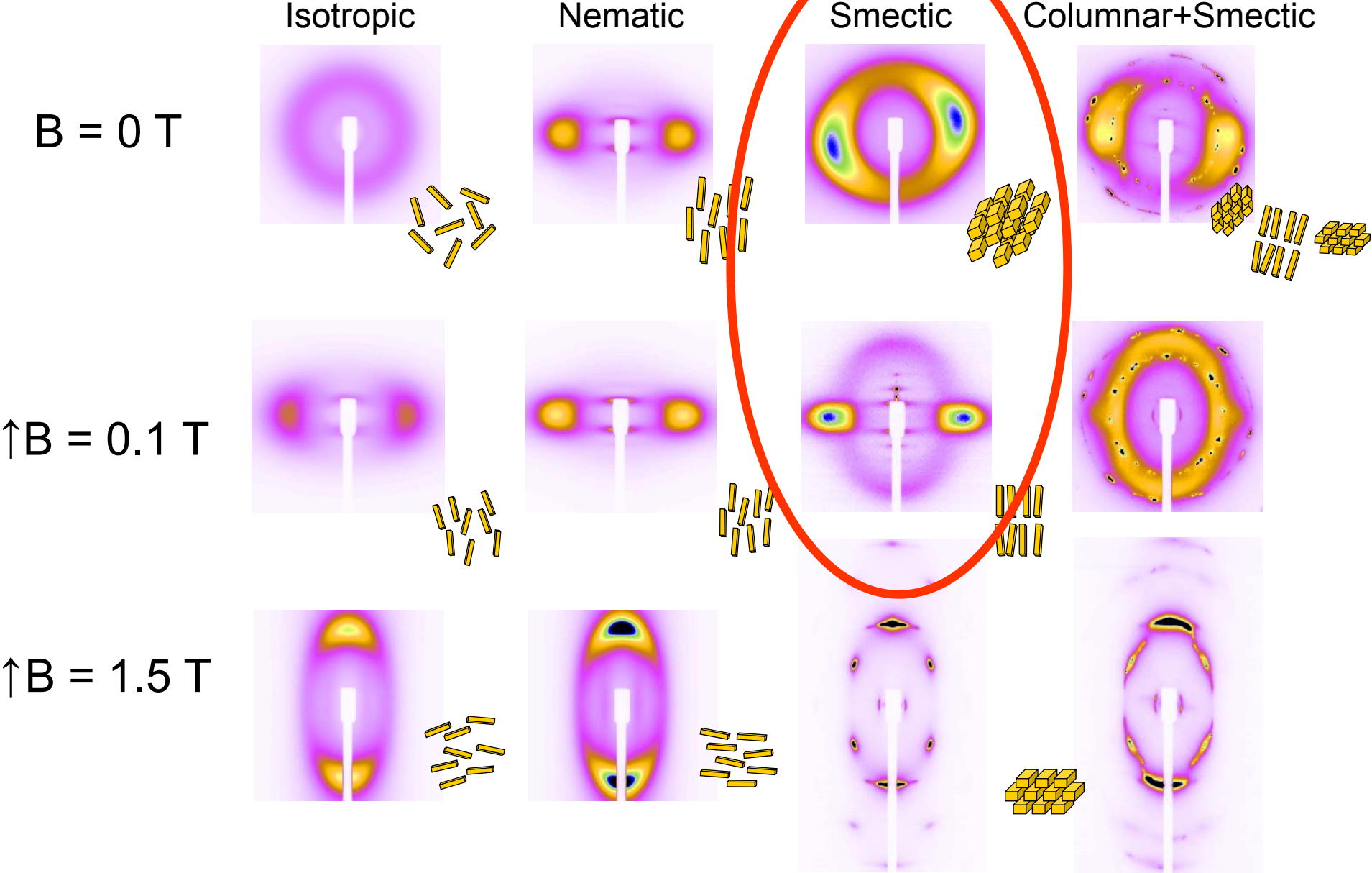
Published by the American Physical Society

APS physics

Volume 103, Number 25



# Influence of an external magnetic field

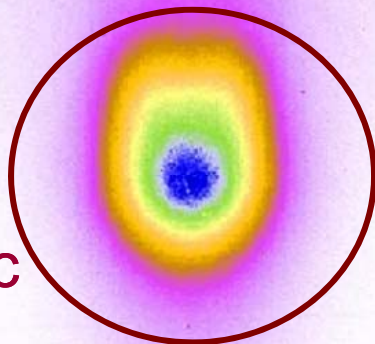


# Smectic goethite: $\mu$ rad XRD

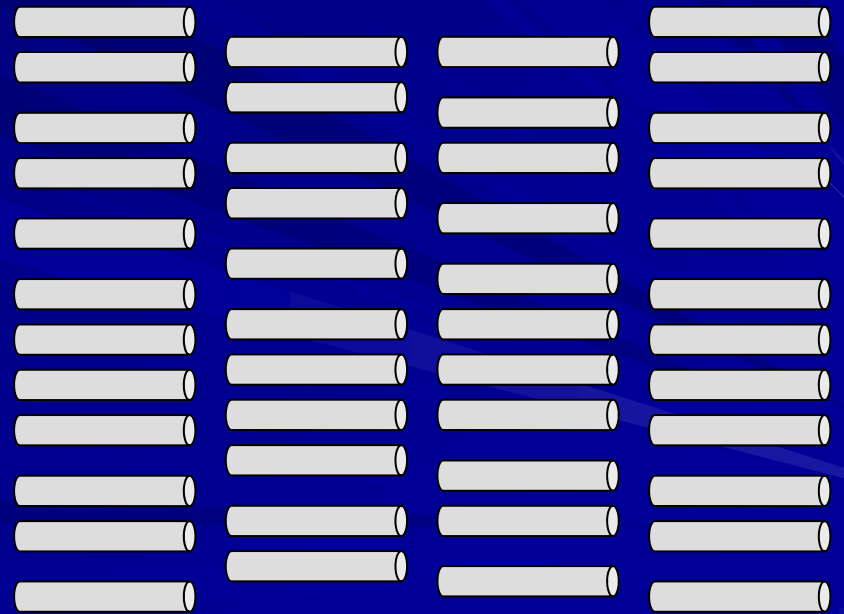
Interlayer periodic structure



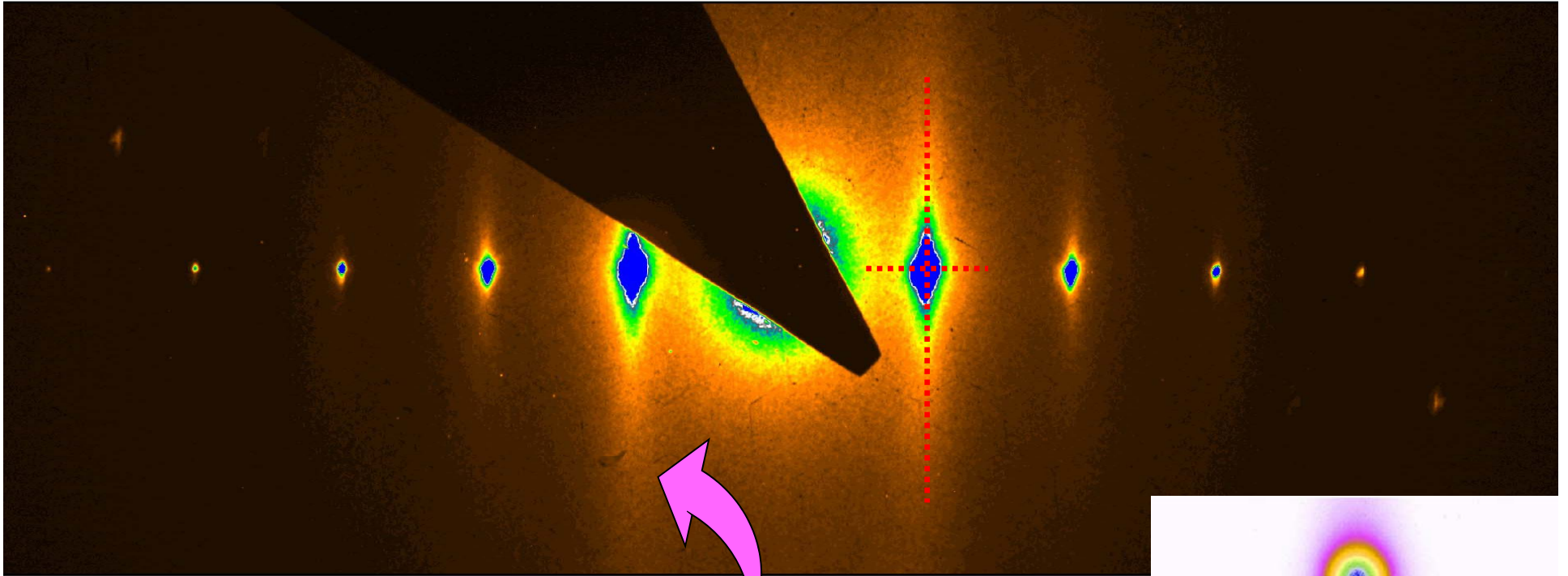
Intralayer  
non-periodic  
structure



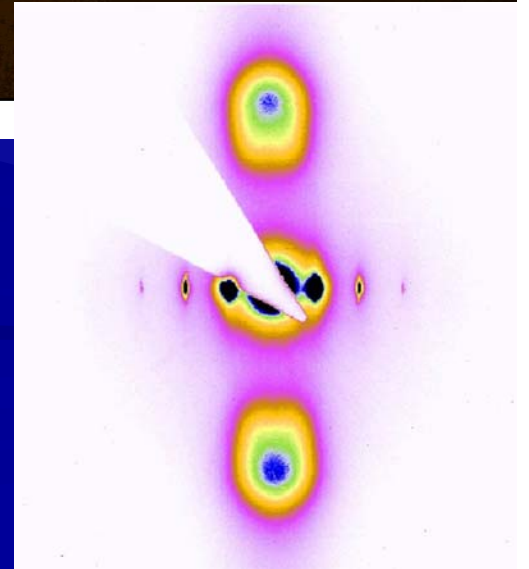
Sample aligned  
in magnetic field



# Closer look:

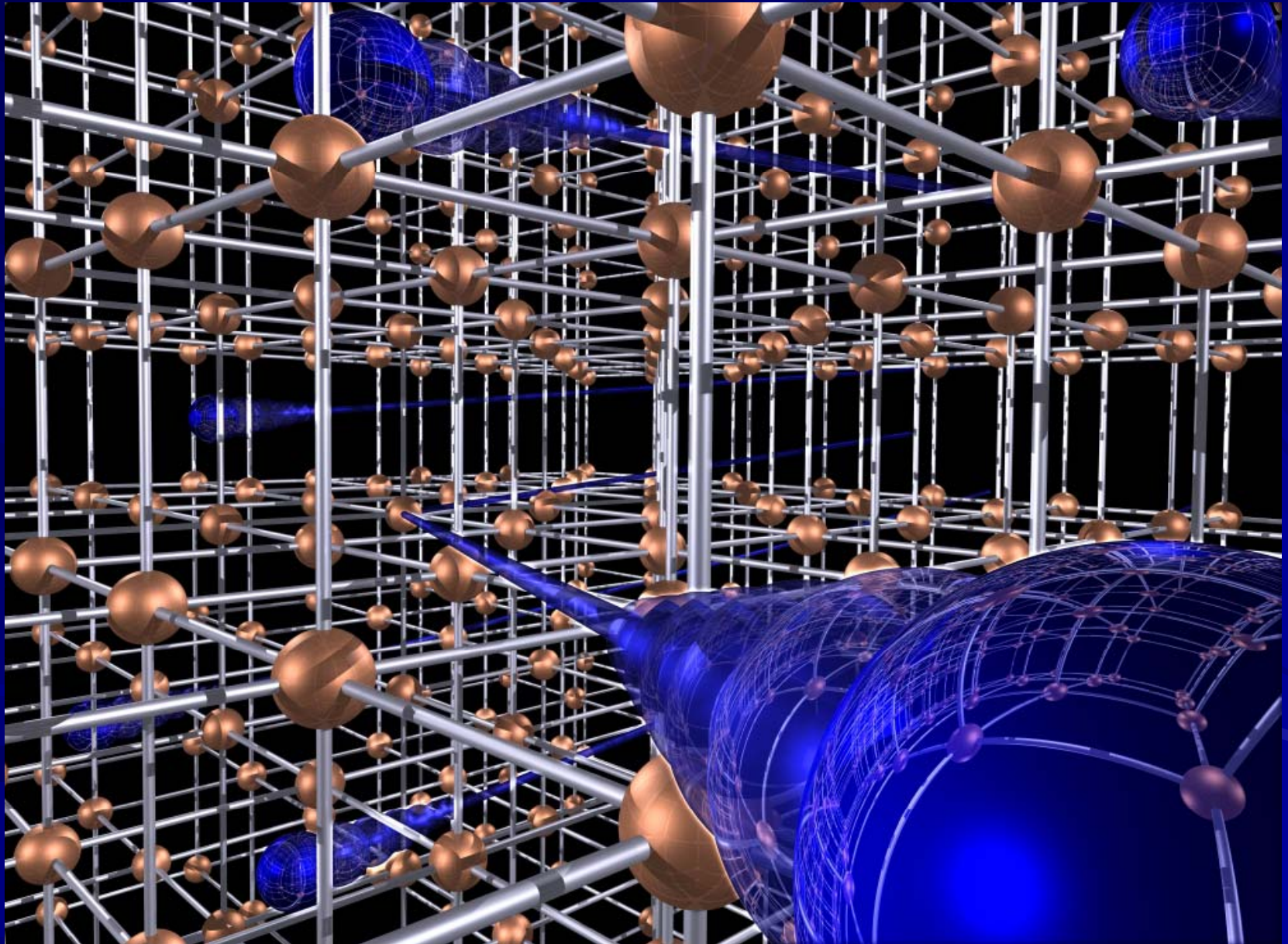


Diffuse scattering 'streaks'





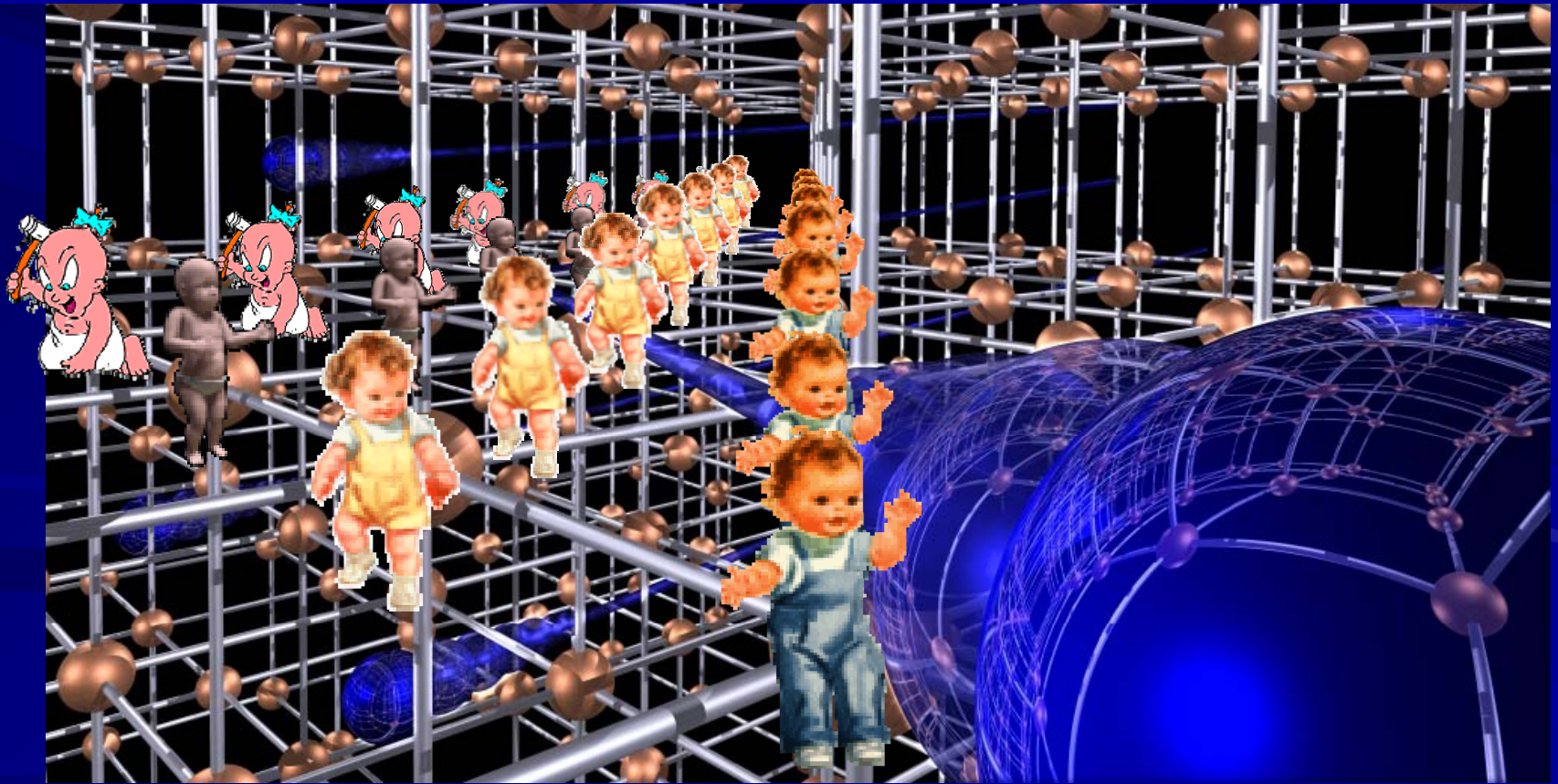
# Long-range order





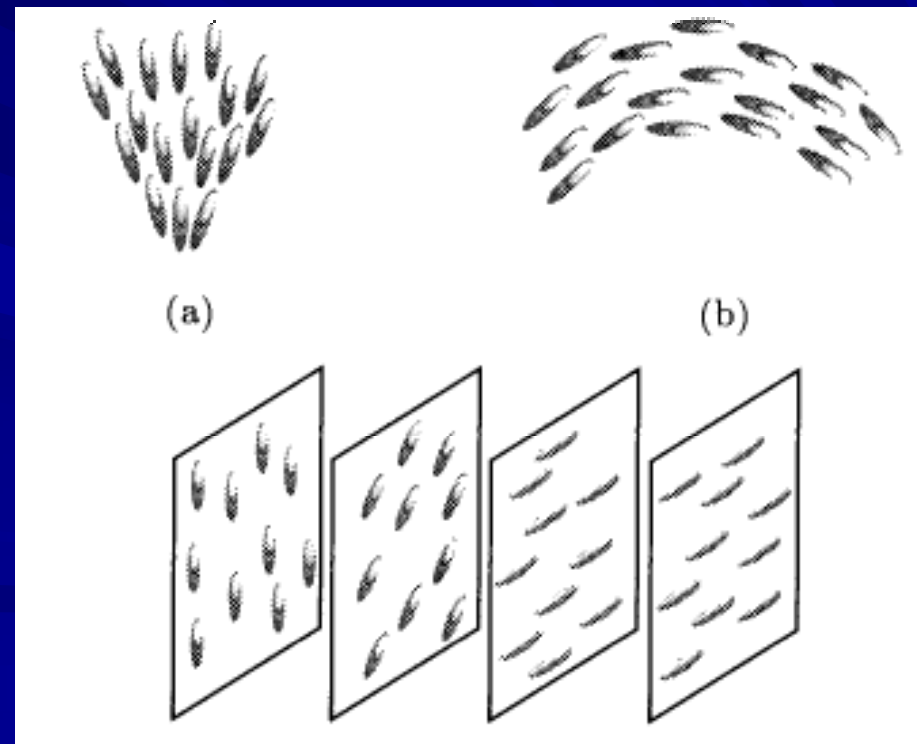
# 3D: Robust Order

few ( $\sim q^2 dq$ ) long-wavelength modes in 3D  
more ( $\sim q^{D-1} dq$ ) in low-dimensional systems  
(Landau-Peierls instability)



# Nematic elasticity

$$F_n = \frac{1}{2} \int d^d x \{ K_1 (\nabla \cdot \mathbf{n})^2 + K_2 [\mathbf{n} \cdot (\nabla \times \mathbf{n})]^2 + K_3 [\mathbf{n} \times (\nabla \times \mathbf{n})]^2 \}$$



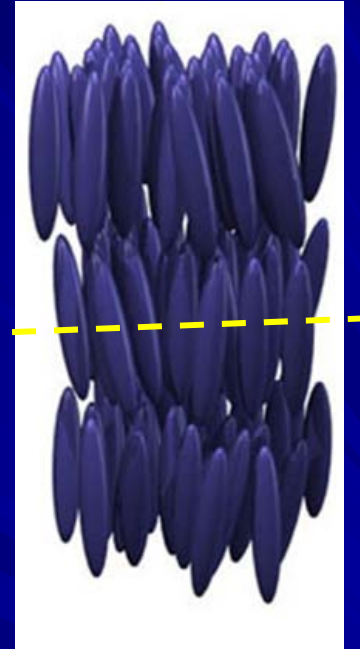
Splay, twist & bend



# Coupling between smectic coordinates and nematic elasticity

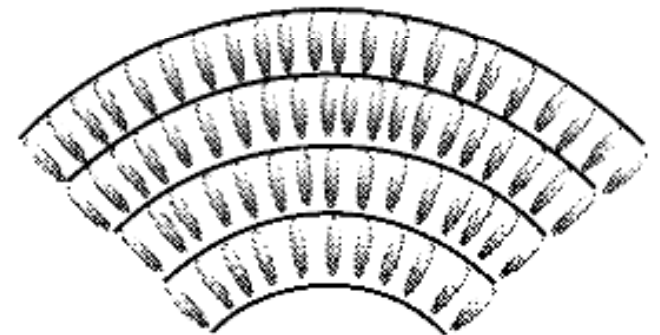
$$\delta n = -\nabla_{\perp} u$$

$u$ : in-layer coordinate



First derivative: rotation

Second derivative: splay



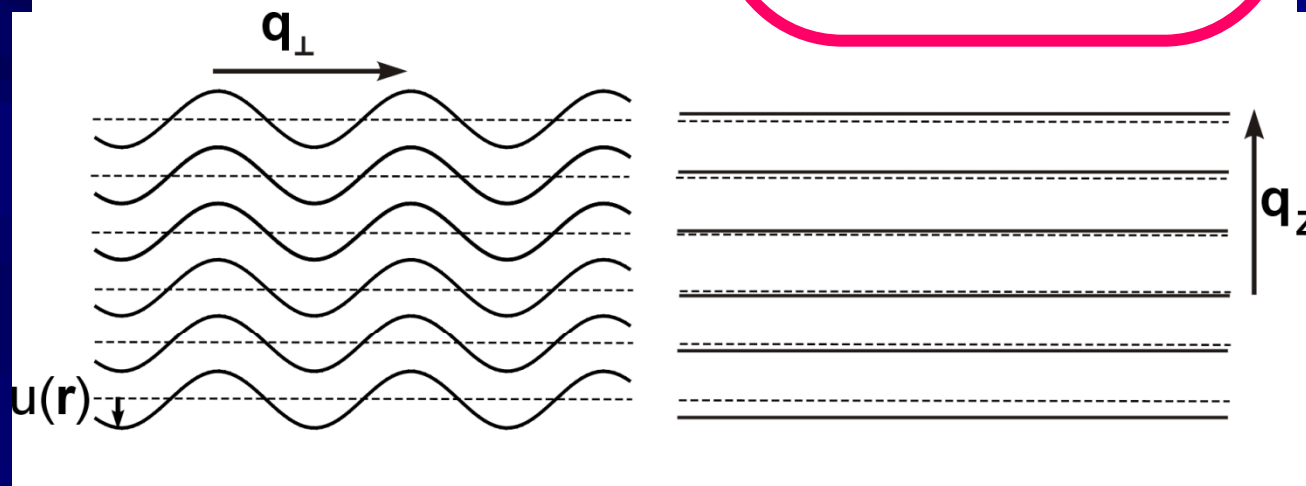
(b)

# Smectic liquid crystals: Landau-De Gennes free energy

$$F_B = \frac{1}{2} \int d^3r \left\{ B \left( \frac{\partial u(\mathbf{r})}{\partial z} \right)^2 - K \left[ \frac{\partial^2 u(\mathbf{r})}{\partial x^2} + \frac{\partial^2 u(\mathbf{r})}{\partial y^2} \right]^2 \right\}$$

$$\propto q^4$$

Ultrasoft  
at low  $q$



Undulation

Compression

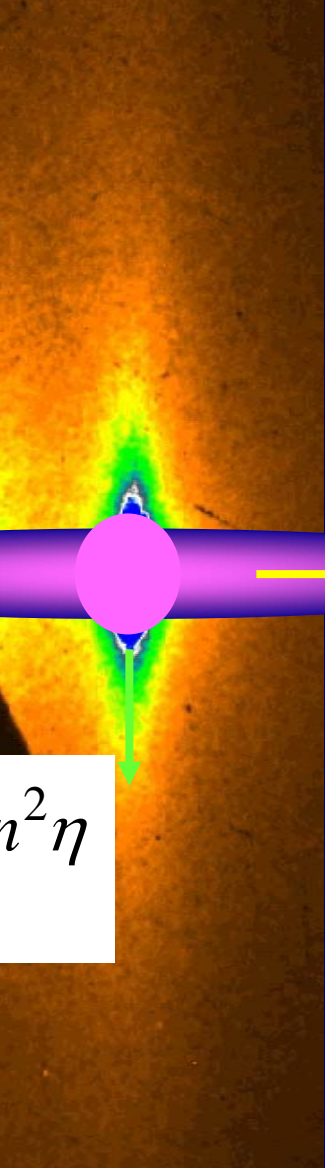
$$\langle u^2(\mathbf{r}) \rangle = \frac{k_B T}{8 \pi \sqrt{KB}} \ln \left( \frac{L}{d} \right)$$

Fluctuations destroy  
layer ordering for large  $L$

Landau – Peierls instability

# Effect of Peierls-Landau instability on reflections:

Our result  
for goethite:

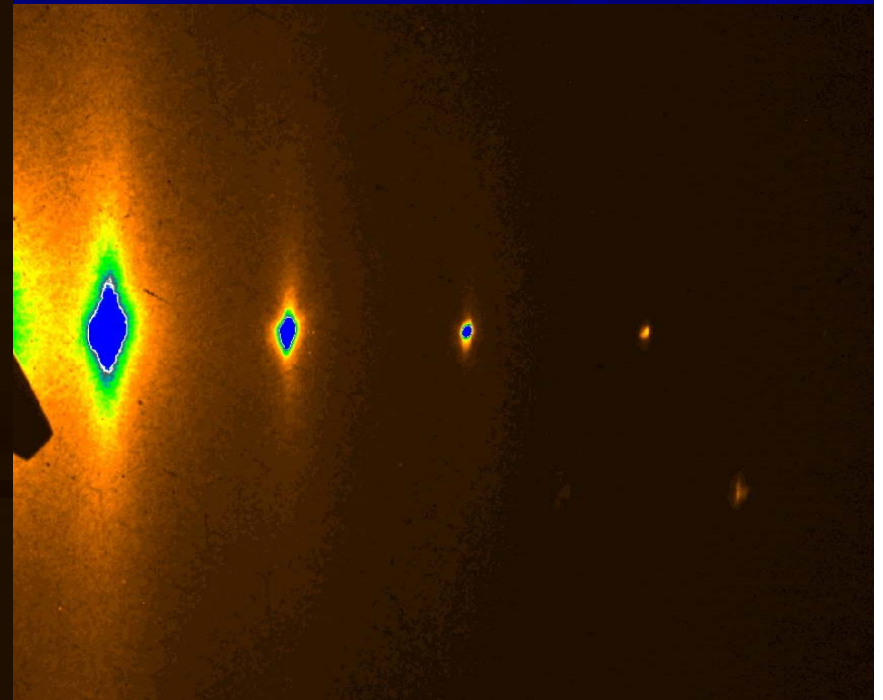
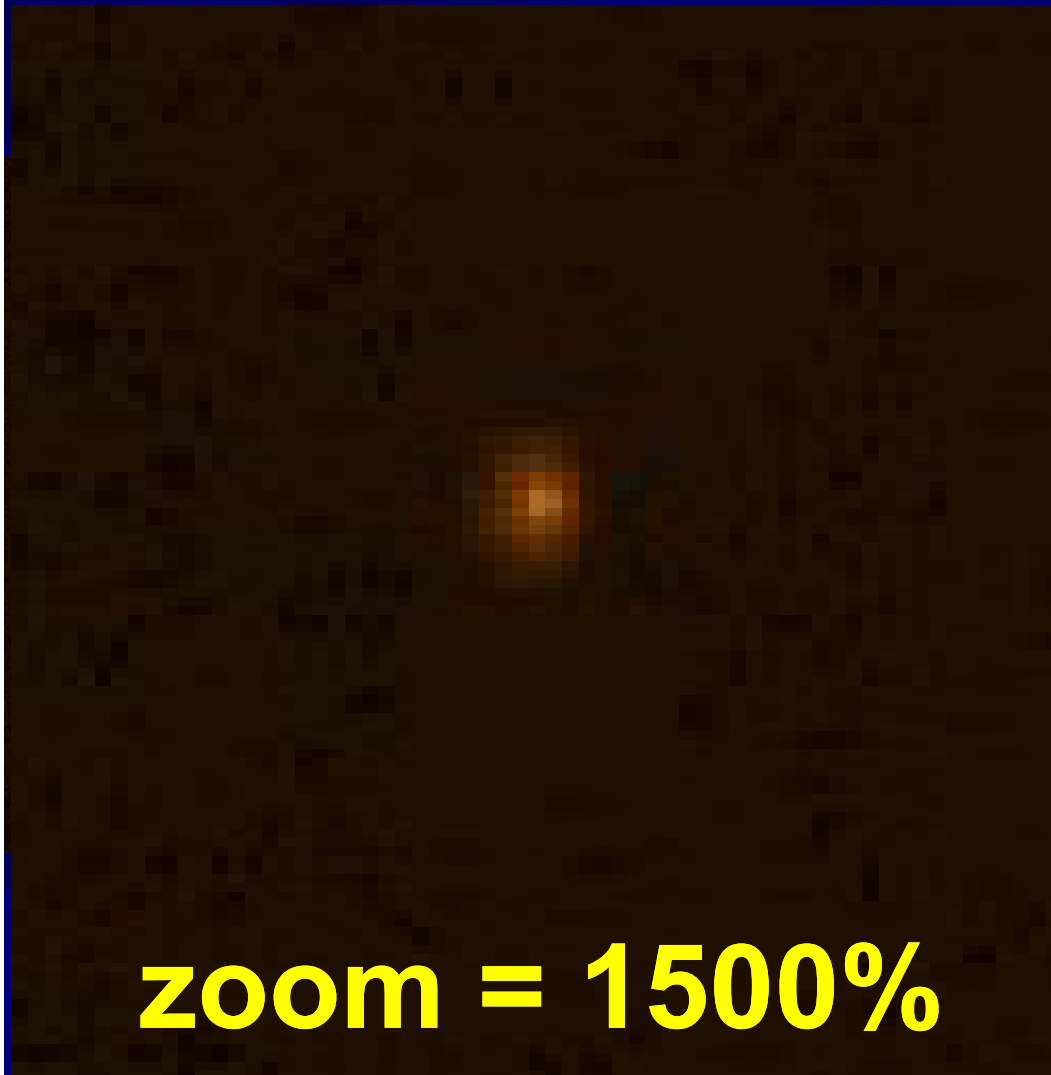

$$\propto 1 / q_{\perp}^{4-2n^2\eta}$$

$$\propto 1 / q_{\perp}^{2-n^2\eta}$$

No agreement!



# No sign of Landau-Peierls instability

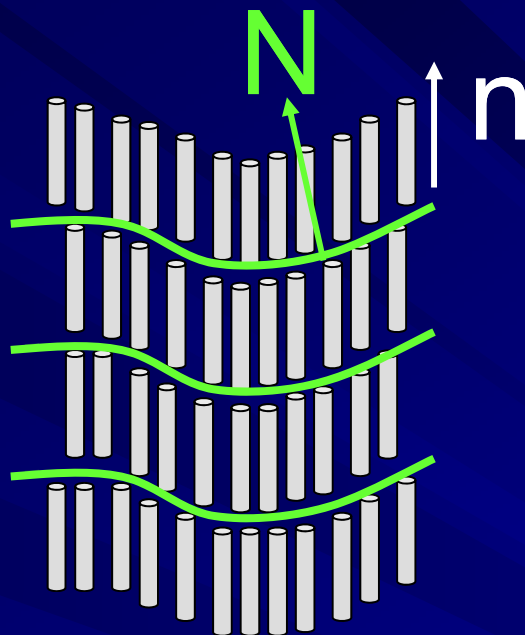
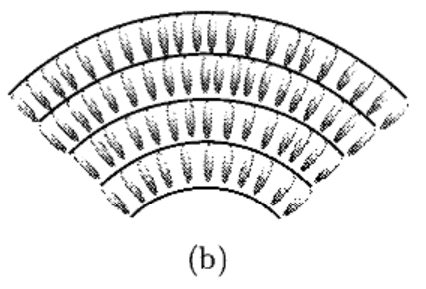


**zoom = 1500%**

# Principles of condensed matter physics

P. M. CHAIKIN  
Princeton University

T. C. LUBENSKY  
University of Pennsylvania



If the layers and the molecules are rotated rigidly together, there is no free energy cost. There will, however, be an energy cost if the molecules are rotated away from their preferred local orientation normal to the layers. Thus, there should

$\propto q^2 \Rightarrow$  **‘Normal’ elastic mode at low  $q$ ?** To

account for deviations from the uniform layered state, an energy proportional to  $(\sigma_{1N} - \sigma_{1n})^2 = (\nabla_{\perp} u + \delta \mathbf{n})^2$  satisfies these requirements. The free energy for the smectic phase should, therefore, be

$$F_{el} = \frac{1}{2} \int d^3x [B(\nabla_{\parallel} u)^2 + D(\nabla_{\perp} u + \delta \mathbf{n})^2] \quad (6.3.11)$$

$$+ \frac{1}{2} \int d^3x [K_1(\nabla \cdot \mathbf{n})^2 + K_2(\mathbf{n} \cdot (\nabla \times \mathbf{n}))^2 + K_3(\mathbf{n} \times (\nabla \times \mathbf{n}))^2].$$

$$F_{el} = \frac{1}{2} \int d^3x [B(\nabla_{\parallel} u)^2 + D(\nabla_{\perp} u + \delta \mathbf{n})^2] \quad (6.3.11)$$

$$+ \frac{1}{2} \int d^3x [K_1(\nabla \cdot \mathbf{n})^2 + K_2(\mathbf{n} \cdot (\nabla \times \mathbf{n}))^2 + K_3(\mathbf{n} \times (\nabla \times \mathbf{n}))^2].$$

D and K define a new scale:

$$q_c = \sqrt{D / K_1}$$

For  $q \ll q_c$  splay ( $K_1$ ) undulations are the softest.

For  $q \gg q_c$  another type undulations should be of importance:

$n \approx \text{Const}$ ;  $n$  and  $N$  are decoupled.



# Our model:

Long wavelength:

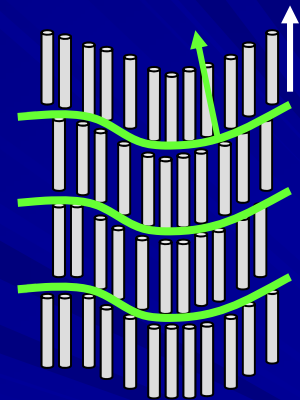
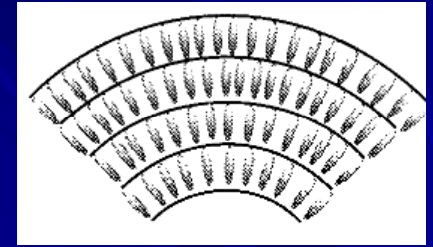
$$F = \frac{1}{2} B (q_{\parallel} u)^2 + \frac{1}{2} K (q_{\perp})^4 u^2$$

Short wavelength:

$$F = \frac{1}{2} B (q_{\parallel} u)^2 + \frac{1}{2} D (q_{\perp} u)^2$$

Leads to diffuse 'halo':

$$I(q) = I_0 / (B q_{\parallel}^2 + D q_{\perp}^2)$$

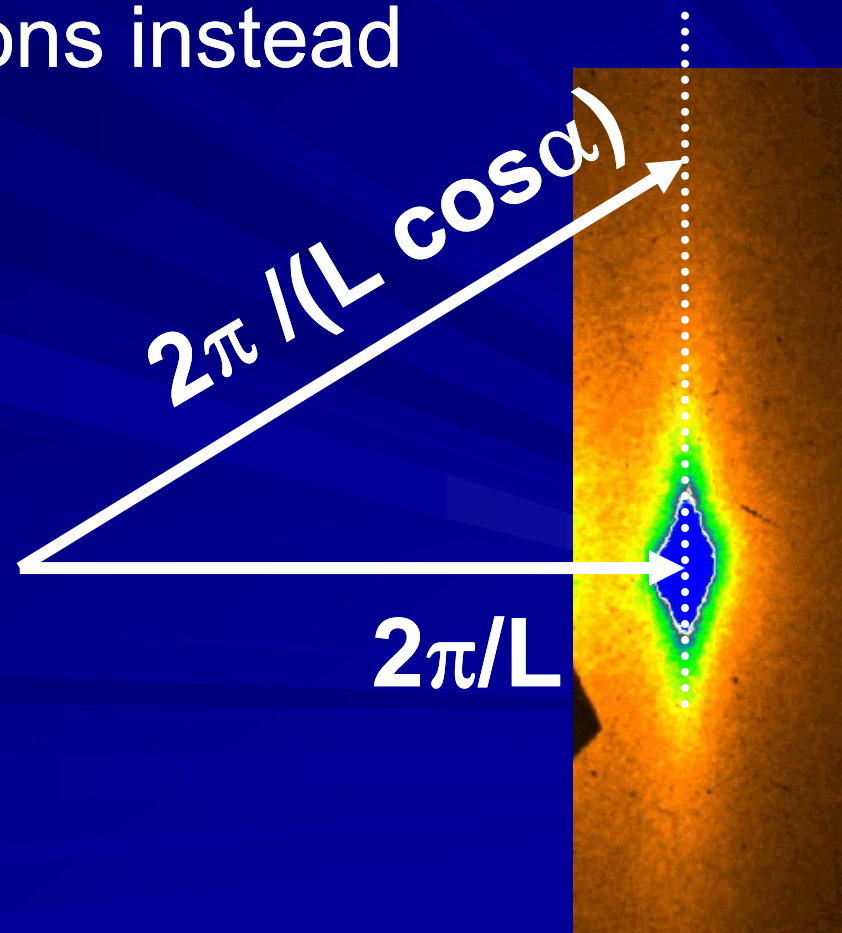
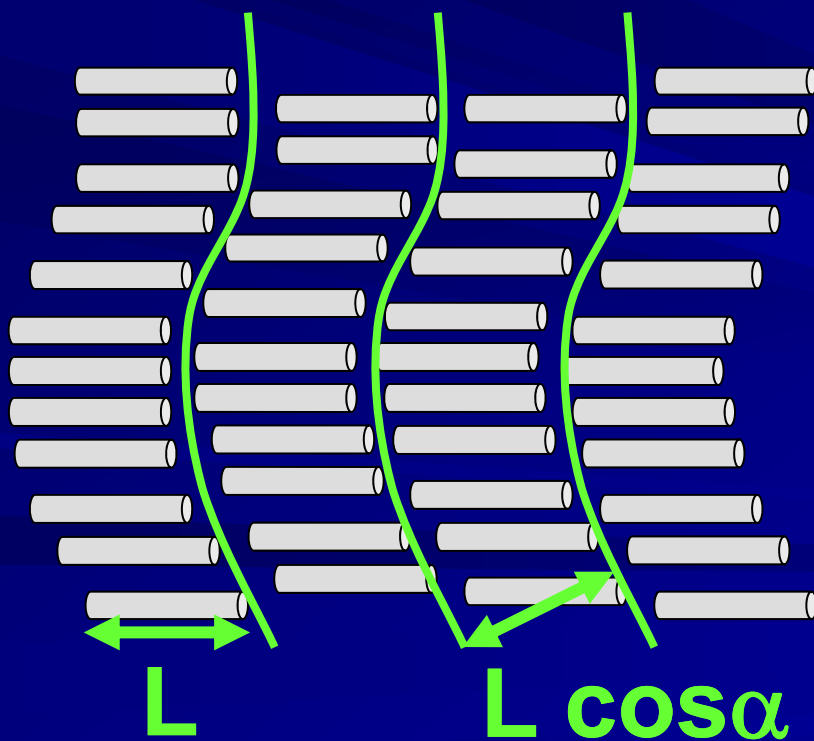


Just like in ordinary crystals but (highly) anisotropic

# Short wavelength undulations:

$n = \text{Const}$  (e.g., due to high splay energy)

'Sliding' layer undulations instead

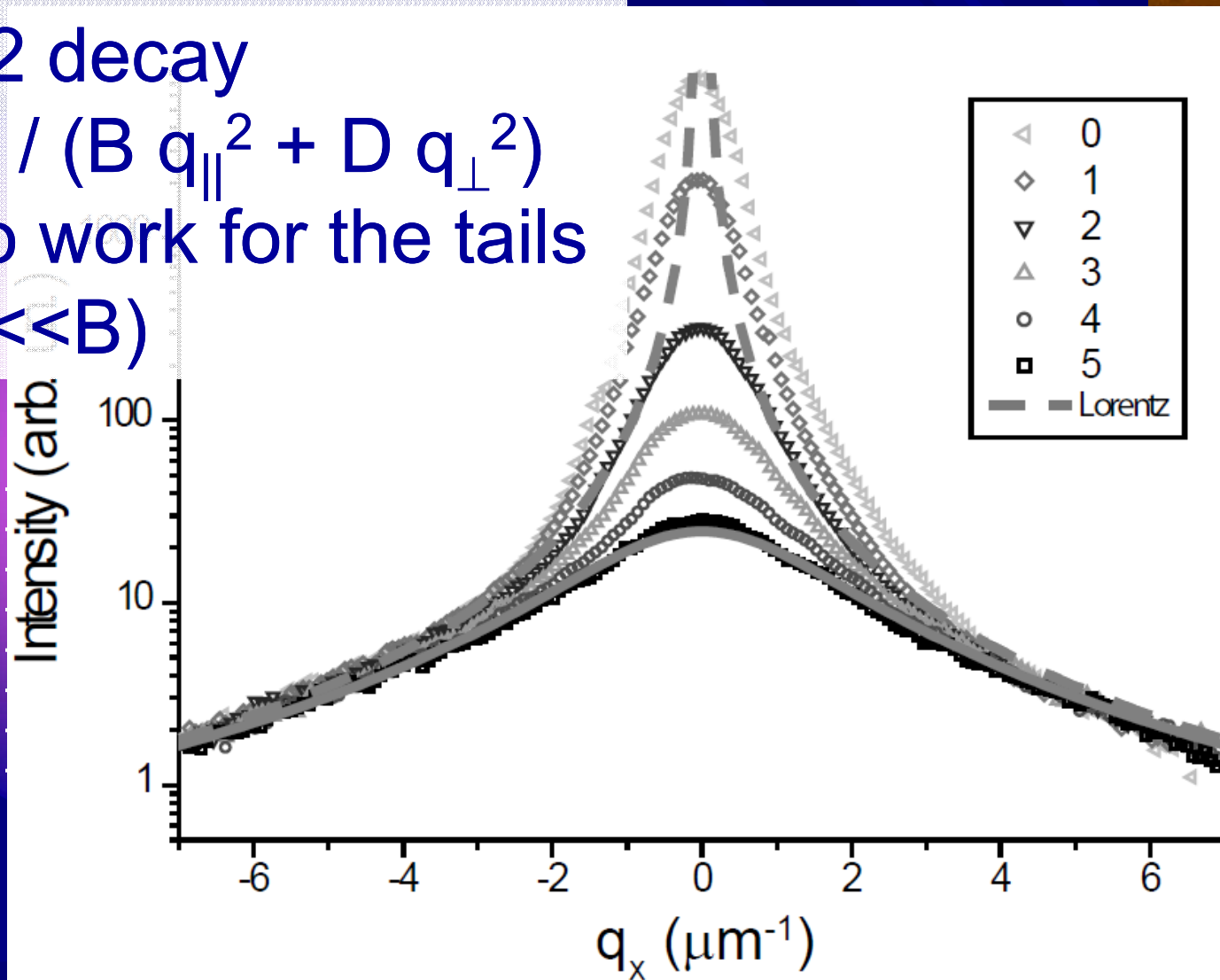


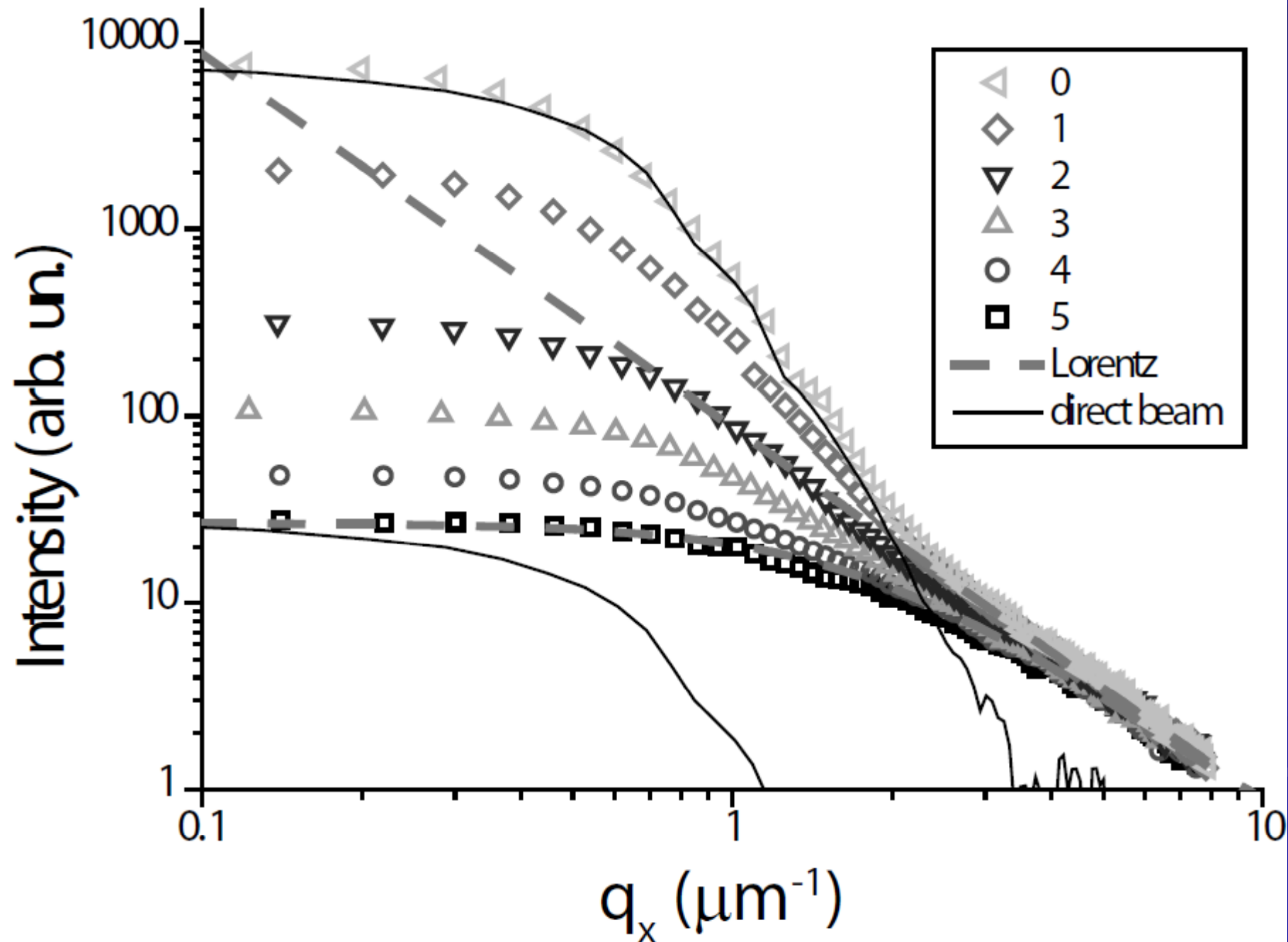
# More exp. data: going 3D

Power 2 decay

$$I(q) = I_0 / (B q_{\parallel}^2 + D q_{\perp}^2)$$

seem to work for the tails  
(with  $D \ll B$ )







## Undulation Properties of the Lamellar Phase of a Diblock Copolymer: SAXS Experiments

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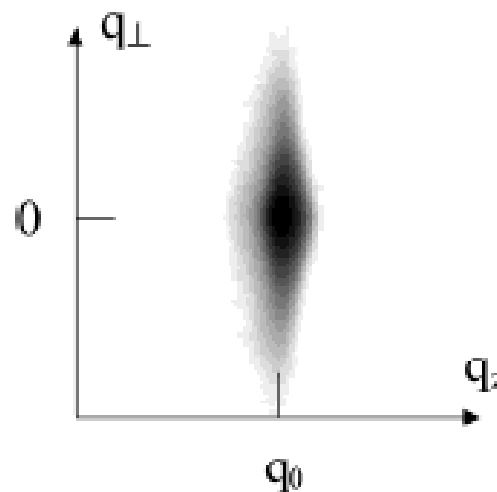
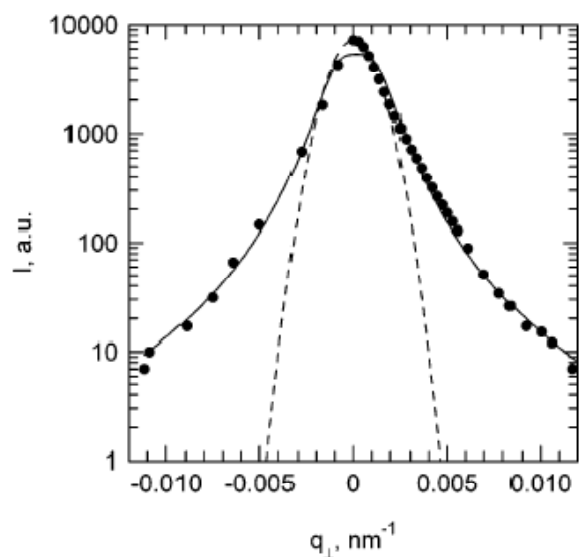
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**Figure 7.** Scan of the Bragg spot in the  $q_{\perp}$  direction. The dashed line corresponds to a Gaussian fit; the line shape is much better described by a Lorentzian law (full line).

reaction spot of the first-order Bragg peak  
= 30 °C. The intensity is represented on a  
z.

Are there  
more  
examples?

# Conclusions: smectic

- Undulation fluctuations:
  - splay
  - slide
- The slide undulations do not lead to Landau-Peierls instability
- Demonstrated in goethite
- Similar story in block co-polymers? [Stepanek et al]
- Indications of similar fluctuations in columnar discotic

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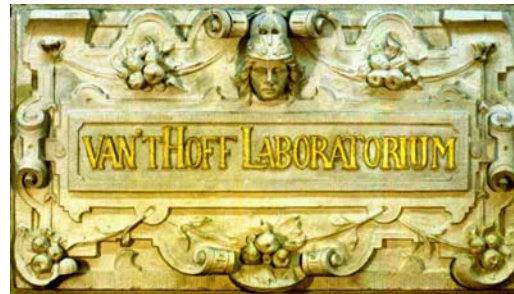
K. Kvashnina, A. Snigirev, ESRF

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**Universiteit Utrecht**



# The conclusions

- Colloids: lot of fun
- Microradian x-ray diffraction: Mind the coherence
- Fine structural details on
  - structure
  - disorder
  - fluctuations

